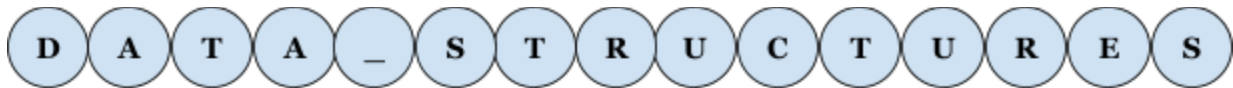

CS261 Data Structures

Assignment 2

Winter 2022

Dynamic Array Implementation (plus a brand new Bag)

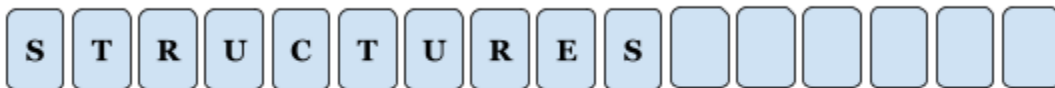


```
da = DynamicArray(list("DATA"))
```



```
self.size = 4  
self.capacity = 4  
self.data = ['D', 'A', 'T', 'A']
```

```
da = DynamicArray(list("STRUCTURES"))
```



```
self.size = 10  
self.capacity = 16  
self.data = ['S', 'T', 'R', 'U', 'C', 'T', 'U', 'R', 'E', 'S', None, None, None, None, None, None]
```

Contents

General Instructions 3

Part 1 - Dynamic Array Implementation

Summary and Specific Instructions	4
resize()	5
append()	6
insert_at_index()	7
remove_at_index()	9
slice()	12
merge()	13
map()	14
filter()	15
reduce()	16
find_mode()	17

Part 2 - Bag ADT Implementation

Summary and Specific Instructions	19
add(), remove()	20
count(), clear()	21
equal()	22
__iter__(), __next__()	23

General Instructions

1. Programs in this assignment must be written in Python v3 and submitted to Gradescope before the due date specified in the syllabus. You may resubmit your code as many times as necessary. Gradescope allows you to choose which submission will be graded.
2. In Gradescope, your code will be run through several tests. Any failed tests will provide a brief explanation of testing conditions to help you with troubleshooting. For full credit you must pass all of the tests.
3. We encourage you to create your own test programs and cases even though this work won't have to be submitted and won't be graded. Gradescope tests are limited in scope and may not cover all edge cases. Your submission must work on all valid inputs. We reserve the right to test your submission with more tests than Gradescope.
4. Your code must have an appropriate level of comments. At a minimum, each method should have a descriptive docstring. Additionally, put comments throughout the code to make it easy to follow and understand any non-obvious code.
5. You will be provided with a starter "skeleton" code, on which you will build your implementation. Methods defined in the skeleton code must retain their names and input / output parameters. Variables defined in the skeleton code must also retain their names. We will only test your solution by making calls to methods defined in the skeleton code and by checking values of variables defined in the skeleton code. You can add more methods and variables, as needed.

However, certain classes and methods cannot be changed in any way. Please see the comments in the skeleton code for guidance. In particular, the content of any methods pre-written for you as part of the skeleton code must not be changed.

Note that the `__iter__()` method in the Bag implementation **will** require you to add variables in that method, and this is permitted.

6. Both the skeleton code and the code examples provided in this document are part of the assignment requirements. They have been carefully selected to demonstrate requirements for each method. Refer to them for a detailed description of expected method behavior, input / output parameters, and the handling of edge cases. Code examples may include assignment requirements not explicitly stated elsewhere.
7. **For each method, you are required to use an iterative solution.** We will specify the maximum input size that your solution must handle.
8. You may not use any imports beyond the ones included in the assignment source code provided.

Part 1 - Summary and Specific Instructions

1. Implement a Dynamic Array class by completing the skeleton code provided in the file `dynamic_array.py`. The `DynamicArray` class will use a `StaticArray` object as its underlying data storage container and will provide many methods similar to those we are used to using when working with Python lists. Once completed, your implementation will include the following methods:

```
resize()
append()
insert_at_index()
remove_at_index()
slice()
merge()
map()
filter()
reduce()
```

* Several class methods, like `is_empty()`, `length()`, `get_at_index()` and `set_at_index()` have been pre-written for you.

