Acceptance Study for SciBooNE Charged-Current Coherent Pion Production Technical Note Rough Draft

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Abstract

We showed that the SciBooNE guys tried to mess physics up by cutting out all of their CC-Coh Pion events from their data that was actually there! Duh.

Do we need an abstract?

1 Introduction

The goal of this document is to provide a reference for the acceptance study performed for the SciBooNE charged current coherent pion re-analysis as well as provide documentation to the code used in this study (in the event anything needs to be revisited in the future).

The code currently lives in this github repository labeled SciBooNE-MC and the corresponding ROOT files used in the simulation can be downloaded from here (insert dropbox/Google Drive Link here)

The paper is structured such that Section 2 outlines samples used in this study, Section 3 describes the SciBooNE detector as it was simulated in this study, Section 5 gives a high level summary of the results including the event-reduction table as well as the CC-Coh-π acceptance results.

Sections **??** - **??** provide supporting plots which are used to generate the acceptance tables found in Section **??**.

The appendix is left to explain how the code is run and the details of the scripts within.

1.1 Goal

The goal of the reanalysis is to examine the acceptance modeling for the SciBooNE results in the presence of modern neutrino generators and updated models in order to understand why SciBooNE did not observe Charged-Current Coherent Pion Production at low neutrino energy. The purpose of this acceptance study is to blah blah blah... (coming back to this later...)

2 Samples

Five different samples were used in this study, three samples for ν-mode and two samples in $\bar{\nu}$-mode.[1] Table 1 summarizes these samples. Details on these samples can be found in Appendix

[1]All of these samples were generated by Callum Wilkinson (Thanks, Callum!)

Summary of samples

Mode	NEUT version	Pion-Model	Number of simulated events
ν	5.3.6	Rein-Sehgal	1,000,000
ν	5.3.6	Berger-Sehgal	1,000,000
ν	x.x.x	Rein-Sehgal	100,000
$\bar{\nu}$	5.3.6	Rein-Sehgal	1,000,000
$\bar{\nu}$	5.3.6	Berger-Sehgal	1,000,000

Table 1: Summary of the samples used to build the acceptance model for this study.

3 Simulation

This section is intended to detail the nuances of this acceptance model, and to detail what assumptions are made in the acceptance modeling to result in accurate classifications of events as Charged-Current Coherent Pion Production.

3.1 The Detector

For the purposes of this acceptance study, the SciBooNE experiment is composed of two sub-detectors. The first (and the more upstream) of the sub-detectors, is the Scintillator Bar Tracker (SciBar) which was originally conceived and constructed to function as the near detector for the K2K experiment [reference]. The second (and more downstream) of the sub-detectors, is the Muon Range Detector (MRD), which is the detector designed and constructed specifically for SciBooNE for measuring the momentum of muons produced from charged-current neutrino interactions up to 1.2 GeV/c by using the observed range of the trajectory of the muon. These detectors and the corresponding coordinate system we will use throughout this note are shown in Figure 3.1

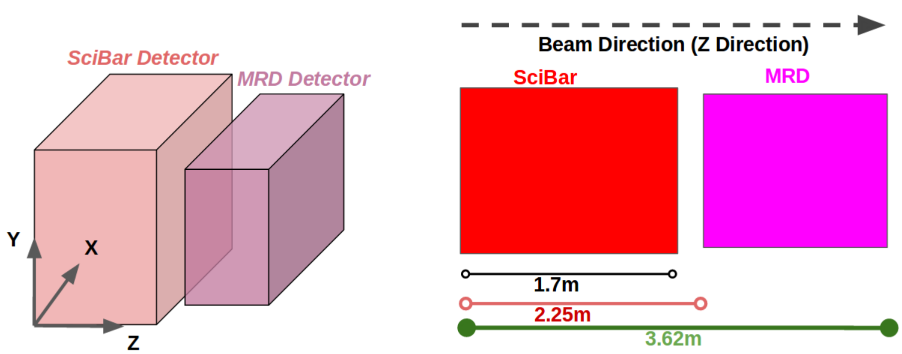


Figure 1: Representation of the SciBooNE detector and the coordinate frame we use in this study

3.1.1 The Scintillator Bar Tracker (SciBar)

The Scintillator Bar Tracker (SciBar) sub-detector is a scintillator detector (go into more detail?). In this acceptance study, the z-direction starts at 0 at the front face of the SciBar sub-detector. The direction of the beam is in the z-direction, which means the xy-plane is perpindicular to the beam. The dimensions of the sub-detector have the x and y dimensions of the same length of 3.0 m. The z dimension is 1.7 m. This simulation models the scintillator materials as having a constant energy depostion (dE/dx) value of 2.04 MeV/cm.

3.1.2 The Muon Range Detector (MRD)

The Muon Range Detector (MRD), depicted in Figure 3.1.2 is located 0.55 m downstream of SciBar in the z-direction, and is a composition of 2 sets of 13 alternating slabs of steel-scintillator layers, where the scintillator layers alternate between being horizontally oriented or vertically oriented, in the xy-plane. The steel layers have a z-direction thickness of 5.08 cm and the scintillator layers have a z-direction thickness of 0.6 cm. Combining all the layers of the different alternating materials results in 26 scintillator layers that "sandwich" 25 steel layers inbetween and gives a total z-direction dimension of being 1.37m. The xy-plane is modeled as a square again (as was the case with SciBar, too) with dimensions in the x-direction and the y-direction of 2.6 m. The energy deposition (dE/dx) of the muon for the scintillator layers is again a constant of 2.04 MeV/cm and the energy deposition for the steel layers are a constant with value 11.43 MeV/cm.

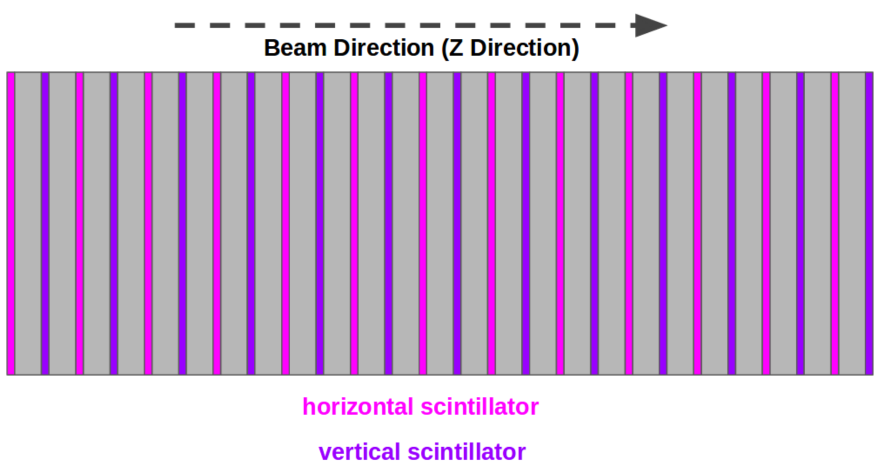


Figure 2: Depiction of the Muon Range Detector (MRB) which consists of alternating layers of horizontal scintillator (shown in pink) steel slabs (showin in grey) and vertical scintillator (shown in purple)

4 Event Selection

4.1 Event Classifications

There were three different classifications for events that qualified as CC-Coh Pion Production events, that the muon made it to the MRD, and the muon penetrated at least three layers of steel. These categories will be referenced multiple times throughout the remainder of this paper, which makes pertinent that the reader has an understanding of what each of the three specifically mean for any event that falls under any of these classifications.

4.1.1 Stopped

An event is classified as "Stopped," if the event qualified as being a CC-Coh Pion Production event, the muon of the event reached the MRD, penetrated three layers of steel, and stopped (or embedded) in the MRD without exiting the sides or the back face. Events that are classified as "Stopped" are included in the combined samples of this acceptance study and are called "Good" events. Maybe put in the dimensions of the xy-plane and z-direction that meet this classification for the MRD? This is shown in the figure below.

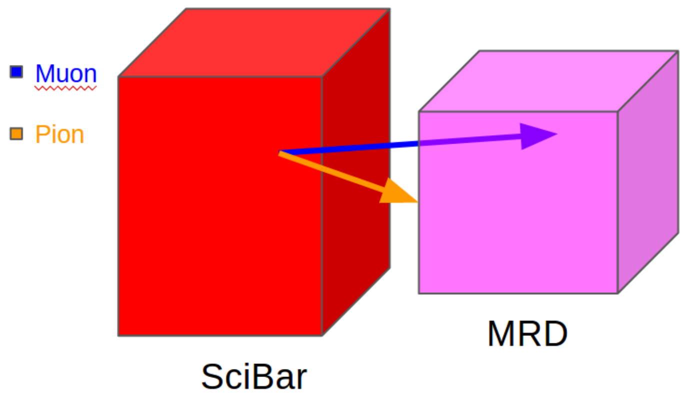


Figure 3: Depiction of an event that was classified as "Stopped."

4.1.2 Not-Stopped

An event is classified as "Not-Stopped," if the event qualified as being a CC-Coh Pion Production event, the muon of the event reached the MRD, and the muon passed out the back face of the MRD without stopping. Events that are classified as "Not-Stopped" are included in the combined samples of this acceptance study and are also called "Good" events. Maybe put in the dimensions of the xy-plane and z-direction that meet this classification for the MRD? This is shown in the figure below.

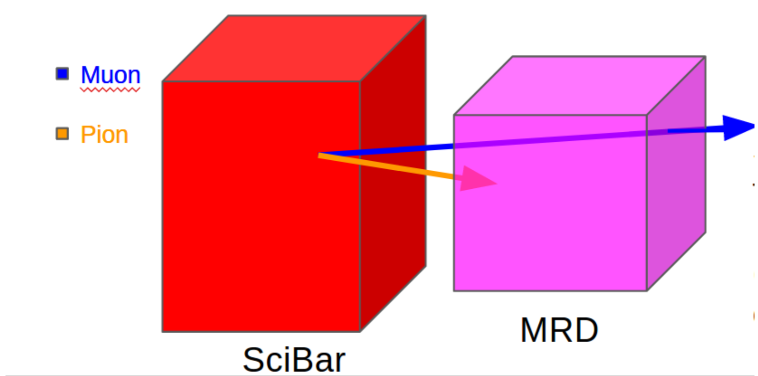


Figure 4: Depiction of an event that was classified as "Not-Stopped."

4.1.3 Out-Side

An event is classified as "Out-Side," if the event qualified as being a CC-Coh Pion Production event, the muon of the event reached the MRD, penetrated three layers of steel, and then passed through one of the sides of the MRD (not including the back face) without stopping. Events that are classified as "Out-Side" are not included in the combined samples because there was not enough material traversal for an accurate reconstruction of the particles momentum and energy to be made. Maybe put in the dimensions of the xy-plane and z-direction that meet this classification for the MRD? This is shown in the figure below.

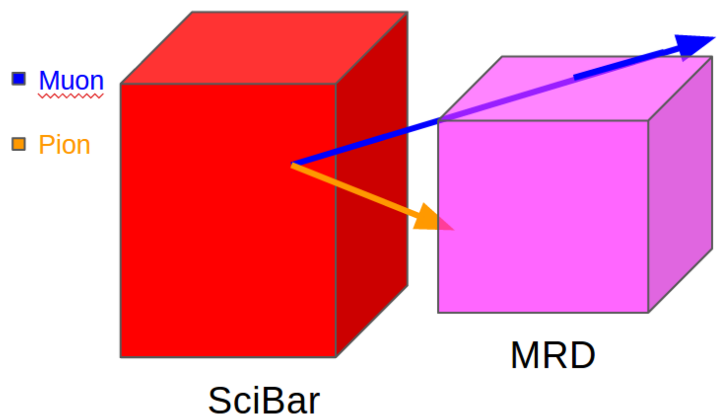


Figure 5: Depiction of an event that was classified as "Out-Side."

4.2 Stepping Through the Detectors Along an Event

I do not know if I am really going to include this here or not...

5 Results

The results of this acceptance study can be broken down into two different classification schemes of events. Those that met the conditions to qualify as a CC-Inclusive event, and those that met the conditions of classification as Charged-Current Coherent Pion Production events. The plots in the two subsections below show our results.

5.1 Charged-Current Inclusive Events

(You should show the momentum and angle spectrum for the CC-inclusive sample and show that your reproduce the previous efficiency curves)

5.2 Charged-Current Coherent Pion Production Events

(Again, you show the momentum and angle spectrum. You show the 1-d efficiencies and you have the 2-d efficiency plots AND A TABLE WHICH LISTS THEM (this is the biggest piece that is missing and I was expecting to see), here you also include the q2 and |t| distributions and their definitions.)

Table 2: Table for 2D Histogram for New NM-Rein-Sehgal

New NM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0	0	0	0.09375	0.259259	0.26087	0.317073	0.45	0.553846	0.716049	0.816092	0.828829	0.842975	0.845455	0.773438	0.875	0.796748	0.798611	0.870504	0.819549
4.5-9 Deg	0	0	0	0.123457	0.244681	0.218182	0.40411	0.490291	0.568376	0.766102	0.824047	0.789617	0.844186	0.80404	0.828302	0.807771	0.816514	0.820841	0.809981	0.79823
9-13.5 Deg	0	0	0	0.0280374	0.150943	0.31	0.334426	0.479167	0.582	0.693122	0.795417	0.787402	0.784336	0.786013	0.779396	0.757746	0.77907	0.784038	0.763083	0.776828
13.5-18 Deg	0	0	0	0.0696203	0.164502	0.242902	0.389937	0.460102	0.524072	0.648363	0.73062	0.742788	0.7373	0.725131	0.707711	0.713192	0.708657	0.71437	0.713376	0.722747
18-22.5 Deg	0	0	0	0.0396825	0.134503	0.220374	0.320233	0.4	0.498252	0.56578	0.666667	0.703245	0.681216	0.694102	0.67205	0.674541	0.661496	0.647185	0.673965	0.656648
22.5-27 Deg	0	0	0	0.0341615	0.120614	0.20088	0.284783	0.356223	0.442424	0.513469	0.590521	0.619898	0.653967	0.628604	0.61255	0.617109	0.601285	0.58894	0.579674	0.578595
27-31.5 Deg	0	0	0	0.0128535	0.0852575	0.146399	0.240517	0.328982	0.381593	0.467435	0.496599	0.55869	0.57336	0.536199	0.537204	0.545332	0.542526	0.532462	0.524605	0.503756
31.5-36 Deg	0	0	0	0.00618557	0.047749	0.138308	0.215553	0.260465	0.322889	0.379459	0.44563	0.489885	0.50075	0.5	0.512734	0.486242	0.465472	0.455387	0.439182	0.459893
36-40.5 Deg	0	0	0	0	0.0376749	0.104341	0.167825	0.228974	0.272658	0.326716	0.35271	0.399772	0.4	0.410602	0.420808	0.416728	0.404237	0.378892	0.371585	0.362308
40.5-45 Deg	0	0	0	0	0.0185547	0.0617036	0.129648	0.175194	0.22549	0.249335	0.297987	0.31442	0.331903	0.342802	0.33975	0.324022	0.312566	0.299735	0.293671	0.284258
45-49.5 Deg	0	0	0	0	0.00241935	0.0461908	0.0861688	0.129907	0.177771	0.209127	0.220634	0.249649	0.260561	0.269592	0.273593	0.258347	0.252889	0.239492	0.238606	0.221135
49.5-54 Deg	0	0	0	0	0	0.0115123	0.0555327	0.102639	0.123702	0.161442	0.165696	0.190045	0.182172	0.214009	0.188606	0.193939	0.207	0.177469	0.140187	0.124514
54-58.5 Deg	0	0	0	0	0	0	0.0248494	0.0445331	0.0810889	0.106105	0.109863	0.131459	0.132259	0.121872	0.135764	0.133188	0.12807	0.106557	0.122172	0.0814815
58.5-63 Deg	0	0	0	0	0	0	0	0.0165922	0.0418139	0.0557781	0.0744786	0.0831667	0.0781828	0.0883686	0.0845225	0.0654045	0.074184	0.0883721	0.0841121	0.0405405
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00645756	0.018006	0.0306081	0.0433498	0.053756	0.044898	0.0724638	0.044586	0.0347222	0.0641026	0.0243902	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00228571	0.0041686	0.0121873	0.017341	0.020155	0.0234114	0.0121212	0.0131579	0.075	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.00540541	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

New NM R-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.834532	0.852174	0.88785	0.762712	0.807692	0.802198	0.811321	0.835443	0.753086	0.779412	0.783333	0.936508	0.8	0.921569	0.921569	0.77193	0.848485	0.861111	0.826087	0.823529
4.5-9 Deg	0.803922	0.828974	0.800875	0.820276	0.789474	0.798982	0.801136	0.774026	0.79868	0.744186	0.742424	0.784091	0.770642	0.790476	0.754717	0.774194	0.79375	0.813793	0.748387	0.785714
9-13.5 Deg	0.74026	0.760633	0.746401	0.713326	0.746803	0.720867	0.735724	0.721683	0.72093	0.716946	0.727468	0.697572	0.704835	0.730978	0.747774	0.70068	0.684982	0.73029	0.623853	0.713615
13.5-18 Deg	0.704342	0.713103	0.697987	0.688694	0.708895	0.681319	0.674493	0.661465	0.680731	0.635036	0.657848	0.664093	0.618938	0.648718	0.634561	0.598291	0.63871	0.638686	0.630252	0.614407
18-22.5 Deg	0.660068	0.632723	0.652881	0.627978	0.634488	0.606524	0.599138	0.600991	0.58926	0.585284	0.56654	0.562092	0.581633	0.546547	0.532051	0.582707	0.517647	0.569507	0.530055	0.5625
22.5-27 Deg	0.57636	0.56538	0.564828	0.553719	0.550962	0.498274	0.550685	0.566828	0.500901	0.497826	0.511166	0.513605	0.453674	0.539095	0.447761	0.428571	0.476821	0.462963	0.379032	0.435185
27-31.5 Deg	0.498278	0.493626	0.481938	0.446392	0.463785	0.474016	0.465487	0.389868	0.438953	0.384615	0.484375	0.360577	0.414634	0.34058	0.242991	0.416667	0.405941	0.333333	0.25974	0.403846
31.5-36 Deg	0.432253	0.403556	0.432373	0.361111	0.379648	0.411483	0.370968	0.307116	0.361702	0.355191	0.294118	0.293578	0.337349	0.328571	0.272727	0.34375	0.227273	0.290323	0.25	0.380952
36-40.5 Deg	0.373851	0.336748	0.352837	0.316279	0.293333	0.333333	0.282609	0.182432	0.261194	0.25	0.430556	0.191489	0.127273	0.238095	0.2	0.25	0.0714286	0.25	0.1	0.333333
40.5-45 Deg	0.264297	0.2897	0.274247	0.191235	0.220238	0.204918	0.309524	0.147059	0.169014	0.30303	0.16	0.0909091	0.1875	0.1875	0.166667	0	0.2	0	0.5	0
45-49.5 Deg	0.144772	0.168675	0.216867	0.15534	0.182927	0.113636	0.0645161	0.148148	0.117647	0.0769231	0	0.6	0	0	0	0.25	0	0	0	0
49.5-54 Deg	0.10119	0.178295	0.145161	0.0740741	0.08	0.142857	0.2	0	0	0.1	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0.0571429	0.1	0.0322581	0	0.1	0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0.136364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 3: Table for 2D Histogram for New NM-Berger-Sehgal

New NM B-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500
0-4.5 Deg	0	0	0	0	0.157895	0.325	0.422222	0.490566	0.615385	0.728571
4.5-9 Deg	0	0	0	0.0625	0.176471	0.235849	0.396694	0.478261	0.581731	0.773279
9-13.5 Deg	0	0	0	0.09375	0.156716	0.223529	0.362963	0.463343	0.5725	0.701245
13.5-18 Deg	0	0	0	0.0382166	0.131222	0.260736	0.330233	0.448833	0.566116	0.634994
18-22.5 Deg	0	0	0	0.039604	0.0973451	0.228145	0.318462	0.419903	0.517013	0.582547
22.5-27 Deg	0	0	0	0.0264026	0.0930736	0.197461	0.321879	0.381265	0.447548	0.521715
27-31.5 Deg	0	0	0	0.00486618	0.0857143	0.152859	0.25358	0.312166	0.395361	0.466491
31.5-36 Deg	0	0	0	0.00754717	0.0815217	0.142292	0.218271	0.283494	0.333753	0.381784
36-40.5 Deg	0	0	0	0	0.032538	0.0817963	0.170164	0.233583	0.275212	0.327416
40.5-45 Deg	0	0	0	0	0.0139147	0.0678972	0.129657	0.192308	0.224483	0.252462
45-49.5 Deg	0	0	0	0	0.00251467	0.0392938	0.0940285	0.141328	0.181437	0.212241
49.5-54 Deg	0	0	0	0	0	0.0110121	0.0531873	0.0958814	0.126534	0.148936
54-58.5 Deg	0	0	0	0	0	0.000456204	0.0199623	0.0552683	0.0810965	0.102659
58.5-63 Deg	0	0	0	0	0	0	0.000714286	0.0128637	0.0467906	0.0568421
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00745573	0.0242928
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.000740466
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New NM B-S	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0.895522	0.807692	0.880435	0.864865	0.843373	0.833333	0.858333	0.833333	0.826087	0.814815
4.5-9 Deg	0.811448	0.817109	0.806366	0.801402	0.814286	0.809211	0.804211	0.755448	0.822709	0.792657
9-13.5 Deg	0.78089	0.798354	0.801724	0.794569	0.782796	0.780287	0.765235	0.773496	0.756598	0.759384
13.5-18 Deg	0.727545	0.736387	0.720152	0.749489	0.762791	0.732403	0.711937	0.704908	0.702804	0.683544
18-22.5 Deg	0.656707	0.692351	0.687027	0.677215	0.689404	0.661647	0.651855	0.661634	0.65554	0.634515
22.5-27 Deg	0.578365	0.637657	0.629688	0.615445	0.637963	0.622396	0.604258	0.581746	0.570899	0.569778
27-31.5 Deg	0.496522	0.564516	0.564264	0.554788	0.551891	0.55257	0.548276	0.521099	0.517559	0.518553
31.5-36 Deg	0.436444	0.472969	0.488325	0.492462	0.479326	0.494505	0.47549	0.45864	0.461108	0.451835
36-40.5 Deg	0.366159	0.387514	0.419254	0.425045	0.403834	0.392764	0.396559	0.400812	0.369942	0.368859
40.5-45 Deg	0.30273	0.319185	0.342679	0.345987	0.330502	0.331052	0.323815	0.305906	0.312284	0.313023
45-49.5 Deg	0.24064	0.244851	0.261486	0.269272	0.268868	0.255423	0.239971	0.254059	0.219613	0.205285
49.5-54 Deg	0.169353	0.187424	0.203203	0.19403	0.204905	0.197958	0.161453	0.159744	0.142512	0.151292
54-58.5 Deg	0.119633	0.118058	0.129529	0.135933	0.125182	0.118211	0.109568	0.118863	0.117073	0.108844
58.5-63 Deg	0.0634228	0.0796216	0.0780856	0.0909091	0.0960929	0.0849558	0.0780781	0.103825	0.0458716	0
63-67.5 Deg	0.0364188	0.0436258	0.0367232	0.039666	0.0363636	0.0426136	0.0162162	0.0357143	0.0227273	0.0416667
67.5-72 Deg	0.00470367	0.0114213	0.0195072	0.0166667	0.0120482	0	0	0.03125	0	0
72-76.5 Deg	0	0	0	0.00280899	0.00649351	0.0123457	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New NM B-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500
0-4.5 Deg	0.778846	0.8	0.813725	0.829268	0.84375	0.78022	0.783133	0.898734	0.85	0.825397
4.5-9 Deg	0.804255	0.824945	0.804494	0.814536	0.784504	0.774295	0.813665	0.792994	0.764706	0.790036
9-13.5 Deg	0.766798	0.776286	0.733735	0.717208	0.731677	0.730769	0.708861	0.728296	0.755835	0.75089
13.5-18 Deg	0.703634	0.7086	0.706101	0.683544	0.700457	0.681775	0.68321	0.68171	0.669251	0.644678
18-22.5 Deg	0.653195	0.635392	0.641326	0.620074	0.60516	0.579566	0.597895	0.612863	0.599419	0.5856
22.5-27 Deg	0.571276	0.570789	0.557559	0.528678	0.526667	0.524138	0.529101	0.509404	0.499093	0.539326
27-31.5 Deg	0.515256	0.490654	0.476651	0.444332	0.474736	0.456456	0.431408	0.465169	0.451791	0.405145
31.5-36 Deg	0.42583	0.411765	0.437118	0.397764	0.406551	0.405963	0.389205	0.33564	0.381395	0.393333
36-40.5 Deg	0.345339	0.357923	0.325411	0.296117	0.300654	0.38785	0.366279	0.328	0.348624	0.204819
40.5-45 Deg	0.294294	0.264706	0.272981	0.214286	0.233918	0.189474	0.197368	0.231884	0.222222	0.157895
45-49.5 Deg	0.236769	0.215859	0.180723	0.158879	0.169014	0.0588235	0.0833333	0.166667	0.136364	0.25
49.5-54 Deg	0.132184	0.133858	0.0869565	0.097561	0.0769231	0.0909091	0	0	0	0
54-58.5 Deg	0.0617284	0.0851064	0.0344828	0.0909091	0	0.111111	0	0	0.5	0
58.5-63 Deg	0.0333333	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0.0714286	0.166667	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New NM B-S	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.873016	0.767442	0.779661	0.847826	0.836735	0.809524	0.861111	0.794872	0.944444	0.833333
4.5-9 Deg	0.793651	0.741784	0.728643	0.759657	0.734884	0.770053	0.780749	0.761905	0.791908	0.794521
9-13.5 Deg	0.708249	0.717833	0.664251	0.747423	0.700581	0.688679	0.681967	0.69338	0.745763	0.685039
13.5-18 Deg	0.668863	0.66548	0.643629	0.637168	0.643038	0.62973	0.607973	0.666667	0.621212	0.622711
18-22.5 Deg	0.590654	0.587156	0.558376	0.564607	0.52568	0.568093	0.52549	0.575342	0.497696	0.557471
22.5-27 Deg	0.484043	0.5	0.535354	0.441767	0.436681	0.482587	0.40113	0.496599	0.461538	0.454545
27-31.5 Deg	0.433735	0.416667	0.362245	0.333333	0.411765	0.283951	0.402439	0.363636	0.285714	0.396825
31.5-36 Deg	0.277372	0.293103	0.308642	0.246753	0.34375	0.181818	0.108108	0.25	0.258065	0.137931
36-40.5 Deg	0.232143	0.186047	0.181818	0.214286	0.285714	0.214286	0.333333	0.166667	0.285714	0.181818
40.5-45 Deg	0.2	0.0526316	0.428571	0.0588235	0.166667	0.166667	0.25	0	0	1
45-49.5 Deg	0.0714286	0.333333	0.2	1	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

Table 4: Table for 2D Histogram for Old NM-Rein-Sehgal

Old NM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0	0	0	0	0.333333	0.5	0.5	0.8	0.857143	0.5	0.666667	1	0.857143	0.7	0.777778	0.875	0.909091	0.777778	1	0.769231
4.5-9 Deg	0	0	0	0	0	0.25	0.285714	0.470588	0.466667	0.608696	0.904762	0.9	0.65	0.8	0.74359	0.877551	0.65	0.782609	0.792453	0.810811
9-13.5 Deg	0	0	0	0	0.0769231	0.181818	0.285714	0.451613	0.625	0.642857	0.765957	0.721519	0.813953	0.734177	0.732558	0.77907	0.744681	0.865979	0.746988	0.76087
13.5-18 Deg	0	0	0	0.0714286	0.15	0.290323	0.365854	0.509091	0.621622	0.630952	0.682692	0.773109	0.722222	0.739726	0.70229	0.719178	0.711656	0.753425	0.726115	0.735099
18-22.5 Deg	0	0	0	0.0571429	0.0689655	0.184211	0.242424	0.505155	0.474227	0.56	0.647482	0.656442	0.609929	0.648936	0.705069	0.695187	0.643216	0.673267	0.651961	0.616505
22.5-27 Deg	0	0	0	0.0416667	0.04	0.247059	0.280488	0.346154	0.518797	0.465969	0.602679	0.631818	0.658291	0.668224	0.632959	0.659574	0.617647	0.593458	0.614213	0.654054
27-31.5 Deg	0	0	0	0.0217391	0.0615385	0.1375	0.16	0.296296	0.390863	0.466981	0.520492	0.59761	0.522727	0.544061	0.550781	0.516981	0.592437	0.524887	0.513228	0.49359
31.5-36 Deg	0	0	0	0.0816327	0.097561	0.07	0.244444	0.290503	0.384259	0.364407	0.435252	0.453925	0.540881	0.461017	0.456311	0.462838	0.493878	0.474654	0.45	0.416667
36-40.5 Deg	0	0	0	0	0.04	0.133333	0.155172	0.235577	0.282609	0.296296	0.37785	0.377049	0.41195	0.424749	0.422222	0.376518	0.409692	0.394737	0.407407	0.360825
40.5-45 Deg	0	0	0	0	0	0.0869565	0.15122	0.161017	0.256228	0.271875	0.289894	0.306818	0.291545	0.340557	0.366534	0.316742	0.337423	0.28777	0.29661	0.257576
45-49.5 Deg	0	0	0	0	0	0.0434783	0.0843882	0.141176	0.163462	0.159322	0.242331	0.231003	0.263699	0.285156	0.27907	0.270115	0.273973	0.259259	0.347222	0.285714
49.5-54 Deg	0	0	0	0	0	0.0108696	0.0636364	0.0816327	0.160819	0.133144	0.170588	0.169381	0.212996	0.220588	0.220238	0.15942	0.142857	0.122807	0.236364	0.129032
54-58.5 Deg	0	0	0	0	0	0	0.023622	0.0238095	0.0320513	0.107463	0.107595	0.110701	0.105991	0.138728	0.186992	0.13253	0.176471	0.131579	0	0.357143
58.5-63 Deg	0	0	0	0	0	0	0	0.0129032	0.0397554	0.0555556	0.0724638	0.0979592	0.0942408	0.0787402	0.0487805	0.0754717	0.15625	0.0416667	0	0.125
63-67.5 Deg	0	0	0	0	0	0	0	0	0.0056338	0.0241379	0.0125523	0.0380952	0.04	0.0869565	0	0.0689655	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00338983	0	0.0212766	0.010989	0.0222222	0	0	0.111111	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Old NM R-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.8	0.777778	1	0.75	0.75	1	0.6	0.833333	1	0.833333	0.909091	0.75	0.666667	1	0	0.666667	0	0.8	1	1
4.5-9 Deg	0.866667	0.807692	0.815789	0.8	0.74359	0.861111	0.923077	0.825	0.875	0.833333	0.761905	0.85	0.8	0.823529	0.652174	0.923077	0.857143	0.882353	0.533333	0.85
9-13.5 Deg	0.747253	0.851064	0.776316	0.683544	0.791045	0.686567	0.862069	0.706897	0.660377	0.755556	0.688889	0.604651	0.933333	0.638298	0.714286	0.826087	0.958333	0.842105	0.777778	0.708333
13.5-18 Deg	0.70068	0.688889	0.705357	0.688679	0.711538	0.705882	0.670588	0.694444	0.68	0.677966	0.586957	0.653846	0.612245	0.65625	0.68	0.7	0.625	0.76	0.75	0.565217
18-22.5 Deg	0.639535	0.641176	0.666667	0.635593	0.59375	0.59375	0.6	0.652174	0.625	0.708333	0.568182	0.634146	0.461538	0.423077	0.625	0.47619	0.47619	0.76	0.611111	0.722222
22.5-27 Deg	0.529801	0.594937	0.503817	0.591398	0.653465	0.52	0.578947	0.413793	0.568966	0.377778	0.666667	0.5	0.444444	0.473684	0.458333	0.647059	0.615385	0.45	0.4	0.333333
27-31.5 Deg	0.531034	0.475	0.521008	0.465116	0.406593	0.517857	0.490566	0.487179	0.444444	0.347826	0.380952	0.4	0.384615	0.454545	0.1	0.333333	0.375	0.625	0.2	0.25
31.5-36 Deg	0.470588	0.465909	0.454545	0.376812	0.436364	0.348837	0.541667	0.238095	0.4	0.266667	0.3125	0.533333	0.352941	0.4	0.571429	0.222222	0.166667	0	0.666667	0.5
36-40.5 Deg	0.317308	0.397436	0.267857	0.272727	0.285714	0.380952	0.176471	0.2	0.117647	0.166667	0.333333	0.333333	0.5	0.285714	0.5	0	0	0	0	0
40.5-45 Deg	0.140351	0.318182	0.307692	0.208333	0.357143	0.25	0.375	0.25	0.2	0	0	0	0.5	0	0	0	0	1	0	0
45-49.5 Deg	0.28	0.217391	0.111111	0.1	0.0833333	0.166667	0.25	0	0.333333	1	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0.0714286	0.1	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0.1	0	0	0	0	0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 5: Table for 2D Histogram for New ANM-Rein-Sehgal

