

# Mathematics, Data Science and Social Impact

**Provocative Debate about their Chemistry if any**

(mine from Big Data perspective)



## *Data*


*is the sword of the twenty first century,  
those who wield it well, the Samurai.*

– Jonathan Rosenberg, former SVP of product management at Google

Source: Rosenberg, Jonathan. 2009. "From the Height of this Place," Official Google Blog <https://googleblog.blogspot.com/2009/02/from-height-of-this-place.html>

## “Big Data” Sources

**It's All Happening On-line**


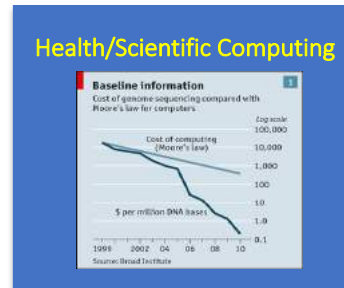


Every:  
Click  
Ad impression  
Billing event  
Fast Forward, pause,...  
Server request  
Transaction  
Network message  
Fault  
...

**User Generated (Web & Mobile)**



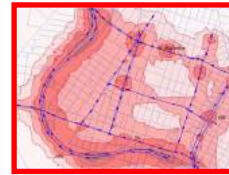
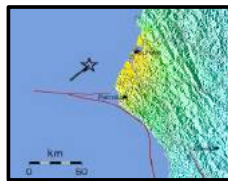
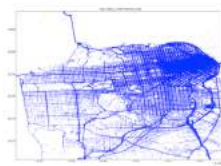

**Internet of Things / M2M**

What can you do with the data?

One example application:

Traffic Prediction and Earthquake Warning



Crowdsourcing + physical modeling + sensing + data assimilation

to produce:



From Alex Bayen, UCB, Director, Institute for Transportation Studies

## Big Data: The Good (Bright and Ubiquitous)

Experiments, observations, and numerical simulations in many areas of science and business are currently generating terabytes of data, and are on the verge of generating petabytes and beyond for some applications.

Analyses of the information contained in these data sets have already led to major breakthroughs in fields ranging from genomics to astronomy and high-energy physics and to the development of new information-based industries.

- Frontiers in Massive Data Analysis, National Research Council of the National Academies

## Big Data: The Bad (Dark and Scarce)

Given a large mass of data, we can, by judicious selection, construct perfectly plausible unassailable theories—all of which, some of which, or none of which may be right.

- Paul Arnold Srere

## Big Data: The Hopeful

The ability to take data—to be able to understand it, to process it, to extract value from it, to visualize it, to communicate it — that's going to be a hugely important skill in the next decades, not only at the professional level but even at the educational level for elementary school kids, for high school kids, for college kids. Because now we really do have essentially free and ubiquitous data. So the complimentary scarce factor is the ability to understand that data and extract value from it.

- Hal Varian, Google's Chief Economist,  
[http://www.mckinsey.com/insights/innovation/hal\\_varian\\_on\\_how\\_the\\_web\\_challenges\\_managers](http://www.mckinsey.com/insights/innovation/hal_varian_on_how_the_web_challenges_managers)

The goal of this summer school: Getting students to be able to think critically about data.

(with the focused theme of Math, Data Science and Social Impact)

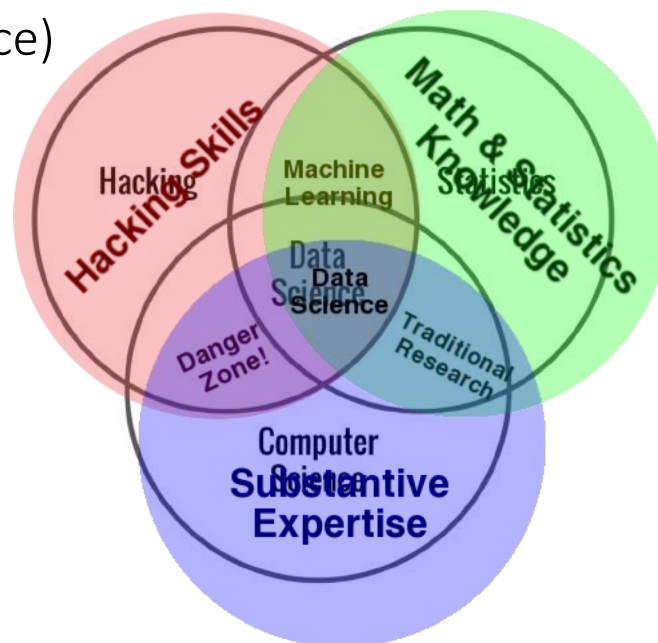
## Big Data: The Hopeful

The ability to take data—to be able to **understand** it, to **process** it, to **extract value** from it, to **visualize** it, to **communicate** it — that's going to be **a hugely important skill in the next decades, not only at the professional level but even at the educational level for elementary school kids, for high school kids, for college kids**. Because now we really do have **essentially free and ubiquitous data**. So the complimentary scarce factor is the ability to understand that data and extract value from it.

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Educate and Learn to be able to think **critically** about data.