2. We will test your implementations with different types of objects, not just integers. We guarantee that all such objects will have correct implementation of methods `__eq__`, `__lt__`, `__gt__`, `__ge__`, `__le__`, and `__str__`.
3. The number of objects stored in the array at any given time will be between 0 and 1,000,000 inclusive. An array must allow for the storage of duplicate objects.
4. Variables in the `DynamicArray` class are not marked as private. For **this** portion of the assignment, you are allowed to access and change their values directly. Note that getter or setter methods have already been provided for you.
5. RESTRICTIONS: You are not allowed to use ANY built-in Python data structures and/or their methods (lists, dictionaries, etc.). You must solve this portion of the assignment by importing and using objects of the `StaticArray` class (prewritten for you) and using class methods to write your solution.

You are also not allowed to directly access any variables of the `StaticArray` class (e.g. `self.data._data[]`). All work must be done by using only `StaticArray` class methods. **Don't forget to include your `StaticArray` class from Assignment 1 in your project.**

resize(self, new_capacity: int) -> None:

This method changes the capacity of the underlying storage for the array elements. It does not change the values or the order of any elements currently stored in the dynamic array.

It is intended to be an **"internal"** method of the Dynamic Array class, called by other class methods, such as `append()`, `remove_at_index()`, or `insert_at_index()`, to manage the capacity of the underlying data structure.

The method should only accept positive integers for `new_capacity`. Additionally, `new_capacity` cannot be smaller than the number of elements currently stored in the dynamic array (which is tracked by the `self.size` variable). If `new_capacity` is not a positive integer or if `new_capacity < self.size`, this method should not do any work and immediately exit.

Example #1:

```
da = DynamicArray()
print(da.size, da.capacity, da.data)
da.resize(8)
print(da.size, da.capacity, da.data)
da.resize(2)
print(da.size, da.capacity, da.data)
da.resize(0)
print(da.size, da.capacity, da.data)
```

Output:

```
0 4 STAT_ARR Size: 4 [None, None, None, None]
0 8 STAT_ARR Size: 8 [None, None, None, None, None, None, None, None]
0 2 STAT_ARR Size: 2 [None, None]
0 2 STAT_ARR Size: 2 [None, None]
```

NOTE: Example 2 below will not work properly unless the `append()` method is implemented.

Example #2:

```
da = DynamicArray([1, 2, 3, 4, 5, 6, 7, 8])
print(da)
da.resize(20)
print(da)
da.resize(4)
print(da)
```

Output:

```
DYN_ARR Size/Cap: 8/8 [1, 2, 3, 4, 5, 6, 7, 8]
DYN_ARR Size/Cap: 8/20 [1, 2, 3, 4, 5, 6, 7, 8]
DYN_ARR Size/Cap: 8/20 [1, 2, 3, 4, 5, 6, 7, 8]
```

append(self, value: object) -> None:

This method adds a new value at the end of the dynamic array.

If the internal storage associated with the dynamic array is already full, you need to DOUBLE its capacity before adding a new value.

Example #1:

```
da = DynamicArray()
print(da.size, da.capacity, da.data)
da.append(1)
print(da.size, da.capacity, da.data)
print(da)
```

Output:

```
0 4 STAT_ARR Size: 4 [None, None, None, None]
1 4 STAT_ARR Size: 4 [1, None, None, None]
DYN_ARR Size/Cap: 1/4 [1]
```

Example #2:

```
da = DynamicArray()
for i in range(9):
    da.append(i + 101)
    print(da)
```

Output:

```
DYN_ARR Size/Cap: 1/4 [101]
DYN_ARR Size/Cap: 2/4 [101, 102]
DYN_ARR Size/Cap: 3/4 [101, 102, 103]
DYN_ARR Size/Cap: 4/4 [101, 102, 103, 104]
DYN_ARR Size/Cap: 5/8 [101, 102, 103, 104, 105]
DYN_ARR Size/Cap: 6/8 [101, 102, 103, 104, 105, 106]
DYN_ARR Size/Cap: 7/8 [101, 102, 103, 104, 105, 106, 107]
DYN_ARR Size/Cap: 8/8 [101, 102, 103, 104, 105, 106, 107, 108]
DYN_ARR Size/Cap: 9/16 [101, 102, 103, 104, 105, 106, 107, 108, 109]
```

Example #3:

```
da = DynamicArray()
for i in range(600):
    da.append(i)
print(da.size)
print(da.capacity)
```

Output:

```
600
1024
```

insert_at_index(self, index: int, value: object) -> None:

This method adds a new value at the specified index position in the dynamic array. Index 0 refers to the beginning of the array. If the provided index is invalid, the method raises a custom "DynamicArrayException". Code for the exception is provided in the skeleton file. If the array contains N elements, valid indices for this method are [0, N] inclusive.