New ANM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0	0	0	0.037037	0.173913	0.225352	0.398693	0.510204	0.585034	0.741325	0.812332	0.808989	0.820399	0.80597	0.846154	0.826087	0.834821	0.846791	0.849776	0.814732
4.5-9 Deg	0	0	0	0.0538922	0.179487	0.264881	0.351406	0.522654	0.611905	0.722011	0.822749	0.806912	0.812763	0.807565	0.807477	0.80314	0.805654	0.802672	0.816404	0.79961
9-13.5 Deg	0	0	0	0.0881226	0.175824	0.272864	0.369565	0.47927	0.562628	0.680187	0.778963	0.784609	0.775579	0.77094	0.780604	0.772247	0.778919	0.774887	0.769928	0.777286
13.5-18 Deg	0	0	0	0.0502959	0.162912	0.264642	0.372408	0.45271	0.529918	0.642998	0.714241	0.754711	0.746173	0.739165	0.72958	0.736591	0.712291	0.723065	0.699029	0.705178
18-22.5 Deg	0	0	0	0.0477273	0.135068	0.240964	0.32415	0.42098	0.500719	0.578125	0.669713	0.700024	0.693197	0.686785	0.675302	0.676973	0.671911	0.662691	0.649262	0.656827
22.5-27 Deg	0	0	0	0.0256881	0.127932	0.186722	0.284972	0.381885	0.46546	0.511835	0.587483	0.641457	0.609761	0.630852	0.616002	0.610015	0.585767	0.589724	0.588134	0.57303
27-31.5 Deg	0	0	0	0.0135747	0.0779102	0.157462	0.237522	0.318072	0.385341	0.455377	0.527993	0.566528	0.573181	0.550737	0.538564	0.550457	0.533736	0.525933	0.509007	0.512922
31.5-36 Deg	0	0	0	0.00265957	0.0702447	0.140581	0.21821	0.292653	0.342622	0.394628	0.429609	0.48047	0.502938	0.499068	0.49538	0.462372	0.47797	0.465828	0.428421	0.439291
36-40.5 Deg	0	0	0	0	0.0358187	0.107342	0.168067	0.222502	0.294331	0.333169	0.361301	0.382382	0.418154	0.431897	0.40234	0.403238	0.388569	0.407134	0.374224	0.366126
40.5-45 Deg	0	0	0	0	0.0164051	0.0757272	0.131076	0.200825	0.226708	0.268313	0.30581	0.320273	0.346117	0.33394	0.333774	0.343066	0.307036	0.329013	0.279793	0.27593
45-49.5 Deg	0	0	0	0	0	0.0478888	0.099454	0.13113	0.177444	0.212046	0.222903	0.250172	0.254128	0.270336	0.280552	0.252766	0.235294	0.240708	0.214834	0.218107
49.5-54 Deg	0	0	0	0	0	0.0114405	0.0658882	0.103003	0.127891	0.149639	0.172282	0.178556	0.193367	0.190678	0.185291	0.18963	0.175556	0.136364	0.150327	0.116279
54-58.5 Deg	0	0	0	0	0	0.000554017	0.0170428	0.0537772	0.0883421	0.116889	0.122696	0.124613	0.143336	0.139043	0.133106	0.130564	0.121076	0.105263	0.0547945	0.114286
58.5-63 Deg	0	0	0	0	0	0	0.0010015	0.020202	0.0406544	0.0526316	0.0724161	0.0817391	0.077907	0.0850662	0.0868263	0.0772947	0.0462963	0.0454545	0.0555556	0
63-67.5 Deg	0	0	0	0	0	0	0	0.00108167	0.00447928	0.0226148	0.0374384	0.0423729	0.0439122	0.0482759	0.0424242	0.025	0.125	0	0.125	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0	0.00515464	0.0103093	0.0144928	0.00714286	0.0289855	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

New ANM R-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.811494	0.835	0.820728	0.821212	0.820946	0.829352	0.86385	0.785124	0.834906	0.820896	0.815642	0.802721	0.80315	0.8	0.836538	0.855556	0.808989	0.783784	0.884058	0.705882
4.5-9 Deg	0.808895	0.780172	0.79495	0.806396	0.799636	0.809524	0.799766	0.790123	0.793201	0.770154	0.790738	0.80036	0.792494	0.733146	0.794798	0.766323	0.734982	0.759091	0.770335	0.812155
9-13.5 Deg	0.764215	0.756151	0.769636	0.756423	0.745802	0.736299	0.725795	0.729068	0.731919	0.712513	0.703791	0.716617	0.724876	0.71537	0.701461	0.718579	0.711409	0.698052	0.719368	0.688776
13.5-18 Deg	0.708415	0.69735	0.68934	0.693381	0.700468	0.682373	0.673329	0.680972	0.660094	0.631818	0.63144	0.590237	0.677481	0.628692	0.681818	0.648734	0.609848	0.615385	0.643275	0.635714
18-22.5 Deg	0.646345	0.649693	0.62265	0.628975	0.613897	0.596406	0.591174	0.582904	0.568153	0.597598	0.59465	0.57381	0.533875	0.509091	0.476852	0.57377	0.569231	0.522523	0.635294	0.603175
22.5-27 Deg	0.583082	0.5553	0.564074	0.557719	0.53367	0.554507	0.527886	0.535211	0.501099	0.488432	0.481343	0.509091	0.469388	0.515385	0.494382	0.472222	0.490909	0.390244	0.647059	0.321429
27-31.5 Deg	0.498878	0.50292	0.473382	0.487885	0.490838	0.454704	0.467192	0.428571	0.405405	0.464286	0.381679	0.402062	0.346154	0.348837	0.358974	0.55	0.307692	0.25	0.125	0.5
31.5-36 Deg	0.425238	0.420697	0.393846	0.374753	0.375394	0.398374	0.379121	0.342857	0.27907	0.290323	0.282051	0.592593	0.333333	0.533333	0.75	0	0.6	1	0	0
36-40.5 Deg	0.347445	0.358079	0.315942	0.337449	0.296512	0.306931	0.295082	0.265625	0.192308	0.2	0.142857	0.166667	0	0.5	0	0	0	0	0	0
40.5-45 Deg	0.311653	0.287736	0.211538	0.186275	0.203125	0.222222	0.111111	0.272727	0.2	0	0.333333	0	0	0	0	0	0	0	0	0
45-49.5 Deg	0.251908	0.234043	0.2	0.307692	0.235294	0	0.4	0	0	0	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0.125	0.181818	0.0833333	0	0.5	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0.157895	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 6: Table for 2D Histogram for New ANM-Berger-Sehgal

New ANM B-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500
0-4.5 Deg	0	0	0	0.0930233	0.144737	0.283186	0.421384	0.494898	0.668161	0.710247
4.5-9 Deg	0	0	0	0.0166667	0.165094	0.269231	0.4	0.541667	0.613402	0.732694
9-13.5 Deg	0	0	0	0.0700935	0.130919	0.271667	0.353012	0.480322	0.569575	0.68139
13.5-18 Deg	0	0	0	0.0401338	0.149742	0.265497	0.336059	0.414129	0.536284	0.638281
18-22.5 Deg	0	0	0	0.0277778	0.137174	0.23849	0.319925	0.423721	0.499227	0.57533
22.5-27 Deg	0	0	0	0.0196464	0.109134	0.204236	0.312057	0.385731	0.447873	0.516755
27-31.5 Deg	0	0	0	0.00315956	0.104046	0.165109	0.256264	0.322028	0.397871	0.445264
31.5-36 Deg	0	0	0	0	0.0525862	0.124857	0.206051	0.275698	0.333971	0.392423
36-40.5 Deg	0	0	0	0	0.0444774	0.105837	0.16809	0.234525	0.286885	0.327259
40.5-45 Deg	0	0	0	0	0.0210938	0.0689829	0.137208	0.172468	0.226261	0.272047
45-49.5 Deg	0	0	0	0	0	0.035913	0.0925481	0.127177	0.17693	0.21244
49.5-54 Deg	0	0	0	0	0	0.0115668	0.0516817	0.101349	0.118959	0.148848
54-58.5 Deg	0	0	0	0	0	0	0.0210526	0.052506	0.080695	0.104636
58.5-63 Deg	0	0	0	0	0	0	0	0.0150616	0.0392791	0.0594262
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00795003	0.0215545
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00182983
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM B-S	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0.805861	0.796703	0.834184	0.844907	0.827907	0.866324	0.843458	0.855072	0.83208	0.813433
4.5-9 Deg	0.797824	0.812245	0.82494	0.814583	0.823051	0.812541	0.792568	0.781479	0.804378	0.794982
9-13.5 Deg	0.781754	0.795837	0.774114	0.785362	0.773578	0.781475	0.76586	0.762567	0.752009	0.761471
13.5-18 Deg	0.728386	0.717996	0.747335	0.748866	0.736466	0.7337	0.731489	0.723615	0.700111	0.714206
18-22.5 Deg	0.655519	0.701815	0.686171	0.689579	0.686069	0.673434	0.65566	0.6686	0.647105	0.657014
22.5-27 Deg	0.600138	0.645331	0.628718	0.629526	0.604035	0.609545	0.603815	0.602548	0.578702	0.597386
27-31.5 Deg	0.512134	0.574856	0.561587	0.558263	0.539545	0.545725	0.538095	0.525974	0.509479	0.506996
31.5-36 Deg	0.431607	0.47668	0.500539	0.496867	0.476983	0.479711	0.460797	0.455385	0.446729	0.424768
36-40.5 Deg	0.353491	0.400137	0.418747	0.422945	0.407023	0.396731	0.398879	0.392036	0.372638	0.364706
40.5-45 Deg	0.300615	0.316995	0.337145	0.348088	0.337621	0.320774	0.311813	0.293856	0.315938	0.294333
45-49.5 Deg	0.229012	0.236659	0.252955	0.271491	0.267346	0.259352	0.254042	0.228395	0.213368	0.222222
49.5-54 Deg	0.169149	0.194822	0.189664	0.203367	0.176355	0.210306	0.188017	0.202572	0.150943	0.148936
54-58.5 Deg	0.120419	0.128324	0.143609	0.149563	0.12426	0.149296	0.141667	0.115044	0.149254	0.285714
58.5-63 Deg	0.0719951	0.0804312	0.088785	0.0819367	0.0946372	0.0851064	0.0535714	0.0888889	0.125	0
63-67.5 Deg	0.0325901	0.0497512	0.0446927	0.0397554	0.0674847	0.0933333	0.0952381	0.047619	0	0
67.5-72 Deg	0.00373599	0.00414938	0.0170648	0.00552486	0.0136986	0	0	0	0	0
72-76.5 Deg	0	0	0	0.0266667	0	0.0833333	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM B-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500
0-4.5 Deg	0.818653	0.841432	0.806366	0.833866	0.867133	0.840741	0.819005	0.813084	0.83	0.886667
4.5-9 Deg	0.805085	0.823664	0.813322	0.809233	0.801491	0.754923	0.791063	0.783712	0.79661	0.793729
9-13.5 Deg	0.748873	0.73664	0.739656	0.735498	0.72956	0.755391	0.720774	0.711163	0.74169	0.714434
13.5-18 Deg	0.71014	0.691088	0.695486	0.679018	0.673116	0.66913	0.689633	0.664591	0.685662	0.667735
18-22.5 Deg	0.636641	0.624197	0.638889	0.646891	0.628604	0.584667	0.586435	0.624873	0.603365	0.570149
22.5-27 Deg	0.569439	0.583187	0.543649	0.537295	0.536066	0.55848	0.548585	0.504687	0.518738	0.493639
27-31.5 Deg	0.501982	0.5	0.4943	0.457645	0.467143	0.448387	0.4447	0.485531	0.401487	0.407609
31.5-36 Deg	0.438768	0.394628	0.38565	0.408915	0.451791	0.342561	0.429348	0.30303	0.322917	0.333333
36-40.5 Deg	0.376984	0.347664	0.323529	0.355856	0.312849	0.325	0.338983	0.410256	0.242424	0.157895
40.5-45 Deg	0.257062	0.283262	0.26	0.298851	0.258065	0.228571	0.210526	0.111111	0.285714	0
45-49.5 Deg	0.229299	0.195652	0.196429	0.142857	0.285714	0.333333	0	0.5	0	0
49.5-54 Deg	0.145455	0.130435	0.142857	0	0	0	1	0	0	0
54-58.5 Deg	0	0.0769231	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM B-S	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.823129	0.825397	0.871795	0.825243	0.824074	0.797297	0.815789	0.774194	0.823529	0.809524
4.5-9 Deg	0.777403	0.774319	0.787879	0.784741	0.817629	0.771523	0.778723	0.776824	0.762376	0.821229
9-13.5 Deg	0.730546	0.70028	0.702786	0.692029	0.698795	0.727488	0.698895	0.694079	0.706827	0.663507
13.5-18 Deg	0.664188	0.656201	0.664884	0.654737	0.652068	0.615894	0.627737	0.628571	0.650888	0.613924
18-22.5 Deg	0.581722	0.600887	0.607558	0.583333	0.531915	0.573034	0.525641	0.527559	0.552632	0.487179
22.5-27 Deg	0.501502	0.469828	0.469945	0.477273	0.443299	0.445783	0.442623	0.297297	0.405405	0.482759
27-31.5 Deg	0.365517	0.330189	0.263889	0.446809	0.4	0.380952	0.136364	0.333333	0.555556	0.333333
31.5-36 Deg	0.285714	0.3	0.333333	0.352941	0.166667	1	1	0.333333	0.5	0
36-40.5 Deg	0.25	0.166667	0	0.5	0	0	0	0	0	0
40.5-45 Deg	1	0.5	0.5	0	0	0	0	0	0	0
45-49.5 Deg	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

ν-Mode $|t|$ and Q^2 plots are below:

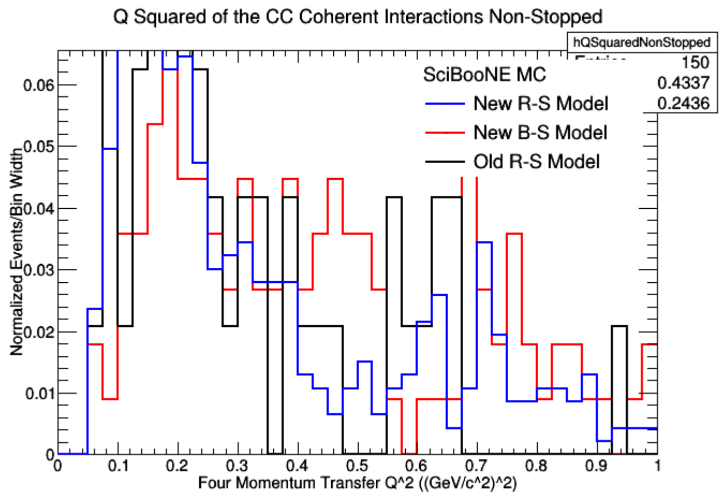


Figure 6:

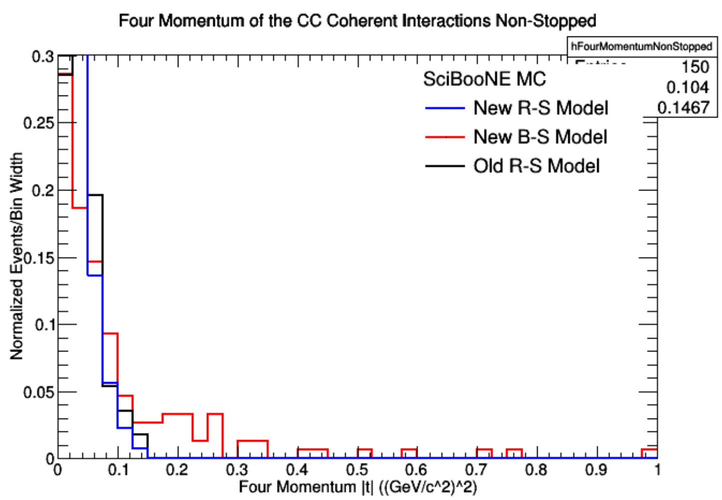


Figure 7:

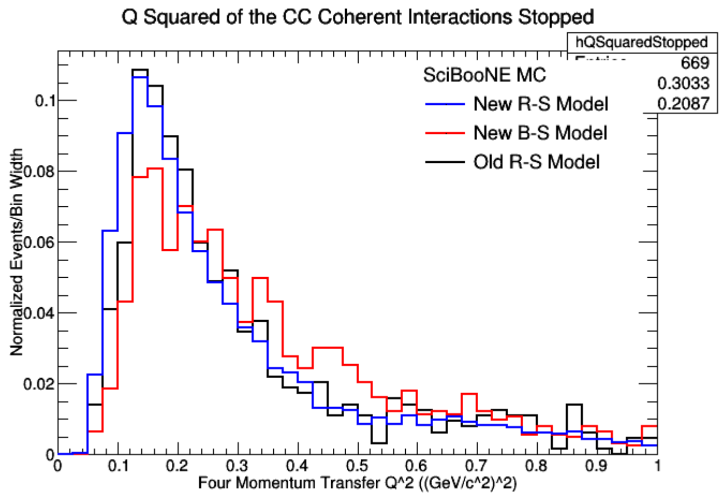


Figure 8:

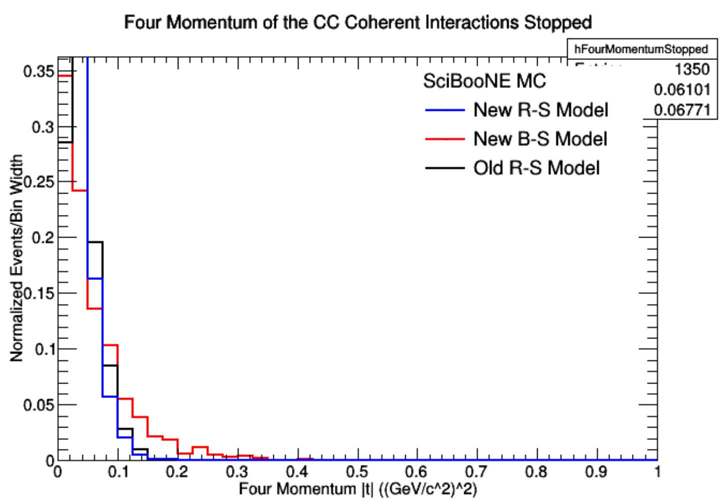


Figure 9:

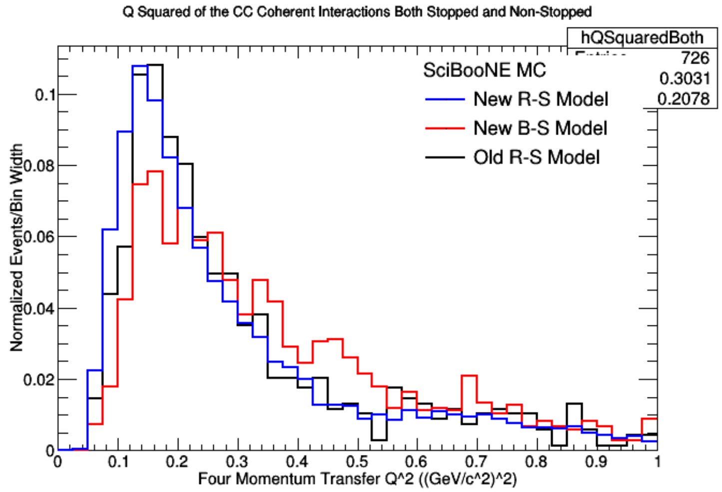


Figure 10:

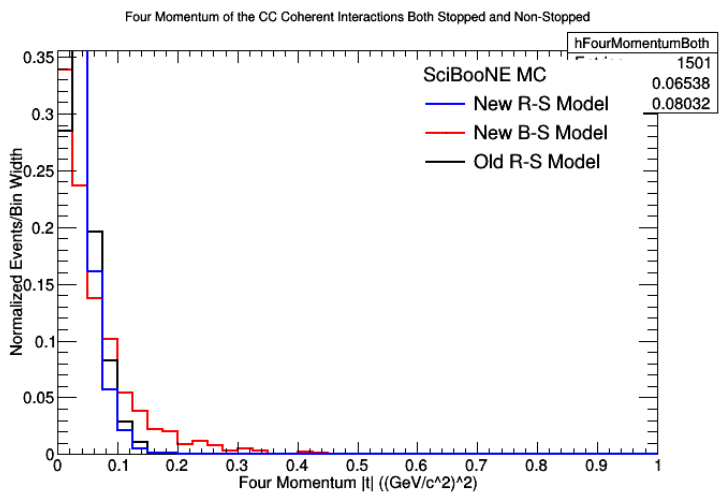


Figure 11:

$\bar{\nu}$-Mode $|t|$ and Q^2 plots are below:

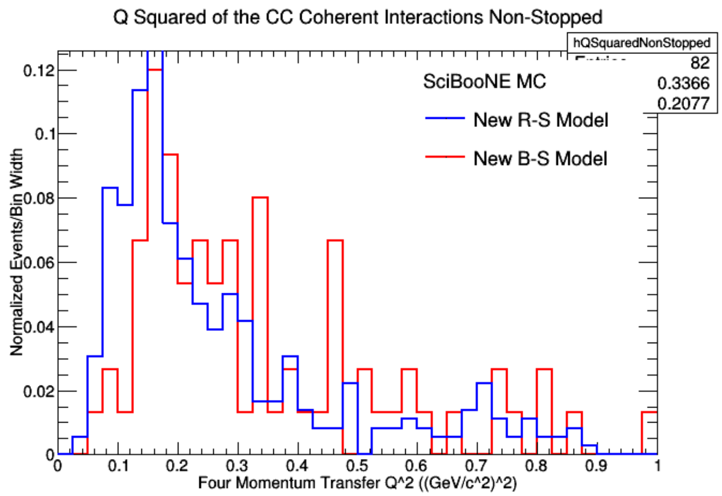


Figure 12:

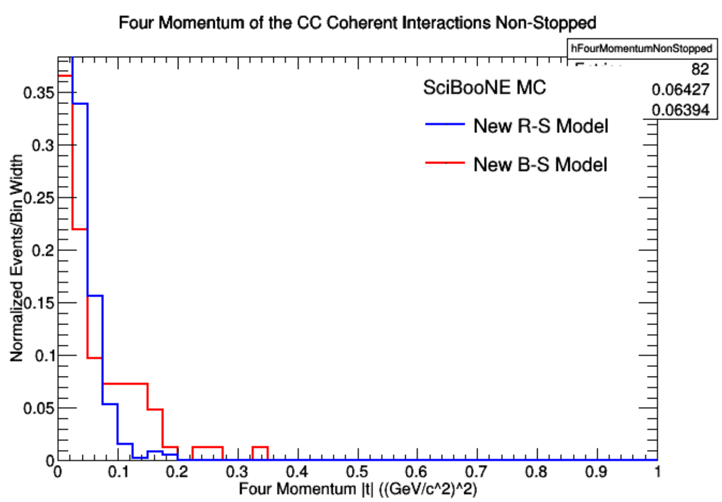


Figure 13:

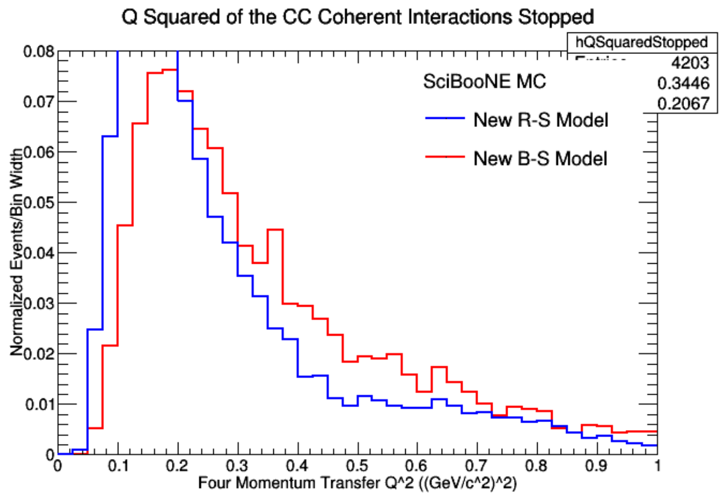


Figure 14:

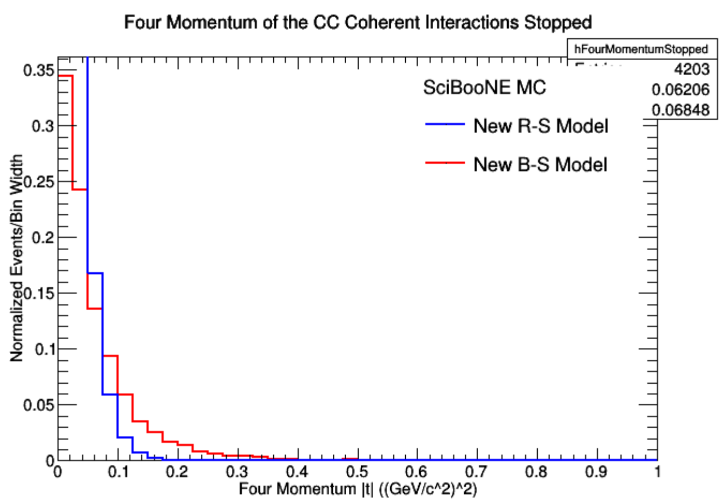


Figure 15:

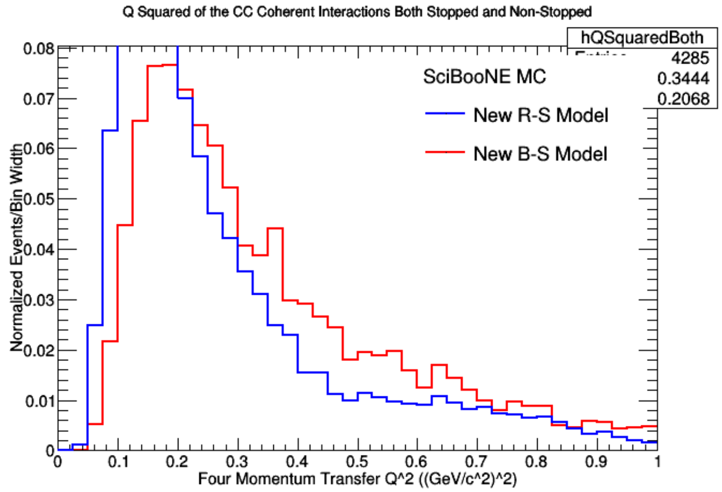


Figure 16:

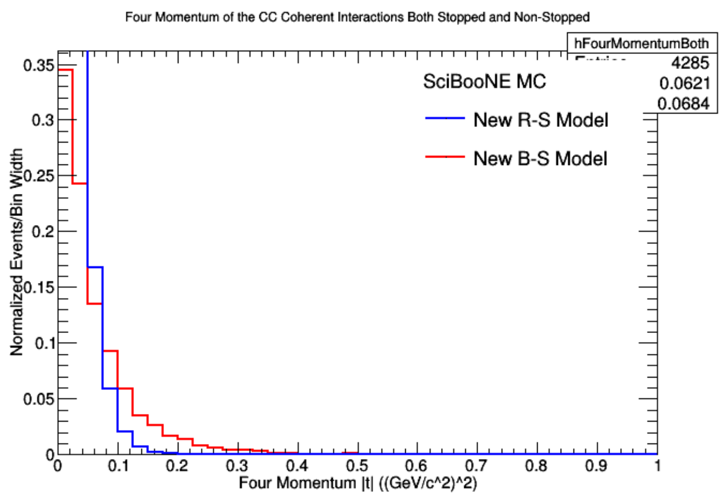


Figure 17:

A Appendix: Sample Details

Appendix on samples

A.1 ν-Mode Rein-Sehgal NEUTv5.3.6

A sample of 1,000,000 ν interactions were simulated using the NEUT generator (v5.3.6) and the Rein-Sehgal model for coherent pion production. This sample correspond to the file labeled

`SciBooNE_numu_coh_RooTrack.root`

found at the following link (put link to sample here).

A.2 ν-Mode Berger-Sehgal NEUTv5.3.6

A sample of 1,000,000 ν interactions were simulated using the NEUT generator (v5.3.6) and the Berger-Sehgal model for coherent pion production. This sample correspond to the file labeled

`SciBooNE_numu_coh_RooTrack_NEW.root`

found at the following link (put link to sample here).

A.3 ν-Mode Rein-Sehgal NEUTvx.x.x

A sample of 100,000 ν interactions were simulated using the NEUT generator (vx.x.x, believed to be the version used by the SciBooNE collaboration in the original publication) and the corresponding older Rein-Sehgal model for coherent pion production. This sample correspond to the file labeled

`SciBooNE_numu_coh_OLDNEUT_RooTrack.root`

found at the following link (put link to sample here).

A.4 $bar\nu$-Mode Rein-Sehgal NEUTv5.3.6

A sample of 1,000,000 $\bar{\nu}$ interactions were simulated using the NEUT generator (v5.3.6) and the Rein-Sehgal model for coherent pion production. This sample correspond to the file labeled

`SciBooNE_numubar_coh_RooTrack.root`

found at the following link (put link to sample here).

A.5 $\bar{\nu}$-Mode Berger-Sehgal NEUTv5.3.6

A sample of 1,000,000 $\bar{\nu}$ interactions were simulated using the NEUT generator (v5.3.6) and the Berger-Sehgal model for coherent pion production. This sample correspond to the file labeled

`SciBooNE_numubar_coh_RooTrack_NEW.root`

found at the following link (put link to sample here).

A.6 Vertex Distributions

The events were all given a random initial point that was generated with the goal that the vertex distributions of this simulation would closely match the vertex distributions that Hiraide (need to put a reference) showed in his thesis. This was done by... etc.

Put in the code **for** how we made the vertex distributions of the interactions.

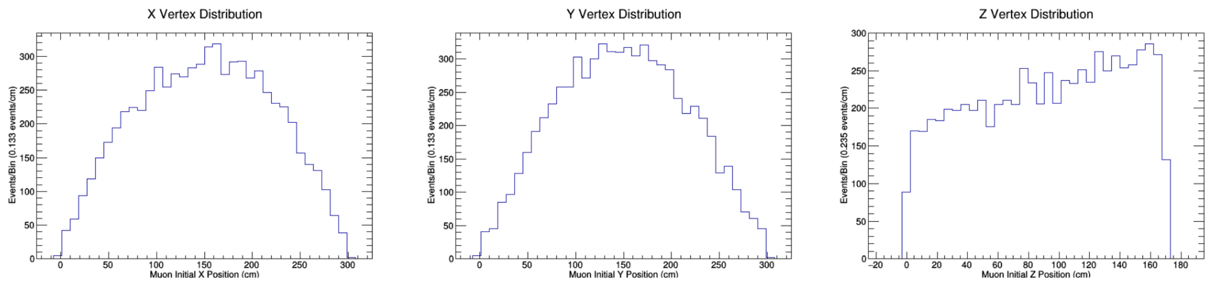


Figure 18: Vertex distributions of the events in the new Rein-Sehgal sample.

A.7 NewNMReinSehgal.C

This file is the macro that corresponds to the "NewNMReinSehgal.h" file, which connects with this file: "SciBooNE_numu_coh_RooTrack.root". This file performs the main analysis for this generated sample, and then organizes the information into many different histograms. The histograms are then written to a file titled "totalmuoninfoRS.root" inside the "ROOTFILES" directory. The "ROOTFILES" directory is included in the SciBooNE-MC repository (it is absolutely pertinent that this directory be located where the macro files are located due to how the calls of the combined data macros reference the now saved histograms). When this macro is run (which can take a while), it also plots a few different histograms. The histograms that are plotted are the ones shown in the figures below with descriptions included with the corresponding figures. The order that the histograms appear in this paper is the same order they will be shown when this macro is run in root.

