

## CSCI 361: Reading Assignment # 14

Your Name: Kunal Pal

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

The variable gadget is diamond-shaped. Depending on whether or not we select a variable  $x_i$  or  $\bar{x}_i$  in clause  $c_j$ , we can detour at a point to get either True or False.

2. What is the clause gadget? How is it connected to the variable gadgets?

The clause gadget is a node. Ultimately, each diamond structure contains a horizontal row of nodes connected by edges in both directions. If a variable  $x_i$  appears in clause  $c_j$ , we add two edges from the  $j^{\text{th}}$  pair in the  $i^{\text{th}}$  diamond to the  $j^{\text{th}}$  clause node.

# CSCI 361: Reading Assignment # 14

Your Name: Noah Cafe

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

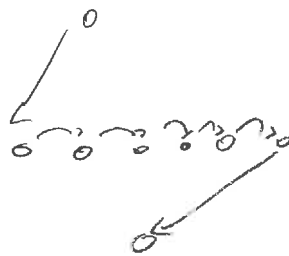
- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

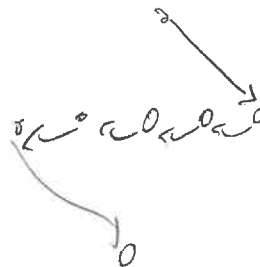
## Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

Diamond shape and path of nodes is circle.



TRUE



FALSE

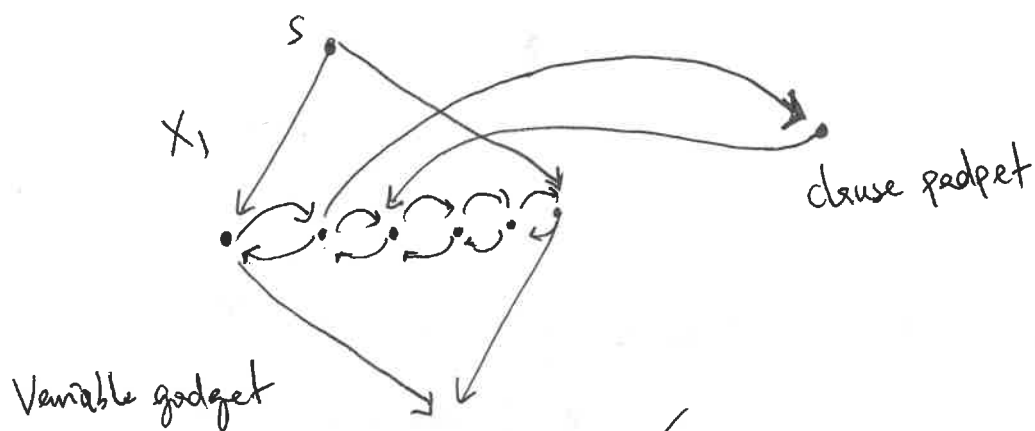
2. What is the clause gadget? How is it connected to the variable gadgets?

For each variable in the path of the diamond there is a clause node that connects input to the node in the path it is in that clause.

## Reading Assignment #14

1) What shape is the variable gadget? How does the order in w/c this shape is traversed correspond to the truth value of the corresponding variable?

⇒ Diamond shape



⊗ If we traverse the graph in this way, we can hit the (zigzag) clause gadget so making the corresponding variable true.

2) What is the clause gadget? How is it connected to variable gadgets?

⇒ Clause gadget is just one of the nodes which forces the graph to make a detour by setting  $x_i$  to be true

## CSCI 361: Reading Assignment # 14

Your Name: Ahmed Hussain

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

The variable gadget is a diamond structure corresponding to the two truth settings. The clause gadget is which can be traversed in either of two ways, corresponding to the two truth values.

2. What is the clause gadget? How is it connected to the variable gadgets?

The clause gadget is a node. If variable  $x_i$  appears in clause  $c_j$ , we add the two edges from the  $j$ th pair in the  $i$ th diamond to the  $j$ th clause.

## CSCI 361: Reading Assignment # 14

Your Name: Ben Lin

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

Diamond shaped

if true, zig-zag left to right

if false, zag-zig

2. What is the clause gadget? How is it connected to the variable gadgets?

node for each clause connected to  
the node pair in ~~the~~ a horizontal row  
in the variable gadgets

# CSCI 361: Reading Assignment # 14

Your Name: Lola Kowalski

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

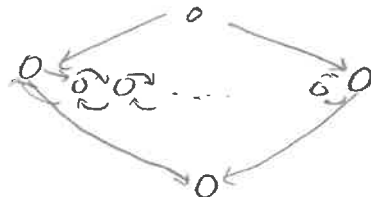
- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

## Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

variable gadget  $\rightarrow$  diamond structure



if variable is true it goes like

" " " false it goes like

2. What is the clause gadget? How is it connected to the variable gadgets?

clause gadget is a single node  $\circ$

If  $x_i$  appears in clause  $c_j$  you make edges from  $j^{\text{th}}$  position in diamond to  $j^{\text{th}}$  clause node like



if  $\bar{x}_i$  order is reversed



## CSCI 361: Reading Assignment # 14

Your Name: Juan Mendez

Due: Tuesday, Nov 19, in class



Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

The variable gadget has a diamond structure w/ a horizontal line of nodes. If  $x_i$  is True, the diamond is traversed in a zig-zag: . If  $x_i$  is False, the diamond is traversed in a "zag-zig": .

2. What is the clause gadget? How is it connected to the variable gadgets?

The clause gadget is just a singular node. Each clause in the Boolean statement has a corresponding node. The clause nodes are connected to the variable gadgets via edges to pairs of nodes in the diamonds.

## CSCI 361: Reading Assignment # 14

Your Name: Prairie

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

Diamond — If the gadget is assigned TRUE, the gadget is traversed left-to-right, right-to-left if FALSE

2. What is the clause gadget? How is it connected to the variable gadgets?

The clause gadget is a single node connected to the variable gadget if  $x_i \in \text{clause } c_j$ , or connected reversely if  $\bar{x}_i \in c_j$ .



## CSCI 361: Reading Assignment # 14

Your Name: Jarin Sutton

Due: Tuesday, Nov 19, in class

Assigned reading for this lecture:

- Sipser Third Edition 7.5 (Additional NP Complete Problems)

Read the Reduction from 3SAT to HAMPATH (Theorem 7.46).

### Questions:

1. What shape is the variable gadget? How does the order in which this shape is traversed correspond to the truth value of the corresponding variable?

The shape of the variable gadget is a diamond.  
One direction corresponds to a truth value of true.  
The other direction corresponds to a truth value of false.

2. What is the clause gadget? How is it connected to the variable gadgets?

The clause gadget is a node.  
If a clause is satisfied, then a path runs through.