If the internal storage associated with the dynamic array is already full, you need to DOUBLE its capacity before adding a new value (hint - you can use your already written `resize()` function for this).

Example #1:

```
da = DynamicArray([100])
print(da)
da.insert_at_index(0, 200)
da.insert_at_index(0, 300)
da.insert_at_index(0, 400)
print(da)
da.insert_at_index(3, 500)
print(da)
da.insert_at_index(1, 600)
print(da)
```

Output:

```
DYN_ARR Size/Cap: 1/4 [100]
DYN_ARR Size/Cap: 4/4 [400, 300, 200, 100]
DYN_ARR Size/Cap: 5/8 [400, 300, 200, 500, 100]
DYN_ARR Size/Cap: 6/8 [400, 600, 300, 200, 500, 100]
```

Example #2:

```
da = DynamicArray()
try:
    da.insert_at_index(-1, 100)
except Exception as e:
    print("Exception raised:", type(e))
da.insert_at_index(0, 200)
try:
    da.insert_at_index(2, 300)
except Exception as e:
    print("Exception raised:", type(e))
print(da)
```

Output:

```
Exception raised: <class '__main__.DynamicArrayException'>
Exception raised: <class '__main__.DynamicArrayException'>
DYN_ARR Size/Cap: 1/4 [200]
```

Example #3:

```
da = DynamicArray()
for i in range(1, 10):
    index, value = i - 4, i * 10
    try:
        da.insert_at_index(index, value)
    except Exception as e:
        print("Cannot insert value", value, "at index", index)
print(da)
```

Output:

```
Cannot insert value 10 at index -3
Cannot insert value 20 at index -2
Cannot insert value 30 at index -1
DYN_ARR Size/Cap: 6/8 [40, 50, 60, 70, 80, 90]
```


remove_at_index(self, index: int) -> None:

This method removes the element at the specified index from the dynamic array. Index 0 refers to the beginning of the array. If the provided index is invalid, the method raises a custom "DynamicArrayException". Code for the exception is provided in the skeleton file. If the array contains N elements, valid indices for this method are [0, N - 1] inclusive.

When the number of elements stored in the array (before removal) is STRICTLY LESS than $\frac{1}{4}$ of its current capacity, the capacity must be reduced to TWICE the number of current elements. This check / capacity adjustment must happen BEFORE removal of the element.

If the current capacity (before reduction) is 10 elements or less, reduction should not happen at all. If the current capacity (before reduction) is greater than 10 elements, the reduced capacity cannot become less than 10 elements. Please see the examples below, especially example #3, for clarification.

Example #1:

```
da = DynamicArray([10, 20, 30, 40, 50, 60, 70, 80])
print(da)
da.remove_at_index(0)
print(da)
da.remove_at_index(6)
print(da)
da.remove_at_index(2)
print(da)
```

Output:

```
DYN_ARR Size/Cap: 8/8 [10, 20, 30, 40, 50, 60, 70, 80]
DYN_ARR Size/Cap: 7/8 [20, 30, 40, 50, 60, 70, 80]
DYN_ARR Size/Cap: 6/8 [20, 30, 40, 50, 60, 70]
DYN_ARR Size/Cap: 5/8 [20, 30, 50, 60, 70]
```

Example #2:

```
da = DynamicArray([1024])
print(da)
for i in range(17):
    da.insert_at_index(i, i)
print(da.size, da.capacity)
for i in range(16, -1, -1):
    da.remove_at_index(0)
print(da)
```

Output:

```
DYN_ARR Size/Cap: 1/4 [1024]
18 32
DYN_ARR Size/Cap: 1/10 [1024]
```