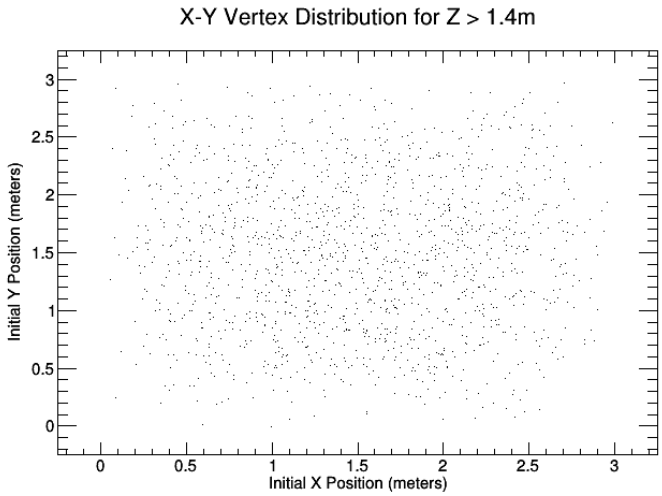


Figure 19: New ν-Mode Rein-Sehgal X-Y vertex distributions for muons that made it to the MRD and penetrated at least to the third layer of steel.

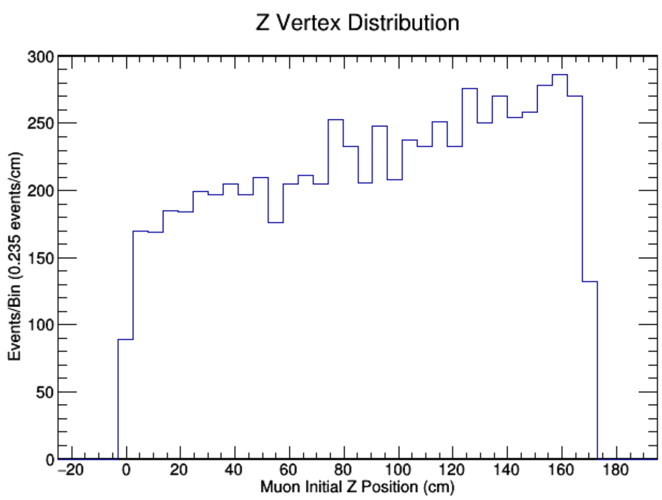


Figure 20: New ν-Mode Rein-Sehgal Z vertex distributions for the interactions.

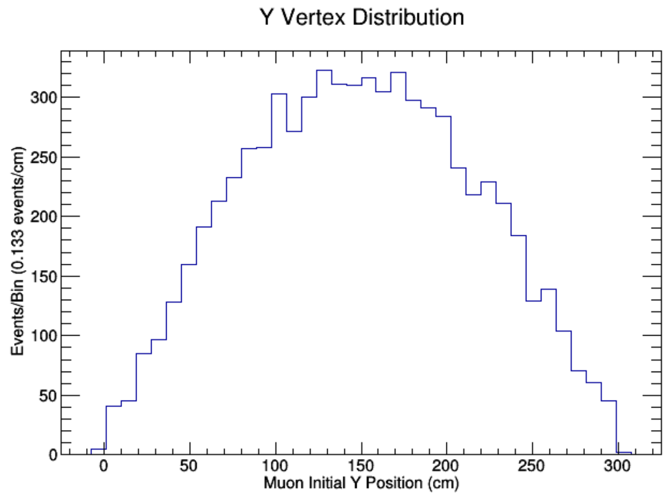


Figure 21: New ν-Mode Rein-Sehgal Y vertex distributions for the interactions.

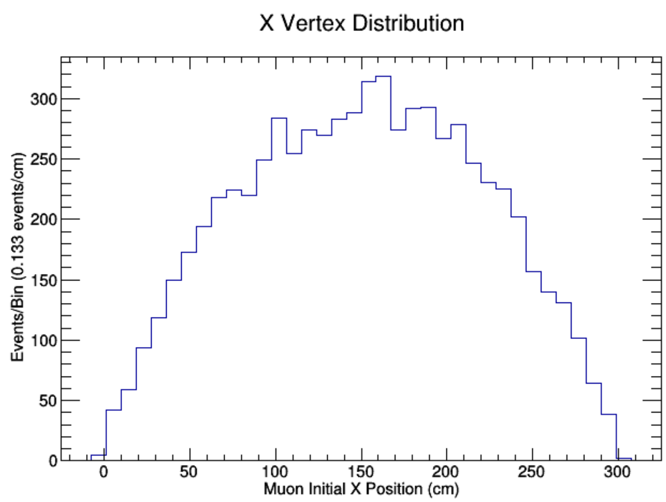


Figure 22: New ν-Mode Rein-Sehgal X vertex distributions for the interactions.

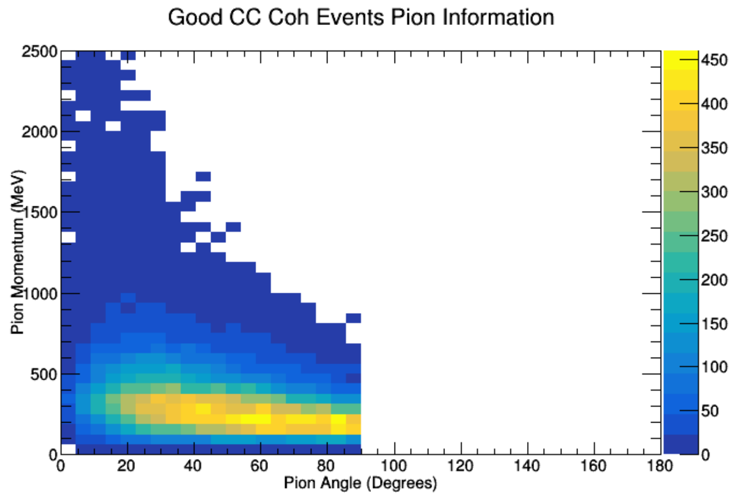


Figure 23: This is a 2D histogram for the momentum and angle of the pion in the CC Coh Pion events that met the qualification of being "good".

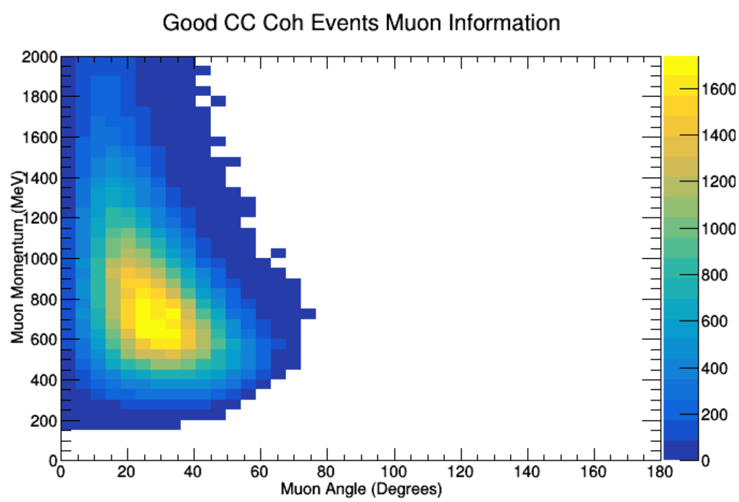


Figure 24: This is a 2D histogram for the momentum and angle of the muon in the CC Coh Pion events that met the qualification of being "good".

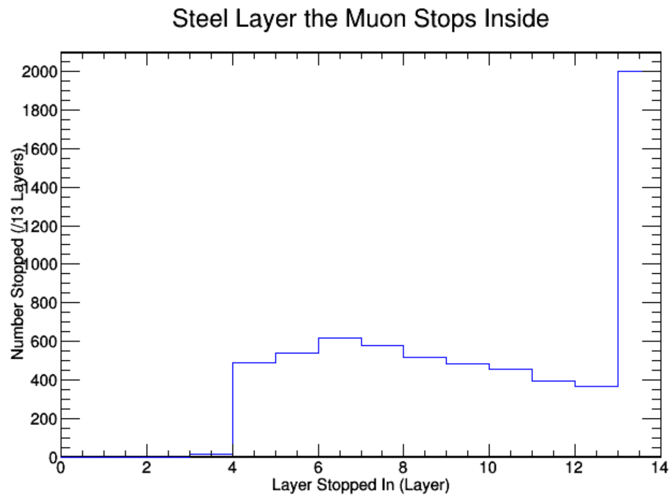


Figure 25: This histogram shows the amount of muons that embedded (or "Stopped") in a corresponding layer of steel in our simulation.

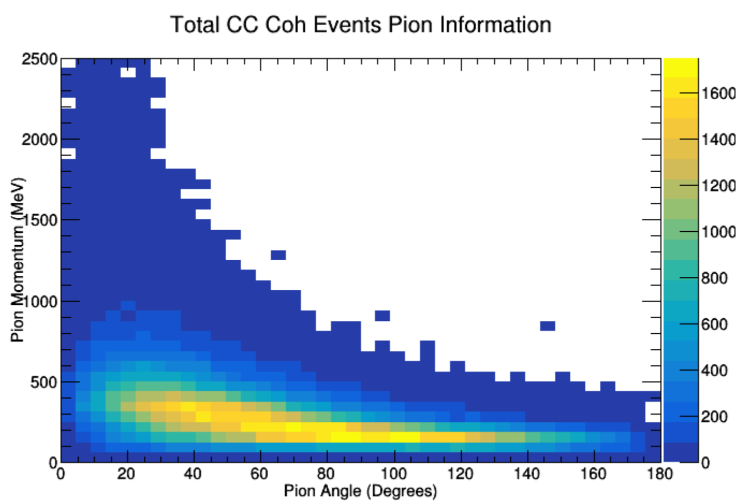


Figure 26: This is a 2D histogram for the momentum and angle of the pion in the total CC Coh Pion events.

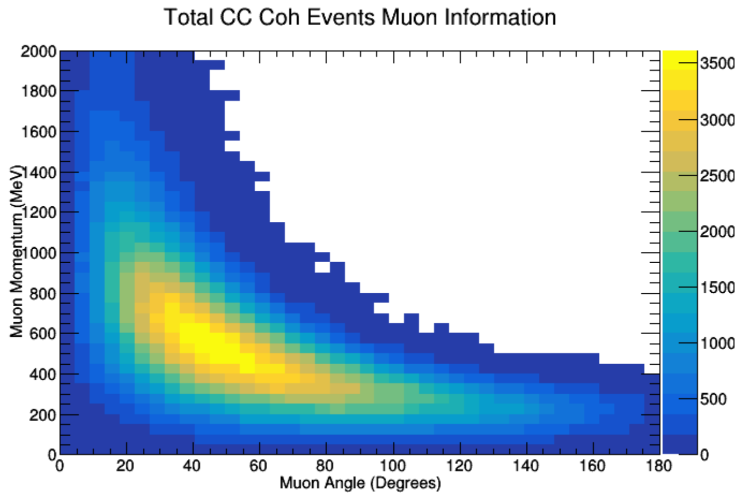


Figure 27: This is a 2D histogram for the momentum and angle of the muon in the total CC Coh Pion events.

The NewNMReinSehgal.C macro also calculates many different quantities for the generated simulation of the events and saves the information in histograms that are later called upon through the plotting macros (which are after all of the analysis macros). The first quantity that is calculated for the different vertexes is the momentum of both the muon and the pion, which are both calculated using the equations:

$$|\vec{p}_\mu| = \sqrt{P_{\mu_x}^2 + P_{\mu_y}^2 + P_{\mu_z}^2} \tag{1}$$

$$|\vec{p}_\pi| = \sqrt{P_{\pi_x}^2 + P_{\pi_y}^2 + P_{\pi_z}^2} \tag{2}$$

The momentum is reported in units of MeV/c.

The next quantity that is calculated in the macro is the angle from the beam-direction for both the muon and the pion, which are labeled as either θ_μ, or θ_π, respectively. The angle from the beam-direction is the same as the angle from the z-direction, and this angle is known as the azimuthal angle. The calculation of the azimuthal angle is slightly more involved than the simple calculation used for finding the magnitude of the momentum of the two particles, and is calculated using the equations:

$$\theta_\mu = tan^{-1}(\sqrt{P_{\mu_x}^2 + P_{\mu_y}^2}/P_{\mu_z}) \tag{3}$$

$$\theta_\pi = tan^{-1}(\sqrt{P_{\pi_x}^2 + P_{\pi_y}^2}/P_{\pi_z}) \tag{4}$$

The angles are reported in units of $^\circ$, and should run from 0° to 180°. In the case of Charged-Current Coherent Pion Production, the angle should never be larger than 90°.

The last two quantities that this analysis macro calculates are the two different types of four-momentum transfers specific to this interaction, which are Q^2 and $|t|$. The Q^2 corresponds to the four-momentum transfer from the neutrino and muon to the nucleus and pion, and is calculated using the equation:

$$Q^2 = |(P_{\nu_\mu} - P_\mu)^2| \tag{5}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute Q^2:

$$Q^2 = |(P_{\nu_{\mu,x}} - P_{\mu_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E})^2| \tag{6}$$

Q^2 is reported in units of $(MeV/c)^2$.

The $|t|$ corresponds to the four-momentum transfer from the neutrino, muon, and pion to the nucleus, and is calculated using the equation:

$$|t| = |(Q - P_\pi)^2| = |(P_{\nu_\mu} - P_\mu - P_\pi)^2| \tag{7}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute $|t|$:

$$|t| = |(P_{\nu_{\mu,x}} - P_{\mu_x} - P_{\pi_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y} - P_{\pi_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z} - P_{\pi_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E} - P_{\pi_E})^2| \tag{8}$$

$|t|$ is reported in units of $(MeV/c)^2$.

A.8 NewNMBergerSehgal.C

This file is the macro that corresponds to the "NewNMBergerSehgal.h" file, which connects with this file: "SciBooNE_numu_coh_RooTrack_NEW.root". This file performs the main analysis for this generated sample, and then organizes the information into many different histograms. The histograms are then written to a file titled "totalmuoninfoBS.root" inside the "ROOTFILES" directory. The "ROOTFILES" directory is included in the SciBooNE-MC repository (it is absolutely pertinent that this directory be located where the macro files are located due to how the calls of the combined data macros reference the now saved histograms).

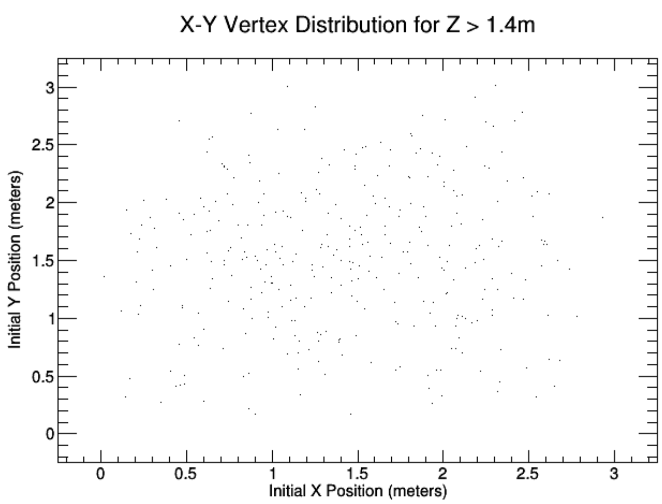


Figure 28: New ν-Mode Berger-Sehgal X-Y vertex distributions for muons that made it to the MRD and penetrated at least to the third layer of steel.

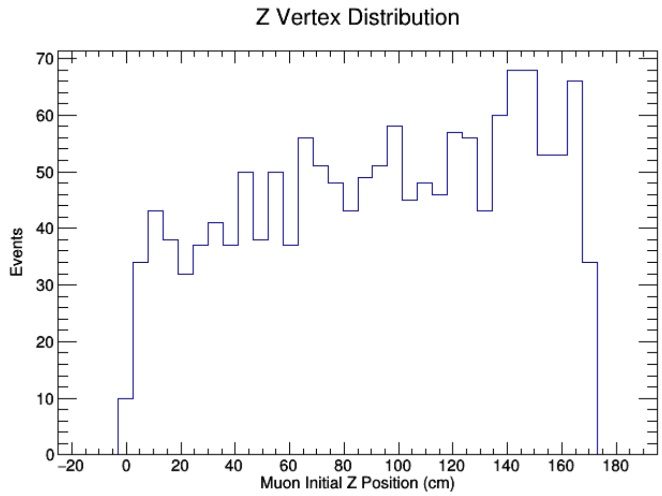


Figure 29: New ν-Mode Berger-Sehgal Z vertex distributions for the interactions.

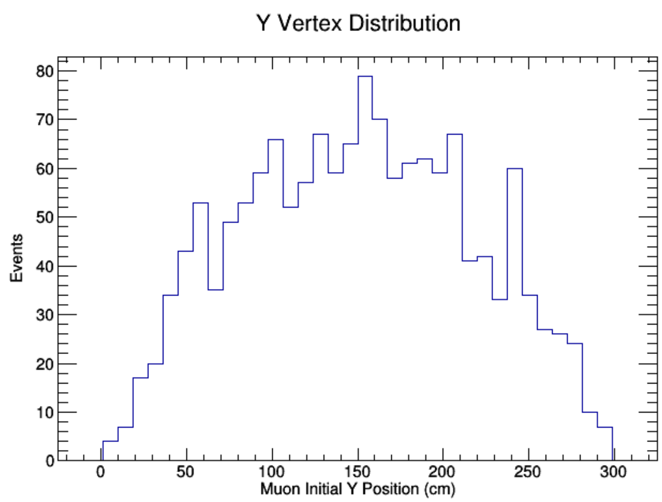


Figure 30: New ν-Mode Berger-Sehgal Y vertex distributions for the interactions.

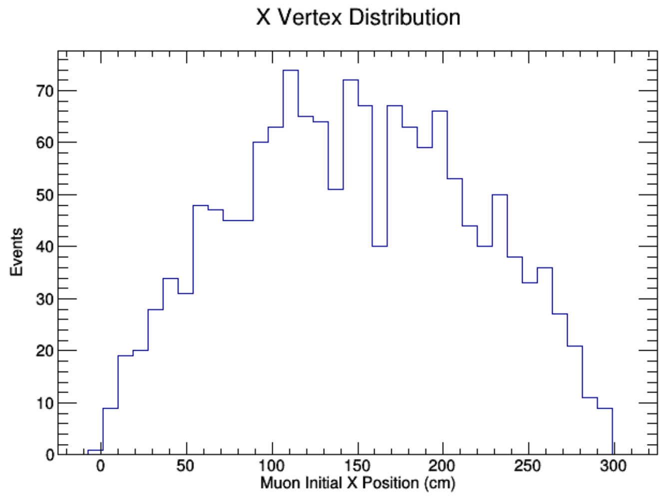


Figure 31: New ν-Mode Berger-Sehgal X vertex distributions for the interactions.

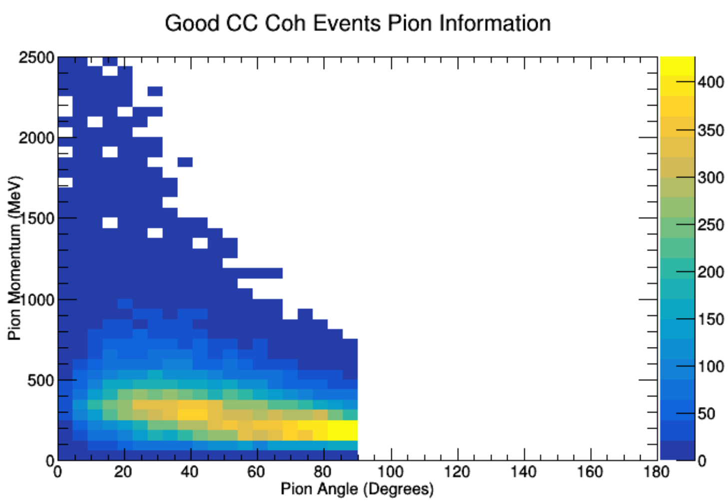


Figure 32: This is a 2D histogram for the momentum and angle of the pion in the CC Coh Pion events that met the qualification of being "good".

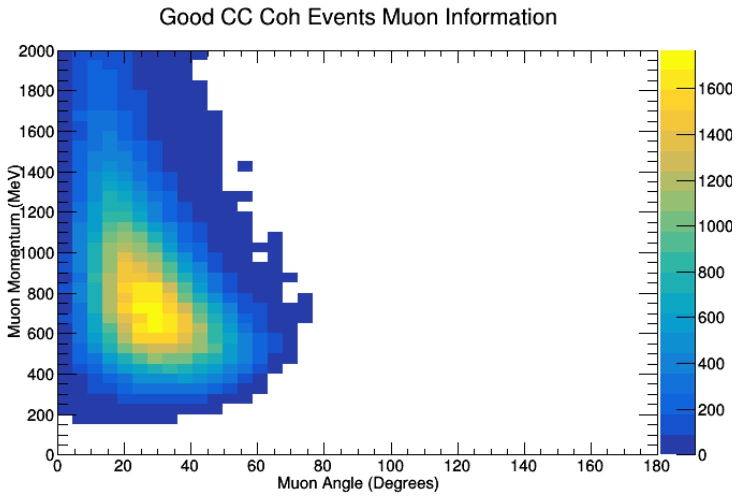


Figure 33: This is a 2D histogram for the momentum and angle of the muon in the CC Coh Pion events that met the qualification of being "good".!

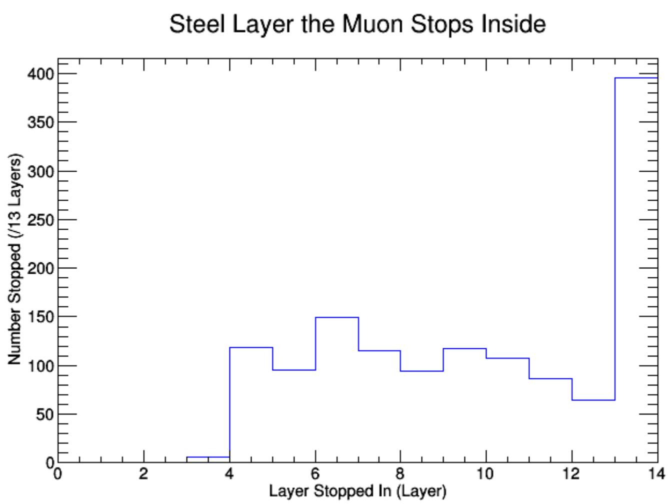


Figure 34: This histogram shows the amount of muons that embedded (or "Stopped") in a corresponding layer of steel in our simulation.

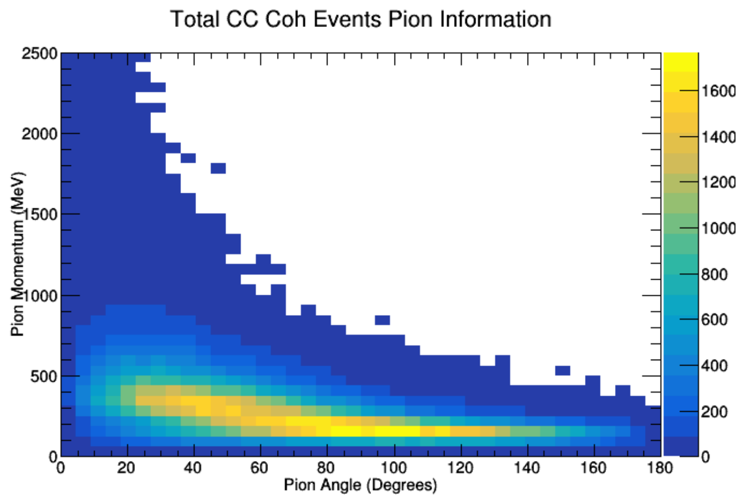


Figure 35: This is a 2D histogram for the momentum and angle of the pion in the total CC Coh Pion events.

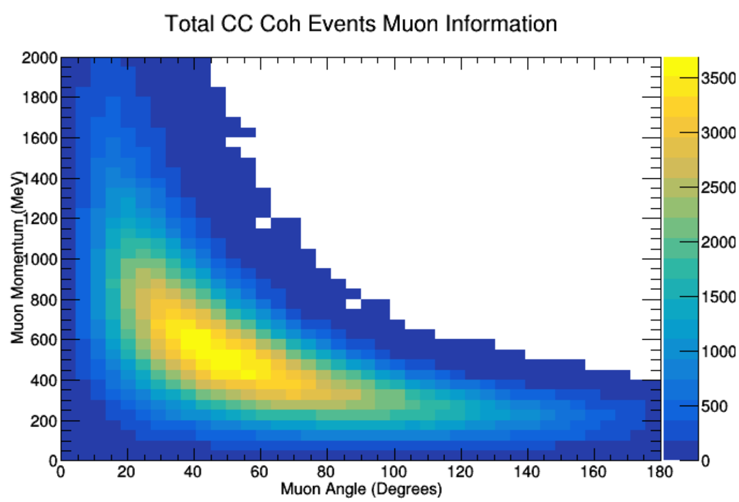


Figure 36: This is a 2D histogram for the momentum and angle of the muon in the total CC Coh Pion events.

The NewNMBergerSehgal.C macro also calculates many different quantities for the generated simulation of the events and saves the information in histograms that are later called upon through the plotting macros (which are after all of the analysis macros). The first quantity that is calculated for the different vertexes is the momentum of both the muon and the pion, which are both calculated using the equations:

$$|\vec{p}_\mu| = \sqrt{P^2_{\mu_x} + P^2_{\mu_y} + P^2_{\mu_z}} \tag{9}$$

$$|\vec{p}_\pi| = \sqrt{P^2_{\pi_x} + P^2_{\pi_y} + P^2_{\pi_z}} \tag{10}$$

The momentum is reported in units of MeV/c.

The next quantity that is calculated in the macro is the angle from the beam-direction for both the muon and the pion, which are labeled as either θ_μ, or θ_π, respectively. The angle from the beam-direction is the same as the angle from the z-direction, and this angle is known as the azimuthal angle. The calculation of the azimuthal angle is slightly more involved than the simple calculation used for finding the magnitude of the momentum of the two particles, and is calculated using the equations:

$$\theta_\mu = tan^{-1}(\sqrt{P_{\mu_x}^2 + P_{\mu_y}^2}/P_{\mu_z}) \tag{11}$$

$$\theta_\pi = tan^{-1}(\sqrt{P_{\pi_x}^2 + P_{\pi_y}^2}/P_{\pi_z}) \tag{12}$$

The angles are reported in units of $^\circ$, and should run from 0° to 180°. In the case of Charged-Current Coherent Pion Production, the angle should never be larger than 90°.

The last two quantities that this analysis macro calculates are the two different types of four-momentum transfers specific to this interaction, which are Q^2 and $|t|$. The Q^2 corresponds to the four-momentum transfer from the neutrino and muon to the nucleus and pion, and is calculated using the equation:

$$Q^2 = |(P_{\nu_\mu} - P_\mu)^2| \tag{13}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute Q^2:

$$Q^2 = |(P_{\nu_{\mu,x}} - P_{\mu_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E})^2| \tag{14}$$

Q^2 is reported in units of $(MeV/c)^2$.

The $|t|$ corresponds to the four-momentum transfer from the neutrino, muon, and pion to the nucleus, and is calculated using the equation:

$$|t| = |(Q - P_\pi)^2| = |(P_{\nu_\mu} - P_\mu - P_\pi)^2| \tag{15}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute $|t|$:

$$|t| = |(P_{\nu_{\mu,x}} - P_{\mu_x} - P_{\pi_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y} - P_{\pi_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z} - P_{\pi_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E} - P_{\pi_E})^2| \tag{16}$$

$|t|$ is reported in units of $(MeV/c)^2$.

A.9 OldNMReinSehgal.C

This file is the macro that corresponds to the "OldNMReinSehgal.h" file, which connects with this file: "SciBooNE_numu_coh_OLDNEUT_RooTrack.root". This file performs the main analysis for this generated sample, and then organizes the information into many different histograms. The histograms are then written to a file titled "totalmuoninfoOBS.root" inside the "ROOTFILES" directory. The "ROOTFILES" directory is included in the SciBooNE-MC repository (it is absolutely pertinent that this directory be located where the macro files are located due to how the calls of the combined data macros reference the now saved histograms).

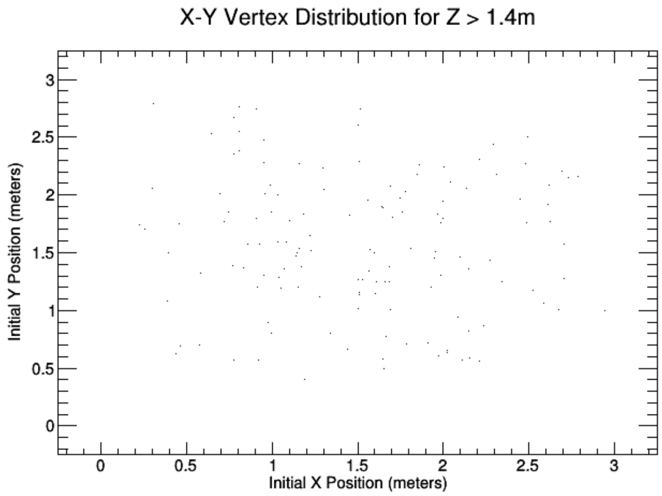


Figure 37: Old ν-Mode Rein-Sehgal X-Y vertex distributions for muons that made it to the MRD and penetrated at least to the third layer of steel.

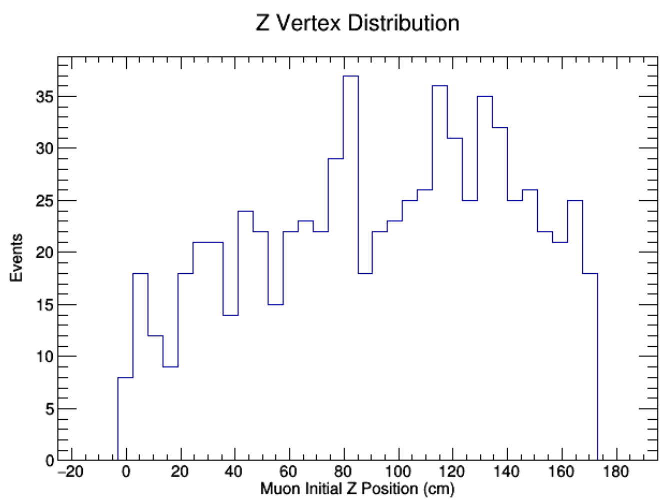


Figure 38: Old ν-Mode Rein-Sehgal Z vertex distributions for the interactions.

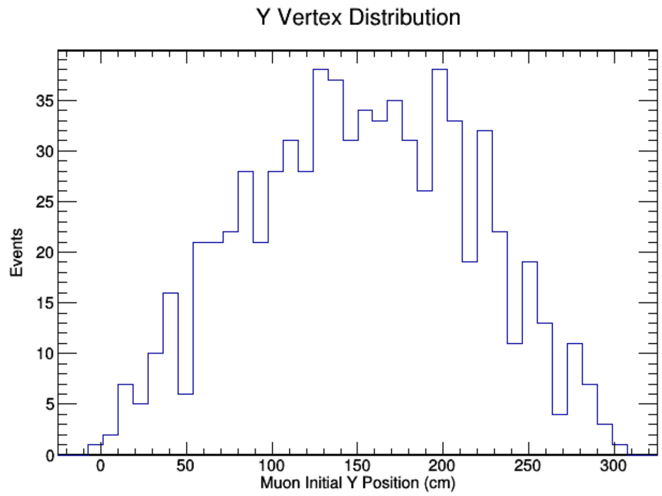


Figure 39: Old ν-Mode Rein-Sehgal Y vertex distributions for the interactions.

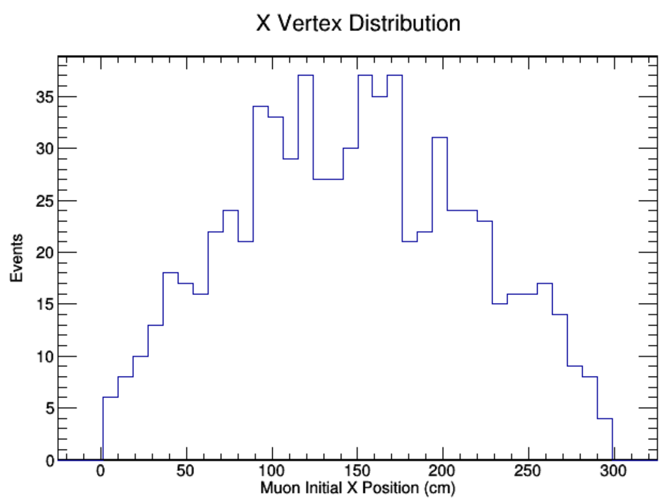


Figure 40: Old ν-Mode Rein-Sehgal X vertex distributions for the interactions.

