



$$\vec{a}_A = \ddot{x} \hat{i}$$

$$F - F_{1x} = M \ddot{x}$$

$$N - F_{1y} = 0$$

$$\begin{aligned} \vec{a}_B &= \frac{l_1}{2} \ddot{\theta}_1 (\cos \theta_1 \hat{i} - \sin \theta_1 \hat{j}) - \frac{l_1}{2} \dot{\theta}_1^2 (\sin \theta_1 \hat{i} + \cos \theta_1 \hat{j}) + \vec{a}_A \\ &= \left(\frac{l_1}{2} \ddot{\theta}_1 \cos \theta_1 - \frac{l_1}{2} \dot{\theta}_1^2 \sin \theta_1 \right) \hat{i} + \left(-\frac{l_1}{2} \ddot{\theta}_1 \sin \theta_1 - \frac{l_1}{2} \dot{\theta}_1^2 \cos \theta_1 \right) \hat{j} \end{aligned}$$

$$F_{1x} - F_{2x} = m_1 \frac{l_1}{2} (\ddot{\theta}_1 \cos \theta_1 - \dot{\theta}_1^2 \sin \theta_1) + m_1 \ddot{x}$$

$$F_{1y} - F_{2y} - m_1 g = m_1 \frac{l_1}{2} (-\ddot{\theta}_1 \sin \theta_1 - \dot{\theta}_1^2 \cos \theta_1)$$

$$F_{1x} \frac{l_1}{2} \cos \theta_1 + F_{2x} \frac{l_1}{2} \cos \theta_1 - F_{1y} \frac{l_1}{2} \sin \theta_1 - F_{2y} \frac{l_1}{2} \sin \theta_1 = -I_1 \ddot{\theta}_1$$

(2)

$$\vec{a}_c = (\ddot{x} + l_1 \ddot{\theta}_1 \cos \theta_1, -l_1 \dot{\theta}_1^2 \sin \theta_1) \vec{i} + (-l_1 \ddot{\theta}_1 \sin \theta_1, -l_1 \dot{\theta}_1^2 \cos \theta_1) \vec{j}$$

$$\vec{a}_D = \vec{a}_c + \frac{l_2}{s} \ddot{\theta}_2 (\cos \theta_2 \vec{i} - \sin \theta_2 \vec{j}) - \frac{l_2}{s} \dot{\theta}_2^2 (\sin \theta_2 \vec{i} + \cos \theta_2 \vec{j})$$

$$= (\ddot{x} + l_1 \ddot{\theta}_1 \cos \theta_1, -l_1 \dot{\theta}_1^2 \sin \theta_1 + \frac{l_2}{s} \ddot{\theta}_2 \cos \theta_2 - \frac{l_2}{s} \dot{\theta}_2^2 \sin \theta_2) \vec{i}$$

$$+ (-l_1 \ddot{\theta}_1 \sin \theta_1 - l_1 \dot{\theta}_1^2 \cos \theta_1, -\frac{l_2}{s} \ddot{\theta}_2 \sin \theta_2 - \frac{l_2}{s} \dot{\theta}_2^2 \cos \theta_2) \vec{j}$$

$$F_{2x} = m_2 (\vec{a}_D)_x$$

$$F_{2y} - m_2 g = m_2 (\vec{a}_D)_y$$

$$F_{2x} \frac{l_2}{s} \cos \theta_2 - F_{2y} \frac{l_2}{s} \sin \theta_2 = -I_2 \ddot{\theta}_2$$

F	F _{1x}	F _{1y}	F _{2x}	F _{2y}
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1	-1			
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	1			
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		-1		
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			1	
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				-1
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				1
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$$M \ddot{x}$$

$$m_1 \ddot{x} + m_1 \frac{l_1}{s} \ddot{\theta}_1 \cos \theta_1 - m_1 \frac{l_1}{s} \dot{\theta}_1^2 \sin \theta_1$$

$$m_1 g - m_1 \frac{l_1}{s} \ddot{\theta}_1 \sin \theta_1 - m_1 \frac{l_1}{s} \dot{\theta}_1^2 \cos \theta_1$$

$$m_2 \ddot{x} + m_2 l_1 \ddot{\theta}_1 \cos \theta_1 - m_2 l_1 \dot{\theta}_1^2 \sin \theta_1 + m_2 \frac{l_2}{s} \ddot{\theta}_2 \cos \theta_2 - m_2 \frac{l_2}{s} \dot{\theta}_2^2 \sin \theta_2$$

$$m_2 g - m_2 l_1 \dot{\theta}_1^2 \sin \theta_1 - m_2 l_1 \ddot{\theta}_1 \cos \theta_1 - m_2 \frac{l_2}{s} \ddot{\theta}_2 \sin \theta_2 - m_2 \frac{l_2}{s} \dot{\theta}_2^2 \cos \theta_2$$