Example #3:

```

da = DynamicArray()
print(da.size, da.capacity)
[da.append(1) for i in range(100)]          # step 1 - add 100 elements
print(da.size, da.capacity)
[da.remove_at_index(0) for i in range(68)]  # step 2 - remove 68 elements
print(da.size, da.capacity)
da.remove_at_index(0)                      # step 3 - remove 1 element
print(da.size, da.capacity)
da.remove_at_index(0)                      # step 4 - remove 1 element
print(da.size, da.capacity)
[da.remove_at_index(0) for i in range(14)]  # step 5 - remove 14 elements
print(da.size, da.capacity)
da.remove_at_index(0)                      # step 6 - remove 1 element
print(da.size, da.capacity)
da.remove_at_index(0)                      # step 7 - remove 1 element
print(da.size, da.capacity)

for i in range(14):
    print("Before remove_at_index(): ", da.size, da.capacity, end="")
    da.remove_at_index(0)
    print(" After remove_at_index(): ", da.size, da.capacity)

```

Output:

```

0 4
100 128
32 128
31 128
30 62
16 62
15 62
14 30
Before remove_at_index(): 14 30 After remove_at_index(): 13 30
Before remove_at_index(): 13 30 After remove_at_index(): 12 30
Before remove_at_index(): 12 30 After remove_at_index(): 11 30
Before remove_at_index(): 11 30 After remove_at_index(): 10 30
Before remove_at_index(): 10 30 After remove_at_index(): 9 30
Before remove_at_index(): 9 30 After remove_at_index(): 8 30
Before remove_at_index(): 8 30 After remove_at_index(): 7 30
Before remove_at_index(): 7 30 After remove_at_index(): 6 14
Before remove_at_index(): 6 14 After remove_at_index(): 5 14
Before remove_at_index(): 5 14 After remove_at_index(): 4 14
Before remove_at_index(): 4 14 After remove_at_index(): 3 14
Before remove_at_index(): 3 14 After remove_at_index(): 2 10
Before remove_at_index(): 2 10 After remove_at_index(): 1 10
Before remove_at_index(): 1 10 After remove_at_index(): 0 10

```

Example #4:

```
da = DynamicArray([1, 2, 3, 4, 5])
print(da)
for _ in range(5):
    da.remove_at_index(0)
    print(da)
```

Output:

```
DYN_ARR Size/Cap: 5/8 [1, 2, 3, 4, 5]
DYN_ARR Size/Cap: 4/8 [2, 3, 4, 5]
DYN_ARR Size/Cap: 3/8 [3, 4, 5]
DYN_ARR Size/Cap: 2/8 [4, 5]
DYN_ARR Size/Cap: 1/8 [5]
DYN_ARR Size/Cap: 0/8 []
```

slice(self, start_index: int, size: int) -> object:

This method returns a new Dynamic Array object that contains the requested number of elements from the original array starting with the element located at the requested start index. If the array contains N elements, a valid `start_index` is in range `[0, N - 1]` inclusive. A valid size is a non-negative integer.

If the provided start index or size is invalid, or if there are not enough elements between the start index and the end of the array to make the slice of the requested size, this method raises a custom "DynamicArrayException". Code for the exception is provided in the skeleton file.

Example #1:

```
da = DynamicArray([1, 2, 3, 4, 5, 6, 7, 8, 9])
da_slice = da.slice(1, 3)
print(da, da_slice, sep="\n")
da_slice.remove_at_index(0)
print(da, da_slice, sep="\n")
```

Output:

```
DYN_ARR Size/Cap: 9/16 [1, 2, 3, 4, 5, 6, 7, 8, 9]
DYN_ARR Size/Cap: 3/4 [2, 3, 4]
DYN_ARR Size/Cap: 9/16 [1, 2, 3, 4, 5, 6, 7, 8, 9]
DYN_ARR Size/Cap: 2/4 [3, 4]
```

Example #2:

```
da = DynamicArray([10, 11, 12, 13, 14, 15, 16])
print("SOURCE:", da)
slices = [(0, 7), (-1, 7), (0, 8), (2, 3), (5, 0), (5, 3), (6, 1), (6, -1)]
for i, cnt in slices:
    print("Slice", i, "/", cnt, end="")
    try:
        print(" --- OK: ", da.slice(i, cnt))
    except:
        print(" --- exception occurred.")
```