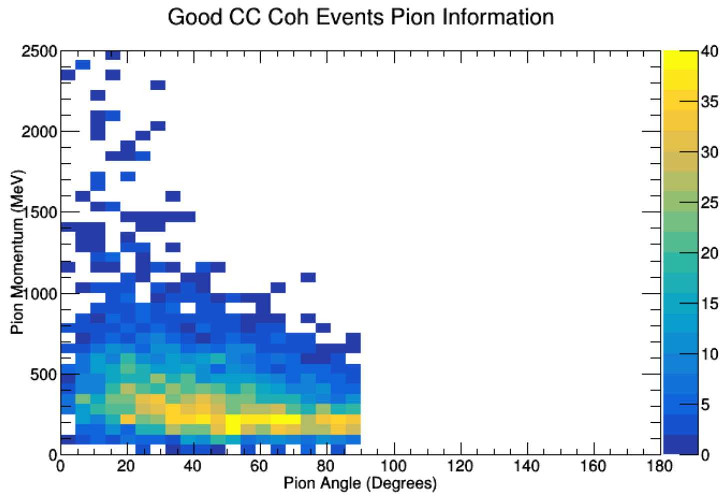


Figure 41: This is a 2D histogram for the momentum and angle of the pion in the CC Coh Pion events that met the qualification of being "good".

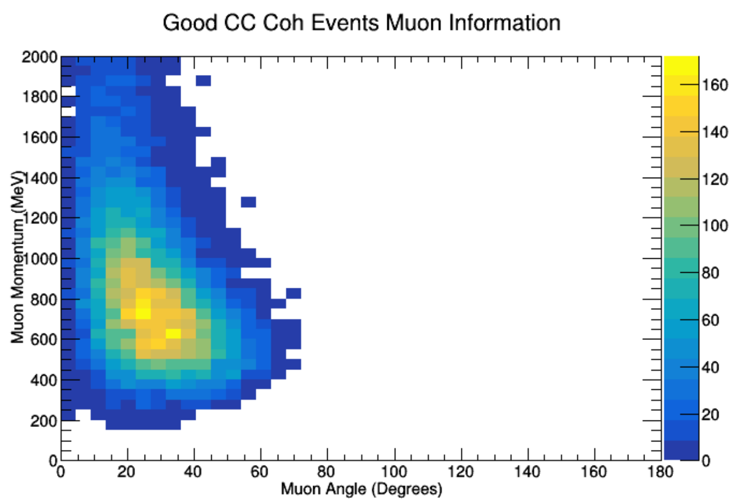


Figure 42: This is a 2D histogram for the momentum and angle of the muon in the CC Coh Pion events that met the qualification of being "good".

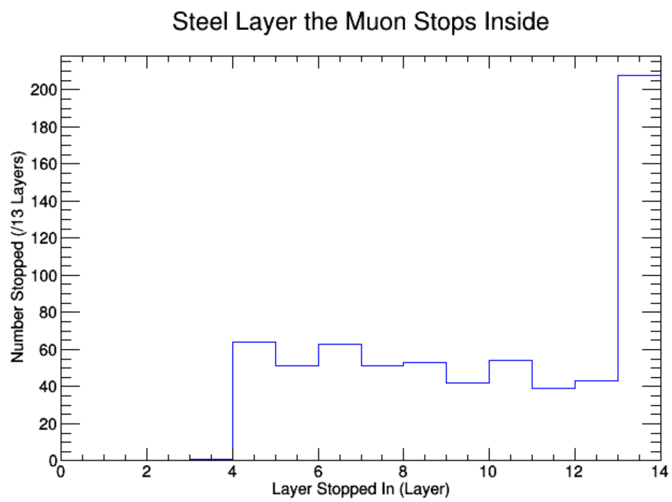


Figure 43: This histogram shows the amount of muons that embedded (or "Stopped") in a corresponding layer of steel in our simulation.

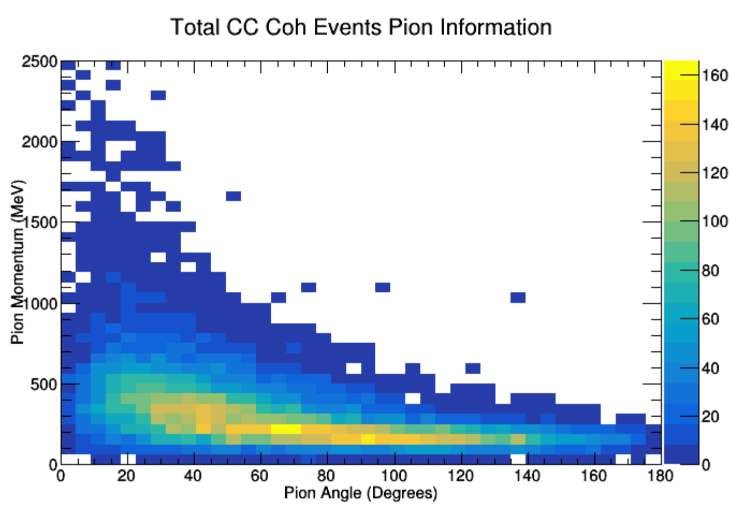


Figure 44: This is a 2D histogram for the momentum and angle of the pion in the total CC Coh Pion events.

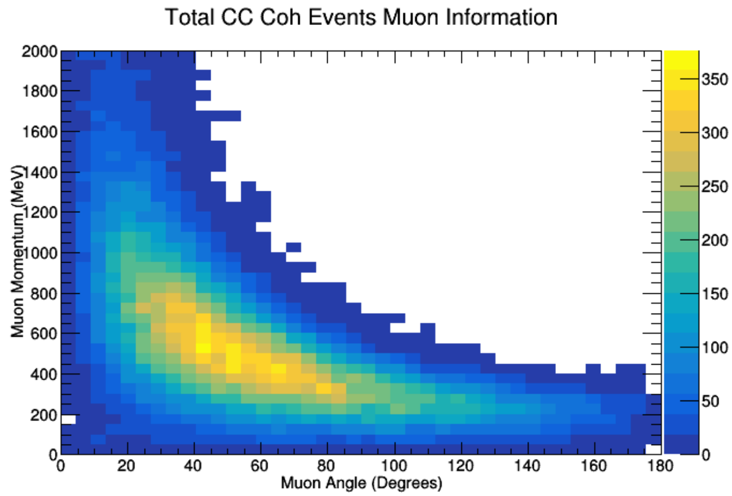


Figure 45: This is a 2D histogram for the momentum and angle of the muon in the total CC Coh Pion events.

The OldNMReinSehgal.C macro also calculates many different quantities for the generated simulation of the events and saves the information in histograms that are later called upon through the plotting macros (which are after all of the analysis macros). The first quantity that is calculated for the different vertexes is the momentum of both the muon and the pion, which are both calculated using the equations:

$$|\vec{p}_{\mu}| = \sqrt{P_{\mu_x}^2 + P_{\mu_y}^2 + P_{\mu_z}^2} \tag{17}$$

$$|\vec{p}_{\pi}| = \sqrt{P_{\pi_x}^2 + P_{\pi_y}^2 + P_{\pi_z}^2} \tag{18}$$

The momentum is reported in units of MeV/c.

The next quantity that is calculated in the macro is the angle from the beam-direction for both the muon and the pion, which are labeled as either θ_{μ}, or θ_{π}, respectively. The angle from the beam-direction is the same as the angle from the z-direction, and this angle is known as the azimuthal angle. The calculation of the azimuthal angle is slightly more involved than the simple calculation used for finding the magnitude of the momentum of the two particles, and is calculated using the equations:

$$\theta_{\mu} = tan^{-1}(\sqrt{P_{\mu_x}^2 + P_{\mu_y}^2}/P_{\mu_z}) \tag{19}$$

$$\theta_{\pi} = tan^{-1}(\sqrt{P_{\pi_x}^2 + P_{\pi_y}^2}/P_{\pi_z}) \tag{20}$$

The angles are reported in units of $^{\circ}$, and should run from 0° to 180°. In the case of Charged-Current Coherent Pion Production, the angle should never be larger than 90°.

The last two quantities that this analysis macro calculates are the two different types of four-momentum transfers specific to this interaction, which are Q^2 and $|t|$. The Q^2 corresponds to the four-momentum transfer from the neutrino and muon to the nucleus and pion, and is calculated using the equation:

$$Q^2 = |(P_{\nu_{\mu}} - P_{\mu})^2| \tag{21}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute Q^2:

$$Q^2 = |(P_{\nu_{\mu,x}} - P_{\mu_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E})^2| \tag{22}$$

Q^2 is reported in units of $(MeV/c)^2$.

The $|t|$ corresponds to the four-momentum transfer from the neutrino, muon, and pion to the nucleus, and is calculated using the equation:

$$|t| = |(Q - P_\pi)^2| = |(P_{\nu_\mu} - P_\mu - P_\pi)^2| \tag{23}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute $|t|$:

$$|t| = |(P_{\nu_{\mu,x}} - P_{\mu_x} - P_{\pi_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y} - P_{\pi_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z} - P_{\pi_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E} - P_{\pi_E})^2| \tag{24}$$

$|t|$ is reported in units of $(MeV/c)^2$.

A.10 NewANMReinSehgal.C

This file is the macro that corresponds to the "NewANMReinSehgal.h" file, which connects with this file: "SciBooNE_numubar_coh_RooTrack.root". This file performs the main analysis for this generated sample, and then organizes the information into many different histograms. The histograms are then written to a file titled "totalmuoninfoRSBar.root" inside the "ROOTFILES" directory. The "ROOTFILES" directory is included in the SciBooNE-MC repository (it is absolutely pertinent that this directory be located where the macro files are located due to how the calls of the combined data macros reference the now saved histograms).

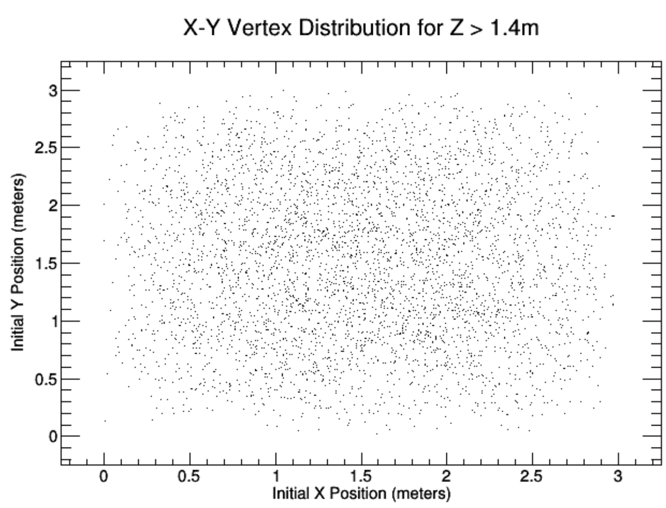


Figure 46: New $\bar{\nu}$-Mode Rein-Sehgal X-Y vertex distributions for muons that made it to the MRD and penetrated at least to the third layer of steel.

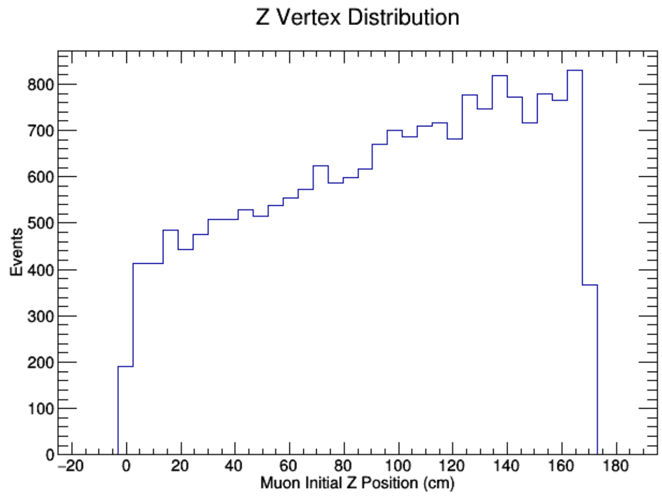


Figure 47: New $\bar{\nu}$-Mode Rein-Sehgal Z vertex distributions for the interactions.

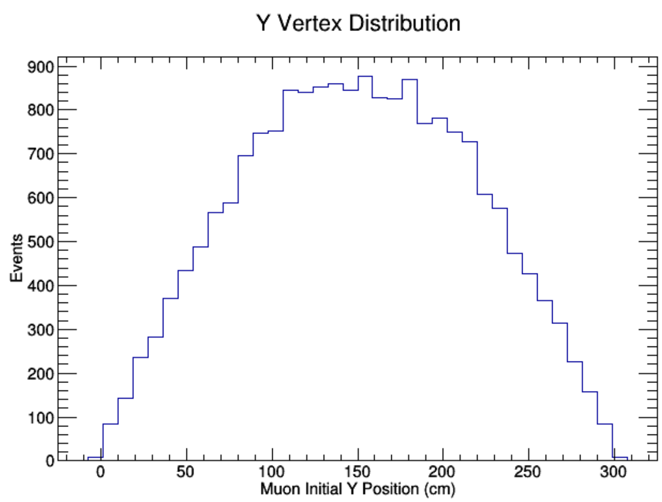


Figure 48: New $\bar{\nu}$-Mode Rein-Sehgal Y vertex distributions for the interactions.

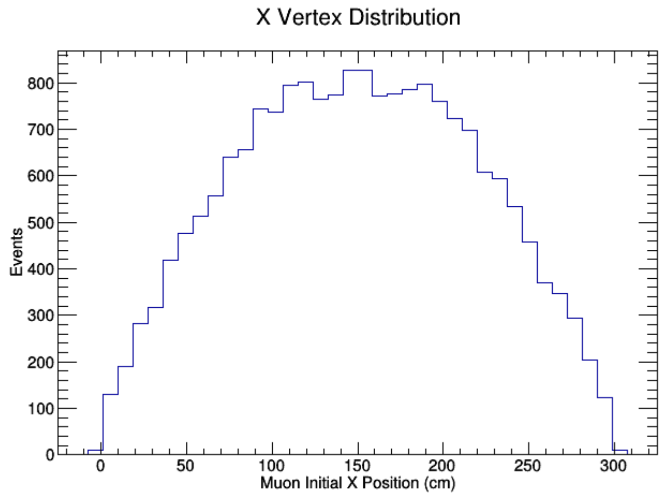


Figure 49: New $\bar{\nu}$-Mode Rein-Sehgal X vertex distributions for the interactions.

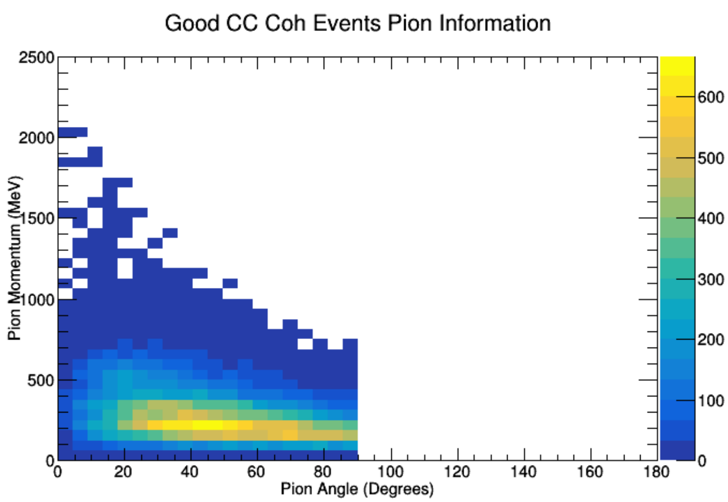


Figure 50: This is a 2D histogram for the momentum and angle of the pion in the CC Coh Pion events that met the qualification of being "good".

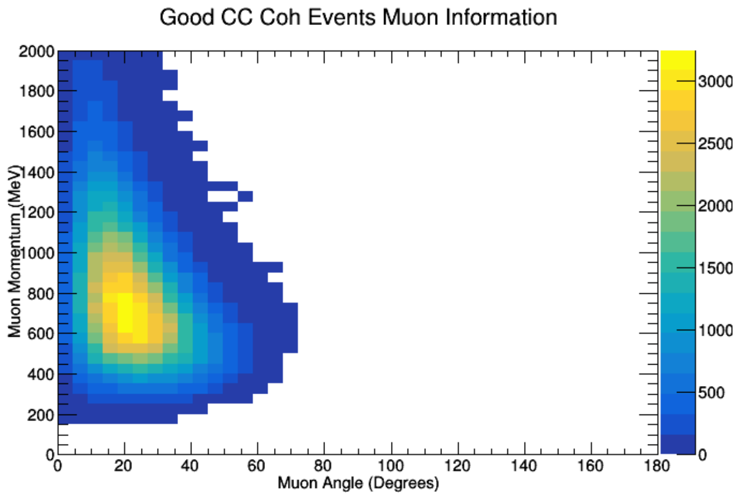


Figure 51: This is a 2D histogram for the momentum and angle of the muon in the CC Coh Pion events that met the qualification of being "good".

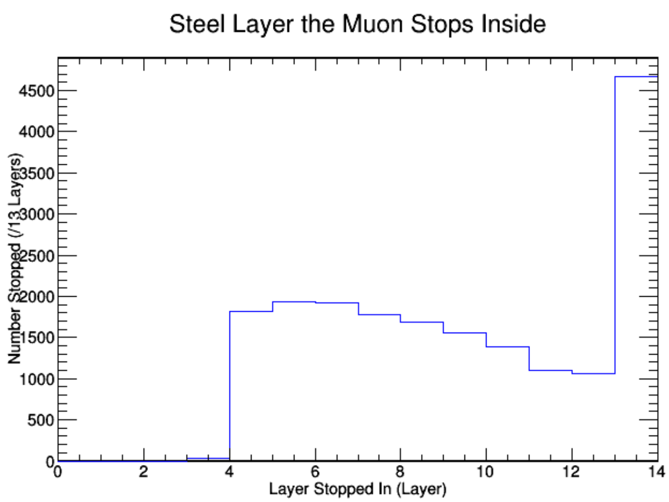


Figure 52: This histogram shows the amount of muons that embedded (or "Stopped") in a corresponding layer of steel in our simulation.

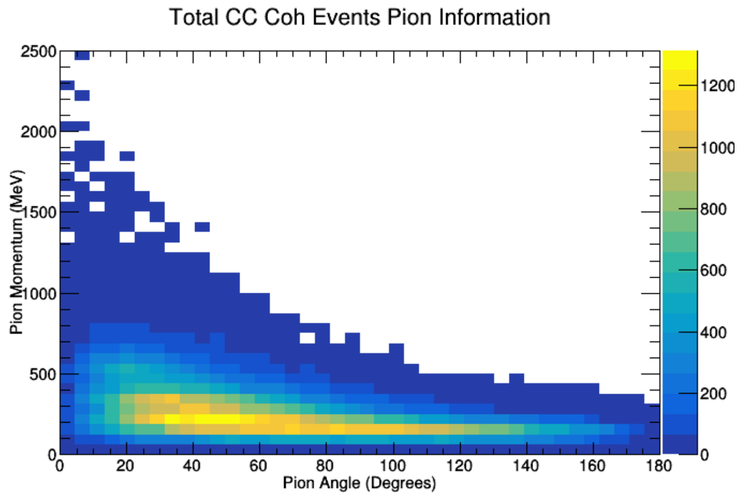


Figure 53: This is a 2D histogram for the momentum and angle of the pion in the total CC Coh Pion events.

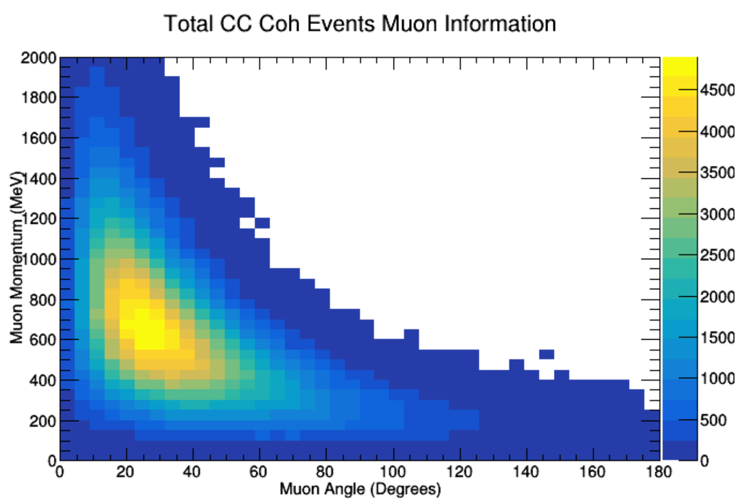


Figure 54: This is a 2D histogram for the momentum and angle of the muon in the total CC Coh Pion events.

The NewANMReinSehgal.C macro also calculates many different quantities for the generated simulation of the events and saves the information in histograms that are later called upon through the plotting macros (which are after all of the analysis macros). The first quantity that is calculated for the different vertexes is the momentum of both the muon and the pion, which are both calculated using the equations:

$$|\vec{p}_\mu| = \sqrt{P_{\mu_x}^2 + P_{\mu_y}^2 + P_{\mu_z}^2} \tag{25}$$

$$|\vec{p}_\pi| = \sqrt{P_{\pi_x}^2 + P_{\pi_y}^2 + P_{\pi_z}^2} \tag{26}$$

The momentum is reported in units of MeV/c.

The next quantity that is calculated in the macro is the angle from the beam-direction for both the muon and the pion, which are labeled as either θ_μ, or θ_π, respectively. The angle from the beam-direction is the same as the angle from the z-direction, and this angle is known as the azimuthal angle. The calculation of the azimuthal angle is slightly more involved than the simple calculation used for finding the magnitude of the momentum of the two particles, and is calculated using the equations:

$$\theta_\mu = tan^{-1}(\sqrt{P_{\mu_x}^2 + P_{\mu_y}^2}/P_{\mu_z}) \tag{27}$$

$$\theta_\pi = tan^{-1}(\sqrt{P_{\pi_x}^2 + P_{\pi_y}^2}/P_{\pi_z}) \tag{28}$$

The angles are reported in units of °, and should run from 0° to 180°. In the case of Charged-Current Coherent Pion Production, the angle should never be larger than 90°.

The last two quantities that this analysis macro calculates are the two different types of four-momentum transfers specific to this interaction, which are Q^2 and $|t|$. The Q^2 corresponds to the four-momentum transfer from the neutrino and muon to the nucleus and pion, and is calculated using the equation:

$$Q^2 = |(P_{\nu_\mu} - P_\mu)^2| \tag{29}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute Q^2:

$$Q^2 = |(P_{\nu_{\mu,x}} - P_{\mu_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E})^2| \tag{30}$$

Q^2 is reported in units of $(MeV/c)^2$.

The $|t|$ corresponds to the four-momentum transfer from the neutrino, muon, and pion to the nucleus, and is calculated using the equation:

$$|t| = |(Q - P_\pi)^2| = |(P_{\nu_\mu} - P_\mu - P_\pi)^2| \tag{31}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute $|t|$:

$$|t| = |(P_{\nu_{\mu,x}} - P_{\mu_x} - P_{\pi_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y} - P_{\pi_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z} - P_{\pi_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E} - P_{\pi_E})^2| \tag{32}$$

$|t|$ is reported in units of $(MeV/c)^2$.

A.11 NewANMBergerSehgal.C

This file is the macro that corresponds to the "NewANMBergerSehgal.h" file, which connects with this file: "SciBooNE_numubar_coh_RooTrack_NEW.root". This file performs the main analysis for this generated sample, and then organizes the information into many different histograms. The histograms are then written to a file titled "totalmuoninfoBSBar.root" inside the "ROOTFILES" directory. The "ROOTFILES" directory is included in the SciBooNE-MC repository (it is absolutely pertinent that this directory be located where the macro files are located due to how the calls of the combined data macros reference the now saved histograms).

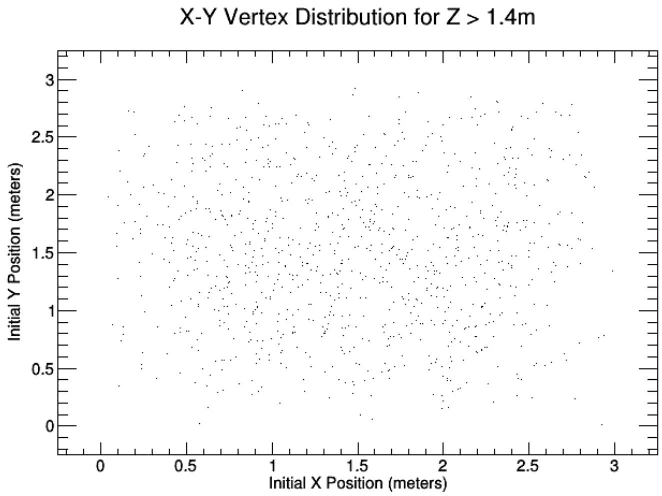


Figure 55: New $\bar{\nu}$-Mode Berger-Sehgal X-Y vertex distributions for muons that made it to the MRD and penetrated at least to the third layer of steel.

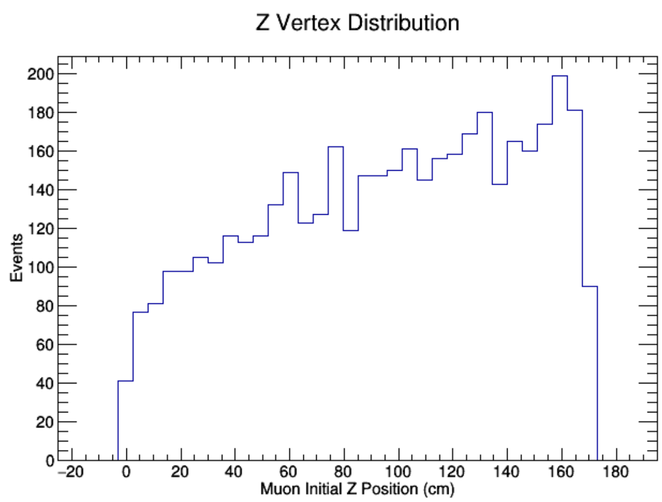


Figure 56: New $\bar{\nu}$-Mode Berger-Sehgal Z vertex distributions for the interactions.

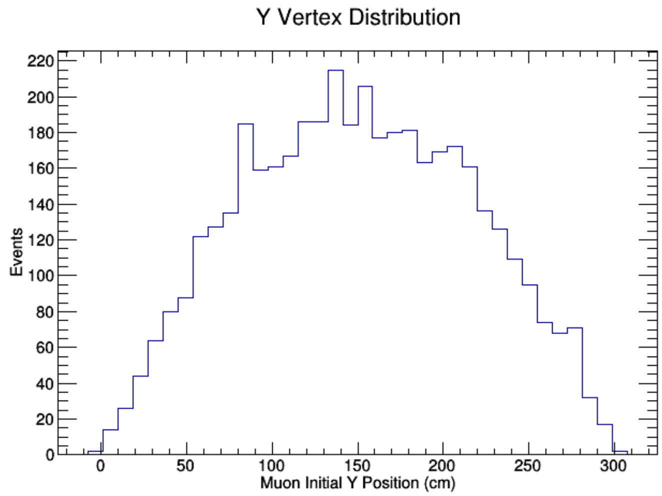


Figure 57: New $\bar{\nu}$-Mode Berger-Sehgal Y vertex distributions for the interactions.

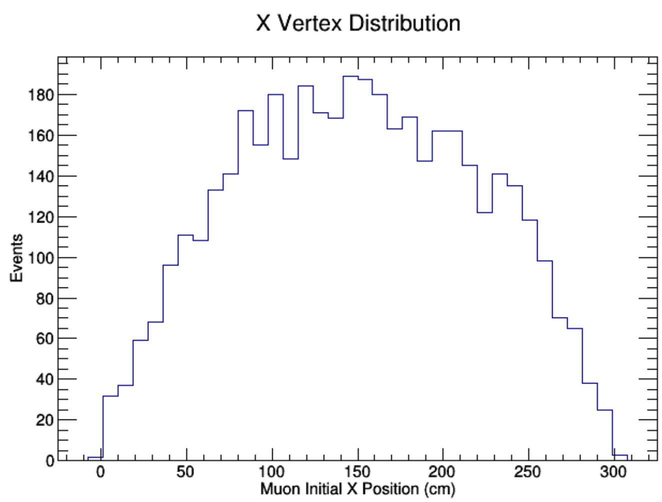


Figure 58: New $\bar{\nu}$-Mode Berger-Sehgal X vertex distributions for the interactions.

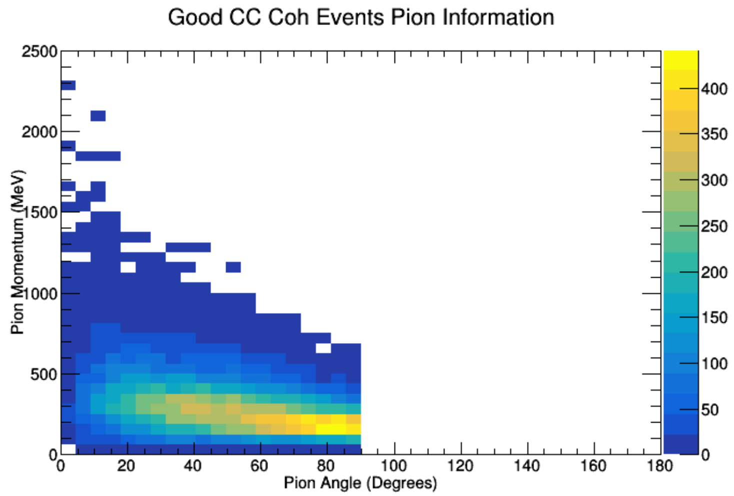


Figure 59: This is a 2D histogram for the momentum and angle of the pion in the CC Coh Pion events that met the qualification of being "good".

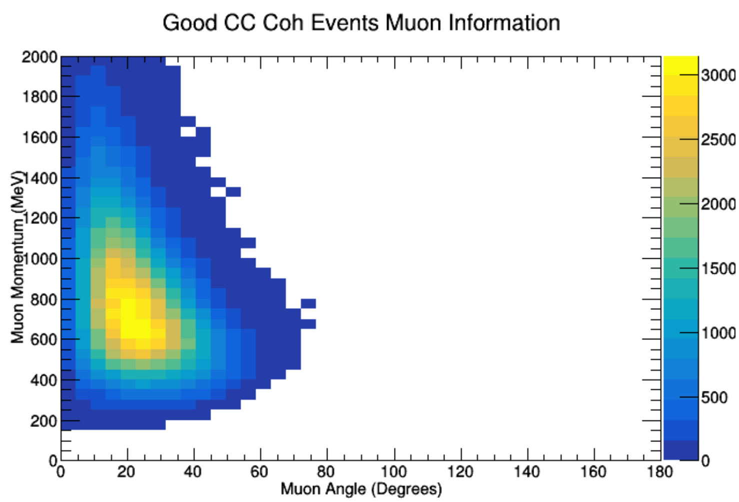


Figure 60: This is a 2D histogram for the momentum and angle of the muon in the CC Coh Pion events that met the qualification of being "good".

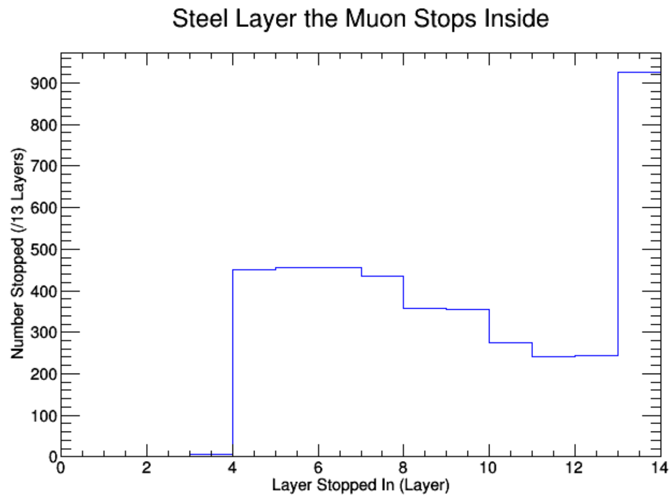


Figure 61: This histogram shows the amount of muons that embedded (or "Stopped") in a corresponding layer of steel in our simulation.

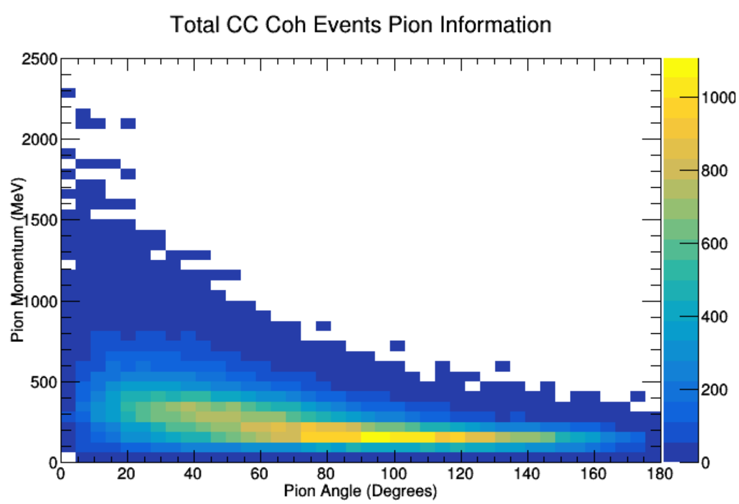


Figure 62: This is a 2D histogram for the momentum and angle of the pion in the total CC Coh Pion events.

