

# Curve DAO

Curve DAO consists of multiple smart contracts connected by Aragon. Apart from that, standard Aragon's 1 token = 1 vote method is replaced with the voting weight also proportional to locktime, as will be described below.

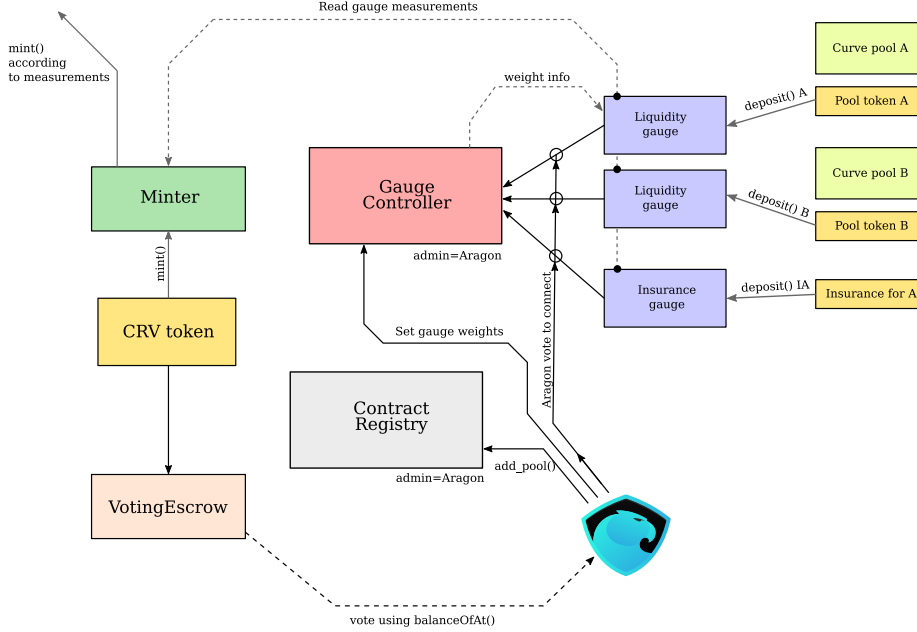


Figure 1: Curve DAO contracts managed by Aragon

Curve DAO has a token CRV which is used for both governance and value accrual.

## Time-weighted voting. Vote-locked tokens in VotingEscrow

Instead of voting with token amount  $a$ , in Curve DAO tokens are lockable in a *VotingEscrow* for a selectable locktime  $t_l$ , where  $t_l < t_{\max}$ , and  $t_{\max} = 4$  years. After locking, the time *left to unlock* is  $t \leq t_l$ . The voting weight is equal to:

$$w = a \frac{t}{t_{\max}}.$$

In other words, the vote is both amount- and time-weighted, where the time counted is how long the tokens cannot be moved in future.

The account which locks the tokens cannot be a smart contract (because can be tradable and/or tokenized), unless it is one of whitelisted smart contracts (for example, widely used multi-signature wallets).

*VotingEscrow* tries to resemble Aragon’s Minime token. Most importantly, `balanceOf()` / `balanceOfAt()` and `totalSupply()` / `totalSupplyAt()` return the time-weighted voting weight  $w$  and the sum of all of those weights  $W = \sum w_i$  respectively. Aragon can interface *VotingEscrow* as if it was a typical governance token.

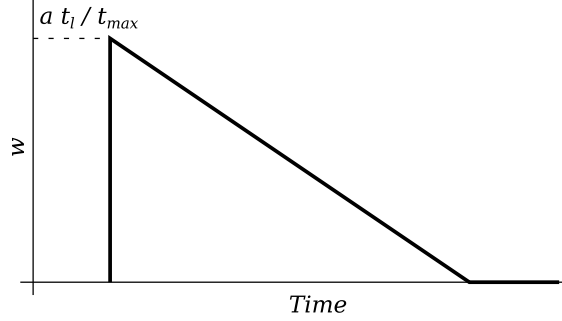


Figure 2: Voting weight of vote-locked tokens

Locks can be created or extended in time or token amount with `deposit()`, and `withdraw()` can remove tokens from the escrow when the lock is expired.

### Implementation details

User voting power  $w_i$  is linearly decreasing since the moment of lock. So does the total voting power  $W$ . In order to avoid periodic check-ins, every time the user deposits, or withdraws, or changes the locktime, we *record user’s slope and bias* for the linear function  $w_i(t)$  in `user_point_history`. We also change slope and bias for the total voting power  $W(t)$  and record in `point_history`. In addition, when user’s lock is scheduled to end, we *schedule* change of slopes of  $W(t)$  in the future in `slope_changes`.

This way we don’t have to iterate over all users to figure out, how much should  $W(t)$  change by, neither we require users to check in periodically. However, we limit the end of user locks to times rounded off by whole weeks.

### Inflation schedule. ERC20CRV

*Warning: exact numbers in the inflation schedule can still be changed!*

Token *ERC20CRV* is an ERC20 token which allows a piecewise linear inflation schedule. The inflation is dropping by  $\sqrt{2}$  every year. Only *Minter* contract can directly mint *ERC20CRV*, but only within the limits defined by inflation.