Output:

```
SOURCE: DYN_ARR Size/Cap: 7/8 [10, 11, 12, 13, 14, 15, 16]
Slice 0 / 7 --- OK: DYN_ARR Size/Cap: 7/8 [10, 11, 12, 13, 14, 15, 16]
Slice -1 / 7 --- exception occurred.
Slice 0 / 8 --- exception occurred.
Slice 2 / 3 --- OK: DYN_ARR Size/Cap: 3/4 [12, 13, 14]
Slice 5 / 0 --- OK: DYN_ARR Size/Cap: 0/4 []
Slice 5 / 3 --- exception occurred.
Slice 6 / 1 --- OK: DYN_ARR Size/Cap: 1/4 [16]
Slice 6 / -1 --- exception occurred.
```

merge(self, second_da: object) -> None:

This method takes another Dynamic Array object as a parameter, and appends all elements from this other array onto the current one, in the same order as they are stored in the array parameter.

Example #1:

```
da = DynamicArray([1, 2, 3, 4, 5])
da2 = DynamicArray([10, 11, 12, 13])
print(da)
da.merge(da2)
print(da)
```

Output:

```
DYN_ARR Size/Cap: 5/8 [1, 2, 3, 4, 5]
DYN_ARR Size/Cap: 9/16 [1, 2, 3, 4, 5, 10, 11, 12, 13]
```

Example #2:

```
da = DynamicArray([1, 2, 3])
da2 = DynamicArray()
da3 = DynamicArray()
da.merge(da2)
print(da)
da2.merge(da3)
print(da2)
da3.merge(da)
print(da3)
```

Output:

```
DYN_ARR Size/Cap: 3/4 [1, 2, 3]
DYN_ARR Size/Cap: 0/4 []
DYN_ARR Size/Cap: 3/4 [1, 2, 3]
```

map(self, map_func) ->object:

This method creates a new Dynamic Array where the value of each element is derived by applying a given `map_func` to the corresponding value from the original array.

It works similarly to the built-in Python `map()` function. If you would like to review how Python's `map()` works, here are some suggested sites:

<https://docs.python.org/3/library/functions.html#map>

<https://www.geeksforgeeks.org/python-map-function/>

Example #1:

```
da = DynamicArray([1, 5, 10, 15, 20, 25])
print(da)
print(da.map(lambda x: (x ** 2)))
```

Output:

```
DYN_ARR Size/Cap: 6/8 [1, 5, 10, 15, 20, 25]
DYN_ARR Size/Cap: 6/8 [1, 25, 100, 225, 400, 625]
```

Example #2:

```
def double(value):
    return value * 2

def square(value):
    return value ** 2

def cube(value):
    return value ** 3

def plus_one(value):
    return value + 1

da = DynamicArray([plus_one, double, square, cube])
for value in [1, 10, 20]:
    print(da.map(lambda x: x(value)))
```

Output:

```
DYN_ARR Size/Cap: 4/4 [2, 2, 1, 1]
DYN_ARR Size/Cap: 4/4 [11, 20, 100, 1000]
DYN_ARR Size/Cap: 4/4 [21, 40, 400, 8000]
```

filter(self, filter_func) ->object:

This method creates a new Dynamic Array populated only with those elements from the original array for which `filter_func` returns True.

It works similarly to the built-in Python `filter()` function. If you would like to review how Python's `filter()` works, here are some suggested sites:

<https://docs.python.org/3/library/functions.html#filter>

<https://www.geeksforgeeks.org/filter-in-python/>

Example #1:

```
def filter_a(e):  
    return e > 10  
  
da = DynamicArray([1, 5, 10, 15, 20, 25])  
print(da)  
result = da.filter(filter_a)  
print(result)  
print(da.filter(lambda x: (10 <= x <= 20)))
```

Output:

```
DYN_ARR Size/Cap: 6/8 [1, 5, 10, 15, 20, 25]  
DYN_ARR Size/Cap: 3/4 [15, 20, 25]  
DYN_ARR Size/Cap: 3/4 [10, 15, 20]
```