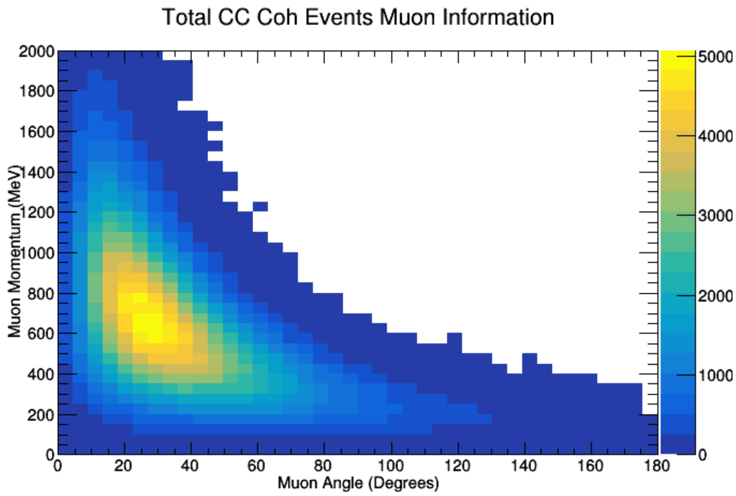


Figure 63: This is a 2D histogram for the momentum and angle of the muon in the total CC Coh Pion events.

The NewANMBergerSehgal.C macro also calculates many different quantities for the generated simulation of the events and saves the information in histograms that are later called upon through the plotting macros (which are after all of the analysis macros). The first quantity that is calculated for the different vertexes is the momentum of both the muon and the pion, which are both calculated using the equations:

$$|\vec{p}_{\mu}| = \sqrt{P^2_{\mu_x} + P^2_{\mu_y} + P^2_{\mu_z}} \tag{33}$$

$$|\vec{p}_{\pi}| = \sqrt{P^2_{\pi_x} + P^2_{\pi_y} + P^2_{\pi_z}} \tag{34}$$

The momentum is reported in units of MeV/c.

The next quantity that is calculated in the macro is the angle from the beam-direction for both the muon and the pion, which are labeled as either θ_{μ}, or θ_{π}, respectively. The angle from the beam-direction is the same as the angle from the z-direction, and this angle is known as the azimuthal angle. The calculation of the azimuthal angle is slightly more involved than the simple calculation used for finding the magnitude of the momentum of the two particles, and is calculated using the equations:

$$\theta_{\mu} = tan^{-1}(\sqrt{P^2_{\mu_x} + P^2_{\mu_y}}/P_{\mu_z}) \tag{35}$$

$$\theta_{\pi} = tan^{-1}(\sqrt{P^2_{\pi_x} + P^2_{\pi_y}}/P_{\pi_z}) \tag{36}$$

The angles are reported in units of $^{\circ}$, and should run from 0° to 180°. In the case of Charged-Current Coherent Pion Production, the angle should never be larger than 90°.

The last two quantities that this analysis macro calculates are the two different types of four-momentum transfers specific to this interaction, which are Q^2 and $|t|$. The Q^2 corresponds to the four-momentum transfer from the neutrino and muon to the nucleus and pion, and is calculated using the equation:

$$Q^2 = |(P_{\nu_{\mu}} - P_{\mu})^2| \tag{37}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute Q^2:

$$Q^2 = |(P_{\nu_{\mu,x}} - P_{\mu_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E})^2| \tag{38}$$

Q^2 is reported in units of $(MeV/c)^2$.

The $|t|$ corresponds to the four-momentum transfer from the neutrino, muon, and pion to the nucleus, and is calculated using the equation:

$$|t| = |(Q - P_\pi)^2| = |(P_{\nu_\mu} - P_\mu - P_\pi)^2| \tag{39}$$

This equation is the four-momentum notational form. The code follows the equation below in order to compute $|t|$:

$$|t| = |(P_{\nu_{\mu,x}} - P_{\mu_x} - P_{\pi_x})^2 + (P_{\nu_{\mu,y}} - P_{\mu_y} - P_{\pi_y})^2 + (P_{\nu_{\mu,z}} - P_{\mu_z} - P_{\pi_z})^2 + (P_{\nu_{\mu,E}} - P_{\mu_E} - P_{\pi_E})^2| \tag{40}$$

$|t|$ is reported in units of $(MeV/c)^2$.

A.12 NMCombinedPlots.C

I need to come back and insert all of my images here.

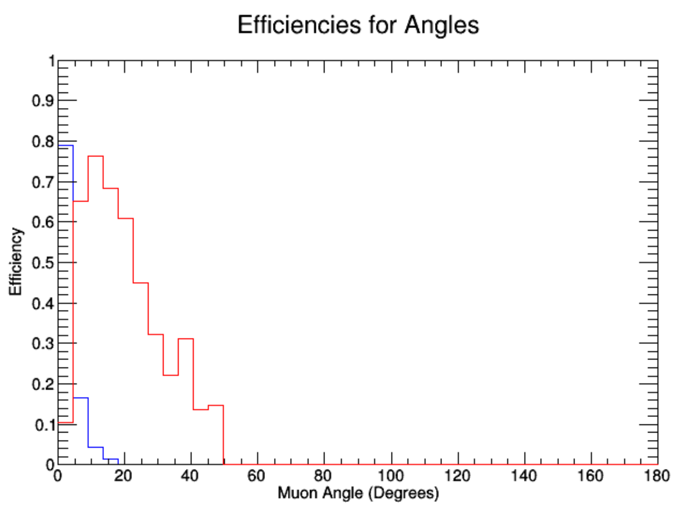


Figure 64:

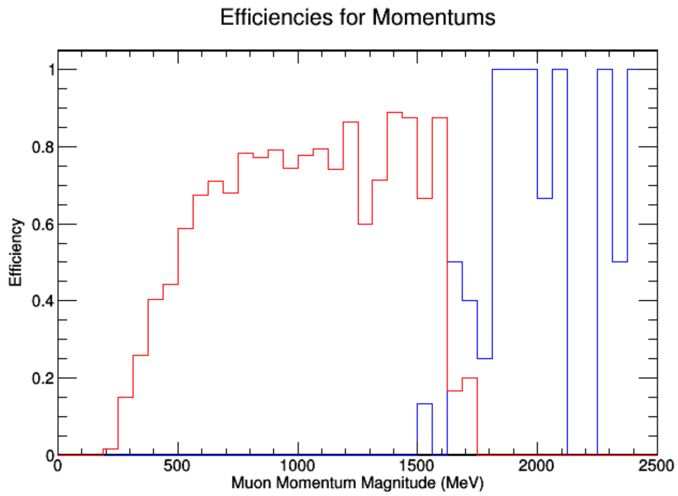


Figure 65:

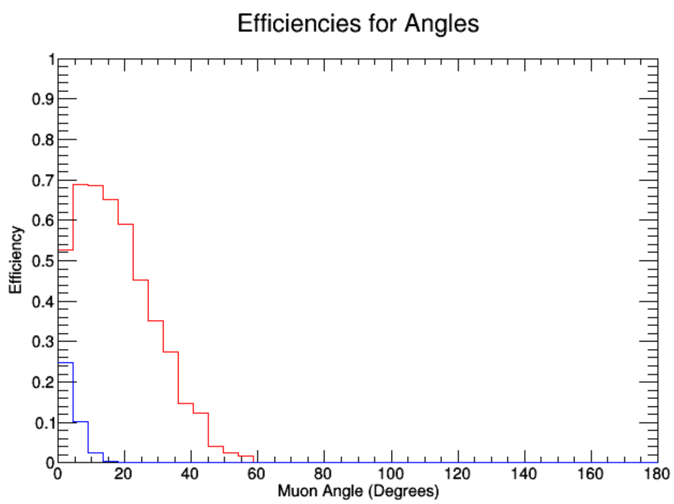


Figure 66:

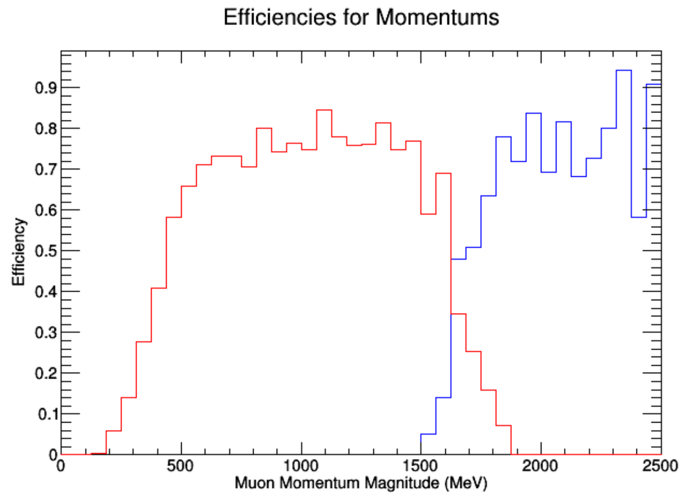
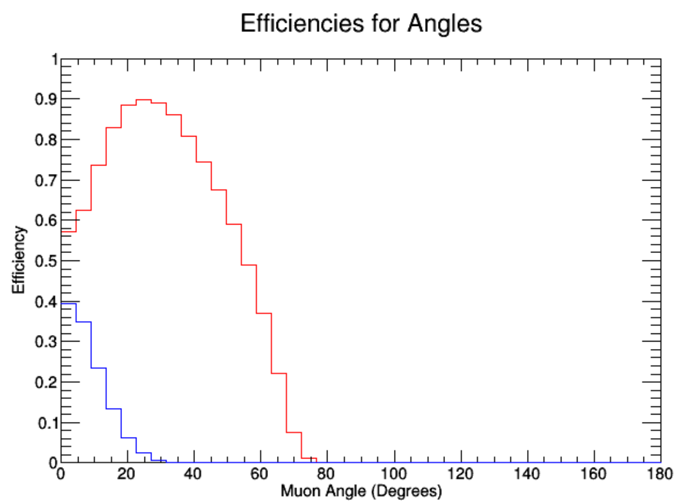


Figure 67:



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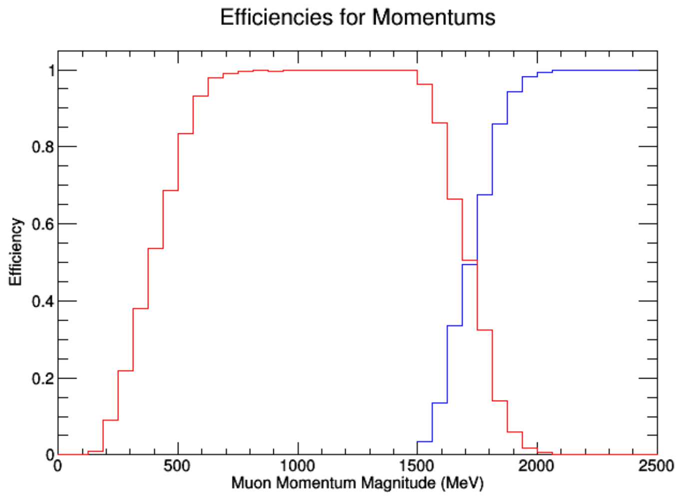

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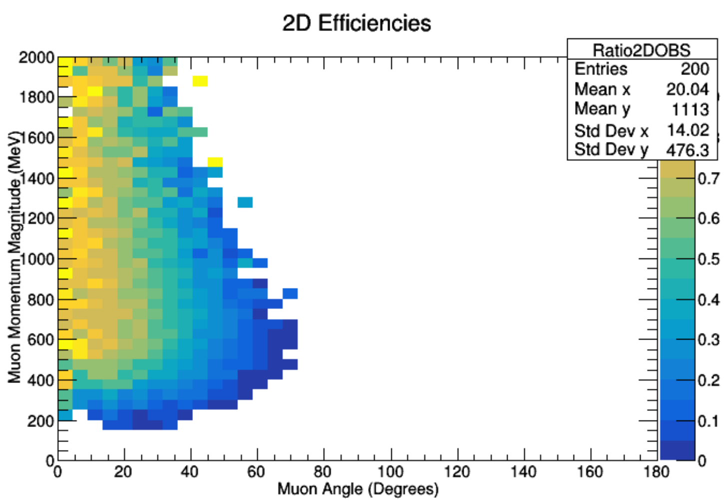
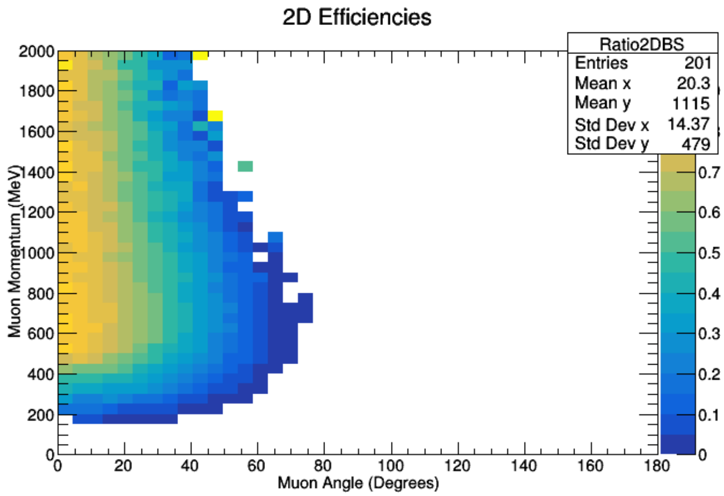


Figure 70:



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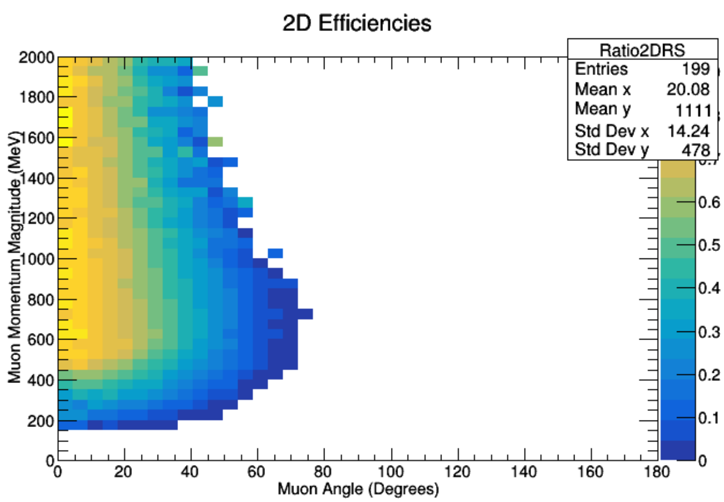

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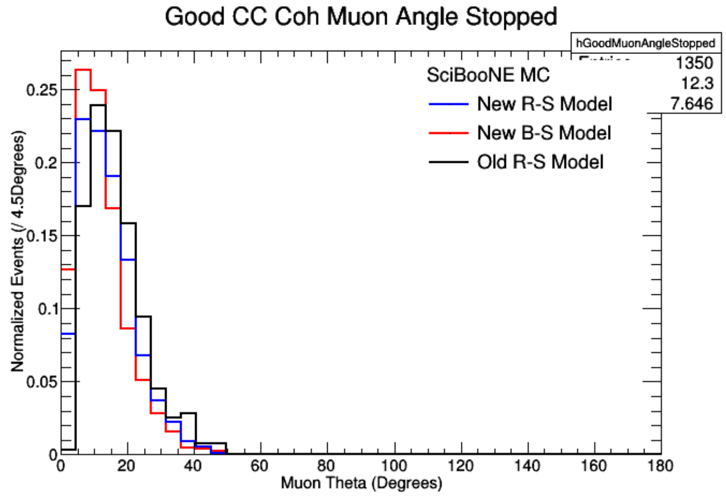

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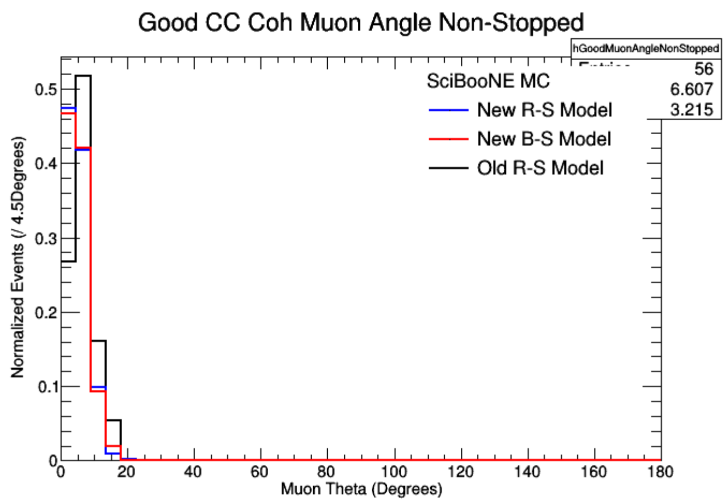

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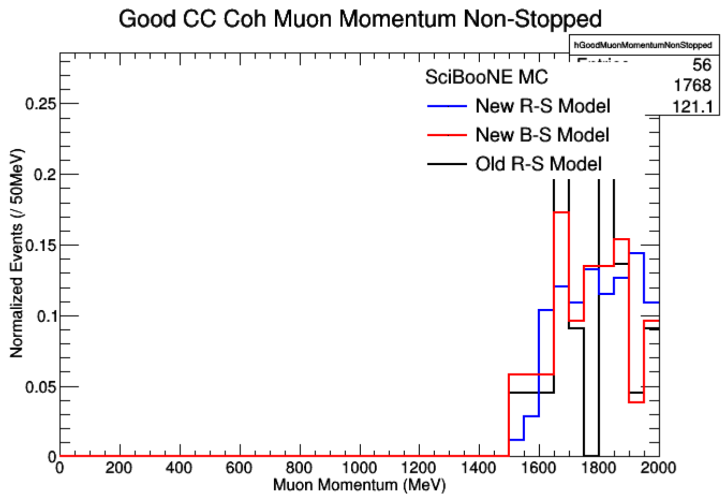

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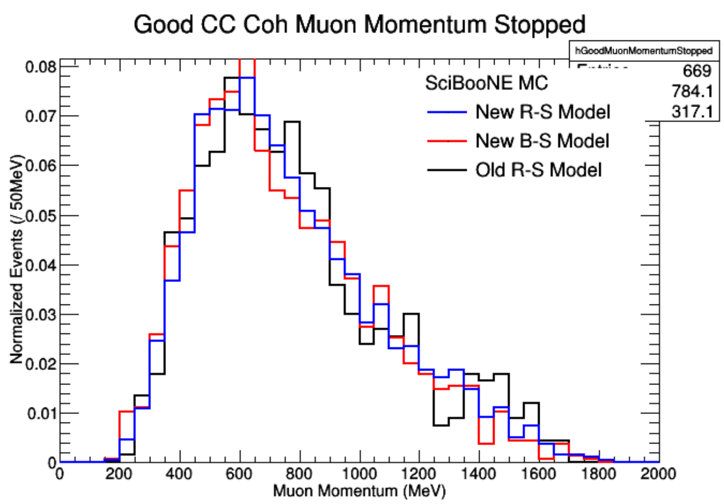

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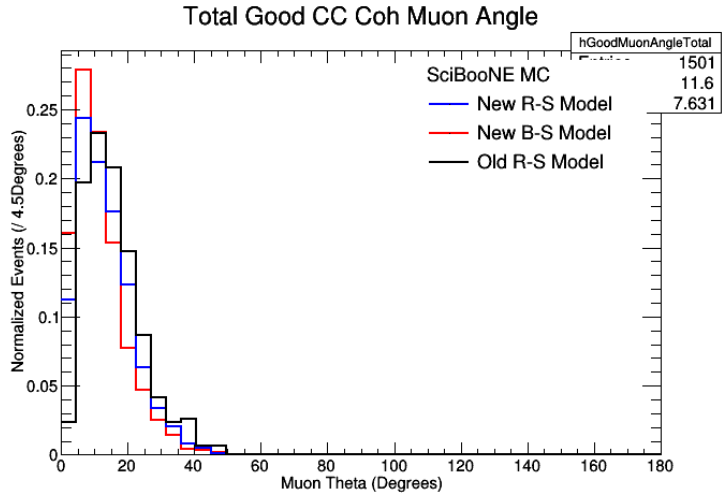


Figure 77:

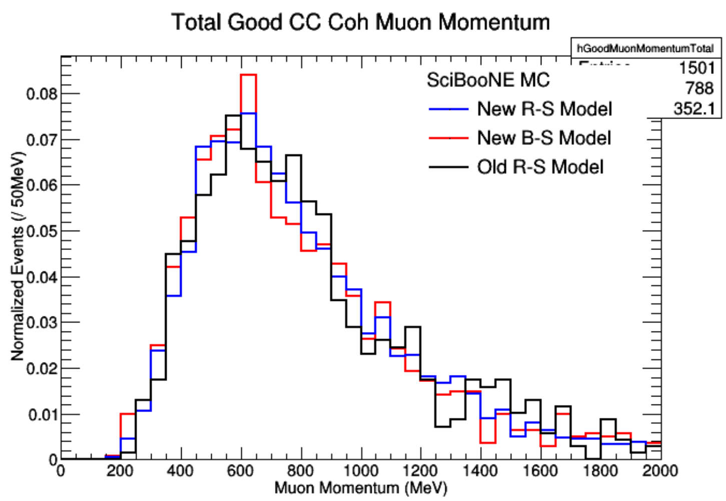


Figure 78:

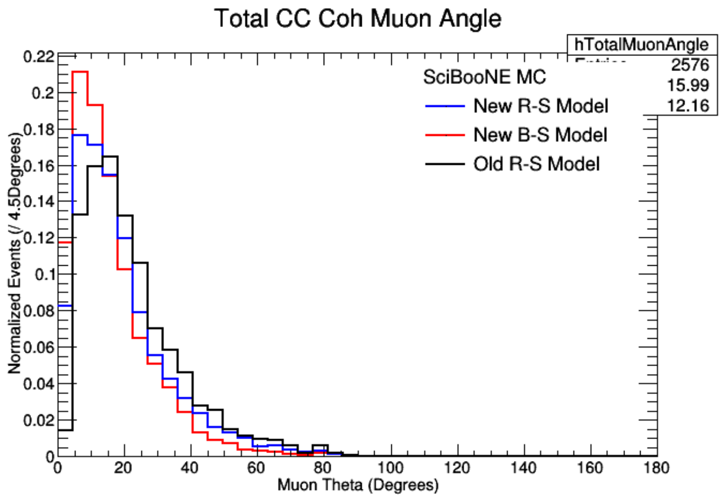


Figure 79:

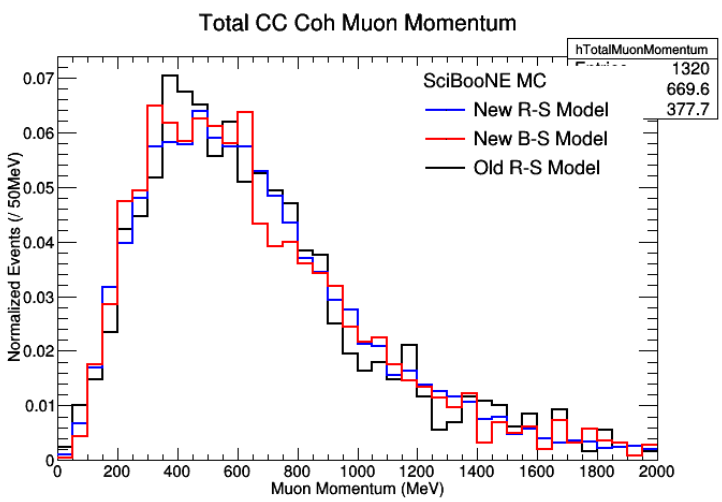
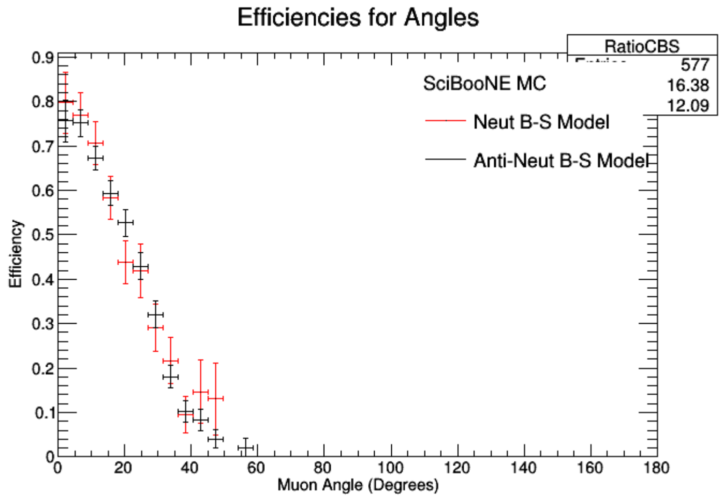


Figure 80:



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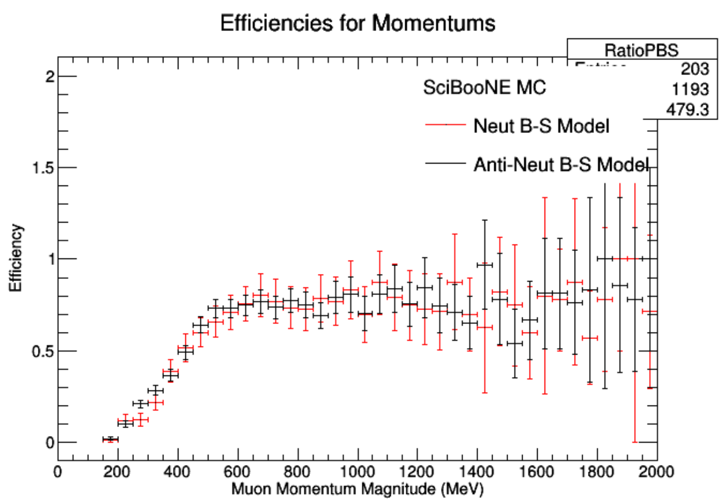

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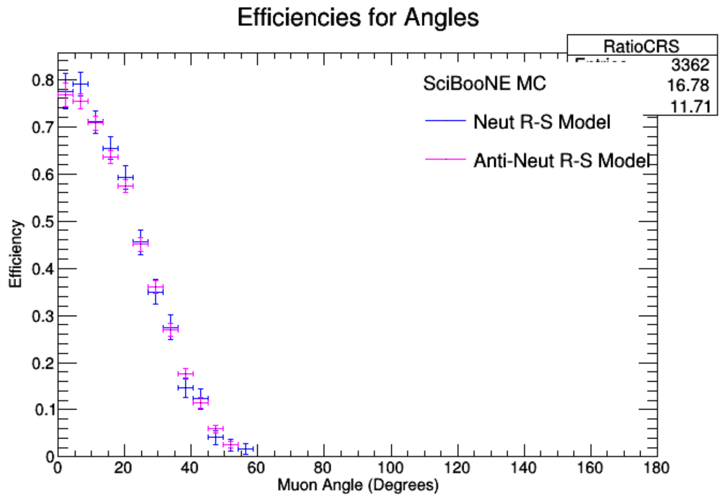


Figure 83:

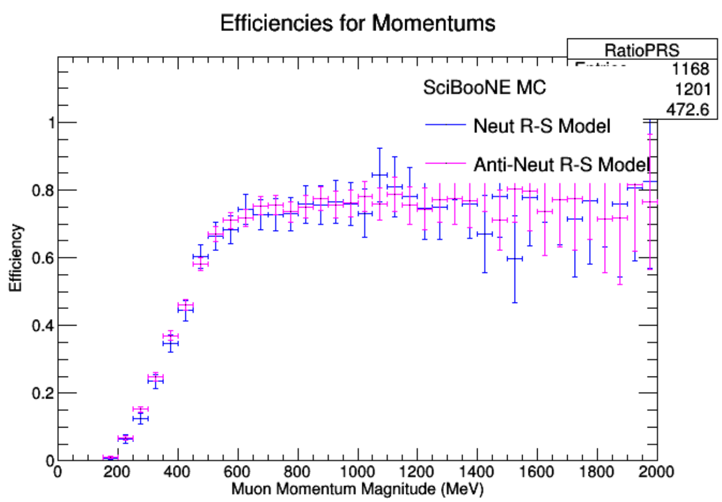
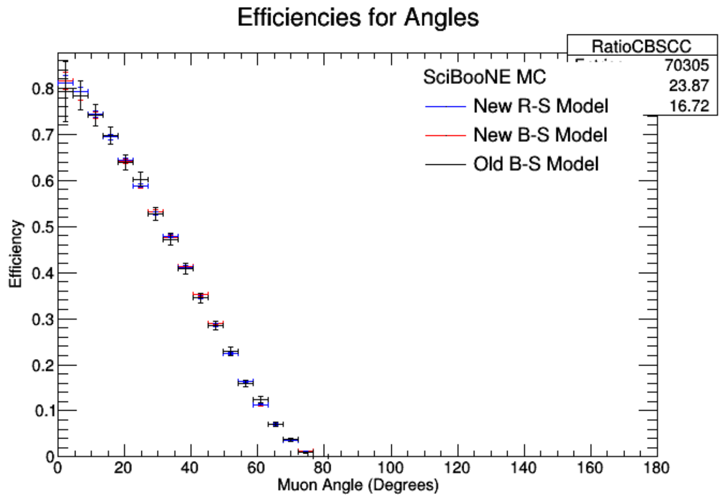


Figure 84:



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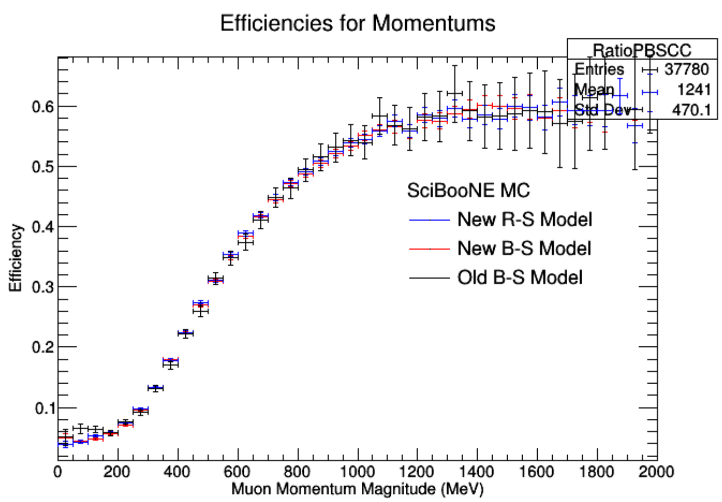

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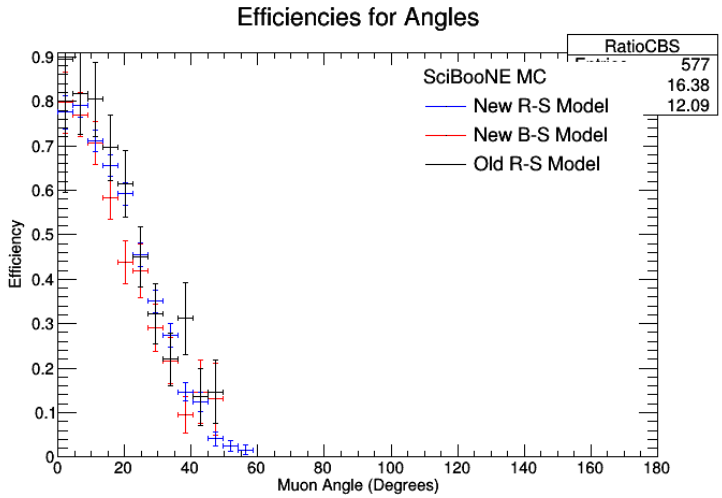

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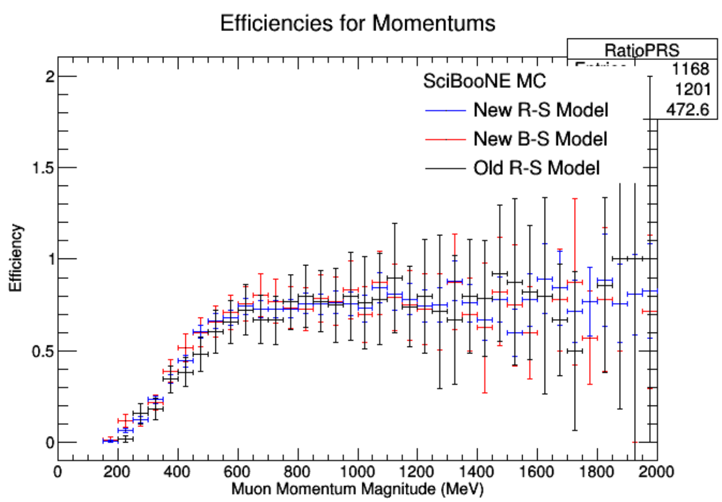


Figure 88:

A.13 NMPionPlotting.C

I need to come back and insert all of my images here.