Each time the inflation changes, a new mining epoch starts.

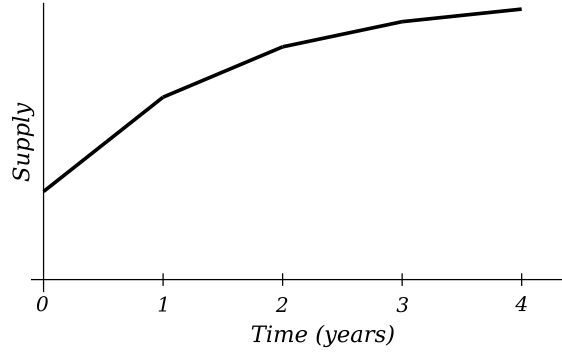


Figure 3: CRV token inflation schedule

Initial supply of CRV is 1 billion tokens, which is 33% of the eventual ( $t \rightarrow \infty$ ) supply of  $\approx 3.03$  billion tokens. The initial inflation rate which supports the above inflation schedule is  $r = 59.5\%$ . All of the inflation is distributed to users of Curve, according to measurements taken by *gauges*.

## System of Gauges. LiquidityGauge and GaugeController

In Curve, inflation is going towards users who use it. The usage is measured with Gauges. Currently there is just *LiquidityGauge* which measures, how much liquidity does the user provide. The same type of gauge can be used to measure “liquidity” provided for insurance.

For *LiquidityGauge* to measure user liquidity over time, the user deposits his LP tokens into the gauge using `deposit()` and can withdraw using `withdraw()`.

Coin rates which the gauge is getting depends on current inflation rate, and gauge *type weights* (which get voted on in Aragon). Each user gets inflation proportional to his LP tokens locked. Additionally, the rewards could be *boosted* by up to factor of 5 if user vote-locks tokens for Curve governance in *VotingEscrow*.

The user *does not* require to periodically check in. We describe how this is achieved in technical details.

*GaugeController* keeps a list of Gauges and their types, with weights of each gauge and type.

Gauges are per pool (each pool has an individual gauge).

## LiquidityGauge implementation details

Suppose we have the inflation rate  $r$  changing with every epoch (1 year), gauge weight  $w_g$  and gauge type weight  $w_t$ . Then, all the gauge handles the stream

of inflation with the rate  $r' = w_g w_t r$  which it can update every time  $w_g$ ,  $w_t$ , or mining epoch changes.

In order to calculate user's fair share of  $r'$ , we essentially need to calculate the integral:

$$I_u = \int \frac{r'(t) b_u(t)}{S(t)} dt,$$

where  $b_u(t)$  is the balance supplied by user (measured in LP tokens) and  $S(t)$  is total liquidity supplied by users, depending on the time  $t$ ; the value  $I_u$  gives the amount of tokens which user has to have minted to him. The user's balance  $b_u$  changes every time user  $u$  makes a deposit or withdrawal, and  $S$  changes every time *any* user makes a deposit or withdrawal (so  $S$  can change many times in between two events for the user  $u$ ). In *LiquidityGauge* contract, the value of  $I_u$  is recorded in the `integrate_fraction` map, per-user.

In order to avoid all users to checkpoint periodically, we keep recording values of the following integral (named `integrate_inv_supply` in the contract):

$$I_{is}(t) = \int_0^t \frac{r'(t)}{S(t)} dt.$$

The value of  $I_{is}$  is recorded at any point any user deposits or withdraws, as well as every time the rate  $r'$  changes (either due to weight change or change of mining epoch).

When a user deposits or withdraws, the change in  $I_u$  can be calculated as the current (before user's action) value of  $I_{is}$  multiplied by the pre-action user's balance.

In order to incentivize users to participate in governance, and additionally create stickiness for liquidity, we implement the following mechanism. User's balance counted in the *LiquidityGauge* gets boosted by users locking CRV tokens in *VotingEscrow*, depending on their vote weight  $w_i$ :

$$b_u^* = \min \left( 0.2 b_u + 0.8 S \frac{w_i}{W}, b_u \right).$$

The value of  $w_i$  is taken at the time user performs any action (deposit, withdrawal, withdrawal of minted CRV tokens) and is applied until the next action this user performs.

If no users vote-lock any CRV (or simply don't have any), the inflation will simply be distributed proportionally to the liquidity  $b_u$  each one of them provided. However, if a user stakes much enough CRV, he is able to boost his stream of CRV by up to factor of 5 (reducing it slightly for all users who are not doing that).

## **GaugeController implementation details**

### **Weight voting for gauges**

Instead of simply voting for weight change in Aragon, users can allocate their vote-locked tokens towards one or other Gauge (pool). That pool will be getting a fraction of CRV tokens minted proportional to how much vote-locked tokens are allocated to it. Each user with tokens in VotingEscrow can change his/her preference at any time.