Example #2:

```
def is_long_word(word, length):  
    return len(word) > length  
  
da = DynamicArray("This is a sentence with some long words".split())  
print(da)  
for length in [3, 4, 7]:  
    print(da.filter(lambda word: is_long_word(word, length)))
```

Output:

```
DYN_ARR Size/Cap: 8/8 [This, is, a, sentence, with, some, long, words]  
DYN_ARR Size/Cap: 6/8 [This, sentence, with, some, long, words]  
DYN_ARR Size/Cap: 2/4 [sentence, words]  
DYN_ARR Size/Cap: 1/4 [sentence]
```

reduce(self, reduce_func, initializer=None) ->object:

This method sequentially applies the `reduce_func` to all elements of the Dynamic Array and returns the resulting value. The method takes an optional initializer parameter. If this parameter is not provided, the first value in the array is used as the initializer. If the Dynamic Array is empty, the method returns the value of the initializer (or `None`, if it was not provided).

This method works similarly to the Python `reduce()` function. If you would like to review how Python's `reduce()` works, here is a suggested site:

<https://www.geeksforgeeks.org/reduce-in-python/>

Example #1:

```
values = [100, 5, 10, 15, 20, 25]
da = DynamicArray(values)
print(da)
print(da.reduce(lambda x, y: x + y ** 2))
print(da.reduce(lambda x, y: x + y ** 2, -1))
```

Output:

```
DYN_ARR Size/Cap: 6/8 [100, 5, 10, 15, 20, 25]
1475
11374
```

Explanation:

$$1475 = 100 + 5^2 + 10^2 + 15^2 + 20^2 + 25^2$$

First value is not squared because it is used as an initializer.

$$11374 = -1 + 100^2 + 5^2 + 10^2 + 15^2 + 20^2 + 25^2$$

Example #2:

```
da = DynamicArray([100])
print(da.reduce(lambda x, y: x + y ** 2))
print(da.reduce(lambda x, y: x + y ** 2, -1))
da.remove_at_index(0)
print(da.reduce(lambda x, y: x + y ** 2))
print(da.reduce(lambda x, y: x + y ** 2, -1))
```

Output:

```
100
9999
None
-1
```


find_mode(arr: DynamicArray) -> (DynamicArray, int):

Write a standalone function outside of the Dynamic Array class that receives a DynamicArray that is sorted in order, either non-descending or non-ascending. The function will return a tuple containing (in this order) a DynamicArray comprising the mode (most-occurring) values in the array, and an integer that represents the highest frequency (how many times they appear).

If there is more than one value that has the highest frequency, all values at that frequency should be included in the array being returned in the order in which they appear in the array parameter. If there is only one mode, return a DynamicArray comprised of just that value.

You may assume that the input array will contain at least one element and that values stored in the array are all of the same type (either all numbers, or strings, or custom objects, but never a mix of these). You do not need to write checks for these conditions.

For full credit, the function must be implemented with $O(N)$ complexity with no additional data structures (beyond the array you return) being created.

Example #1:

```
test_cases = (
    [1, 1, 2, 3, 4, 4],
    [1, 2, 3, 4, 5],
    ["Apple", "Banana", "Banana", "Carrot", "Carrot", "Date", "Date", "Date",
    "Eggplant", "Eggplant", "Eggplant", "Fig", "Fig", "Grape"],
    [4, 3, 3, 2, 2, 2, 1, 1, 1, 1]
)

for case in test_cases:
    da = DynamicArray(case)
    mode, frequency = find_mode(da)
    print(f"{da}\nMode: {mode}, Frequency: {frequency}\n")

case = [4, 3, 3, 2, 2, 2, 1, 1, 1, 1]
da = DynamicArray()
for x in range(len(case)):
    da.append(case[x])
    mode, frequency = find_mode(da)
    print(f"{da}\nMode: {mode}, Frequency: {frequency}\n")
```