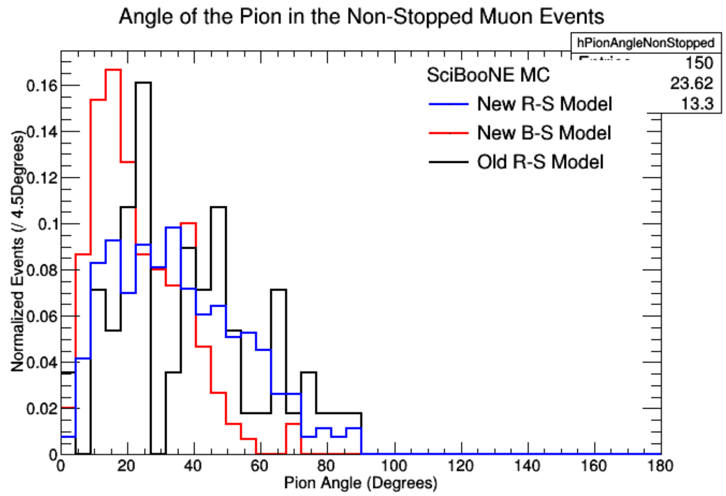


Figure 89:

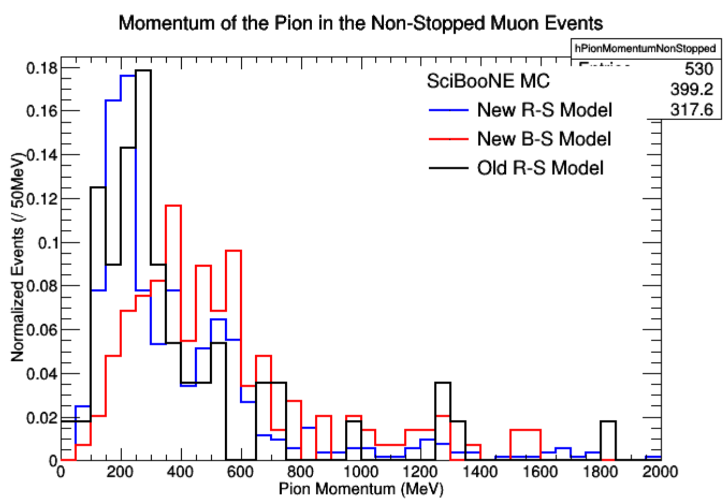


Figure 90:

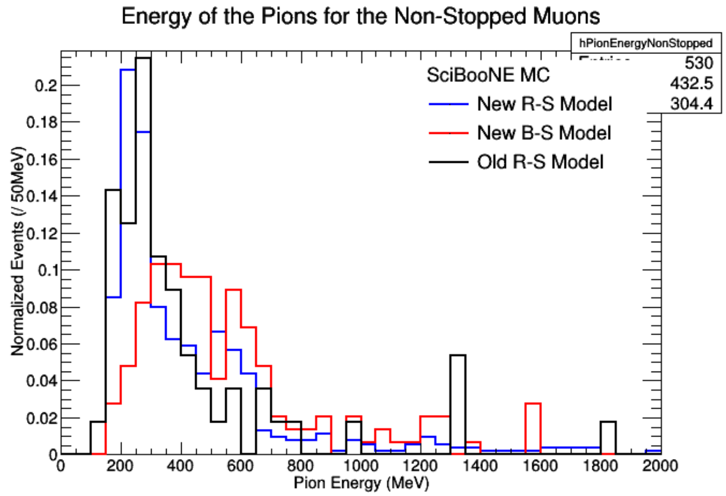


Figure 91:

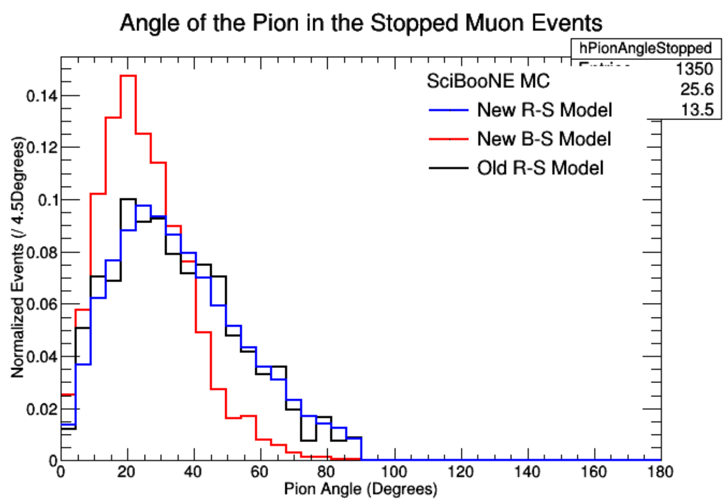
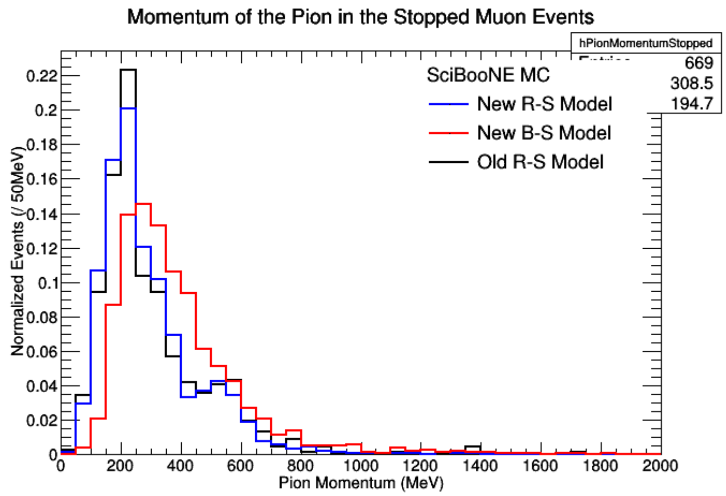


Figure 92:



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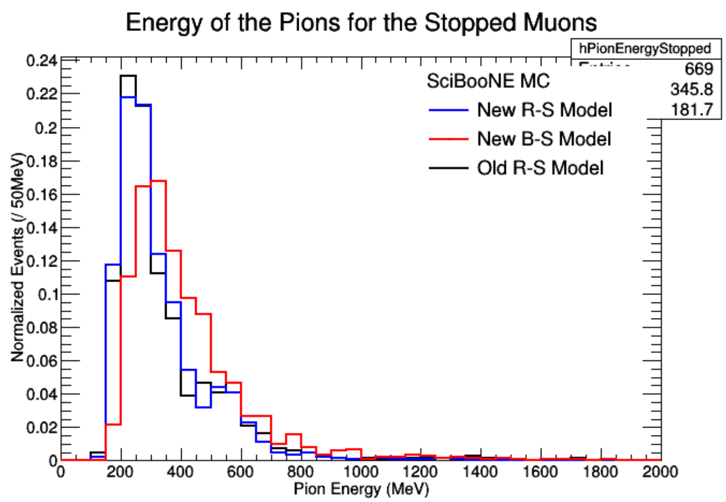


Figure 94:

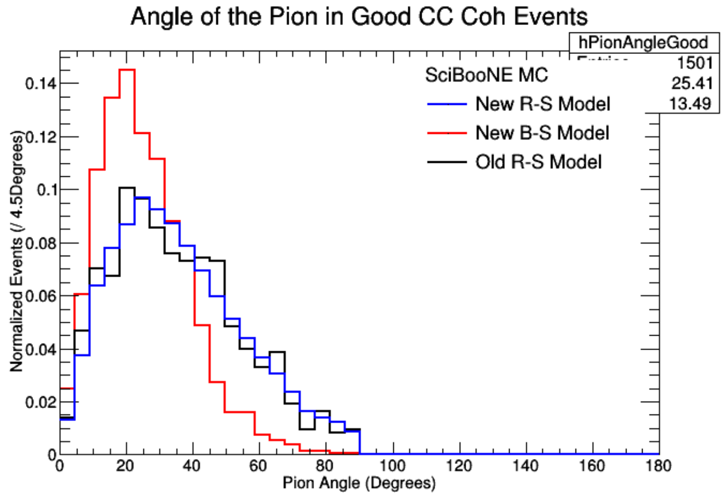


Figure 95:

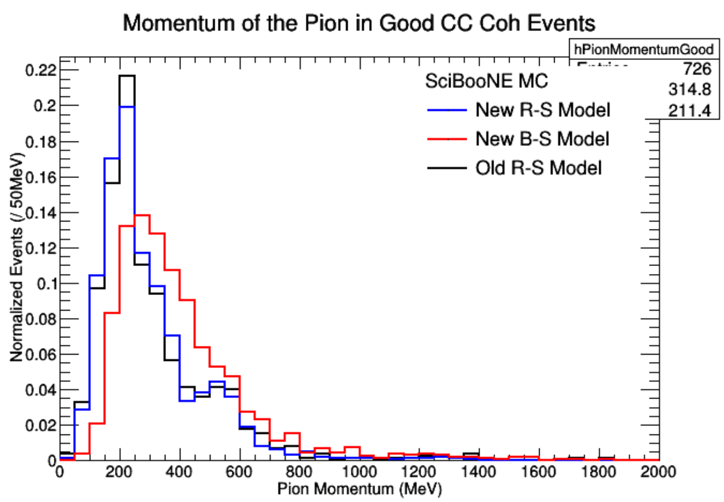


Figure 96:

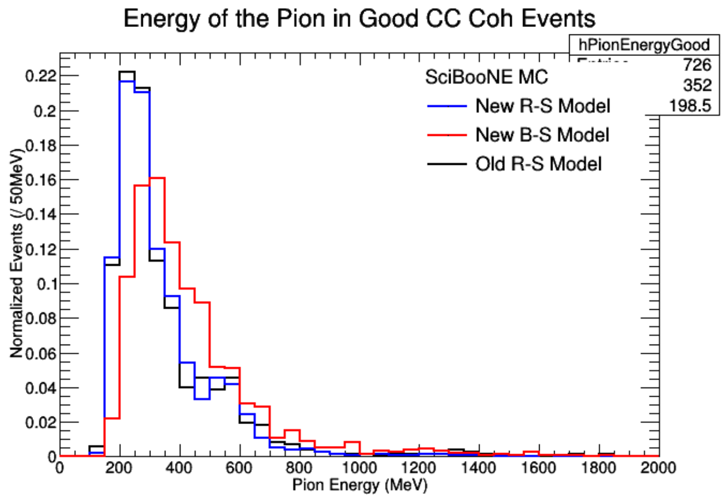


Figure 97:

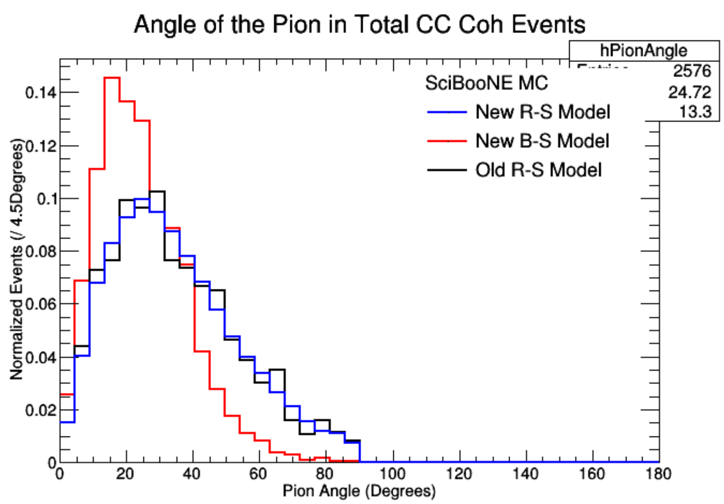


Figure 98:

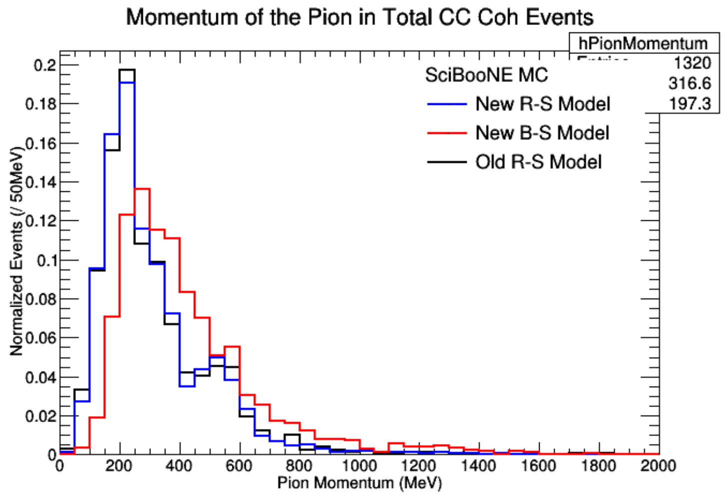


Figure 99:

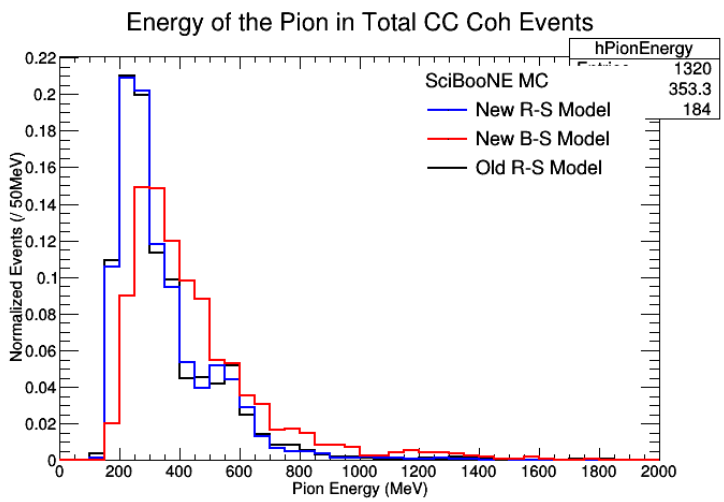


Figure 100:

A.14 NMFourSquaredPlotting.C

I need to come back and insert all of my images here.

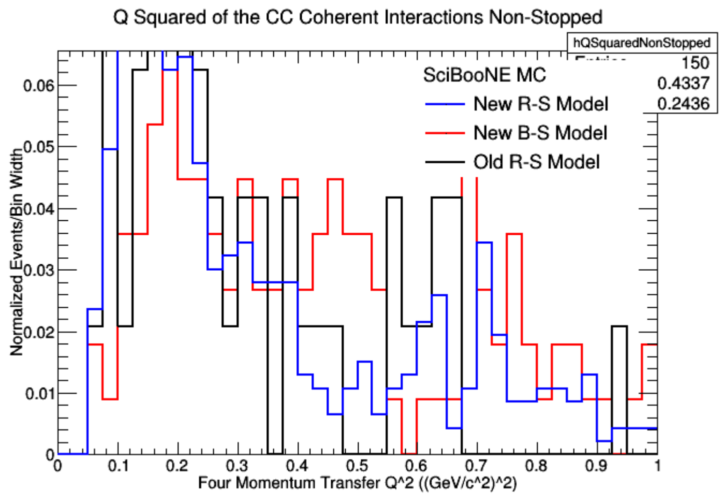


Figure 101:

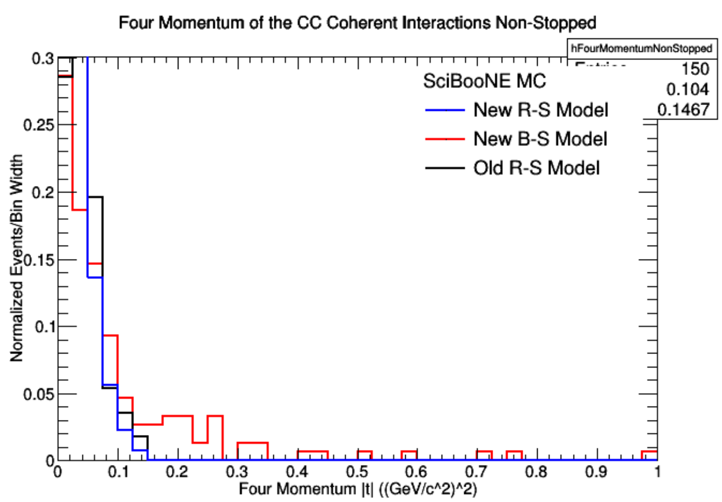


Figure 102:

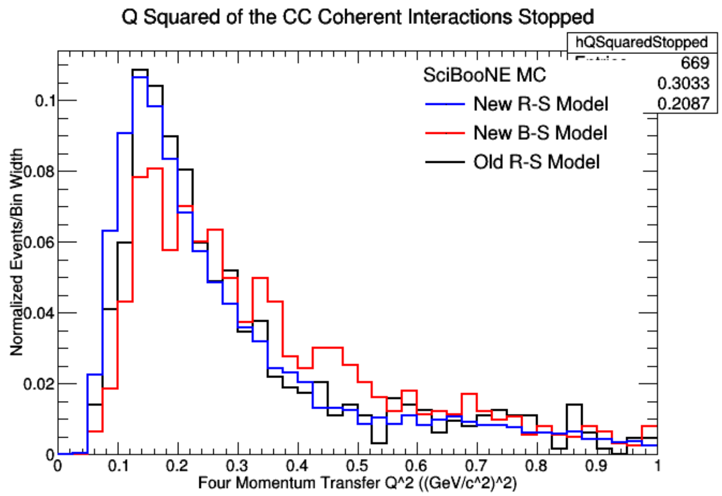


Figure 103:

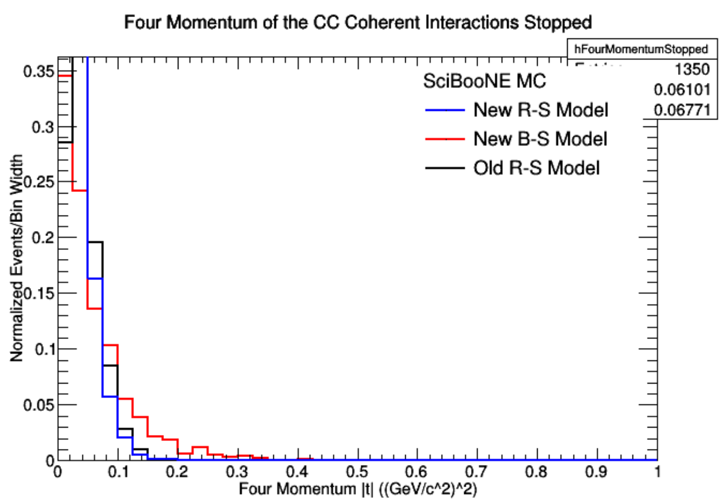
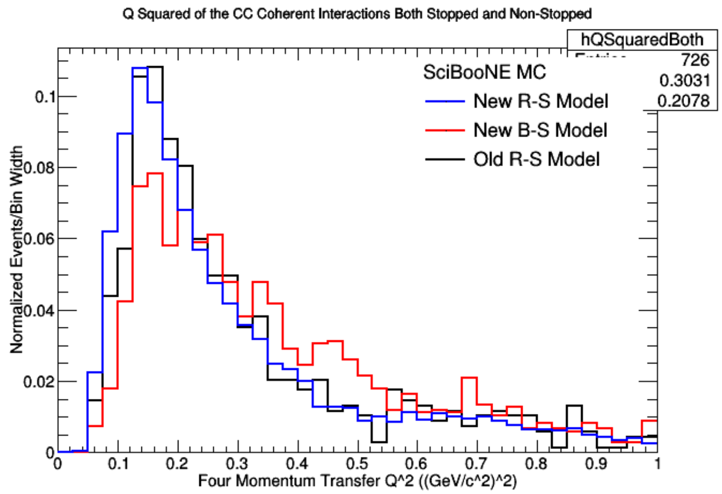


Figure 104:



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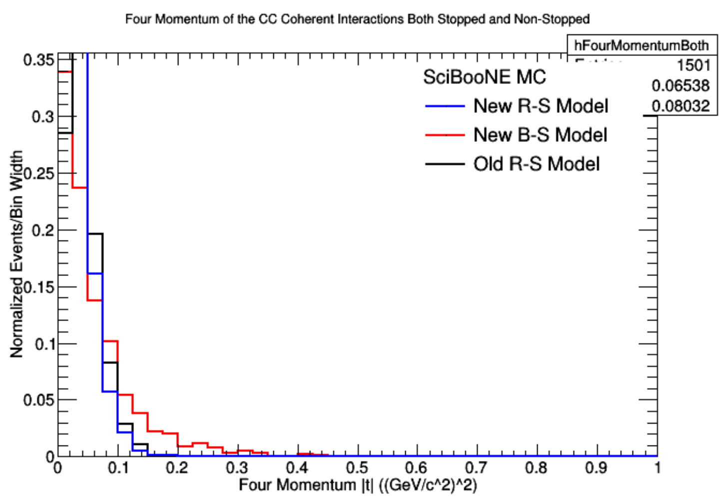


Figure 106:

A.15 ANMCombinedPlots.C

I need to come back and insert all of my images here.

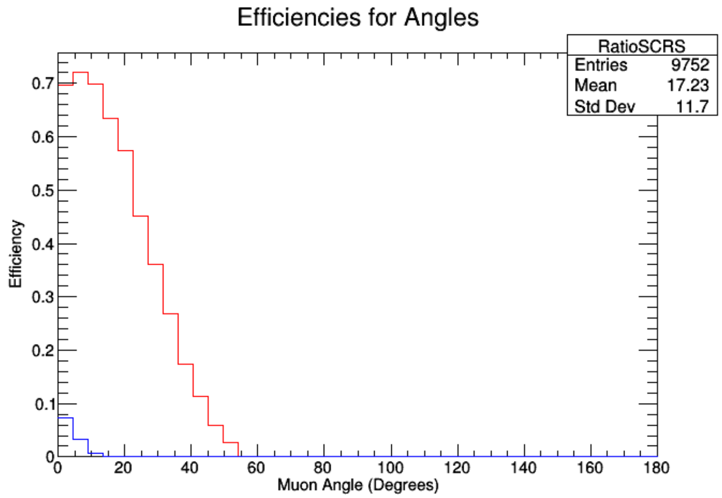


Figure 107:

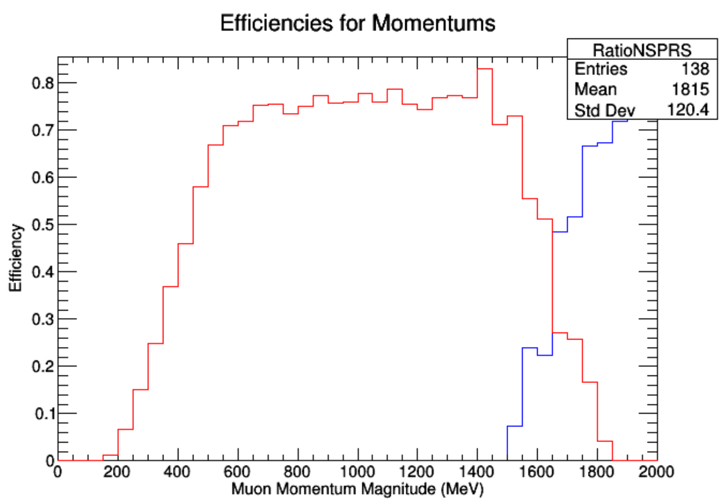


Figure 108:

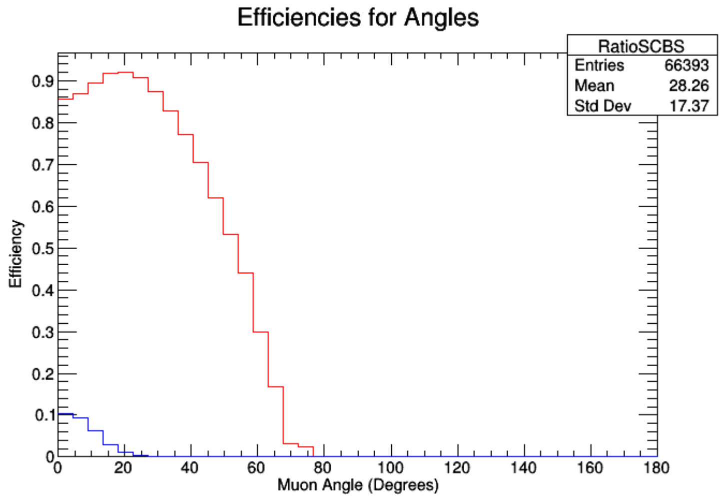


Figure 109:

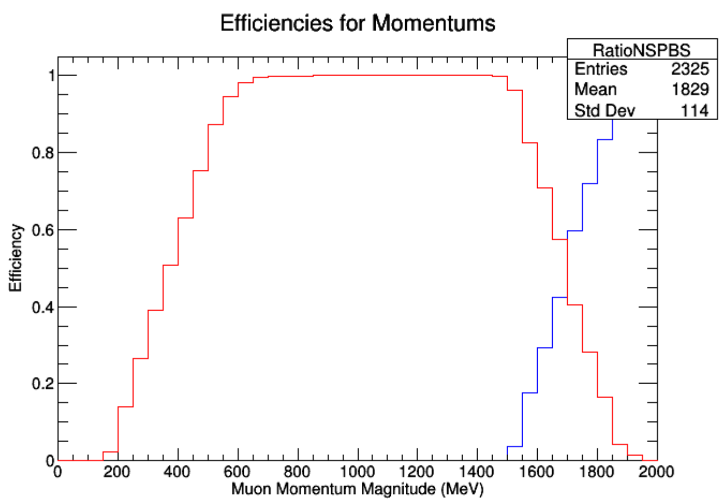


Figure 110:

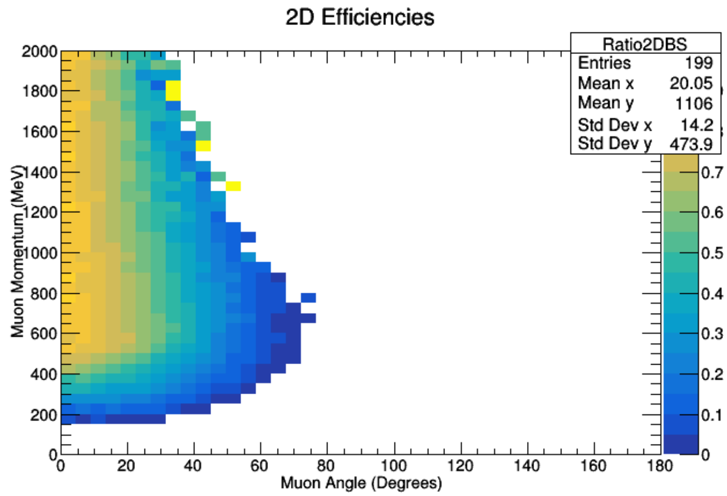


Figure 111:

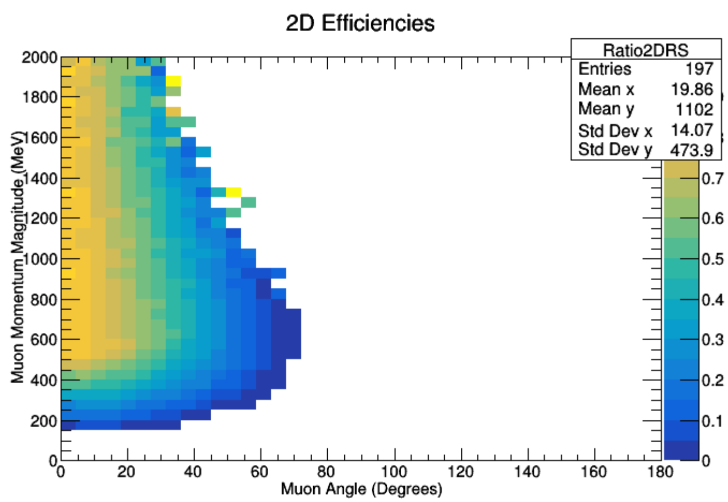


Figure 112:

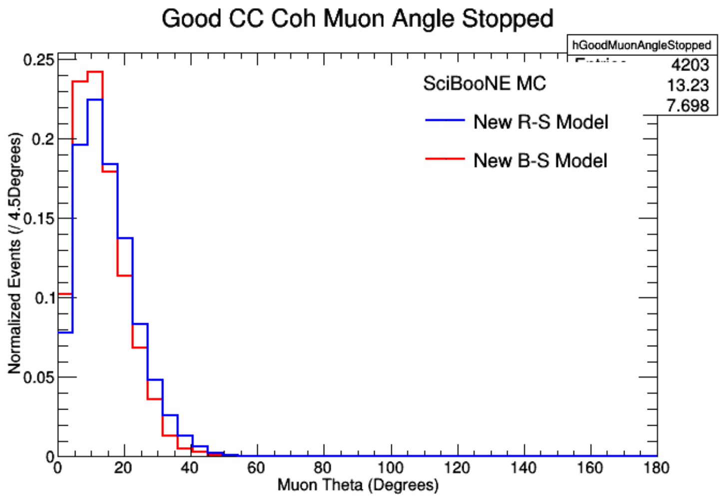


Figure 113:

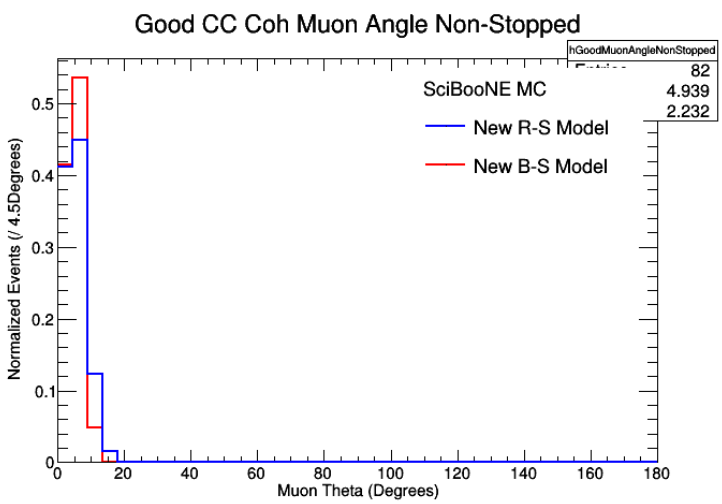


Figure 114:

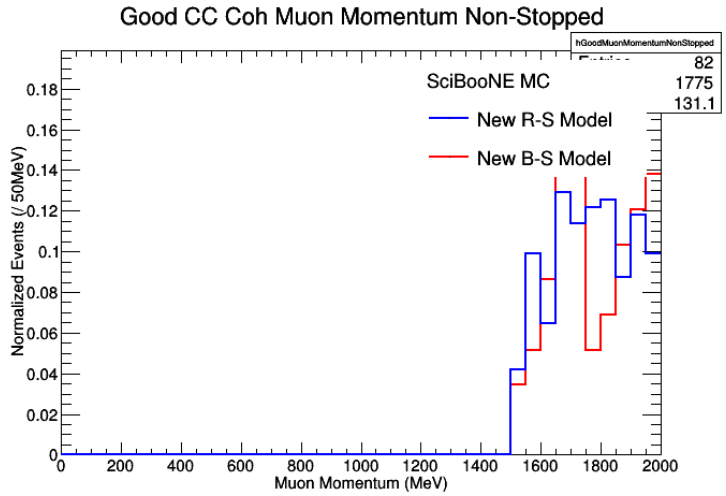


Figure 115:

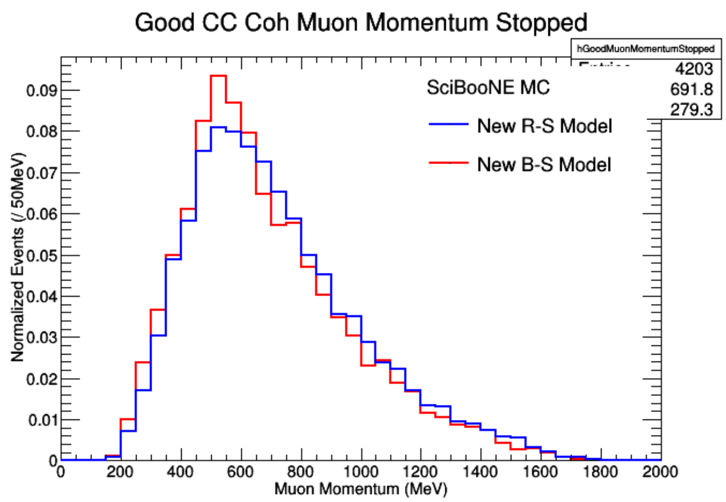


Figure 116:

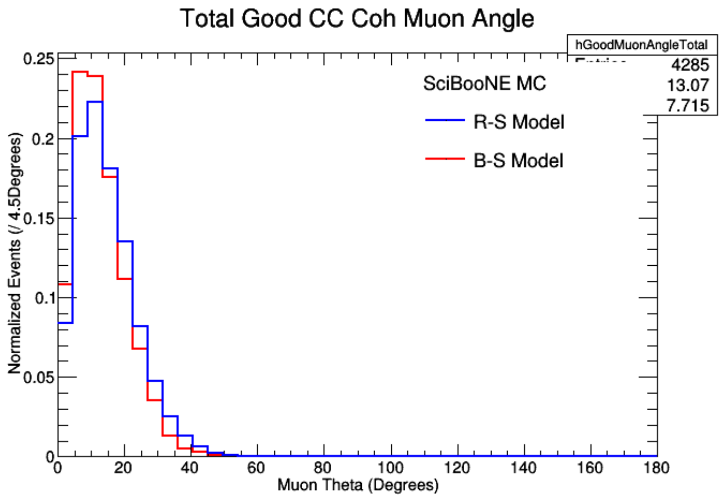


Figure 117:

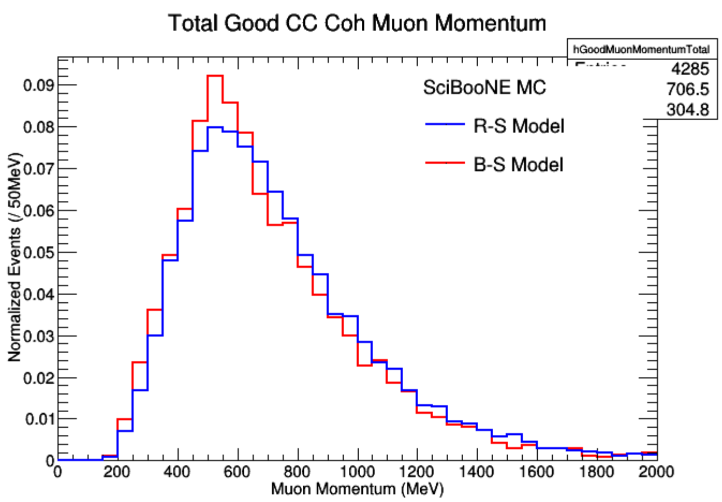


Figure 118:

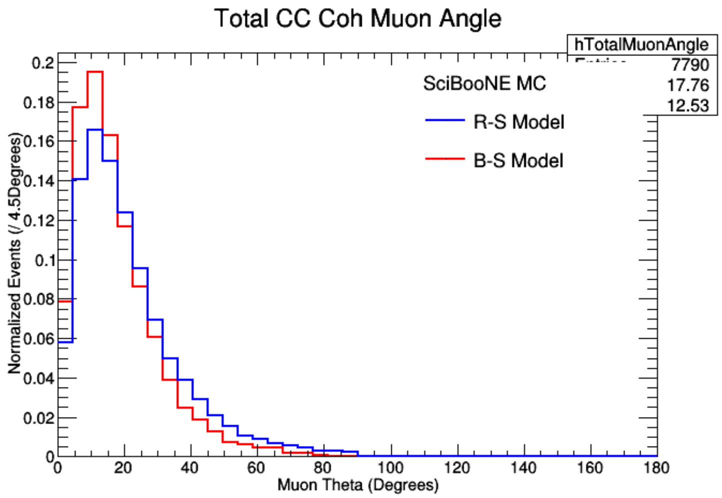


Figure 119:

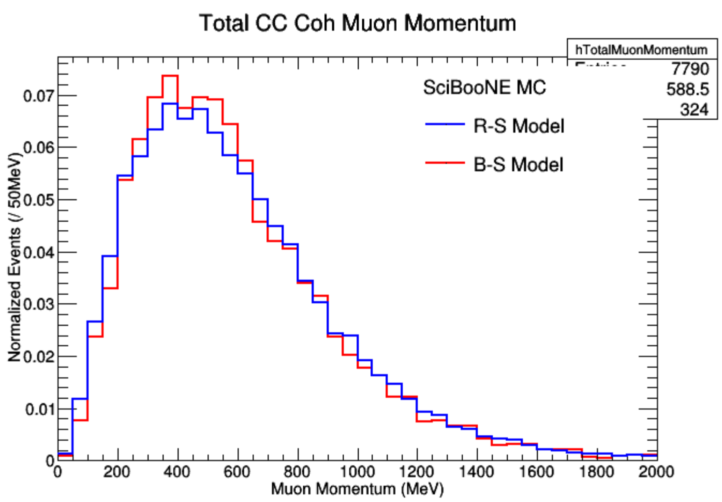


Figure 120:

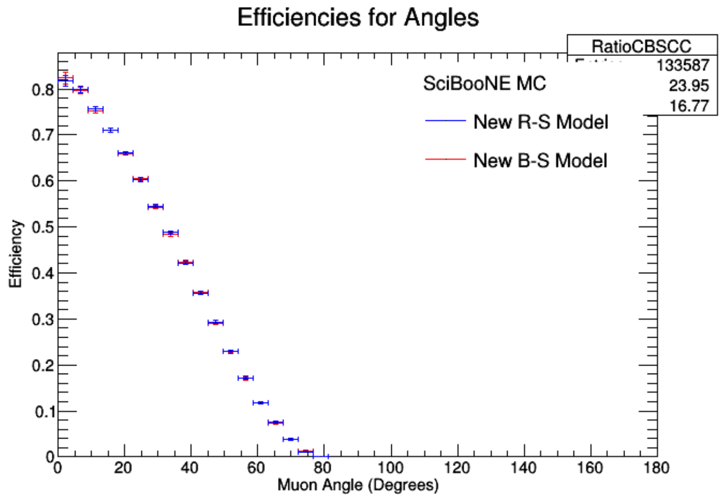


Figure 121:

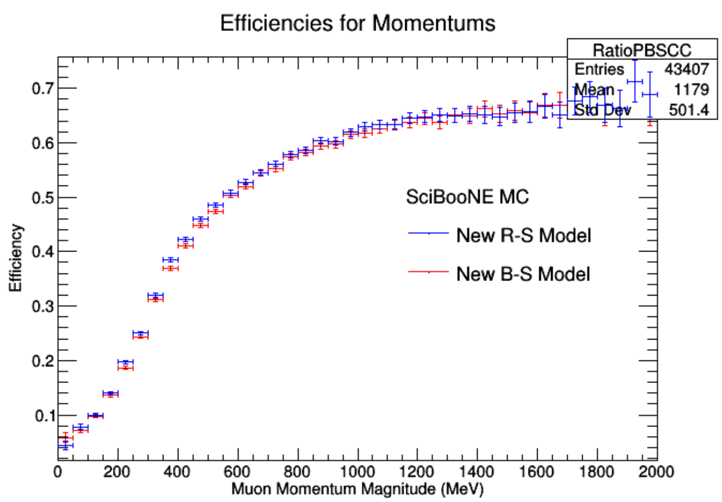
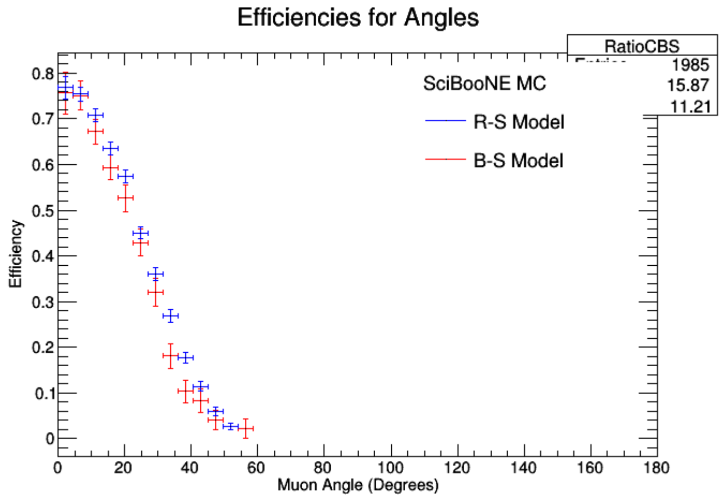


Figure 122:



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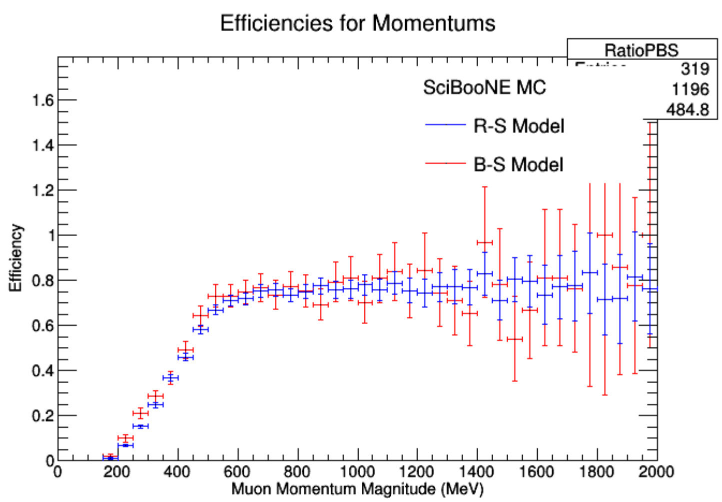

Figure 124:

A.16 ANMPionPlotting.C

I need to come back and insert all of my images here.

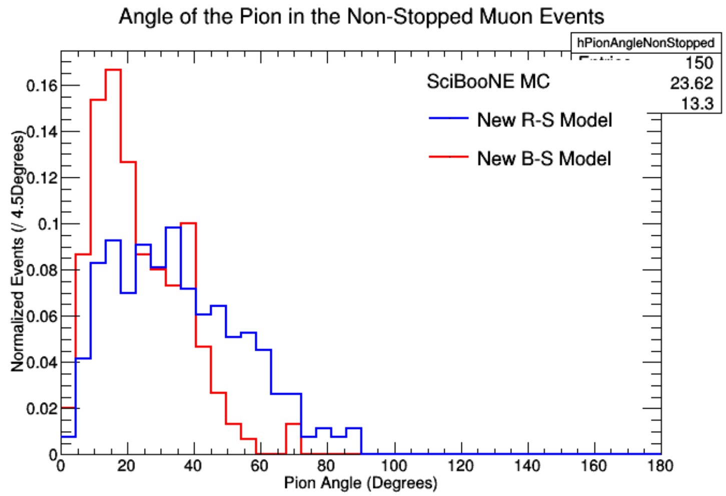

Figure 125:

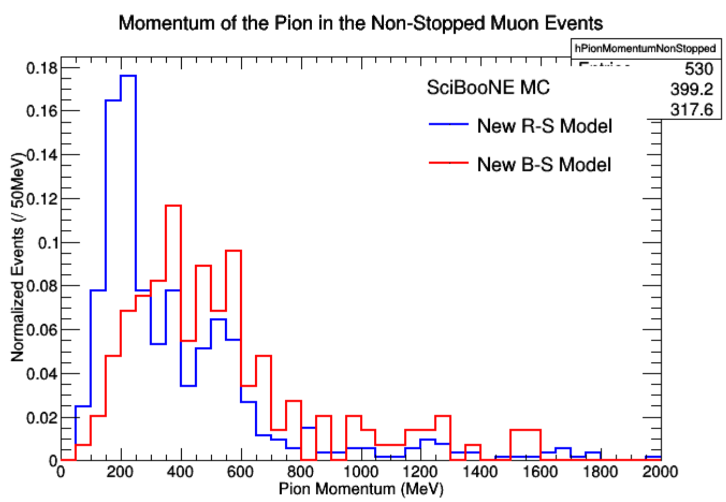

Figure 126:

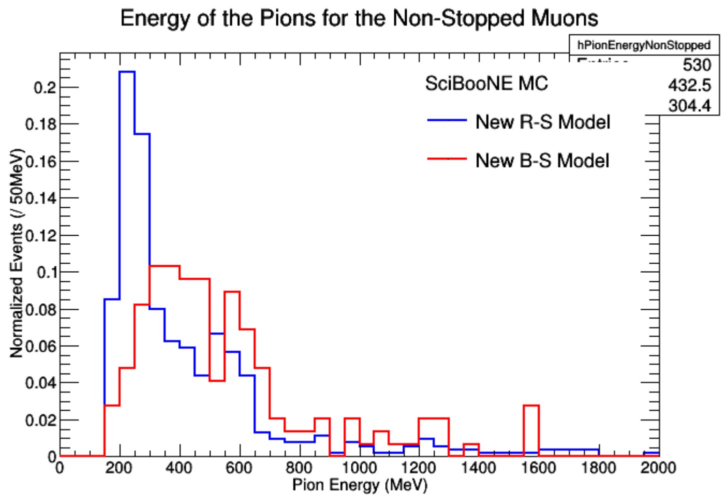

Figure 127:

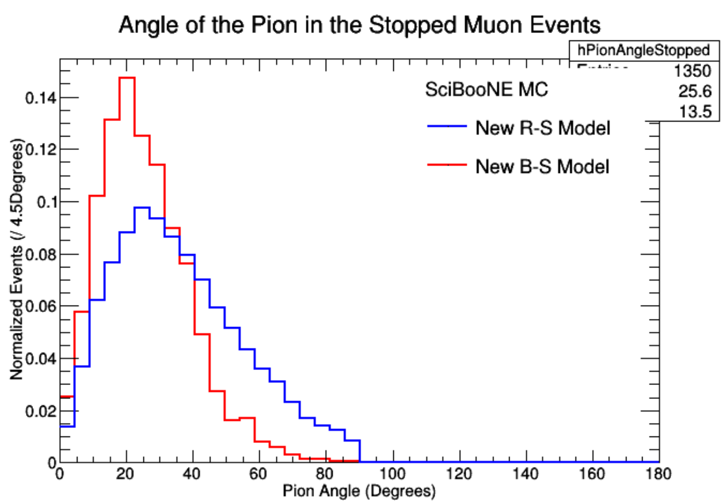

Figure 128:

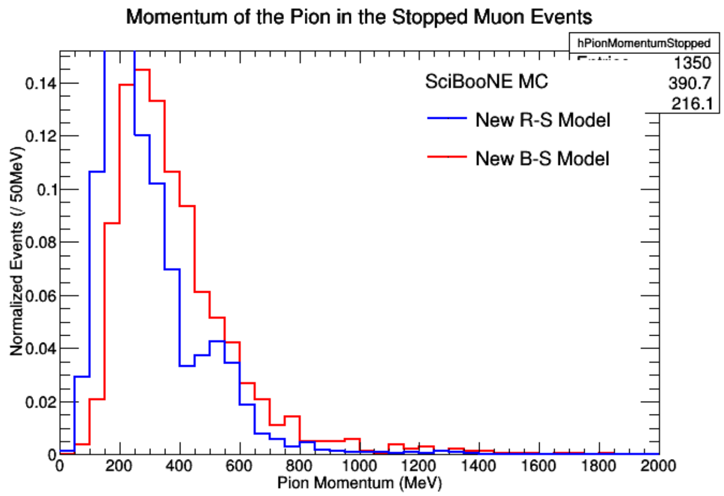

Figure 129:

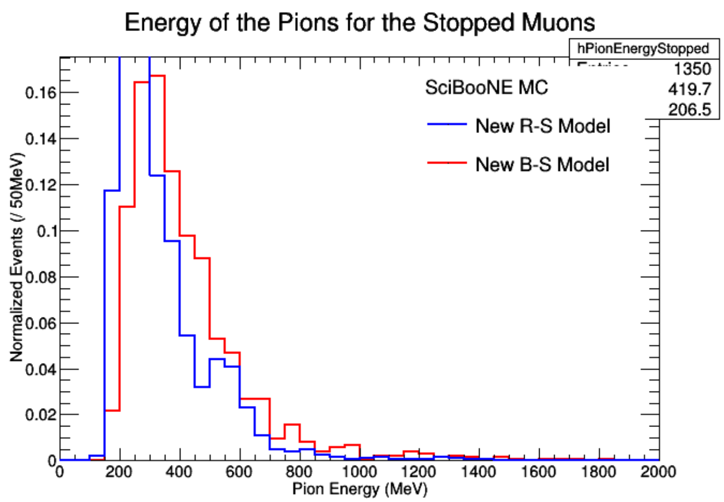

Figure 130:

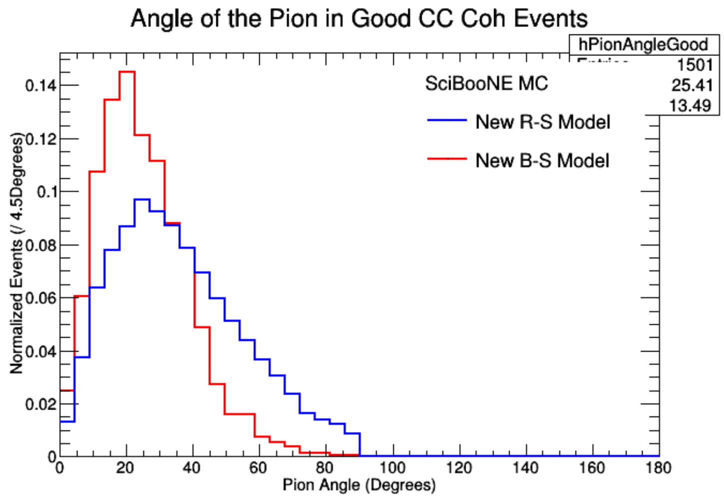

Figure 131:

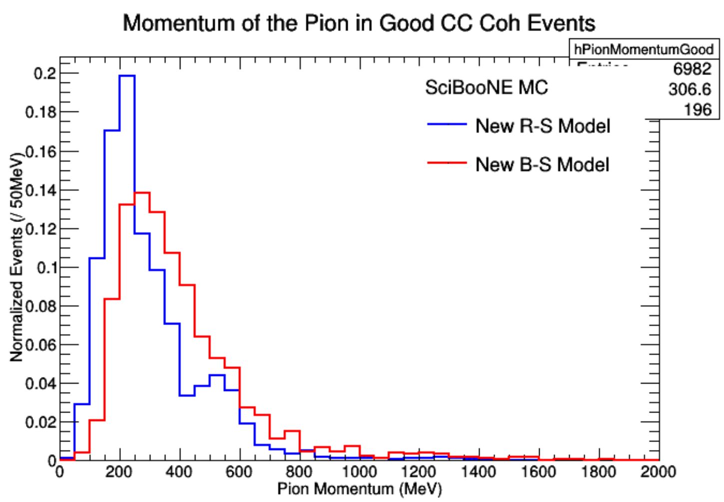

Figure 132:

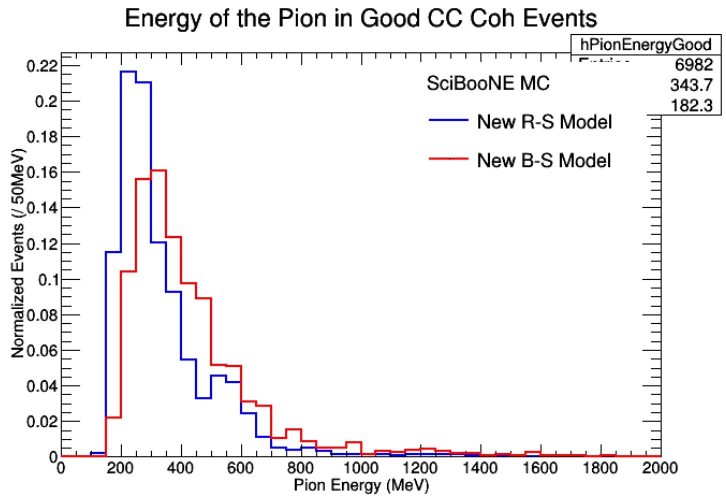

Figure 133:

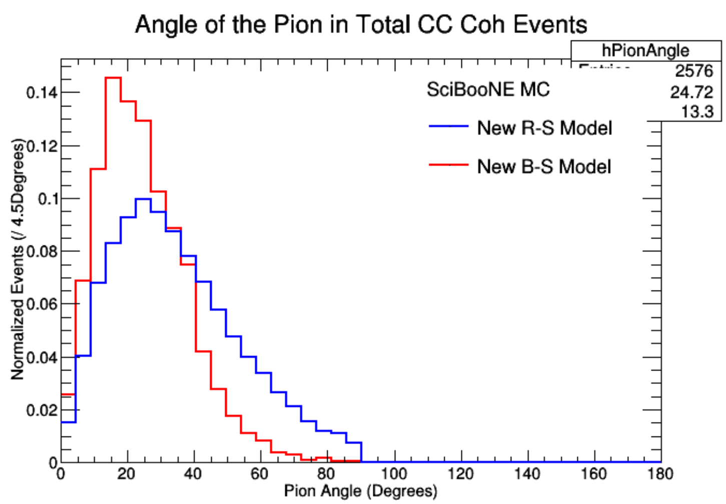

Figure 134:

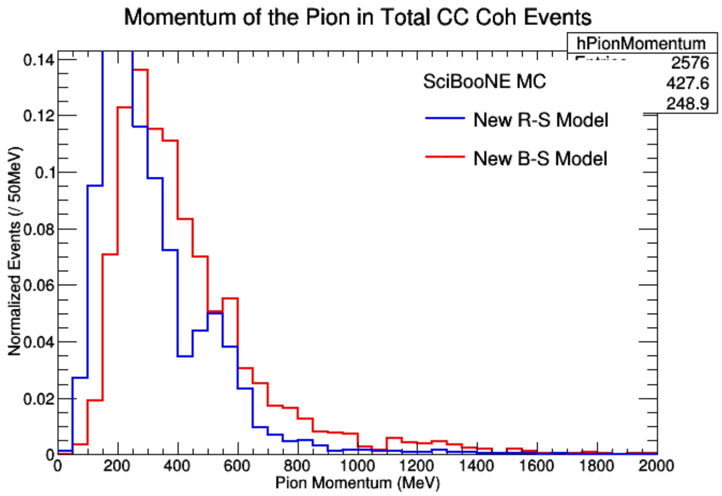

Figure 135:

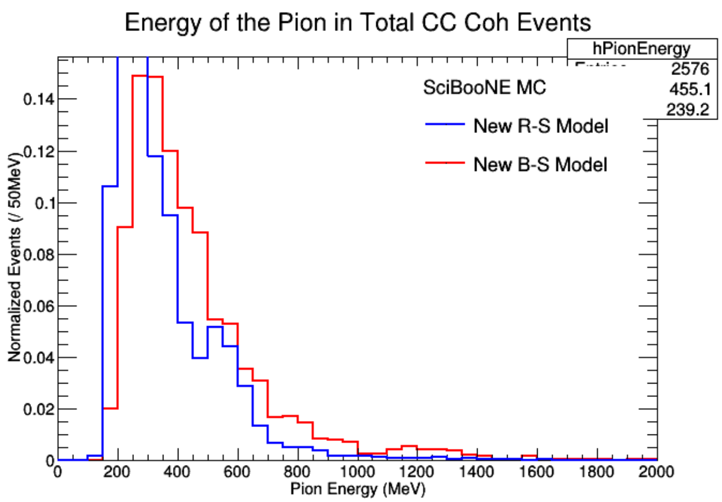

Figure 136:

A.17 ANMFourSquaredPlotting.C

I need to come back and insert all of my images here.

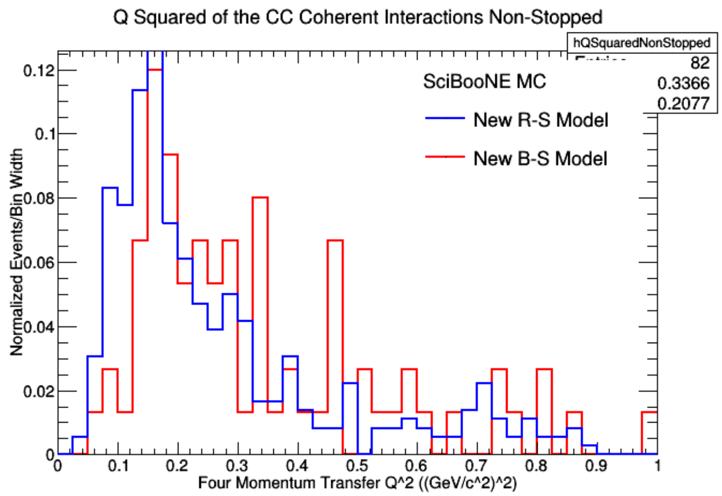

Figure 137:

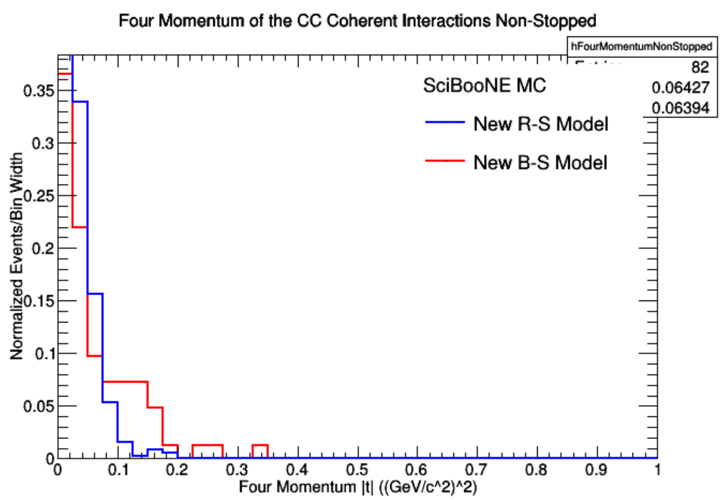

Figure 138:

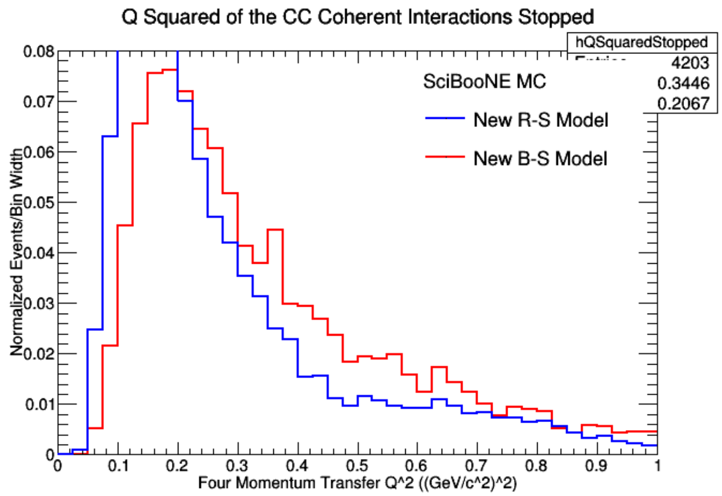

Figure 139:

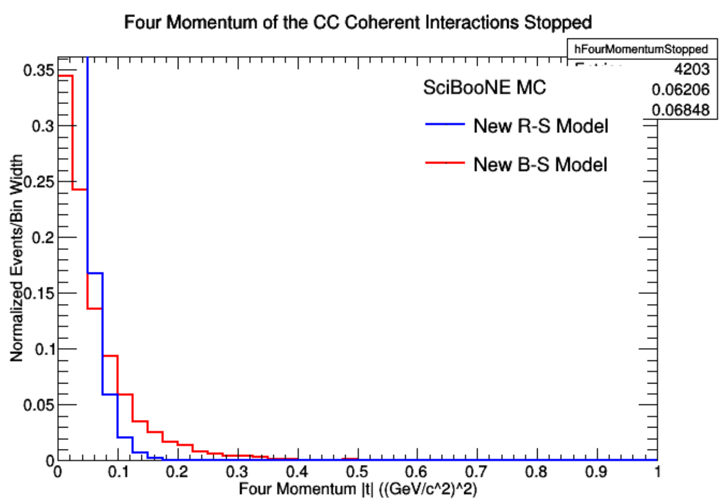

Figure 140:

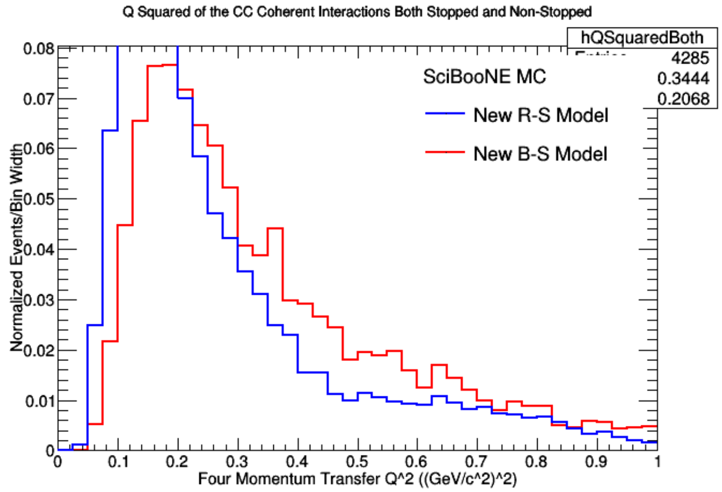

Figure 141:

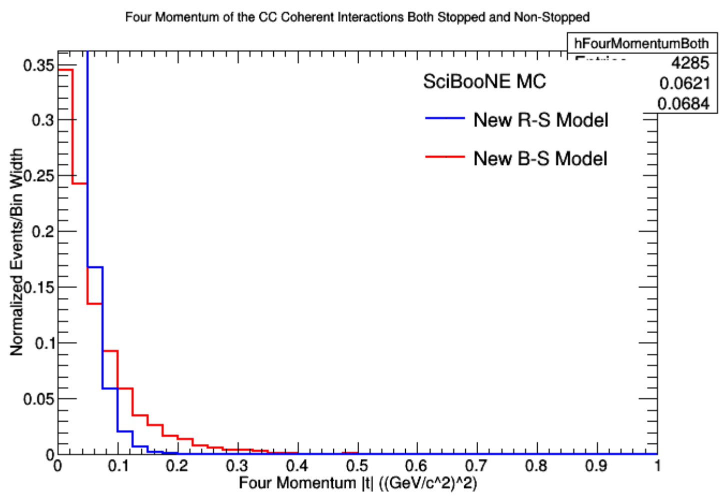

Figure 142:

B Steps for Running the Code

The instructions on how to run the code and the order the files need to run in so that there are no resulting error messages, or other issues while running the code, are detailed in this section.

Step 1: This is the first step. (Run the NewNM macros and the NewANM macros and the OldNM macro.)

Step 2: This is the second step. (Run the combined plotting macros.)

Step 3: This is the third step. (Run the Pion Plotting macros.)

Step 4: Etc. (Run the FourSquaredMomentum macros.)

C Closing Remarks and Cautions

These are just a few cautionary suggestions for potential issues that might be encountered while trying to use this code. This will also be where and further closing remarks can be made.

D Acknowledgements

Thank everyone who helped, and thank everyone who gave their inputs into your acceptance study. YOU NEED TO GIVE A HUGE AND SPECIAL THANKS TO DR. ASAADI RIGHT HERE! (He has been suuuuuuuper patient...)

E Figures and Tables

E.1 List of Figures

There will eventually be a huge list of figures here.

E.2 List of Tables

There will eventually be the event reduction tables and 2D histogram tables here.