$$F = (M + m_1 + m_2) \ddot{x} + (m_1 \frac{l_1}{s} + m_2 l_1) \cos \theta_1 \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \cos \theta_2 \ddot{\theta}_2 - (m_1 \frac{l_1}{s} + m_2 l_1) \sin \theta_1 \dot{\theta}_1^2 - (m_2 \frac{l_2}{s}) \sin \theta_2 \dot{\theta}_2^2 \quad (3) \quad - (1)$$

$$F_{ix} = (m_1 + m_2) \ddot{x} + (m_1 \frac{l_1}{s} + m_2 l_1) \cos \theta_1 \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \cos \theta_2 \ddot{\theta}_2 - (m_1 \frac{l_1}{s} + m_2 l_1) \sin \theta_1 \dot{\theta}_1^2 - (m_2 \frac{l_2}{s}) \sin \theta_2 \dot{\theta}_2^2$$

$$F_{iy} = (m_1 + m_2) g - (m_1 \frac{l_1}{s} + m_2 l_1) \sin \theta_1 \ddot{\theta}_1 - (m_2 \frac{l_2}{s}) \sin \theta_2 \ddot{\theta}_2 - (m_1 \frac{l_1}{s} + m_2 l_1) \cos \theta_1 \dot{\theta}_1^2 - (m_2 \frac{l_2}{s}) \cos \theta_2 \dot{\theta}_2^2$$

$$F_{2x} = (m_2) \ddot{x} + (m_2 l_1) \cos \theta_1 \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \cos \theta_2 \ddot{\theta}_2 - (m_2 l_1) \sin \theta_1 \dot{\theta}_1^2 - (m_2 \frac{l_2}{s}) \sin \theta_2 \dot{\theta}_2^2$$

$$F_{2y} = (m_2) g - (m_2 l_1) \sin \theta_1 \ddot{\theta}_1 - (m_2 \frac{l_2}{s}) \sin \theta_2 \ddot{\theta}_2 - (m_2 l_1) \cos \theta_1 \dot{\theta}_1^2 - (m_2 \frac{l_2}{s}) \cos \theta_2 \dot{\theta}_2^2$$

$$F_{ix} \cos \theta_1 - F_{iy} \sin \theta_1 + F_{2x} \cos \theta_1 - F_{2y} \sin \theta_1 = -I_1 \ddot{\theta}_1 \frac{1}{l_1}$$

$$(m_1 + m_2) \cos \theta_1 \ddot{x} - (m_1 + m_2) \sin \theta_1 g + (m_1 \frac{l_1}{s} + m_2 l_1) \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \cos (\theta_2 - \theta_1) \ddot{\theta}_2 - (m_2 \frac{l_2}{s}) \sin (\theta_2 - \theta_1) \dot{\theta}_2^2 \\ (m_2) \cos \theta_1 \ddot{x} - (m_2) \sin \theta_1 g + (m_2 l_1) \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \cos (\theta_2 - \theta_1) \ddot{\theta}_2 - (m_2 \frac{l_2}{s}) \sin (\theta_2 - \theta_1) \dot{\theta}_2^2 = -I_1 \ddot{\theta}_1 \frac{1}{l_1}$$

$$(m_1 \frac{l_1}{s} + m_2 l_1) \cos \theta_1 \ddot{x} - (m_1 \frac{l_1}{s} + m_2 l_1) \sin \theta_1 g + (I_1 + m_1 \frac{l_1^2}{4} + m_2 l_1^2) \ddot{\theta}_1 + (m_2 \frac{l_1 l_2}{s}) \cos (\theta_2 - \theta_1) \ddot{\theta}_2 - (m_2 \frac{l_1 l_2}{s}) \sin (\theta_2 - \theta_1) \dot{\theta}_2^2 = 0$$

$$F_{2x} \cos \theta_2 - F_{2y} \sin \theta_2 = -I_2 \ddot{\theta}_2 \frac{1}{l_2} \quad - (2)$$

$$(m_2) \cos \theta_2 \ddot{x} - (m_2) \sin \theta_2 g + (m_2 l_1) \cos (\theta_2 - \theta_1) \ddot{\theta}_1 + (m_2 \frac{l_2}{s}) \ddot{\theta}_2 - (m_2 l_1) \sin (\theta_2 - \theta_1) \dot{\theta}_1^2 = -I_2 \ddot{\theta}_2 \frac{1}{l_2}$$

$$(m_2 \frac{l_2}{s}) \cos \theta_2 \ddot{x} - (m_2 \frac{l_2}{s}) \sin \theta_2 g + (m_2 \frac{l_1 l_2}{s}) \cos (\theta_2 - \theta_1) \ddot{\theta}_1 + (I_2 + m_2 \frac{l_2^2}{4}) \ddot{\theta}_2 - (m_2 \frac{l_1 l_2}{s}) \sin (\theta_2 - \theta_1) \dot{\theta}_1^2 = 0 \quad - (3)$$