Output:

```
# find_mode - example 1
DYN_ARR Size/Cap: 6/8 [1, 1, 2, 3, 4, 4]
Mode: DYN_ARR Size/Cap: 2/4 [1, 4], Frequency: 2

DYN_ARR Size/Cap: 5/8 [1, 2, 3, 4, 5]
Mode: DYN_ARR Size/Cap: 5/8 [1, 2, 3, 4, 5], Frequency: 1

DYN_ARR Size/Cap: 14/16 [Apple, Banana, Banana, Carrot, Carrot, Date, Date,
Date, Eggplant, Eggplant, Eggplant, Fig, Fig, Grape]
Mode: DYN_ARR Size/Cap: 2/4 [Date, Eggplant], Frequency: 3

DYN_ARR Size/Cap: 1/4 [4]
Mode: DYN_ARR Size/Cap: 1/4 [4], Frequency: 1
DYN_ARR Size/Cap: 2/4 [4, 3]
Mode: DYN_ARR Size/Cap: 2/4 [4, 3], Frequency: 1
DYN_ARR Size/Cap: 3/4 [4, 3, 3]
Mode: DYN_ARR Size/Cap: 1/4 [3], Frequency: 2
DYN_ARR Size/Cap: 4/4 [4, 3, 3, 2]
Mode: DYN_ARR Size/Cap: 1/4 [3], Frequency: 2
DYN_ARR Size/Cap: 5/8 [4, 3, 3, 2, 2]
Mode: DYN_ARR Size/Cap: 2/4 [3, 2], Frequency: 2
DYN_ARR Size/Cap: 6/8 [4, 3, 3, 2, 2, 2]
Mode: DYN_ARR Size/Cap: 1/4 [2], Frequency: 3
DYN_ARR Size/Cap: 7/8 [4, 3, 3, 2, 2, 2, 1]
Mode: DYN_ARR Size/Cap: 1/4 [2], Frequency: 3
DYN_ARR Size/Cap: 8/8 [4, 3, 3, 2, 2, 2, 1, 1]
Mode: DYN_ARR Size/Cap: 1/4 [2], Frequency: 3
DYN_ARR Size/Cap: 9/16 [4, 3, 3, 2, 2, 2, 1, 1, 1]
Mode: DYN_ARR Size/Cap: 2/4 [2, 1], Frequency: 3
DYN_ARR Size/Cap: 10/16 [4, 3, 3, 2, 2, 2, 1, 1, 1, 1]
Mode: DYN_ARR Size/Cap: 1/4 [1], Frequency: 4
```

Part 2 - Summary and Specific Instructions

1. Implement a Bag ADT class by completing the skeleton code provided in the file `bag_da.py`. You will use the Dynamic Array data structure that you implemented in Part 1 of this assignment as the underlying data storage for your Bag ADT.
2. Once completed, your implementation will include the following methods:

```
add()
remove()
count()
clear()
equal()
__iter__()
__next__()
```

3. We will test your implementation with different types of objects, not just integers. We guarantee that all such objects will have correct implementation of methods `__eq__`, `__lt__`, `__gt__`, `__ge__`, `__le__`, and `__str__`.
4. The number of objects stored in the Bag at any given time will be between 0 and 1,000,000 inclusive. The bag must allow for the storage of duplicate objects.
5. RESTRICTIONS: You are not allowed to use ANY built-in Python data structures and/or their methods. You must solve this portion of the assignment by importing the `DynamicArray` class that you wrote in Part 1 and using class methods to write your solution.

You are also **not** allowed to directly access any variables of the `DynamicArray` class (like `self.size`, `self.capacity` and `self.data` in Part 1). All work must be done using only class methods.

add(self, value: object) -> None:

This method adds a new element to the bag. It must be implemented with $O(1)$ amortized runtime complexity.

Example #1:

```
bag = Bag()
print(bag)
values = [10, 20, 30, 10, 20, 30]
for value in values:
    bag.add(value)
print(bag)
```

Output:

```
BAG: 0 elements. []
BAG: 6 elements. [10, 20, 30, 10, 20, 30]
```

remove(self, value: object) -> bool:

This method removes any one element from the bag that matches the provided `value` object. The method returns `True` if some object was actually removed from the bag. Otherwise it returns `False`. This method must be implemented with $O(N)$ runtime complexity.

