

**CSCI 136**

**Data Structures &**

**Advanced Programming**

**Lab : Exam Scheduling**

# High-level Overview

**Input:** a set of student schedules

**Output:** a schedule (set of time slots) for exams where

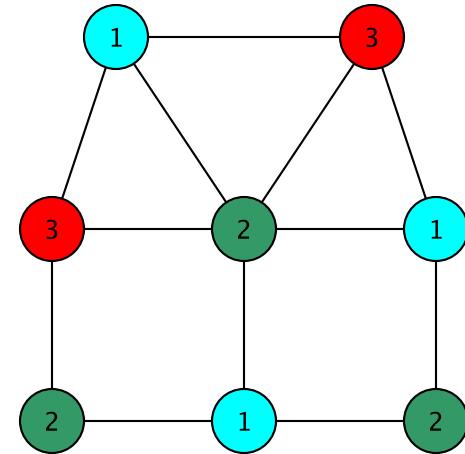
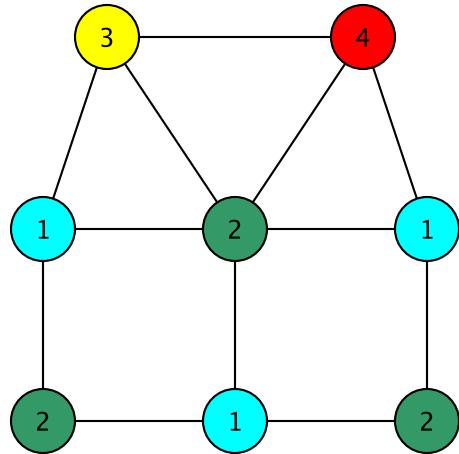
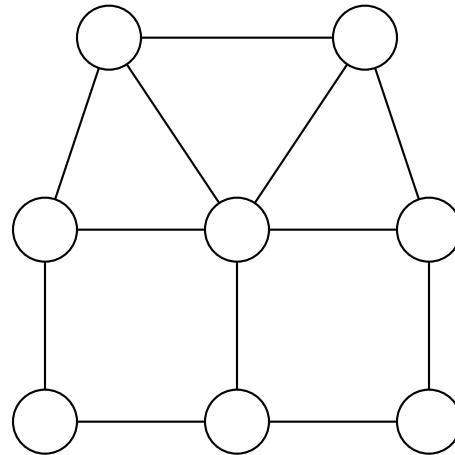
- Every course is in some time slot
- No student has two exams in the same time slot
- The number of time slots is as small as possible

We can complete this task by representing the data using a graph, and then manipulating the graph using a **greedy algorithm**.

# Greedy Algorithms

- A **greedy algorithm** attempts to find a **globally** optimum solution to a problem by making **locally** optimum (greedy) choices
- Example: **Graph Coloring**
  - A (proper) **coloring** of a graph  $G = (V, E)$  is an assignment of a value (color) to each vertex so that adjacent vertices get different values (colors)
  - (Typically, we would try to minimize the number of colors we use)

# Greedy Coloring



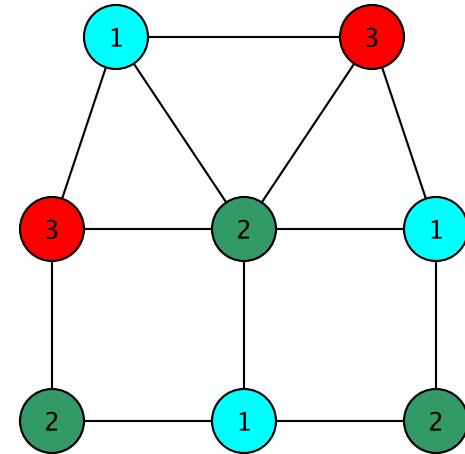
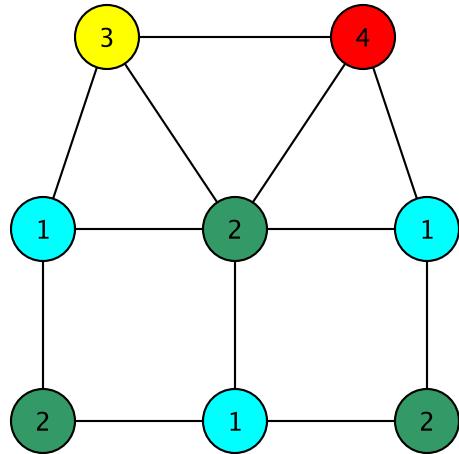
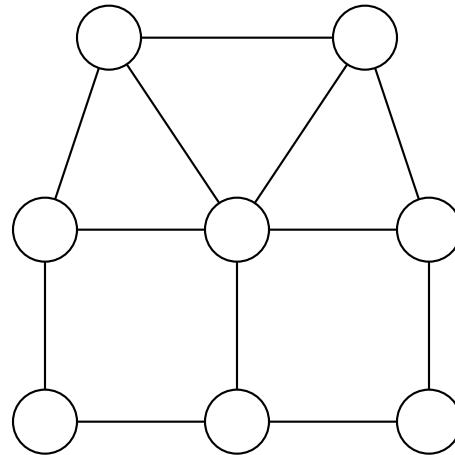
# Greedy Coloring : Pseudocode

(Builds a structure C of lists of vertices, where each list represents vertices of a single “color”)

```
let C = a structure to hold a collection of lists  
while G is not empty:
```

```
    let L = a new empty list;  
    pick some vertex v in G;  
    L.add(v);  
    for each vertex u ≠ v in G:  
        if u is not adjacent to any vertex of L:  
            add u to L  
    remove all vertices of L from G  
    add L to C  
Return C as the coloring
```

# Greedy Coloring



# Greedy Coloring Observations

- Each list (color class)  $L$  is a set of vertices, no two of which are adjacent (an *independent set*)
- Each color class is **maximal**: cannot be made any larger (if it could have, we would have added that vertex to our list!)
  - The hope is that this results in fewer colors being needed
  - But the solution is not always optimum!

# Lab : Exam Scheduling

**Goal:** Find a schedule (set of time slots) for exams so that

- No student has two exams in the same time slot
- Every course appears in exactly one time slot
- The number of time slots is as small as possible

This is just the graph coloring problem in disguise!

- Each course is a vertex
- Two vertices are adjacent if the courses share student(s)
- A slot must be an independent set of vertices (that is, a color class)

# Lab Notes: Using Graphs

- Create a new graph in structure5:
  - GraphListDirected, GraphListUndirected,
  - GraphMatrixDirected, GraphMatrixUndirected

```
Graph<V,E> conflictGraph = new GraphListUndirected<V,E>();
```

# Lab : Useful Graph Methods

- `void add(V label)`
  - add vertex to graph
- `void addEdge(V vtx1, V vtx2, E label)`
  - add edge between vtx1 and vtx2
- `Iterator<V> neighbors(V vtx1)`
  - Get iterator for all neighbors to vtx1
- `boolean isEmpty()`
  - Returns true iff graph is empty
- `Iterator<V> iterator()`
  - Get vertex iterator
- `V remove(V label)`
  - Remove a vertex from the graph
- `E removeEdge(V vLabel1, V vLabel2)`
  - Remove an edge from graph