

COMP26120 Lab 10

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1 The small-world hypothesis

I think the small-world hypothesis is false, and I will test for it by checking:

for each 2 people in the graph, try to find a shortest path whose length is less than 6.

2 Complexity Arguments

Compare time complexity of Dijkstra and Floyd algorithm:

Dijkstra using priority queue has the complexity of $O((|E| + |V|) \log |V|)$, where E is the number of edges, and V is the number of vertexes. We also need to apply Dijkstra for every pair of vertexes, which means that the overall complexity would be $O(|V| * ((|E| + |V|) \log |V|))$.

Floyd has the complexity of $O(|V|^3)$, where V is the number of vertexes.

And we can approximately calculate the scale of time for Caltech.gx and Oklahoma.gx using Dijkstra and Floyd:

Dijkstra: $O(|V| * ((|E| + |V|) \log |V|))$

(1) Caltech.gx: $769 * ((33312 + 769) * \log(769)) = 251,254,668$

(2) Oklahoma.gx: $17425 * ((1785056 + 17425) * \log(17425)) = 442,506,552,000$

Floyd: $O(|V|^3)$

(1) Caltech.gx: $769^3 = 454,756,609$

(2) Oklahoma.gx: $17425^3 = 5,290,763,640,625$

We can see from the approximation calculated using time complexity, Dijkstra algorithm is much less than Floyd algorithm, so Dijkstra algorithm is more efficient.

3 Part 2 results

Statistics of Caltech.gx and Oklahoma.gx:

Caltech: Time: 0.43s,

Average unreachable: 13.91,

Average larger than six: 0,

Average distance: 2.32,

Conclusion: it is not a "small world".

Oklahoma: Time: 2583.18s,

Average unreachable: 10,

Average larger than six: 0.19,

Average distance: 2.77,

Conclusion: it is not a "small world".

Compare Caltech.gx and Oklahoma.gx:

According to the time scale we calculated in part1, time scale of Oklahoma.gx is $442,506,552,000/251,254,668 = 1761.19$ times larger than Caltech.gx, and according to the execution time we recorded, Oklahoma is $2583.18/0.43 = 6007.4$ times longer than Caltech.gx, which is considered to be agreed with the time complexity if we consider some small issues like different execution environment(server cpu), constant factor, initialize arrays to zeros, etc.

4 Part 3 results

Statistics of Caltech.gx and Oklahoma.gx:

Caltech:

Time: 0.38s,

Average unreachable: 36.81,

Average larger than six: 208.93,

Average distance: 15.50,

Conclusion: it is not a "small world".

Oklahoma:

Time: 497.64s,

Average unreachable: 3164.17,

Average larger than six: 8766.88,

Average distance: 67.67,

Conclusion: it is not a "small world".

5 Conclusions

Conclusions of experiments of part2 and part3:

Part2:

Both Caltech.gx and Oklahoma.gx are not "small world", the graphs have some "isolated" people that cannot be reached. Apart from that, there are not much distance more than six shortest paths in these two graphs. So in my opinion, these two graphs are close to "small world" but they are not.

Part3:

Compared with part2, the number of average unreachable nodes and average shortest distance between nodes and the number of distance larger than six nodes has increased a lot, the time complexity and running for this algorithm is lower, however, the actual results we get have limited accuracy. We have so

many nodes that is miscalculated as unreachable, not to mention distance larger than six nodes, especially when we implement this on a graph with large scale.

To what extent it works:

We can evaluate the algorithm compared with Dijkstra (miscalculated rate: "0" regarded as perfect):

Caltech: $((36.81 + 208.93) - (13.91 + 0))/769 = 30.1\%$

Oklahoma: $((3164.17 + 8766.88) - (10 + 0.19))/17425 = 68.4\%$

So we can see that the algorithm become worse when the scale of graph becomes larger.