Table 7: Table for 2D Histogram for New NM-Rein-Sehgal

New NM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0	0	0	0.09375	0.259259	0.26087	0.317073	0.45	0.553846	0.716049	0.816092	0.828829	0.842975	0.845455	0.773438	0.875	0.796748	0.798611	0.870504	0.819549	0.834532	0.852174	0.88785	0.762712	0.807692	0.802198	0.811321	0.835443	0.753086	0.779412	0.783333	0.936508	0.8	0.921569	0.921569	0.77193	0.848485	0.861111	0.826087	0.823529
4.5-9 Deg	0	0	0	0.123457	0.244681	0.218182	0.40411	0.490291	0.568376	0.766102	0.824047	0.789617	0.844186	0.80404	0.828302	0.807771	0.816514	0.820841	0.809981	0.79823	0.803922	0.828974	0.800875	0.820276	0.789474	0.798982	0.801136	0.774026	0.79868	0.744186	0.742424	0.784091	0.770642	0.790476	0.754717	0.774194	0.79375	0.813793	0.748387	0.785714
9-13.5 Deg	0	0	0	0.0280374	0.150943	0.31	0.334426	0.479167	0.582	0.693122	0.795417	0.787402	0.784336	0.786013	0.779396	0.757746	0.77907	0.784038	0.763083	0.776828	0.74026	0.760633	0.746401	0.713326	0.746803	0.720867	0.735724	0.721683	0.72093	0.716946	0.727468	0.697572	0.704835	0.730978	0.747774	0.70068	0.684982	0.73029	0.623853	0.713615
13.5-18 Deg	0	0	0	0.0696203	0.164502	0.242902	0.389937	0.460102	0.524072	0.648363	0.73062	0.742788	0.7373	0.725131	0.707711	0.713192	0.708657	0.71437	0.713376	0.722747	0.704342	0.713103	0.697987	0.688694	0.708895	0.681319	0.674493	0.661465	0.680731	0.635036	0.657848	0.664093	0.618938	0.648718	0.634561	0.598291	0.63871	0.638686	0.630252	0.614407
18-22.5 Deg	0	0	0	0.0396825	0.134503	0.220374	0.320233	0.4	0.498252	0.56578	0.666667	0.703245	0.681216	0.694102	0.67205	0.674541	0.661496	0.647185	0.673965	0.656648	0.660068	0.632723	0.652881	0.627978	0.634488	0.606524	0.599138	0.600991	0.58926	0.585284	0.56654	0.562092	0.581633	0.546547	0.532051	0.582707	0.517647	0.569507	0.530055	0.5625
22.5-27 Deg	0	0	0	0.0341615	0.120614	0.20088	0.284783	0.356223	0.442424	0.513469	0.590521	0.619898	0.653967	0.628604	0.61255	0.617109	0.601285	0.58894	0.579674	0.578595	0.57636	0.56538	0.564828	0.553719	0.550962	0.498274	0.550685	0.566828	0.500901	0.497826	0.511166	0.513605	0.453674	0.539095	0.447761	0.428571	0.476821	0.462963	0.379032	0.435185
27-31.5 Deg	0	0	0	0.0128535	0.0852575	0.146399	0.240517	0.328982	0.381593	0.467435	0.496599	0.55869	0.57336	0.536199	0.537204	0.545332	0.542526	0.532462	0.524605	0.503756	0.498278	0.493626	0.481938	0.446392	0.463785	0.474016	0.465487	0.389868	0.438953	0.384615	0.484375	0.360577	0.414634	0.34058	0.242991	0.416667	0.405941	0.333333	0.25974	0.403846
31.5-36 Deg	0	0	0	0.00618557	0.047749	0.138308	0.215553	0.260465	0.322889	0.379459	0.44563	0.489885	0.50075	0.5	0.512734	0.486242	0.465472	0.455387	0.439182	0.459893	0.432253	0.403556	0.432373	0.361111	0.379648	0.411483	0.370968	0.307116	0.361702	0.355191	0.294118	0.293578	0.337349	0.328571	0.272727	0.34375	0.227273	0.290323	0.25	0.380952
36-40.5 Deg	0	0	0	0	0.0376749	0.104341	0.167825	0.228974	0.272658	0.326716	0.35271	0.399772	0.4	0.410602	0.420808	0.416728	0.404237	0.378892	0.371585	0.362308	0.373851	0.336748	0.352837	0.316279	0.293333	0.333333	0.282609	0.182432	0.261194	0.25	0.430556	0.191489	0.127273	0.238095	0.2	0.25	0.0714286	0.25	0.1	0.333333
40.5-45 Deg	0	0	0	0	0.0185547	0.0617036	0.129648	0.175194	0.22549	0.249335	0.297987	0.31442	0.331903	0.342802	0.33975	0.324022	0.312566	0.299735	0.293671	0.284258	0.264297	0.2897	0.274247	0.191235	0.220238	0.204918	0.309524	0.147059	0.169014	0.30303	0.16	0.0909091	0.1875	0.1875	0.166667	0	0.2	0	0.5	0
45-49.5 Deg	0	0	0	0	0.00241935	0.0461908	0.0861688	0.129907	0.177771	0.209127	0.220634	0.249649	0.260561	0.269592	0.273593	0.258347	0.252889	0.239492	0.238606	0.221135	0.144772	0.168675	0.216867	0.15534	0.182927	0.113636	0.0645161	0.148148	0.117647	0.0769231	0	0.6	0	0	0	0.25	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0.0115123	0.0555327	0.102639	0.123702	0.161442	0.165696	0.190045	0.182172	0.214009	0.188606	0.193939	0.207	0.177469	0.140187	0.124514	0.10119	0.178295	0.145161	0.0740741	0.08	0.142857	0.2	0	0	0.1	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0.0248494	0.0445331	0.0810889	0.106105	0.109863	0.131459	0.132259	0.121872	0.135764	0.133188	0.12807	0.106557	0.122172	0.0814815	0.0571429	0.1	0.0322581	0	0.1	0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0.0165922	0.0418139	0.0557781	0.0744786	0.0831667	0.0781828	0.0883686	0.0845225	0.0654045	0.074184	0.0883721	0.0841121	0.0405405	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00645756	0.018006	0.0306081	0.0433498	0.053756	0.044898	0.0724638	0.044586	0.0347222	0.0641026	0.0243902	0	0.136364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00228571	0.0041686	0.0121873	0.017341	0.020155	0.0234114	0.0121212	0.0131579	0.075	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.00540541	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 8: Table for 2D Histogram for New NM-Berger-Sehgal

New NM B-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0	0	0	0	0.157895	0.325	0.422222	0.490566	0.615385	0.728571	0.895522	0.807692	0.880435	0.864865	0.843373	0.833333	0.858333	0.833333	0.826087	0.814815	0.778846	0.8	0.813725	0.829268	0.84375	0.78022	0.783133	0.898734	0.85	0.825397	0.873016	0.767442	0.779661	0.847826	0.836735	0.809524	0.861111	0.794872	0.944444	0.833333
4.5-9 Deg	0	0	0	0.0625	0.176471	0.235849	0.396694	0.478261	0.581731	0.773279	0.811448	0.817109	0.806366	0.801402	0.814286	0.809211	0.804211	0.755448	0.822709	0.792657	0.804255	0.824945	0.804494	0.814536	0.784504	0.774295	0.813665	0.792994	0.764706	0.790036	0.793651	0.741784	0.728643	0.759657	0.734884	0.770053	0.780749	0.761905	0.791908	0.794521
9-13.5 Deg	0	0	0	0.09375	0.156716	0.223529	0.362963	0.463343	0.5725	0.701245	0.78089	0.798354	0.801724	0.794569	0.782796	0.780287	0.765235	0.773496	0.756598	0.759384	0.766798	0.776286	0.733735	0.717208	0.731677	0.730769	0.708861	0.728296	0.755835	0.75089	0.708249	0.717833	0.664251	0.747423	0.700581	0.688679	0.681967	0.69338	0.745763	0.685039
13.5-18 Deg	0	0	0	0.0382166	0.131222	0.260736	0.330233	0.448833	0.566116	0.634994	0.727545	0.736387	0.720152	0.749489	0.762791	0.732403	0.711937	0.704908	0.702804	0.683544	0.703634	0.7086	0.706101	0.683544	0.700457	0.681775	0.68321	0.68171	0.669251	0.644678	0.668863	0.66548	0.643629	0.637168	0.643038	0.62973	0.607973	0.666667	0.621212	0.622711
18-22.5 Deg	0	0	0	0.039604	0.0973451	0.228145	0.318462	0.419903	0.517013	0.582547	0.656707	0.692351	0.687027	0.677215	0.689404	0.661647	0.651855	0.661634	0.65554	0.634515	0.653195	0.635392	0.641326	0.620074	0.60516	0.579566	0.597895	0.612863	0.599419	0.5856	0.590654	0.587156	0.558376	0.564607	0.52568	0.568093	0.52549	0.575342	0.497696	0.557471
22.5-27 Deg	0	0	0	0.0264026	0.0930736	0.197461	0.321879	0.381265	0.447548	0.521715	0.578365	0.637657	0.629688	0.615445	0.637963	0.622396	0.604258	0.581746	0.570899	0.569778	0.571276	0.570789	0.557559	0.528678	0.526667	0.524138	0.529101	0.509404	0.499093	0.539326	0.484043	0.5	0.535354	0.441767	0.436681	0.482587	0.40113	0.496599	0.461538	0.454545
27-31.5 Deg	0	0	0	0.00486618	0.0857143	0.152859	0.25358	0.312166	0.395361	0.466491	0.496522	0.564516	0.564264	0.554788	0.551891	0.55257	0.548276	0.521099	0.517559	0.518553	0.515256	0.490654	0.476651	0.444332	0.474736	0.456456	0.431408	0.465169	0.451791	0.405145	0.433735	0.416667	0.362245	0.333333	0.411765	0.283951	0.402439	0.363636	0.285714	0.396825
31.5-36 Deg	0	0	0	0.00754717	0.0815217	0.142292	0.218271	0.283494	0.333753	0.381784	0.436444	0.472969	0.488325	0.492462	0.479326	0.494505	0.47549	0.45864	0.461108	0.451835	0.42583	0.411765	0.437118	0.397764	0.406551	0.405963	0.389205	0.33564	0.381395	0.393333	0.277372	0.293103	0.308642	0.246753	0.34375	0.181818	0.108108	0.25	0.258065	0.137931
36-40.5 Deg	0	0	0	0	0.032538	0.0817963	0.170164	0.233583	0.275212	0.327416	0.366159	0.387514	0.419254	0.425045	0.403834	0.392764	0.396559	0.400812	0.369942	0.368859	0.345339	0.357923	0.325411	0.296117	0.300654	0.38785	0.366279	0.328	0.348624	0.204819	0.232143	0.186047	0.181818	0.214286	0.285714	0.214286	0.333333	0.166667	0.285714	0.181818
40.5-45 Deg	0	0	0	0	0.0139147	0.0678972	0.129657	0.192308	0.224483	0.252462	0.30273	0.319185	0.342679	0.345987	0.330502	0.331052	0.323815	0.305906	0.312284	0.313023	0.294294	0.264706	0.272981	0.214286	0.233918	0.189474	0.197368	0.231884	0.222222	0.157895	0.2	0.0526316	0.428571	0.0588235	0.166667	0.166667	0.25	0	0	1
45-49.5 Deg	0	0	0	0	0.00251467	0.0392938	0.0940285	0.141328	0.181437	0.212241	0.24064	0.244851	0.261486	0.269272	0.268868	0.255423	0.239971	0.254059	0.219613	0.205285	0.236769	0.215859	0.180723	0.158879	0.169014	0.0588235	0.0833333	0.166667	0.136364	0.25	0.0714286	0.333333	0.2	1	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0.0110121	0.0531873	0.0958814	0.126534	0.148936	0.169353	0.187424	0.203203	0.19403	0.204905	0.197958	0.161453	0.159744	0.142512	0.151292	0.132184	0.133858	0.0869565	0.097561	0.0769231	0.0909091	0	0	0	0	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0.000456204	0.0199623	0.0552683	0.0810965	0.102659	0.119633	0.118058	0.129529	0.135933	0.125182	0.118211	0.109568	0.118863	0.117073	0.108844	0.0617284	0.0851064	0.0344828	0.0909091	0	0.111111	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0.000714286	0.0128637	0.0467906	0.0568421	0.0634228	0.0796216	0.0780856	0.0909091	0.0960929	0.0849558	0.0780781	0.103825	0.0458716	0	0.0333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00745573	0.0242928	0.0364188	0.0436258	0.0367232	0.039666	0.0363636	0.0426136	0.0162162	0.0357143	0.0227273	0.0416667	0.0714286	0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.000740466	0.00470367	0.0114213	0.0195072	0.0166667	0.0120482	0	0	0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0.00280899	0.00649351	0.0123457	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 9: Table for 2D Histogram for Old NM-Rein-Sehgal

Old NM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700
0-4.5 Deg	0	0	0	0	0.333333	0.5	0.5	0.8	0.857143	0.5	0.666667	1	0.857143	0.7
4.5-9 Deg	0	0	0	0	0	0.25	0.285714	0.470588	0.466667	0.608696	0.904762	0.9	0.65	0.8
9-13.5 Deg	0	0	0	0	0.0769231	0.181818	0.285714	0.451613	0.625	0.642857	0.765957	0.721519	0.813953	0.734177
13.5-18 Deg	0	0	0	0.0714286	0.15	0.290323	0.365854	0.509091	0.621622	0.630952	0.682692	0.773109	0.722222	0.739726
18-22.5 Deg	0	0	0	0.0571429	0.0689655	0.184211	0.242424	0.505155	0.474227	0.56	0.647482	0.656442	0.609929	0.648936
22.5-27 Deg	0	0	0	0.0416667	0.04	0.247059	0.280488	0.346154	0.518797	0.465969	0.602679	0.631818	0.658291	0.668224
27-31.5 Deg	0	0	0	0.0217391	0.0615385	0.1375	0.16	0.296296	0.390863	0.466981	0.520492	0.59761	0.522727	0.544061
31.5-36 Deg	0	0	0	0.0816327	0.097561	0.07	0.244444	0.290503	0.384259	0.364407	0.435252	0.453925	0.540881	0.461017
36-40.5 Deg	0	0	0	0	0.04	0.133333	0.155172	0.235577	0.282609	0.296296	0.37785	0.377049	0.41195	0.424749
40.5-45 Deg	0	0	0	0	0	0.0869565	0.15122	0.161017	0.256228	0.271875	0.289894	0.306818	0.291545	0.340557
45-49.5 Deg	0	0	0	0	0	0.0434783	0.0843882	0.141176	0.163462	0.159322	0.242331	0.231003	0.263699	0.285156
49.5-54 Deg	0	0	0	0	0	0.0108696	0.0636364	0.0816327	0.160819	0.133144	0.170588	0.169381	0.212996	0.220588
54-58.5 Deg	0	0	0	0	0	0	0.023622	0.0238095	0.0320513	0.107463	0.107595	0.110701	0.105991	0.138728
58.5-63 Deg	0	0	0	0	0	0	0	0.0129032	0.0397554	0.0555556	0.0724638	0.0979592	0.0942408	0.0787402
63-67.5 Deg	0	0	0	0	0	0	0	0	0.0056338	0.0241379	0.0125523	0.0380952	0.04	0.0869565
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00338983	0	0.0212766	0.010989	0.0222222
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Old NM R-S	700-750	750-800	800-850	850-900	900-950	950-1000	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400
0-4.5 Deg	0.777778	0.875	0.909091	0.777778	1	0.769231	0.8	0.777778	1	0.75	0.75	1	0.6	0.833333
4.5-9 Deg	0.74359	0.877551	0.65	0.782609	0.792453	0.810811	0.866667	0.807692	0.815789	0.8	0.74359	0.861111	0.923077	0.825
9-13.5 Deg	0.732558	0.77907	0.744681	0.865979	0.746988	0.76087	0.747253	0.851064	0.776316	0.683544	0.791045	0.686567	0.862069	0.706897
13.5-18 Deg	0.70229	0.719178	0.711656	0.753425	0.726115	0.735099	0.70068	0.688889	0.705357	0.688679	0.711538	0.705882	0.670588	0.694444
18-22.5 Deg	0.705069	0.695187	0.643216	0.673267	0.651961	0.616505	0.639535	0.641176	0.666667	0.635593	0.59375	0.59375	0.6	0.652174
22.5-27 Deg	0.632959	0.659574	0.617647	0.593458	0.614213	0.654054	0.529801	0.594937	0.503817	0.591398	0.653465	0.52	0.578947	0.413793
27-31.5 Deg	0.550781	0.516981	0.592437	0.524887	0.513228	0.49359	0.531034	0.475	0.521008	0.465116	0.406593	0.517857	0.490566	0.487179
31.5-36 Deg	0.456311	0.462838	0.493878	0.474654	0.45	0.416667	0.470588	0.465909	0.454545	0.376812	0.436364	0.348837	0.541667	0.238095
36-40.5 Deg	0.422222	0.376518	0.409692	0.394737	0.407407	0.360825	0.317308	0.397436	0.267857	0.272727	0.285714	0.380952	0.176471	0.2
40.5-45 Deg	0.366534	0.316742	0.337423	0.28777	0.29661	0.257576	0.140351	0.318182	0.307692	0.208333	0.357143	0.25	0.375	0.25
45-49.5 Deg	0.27907	0.270115	0.273973	0.259259	0.347222	0.285714	0.28	0.217391	0.111111	0.1	0.0833333	0.166667	0.25	0
49.5-54 Deg	0.220238	0.15942	0.142857	0.122807	0.236364	0.129032	0.0714286	0.1	0.142857	0	0	0	0	0
54-58.5 Deg	0.186992	0.13253	0.176471	0.131579	0	0.357143	0.1	0	0	0	0	0.333333	0	0
58.5-63 Deg	0.0487805	0.0754717	0.15625	0.0416667	0	0.125	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0.0689655	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0.111111	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Old NM R-S	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	1	0.833333	0.909091	0.75	0.666667	1	0	0.666667	0	0.8	1	1
4.5-9 Deg	0.875	0.833333	0.761905	0.85	0.8	0.823529	0.652174	0.923077	0.857143	0.882353	0.533333	0.85
9-13.5 Deg	0.660377	0.755556	0.688889	0.604651	0.933333	0.638298	0.714286	0.826087	0.958333	0.842105	0.777778	0.708333
13.5-18 Deg	0.68	0.677966	0.586957	0.653846	0.612245	0.65625	0.68	0.7	0.625	0.76	0.75	0.565217
18-22.5 Deg	0.625	0.708333	0.568182	0.634146	0.461538	0.423077	0.625	0.47619	0.47619	0.76	0.611111	0.722222
22.5-27 Deg	0.568966	0.377778	0.666667	0.5	0.444444	0.473684	0.458333	0.647059	0.615385	0.45	0.4	0.333333
27-31.5 Deg	0.444444	0.347826	0.380952	0.4	0.384615	0.454545	0.1	0.333333	0.375	0.625	0.2	0.25
31.5-36 Deg	0.4	0.266667	0.3125	0.533333	0.352941	0.4	0.571429	0.222222	0.166667	0	0.666667	0.5
36-40.5 Deg	0.117647	0.166667	0.333333	0.333333	0.5	0.285714	0.5	0	0	0	0	0
40.5-45 Deg	0.2	0	0	0	0.5	0	0	0	0	1	0	0
45-49.5 Deg	0.333333	1	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0

Table 10: Table for 2D Histogram for New ANM-Rein-Sehgal

New ANM R-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500
0-4.5 Deg	0	0	0	0.037037	0.173913	0.225352	0.398693	0.510204	0.585034	0.741325
4.5-9 Deg	0	0	0	0.0538922	0.179487	0.264881	0.351406	0.522654	0.611905	0.722011
9-13.5 Deg	0	0	0	0.0881226	0.175824	0.272864	0.369565	0.47927	0.562628	0.680187
13.5-18 Deg	0	0	0	0.0502959	0.162912	0.264642	0.372408	0.45271	0.529918	0.642998
18-22.5 Deg	0	0	0	0.0477273	0.135068	0.240964	0.32415	0.42098	0.500719	0.578125
22.5-27 Deg	0	0	0	0.0256881	0.127932	0.186722	0.284972	0.381885	0.46546	0.511835
27-31.5 Deg	0	0	0	0.0135747	0.0779102	0.157462	0.237522	0.318072	0.385341	0.455377
31.5-36 Deg	0	0	0	0.00265957	0.0702447	0.140581	0.21821	0.292653	0.342622	0.394628
36-40.5 Deg	0	0	0	0	0.0358187	0.107342	0.168067	0.222502	0.294331	0.333169
40.5-45 Deg	0	0	0	0	0.0164051	0.0757272	0.131076	0.200825	0.226708	0.268313
45-49.5 Deg	0	0	0	0	0	0.0478888	0.099454	0.13113	0.177444	0.212046
49.5-54 Deg	0	0	0	0	0	0.0114405	0.0658882	0.103003	0.127891	0.149639
54-58.5 Deg	0	0	0	0	0	0.000554017	0.0170428	0.0537772	0.0883421	0.116889
58.5-63 Deg	0	0	0	0	0	0	0.0010015	0.020202	0.0406544	0.0526316
63-67.5 Deg	0	0	0	0	0	0	0	0.00108167	0.00447928	0.0226148
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM R-S	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000
0-4.5 Deg	0.812332	0.808989	0.820399	0.80597	0.846154	0.826087	0.834821	0.846791	0.849776	0.814732
4.5-9 Deg	0.822749	0.806912	0.812763	0.807565	0.807477	0.80314	0.805654	0.802672	0.816404	0.79961
9-13.5 Deg	0.778963	0.784609	0.775579	0.77094	0.780604	0.772247	0.778919	0.774887	0.769928	0.777286
13.5-18 Deg	0.714241	0.754711	0.746173	0.739165	0.72958	0.736591	0.712291	0.723065	0.699029	0.705178
18-22.5 Deg	0.669713	0.700024	0.693197	0.686785	0.675302	0.676973	0.671911	0.662691	0.649262	0.656827
22.5-27 Deg	0.587483	0.641457	0.609761	0.630852	0.616002	0.610015	0.585767	0.589724	0.588134	0.57303
27-31.5 Deg	0.527993	0.566528	0.573181	0.550737	0.538564	0.550457	0.533736	0.525933	0.509007	0.512922
31.5-36 Deg	0.429609	0.48047	0.502938	0.499068	0.49538	0.462372	0.47797	0.465828	0.428421	0.439291
36-40.5 Deg	0.361301	0.382382	0.418154	0.431897	0.40234	0.403238	0.388569	0.407134	0.374224	0.366126
40.5-45 Deg	0.30581	0.320273	0.346117	0.33394	0.333774	0.343066	0.307036	0.329013	0.279793	0.27593
45-49.5 Deg	0.222903	0.250172	0.254128	0.270336	0.280552	0.252766	0.235294	0.240708	0.214834	0.218107
49.5-54 Deg	0.172282	0.178556	0.193367	0.190678	0.185291	0.18963	0.175556	0.136364	0.150327	0.116279
54-58.5 Deg	0.122696	0.124613	0.143336	0.139043	0.133106	0.130564	0.121076	0.105263	0.0547945	0.114286
58.5-63 Deg	0.0724161	0.0817391	0.077907	0.0850662	0.0868263	0.0772947	0.0462963	0.0454545	0.0555556	0
63-67.5 Deg	0.0374384	0.0423729	0.0439122	0.0482759	0.0424242	0.025	0.125	0	0.125	0
67.5-72 Deg	0.00515464	0.0103093	0.0144928	0.00714286	0.0289855	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM R-S	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500
0-4.5 Deg	0.811494	0.835	0.820728	0.821212	0.820946	0.829352	0.86385	0.785124	0.834906	0.820896
4.5-9 Deg	0.808895	0.780172	0.79495	0.806396	0.799636	0.809524	0.799766	0.790123	0.793201	0.770154
9-13.5 Deg	0.764215	0.756151	0.769636	0.756423	0.745802	0.736299	0.725795	0.729068	0.731919	0.712513
13.5-18 Deg	0.708415	0.69735	0.68934	0.693381	0.700468	0.682373	0.673329	0.680972	0.660094	0.631818
18-22.5 Deg	0.646345	0.649693	0.62265	0.628975	0.613897	0.596406	0.591174	0.582904	0.568153	0.597598
22.5-27 Deg	0.583082	0.5553	0.564074	0.557719	0.53367	0.554507	0.527886	0.535211	0.501099	0.488432
27-31.5 Deg	0.498878	0.50292	0.473382	0.487885	0.490838	0.454704	0.467192	0.428571	0.405405	0.464286
31.5-36 Deg	0.425238	0.420697	0.393846	0.374753	0.375394	0.398374	0.379121	0.342857	0.27907	0.290323
36-40.5 Deg	0.347445	0.358079	0.315942	0.337449	0.296512	0.306931	0.295082	0.265625	0.192308	0.2
40.5-45 Deg	0.311653	0.287736	0.211538	0.186275	0.203125	0.222222	0.111111	0.272727	0.2	0
45-49.5 Deg	0.251908	0.234043	0.2	0.307692	0.235294	0	0.4	0	0	0
49.5-54 Deg	0.125	0.181818	0.0833333	0	0.5	0	1	0	0	0
54-58.5 Deg	0.157895	0	0	0	0	0.5	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

New ANM R-S	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0.815642	0.802721	0.80315	0.8	0.836538	0.855556	0.808989	0.783784	0.884058	0.705882
4.5-9 Deg	0.790738	0.80036	0.792494	0.733146	0.794798	0.766323	0.734982	0.759091	0.770335	0.812155
9-13.5 Deg	0.703791	0.716617	0.724876	0.71537	0.701461	0.718579	0.711409	0.698052	0.719368	0.688776
13.5-18 Deg	0.63144	0.590237	0.677481	0.628692	0.681818	0.648734	0.609848	0.615385	0.643275	0.635714
18-22.5 Deg	0.59465	0.57381	0.533875	0.509091	0.476852	0.57377	0.569231	0.522523	0.635294	0.603175
22.5-27 Deg	0.481343	0.509091	0.469388	0.515385	0.494382	0.472222	0.490909	0.390244	0.647059	0.321429
27-31.5 Deg	0.381679	0.402062	0.346154	0.348837	0.358974	0.55	0.307692	0.25	0.125	0.5
31.5-36 Deg	0.282051	0.592593	0.333333	0.533333	0.75	0	0.6	1	0	0
36-40.5 Deg	0.142857	0.166667	0	0.5	0	0	0	0	0	0
40.5-45 Deg	0.333333	0	0	0	0	0	0	0	0	0
45-49.5 Deg	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0

Table 11: Table for 2D Histogram for New ANM-Berger-Sehgal

New ANM B-S	0-50 MeV/c	50-100	100-150	150-200	200-250	250-300	300-350	350-400	400-450	450-500	500-550	550-600	600-650	650-700	700-750	750-800	800-850	850-900	900-950	950-1000	1000-1050	1050-1100	1100-1150	1150-1200	1200-1250	1250-1300	1300-1350	1350-1400	1400-1450	1450-1500	1500-1550	1550-1600	1600-1650	1650-1700	1700-1750	1750-1800	1800-1850	1850-1900	1900-1950	1950-2000
0-4.5 Deg	0	0	0	0.0930233	0.144737	0.283186	0.421384	0.494898	0.668161	0.710247	0.805861	0.796703	0.834184	0.844907	0.827907	0.866324	0.843458	0.855072	0.83208	0.813433	0.818653	0.841432	0.806366	0.833866	0.867133	0.840741	0.819005	0.813084	0.83	0.886667	0.823129	0.825397	0.871795	0.825243	0.824074	0.797297	0.815789	0.774194	0.823529	0.809524
4.5-9 Deg	0	0	0	0.0166667	0.165094	0.269231	0.4	0.541667	0.613402	0.732694	0.797824	0.812245	0.82494	0.814583	0.823051	0.812541	0.792568	0.781479	0.804378	0.794982	0.805085	0.823664	0.813322	0.809233	0.801491	0.754923	0.791063	0.783712	0.79661	0.793729	0.777403	0.774319	0.787879	0.784741	0.817629	0.771523	0.778723	0.776824	0.762376	0.821229
9-13.5 Deg	0	0	0	0.0700935	0.130919	0.271667	0.353012	0.480322	0.569575	0.68139	0.781754	0.795837	0.774114	0.785362	0.773578	0.781475	0.76586	0.762567	0.752009	0.761471	0.748873	0.73664	0.739656	0.735498	0.72956	0.755391	0.720774	0.711163	0.74169	0.714434	0.730546	0.70028	0.702786	0.692029	0.698795	0.727488	0.698895	0.694079	0.706827	0.663507
13.5-18 Deg	0	0	0	0.0401338	0.149742	0.265497	0.336059	0.414129	0.536284	0.638281	0.728386	0.717996	0.747335	0.748866	0.736466	0.7337	0.731489	0.723615	0.700111	0.714206	0.71014	0.691088	0.695486	0.679018	0.673116	0.66913	0.689633	0.664591	0.685662	0.667735	0.664188	0.656201	0.664884	0.654737	0.652068	0.615894	0.627737	0.628571	0.650888	0.613924
18-22.5 Deg	0	0	0	0.0277778	0.137174	0.23849	0.319925	0.423721	0.499227	0.57533	0.655519	0.701815	0.686171	0.689579	0.686069	0.673434	0.65566	0.6686	0.647105	0.657014	0.636641	0.624197	0.638889	0.646891	0.628604	0.584667	0.586435	0.624873	0.603365	0.570149	0.581722	0.600887	0.607558	0.583333	0.531915	0.573034	0.525641	0.527559	0.552632	0.487179
22.5-27 Deg	0	0	0	0.0196464	0.109134	0.204236	0.312057	0.385731	0.447873	0.516755	0.600138	0.645331	0.628718	0.629526	0.604035	0.609545	0.603815	0.602548	0.578702	0.597386	0.569439	0.583187	0.543649	0.537295	0.536066	0.55848	0.548585	0.504687	0.518738	0.493639	0.501502	0.469828	0.469945	0.477273	0.443299	0.445783	0.442623	0.297297	0.405405	0.482759
27-31.5 Deg	0	0	0	0.00315956	0.104046	0.165109	0.256264	0.322028	0.397871	0.445264	0.512134	0.574856	0.561587	0.558263	0.539545	0.545725	0.538095	0.525974	0.509479	0.506996	0.501982	0.5	0.4943	0.457645	0.467143	0.448387	0.4447	0.485531	0.401487	0.407609	0.365517	0.330189	0.263889	0.446809	0.4	0.380952	0.136364	0.333333	0.555556	0.333333
31.5-36 Deg	0	0	0	0	0.0525862	0.124857	0.206051	0.275698	0.333971	0.392423	0.431607	0.47668	0.500539	0.496867	0.476983	0.479711	0.460797	0.455385	0.446729	0.424768	0.438768	0.394628	0.38565	0.408915	0.451791	0.342561	0.429348	0.30303	0.322917	0.333333	0.285714	0.3	0.333333	0.352941	0.166667	1	1	0.333333	0.5	0
36-40.5 Deg	0	0	0	0	0.0444774	0.105837	0.16809	0.234525	0.286885	0.327259	0.353491	0.400137	0.418747	0.422945	0.407023	0.396731	0.398879	0.392036	0.372638	0.364706	0.376984	0.347664	0.323529	0.355856	0.312849	0.325	0.338983	0.410256	0.242424	0.157895	0.25	0.166667	0	0.5	0	0	0	0	0	0
40.5-45 Deg	0	0	0	0	0.0210938	0.0689829	0.137208	0.172468	0.226261	0.272047	0.300615	0.316995	0.337145	0.348088	0.337621	0.320774	0.311813	0.293856	0.315938	0.294333	0.257062	0.283262	0.26	0.298851	0.258065	0.228571	0.210526	0.111111	0.285714	0	1	0.5	0.5	0	0	0	0	0	0	0
45-49.5 Deg	0	0	0	0	0	0.035913	0.0925481	0.127177	0.17693	0.21244	0.229012	0.236659	0.252955	0.271491	0.267346	0.259352	0.254042	0.228395	0.213368	0.222222	0.229299	0.195652	0.196429	0.142857	0.285714	0.333333	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0
49.5-54 Deg	0	0	0	0	0	0.0115668	0.0516817	0.101349	0.118959	0.148848	0.169149	0.194822	0.189664	0.203367	0.176355	0.210306	0.188017	0.202572	0.150943	0.148936	0.145455	0.130435	0.142857	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
54-58.5 Deg	0	0	0	0	0	0	0.0210526	0.052506	0.080695	0.104636	0.120419	0.128324	0.143609	0.149563	0.12426	0.149296	0.141667	0.115044	0.149254	0.285714	0	0.0769231	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
58.5-63 Deg	0	0	0	0	0	0	0	0.0150616	0.0392791	0.0594262	0.0719951	0.0804312	0.088785	0.0819367	0.0946372	0.0851064	0.0535714	0.0888889	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
63-67.5 Deg	0	0	0	0	0	0	0	0	0.00795003	0.0215545	0.0325901	0.0497512	0.0446927	0.0397554	0.0674847	0.0933333	0.0952381	0.047619	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
67.5-72 Deg	0	0	0	0	0	0	0	0	0	0.00182983	0.00373599	0.00414938	0.0170648	0.00552486	0.0136986	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
72-76.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0266667	0	0.0833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
76.5-81 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
81-85.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
85.5-90 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
90-94.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
94.5-99 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
99-103.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103.5-108 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
108-112.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
112.5-117 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
117-121.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
121.5-126 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
126-130.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
130.5-135 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
135-139.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
139.5-144 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
144-148.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
148.5-153 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
153-157.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
157.5-162 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
162-166.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
166.5-171 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
171-175.5 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
175.5-180 Deg	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0