Example #1:

```
bag = Bag([1, 2, 3, 1, 2, 3, 1, 2, 3])
print(bag)
print(bag.remove(7), bag)
print(bag.remove(3), bag)
print(bag.remove(3), bag)
print(bag.remove(3), bag)
print(bag.remove(3), bag)
```

Output:

```
BAG: 9 elements. [1, 2, 3, 1, 2, 3, 1, 2, 3]
False BAG: 9 elements. [1, 2, 3, 1, 2, 3, 1, 2, 3]
True BAG: 8 elements. [1, 2, 1, 2, 3, 1, 2, 3]
True BAG: 7 elements. [1, 2, 1, 2, 1, 2, 3]
True BAG: 6 elements. [1, 2, 1, 2, 1, 2]
False BAG: 6 elements. [1, 2, 1, 2, 1, 2]
```

count(self, value: object) -> int:

This method returns the number of elements in the bag that match the provided `value` object. This method must be implemented with $O(N)$ runtime complexity.

Example #1:

```
bag = Bag([1, 2, 3, 1, 2, 2])
print(bag, bag.count(1), bag.count(2), bag.count(3), bag.count(4))
```

Output:

```
BAG: 6 elements. [1, 2, 3, 1, 2, 2] 2 3 1 0
```

clear(self) -> None:

This method clears the contents of the bag. It must be implemented with $O(1)$ runtime complexity.

Example #1:

```
bag = Bag([1, 2, 3, 1, 2, 3])
print(bag)
bag.clear()
print(bag)
```

Output:

```
BAG: 6 elements. [1, 2, 3, 1, 2, 3]
BAG: 0 elements. []
```

equal(self, second_bag: object) -> bool:

This method compares the contents of a bag with the content of a second bag provided as a parameter. The method returns `True` if the bags are equal (have the same number of elements and contain the same elements without regards to the order of elements). Otherwise, it returns `False`. An empty bag is only considered equal to another empty bag. This method must not change the contents of either bag.

The runtime complexity of this implementation should be no worse than $O(N^2)$. The maximum test case size for this method will be limited to bags with 1,000 items in each.

Example #1:

```
bag1 = Bag([10, 20, 30, 40, 50, 60])
bag2 = Bag([60, 50, 40, 30, 20, 10])
bag3 = Bag([10, 20, 30, 40, 50])
bag_empty = Bag()

print(bag1, bag2, bag3, bag_empty, sep="\n")
print(bag1.equal(bag2), bag2.equal(bag1))
print(bag1.equal(bag3), bag3.equal(bag1))
print(bag2.equal(bag3), bag3.equal(bag2))
print(bag1.equal(bag_empty), bag_empty.equal(bag1))
print(bag_empty.equal(bag_empty))
print(bag1, bag2, bag3, bag_empty, sep="\n")

bag1 = Bag([100, 200, 300, 200])
bag2 = Bag([100, 200, 30, 100])
print(bag1.equal(bag2))
```

Output:

```
BAG: 6 elements. [10, 20, 30, 40, 50, 60]
BAG: 6 elements. [60, 50, 40, 30, 20, 10]
BAG: 5 elements. [10, 20, 30, 40, 50]
BAG: 0 elements. []
True True
False False
False False
False False
True
BAG: 6 elements. [10, 20, 30, 40, 50, 60]
BAG: 6 elements. [60, 50, 40, 30, 20, 10]
BAG: 5 elements. [10, 20, 30, 40, 50]
BAG: 0 elements. []
False
```

__iter__():

This method enables the Bag to iterate across itself. Implement this method similar to the example in Exploration: Encapsulation and Iterators.

You **ARE** permitted (and will need to) add a variable in this method to track the iterator's progress through the Bag's contents.

You can use either of the models shown in the Exploration - you can build the iterator functionality inside the Bag or create a separate iterator class.

Example #1:

```
bag = Bag([5, 4, -8, 7, 10])
print(bag)
for item in bag:
    print(item)
```

Output:

```
BAG: 5 elements. [5, 4, -8, 7, 10]
5
4
-8
7
10
```

__next__():

This method will return the next item in the Bag, based on the current location of the iterator. Implement this method similar to the example in Exploration: Encapsulation and Iterators.

Example #2:

```
bag = Bag(["orange", "apple", "pizza", "ice cream"])
print(bag)
for item in bag:
    print(item)
```

Output:

```
BAG: 4 elements. [orange, apple, pizza, ice cream]
orange
apple
pizza
ice cream
```