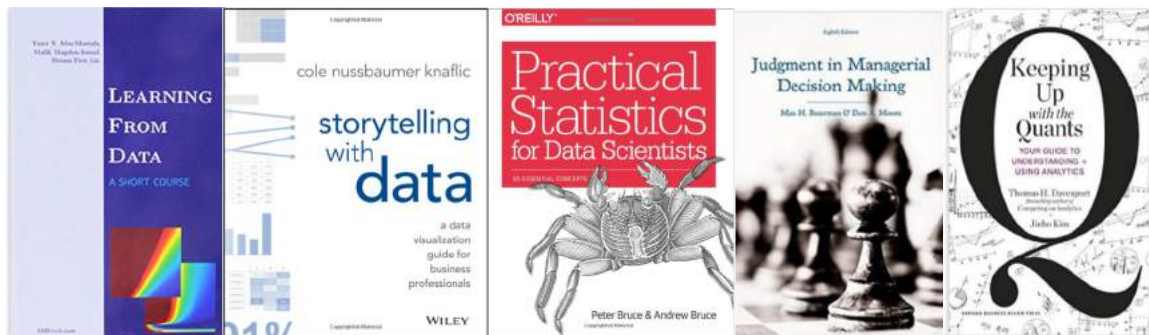
## Data Science – A Visual Definition (Skills for Data Science)



<http://drewconway.com/zia/2013/3/26/the-data-science-venn-diagram>

## Business Intelligence v.s. Data Science

Business Intelligence	Data Science
Querying the past	Querying the past present and future



## Machine Learning v.s. Data Science

### Machine Learning

Develop new (individual) models

Prove mathematical properties of models

Improve/validate on a few, relatively clean, small datasets

Publish a paper

### Data Science

Explore many models, build and tune hybrids

Understand empirical properties of models

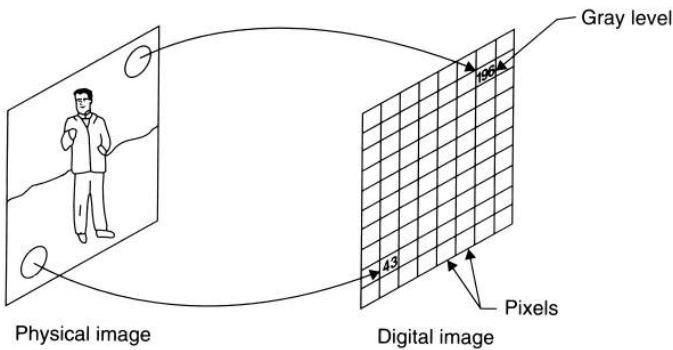
Develop/use tools that can handle massive datasets

Take action!

Turn **data** into **data products**

# Mathematics and Data Science: Strong Chemistry

## Digital Images and Problems

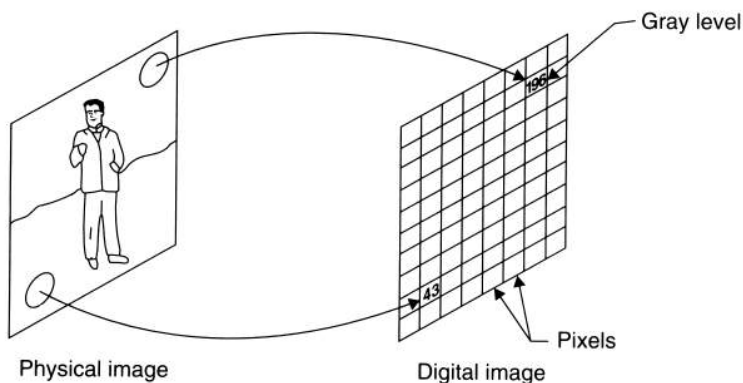


**Figure 1-1** A physical image and a corresponding digital image

## Mining Images with ML and Deep Neural Networks

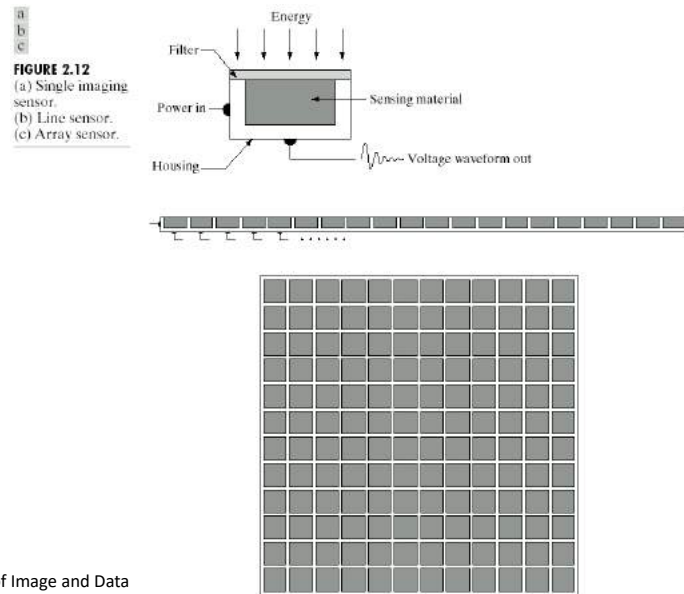
- Mathematical techniques (Fourier, wavelets, SVD, etc.)
- Problems from data analysis (mainly image analysis)

## What's a Digital Image?



**Figure 1-1** A physical image and a corresponding digital image

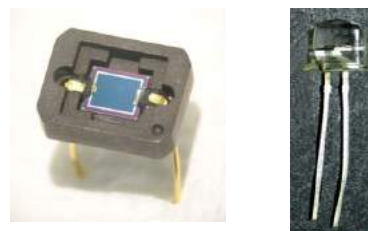
## Mechanism for digitizing



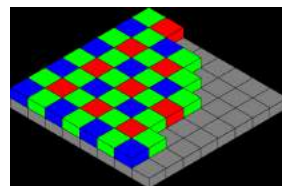
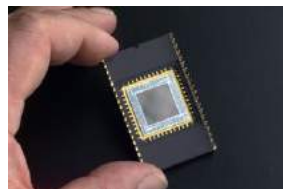
Introduction to the Mathematics of Image and Data  
 Analysis by Gilad Lerman@umn.edu

## Examples of Sensors

Well known from physics courses...  
 photodiode



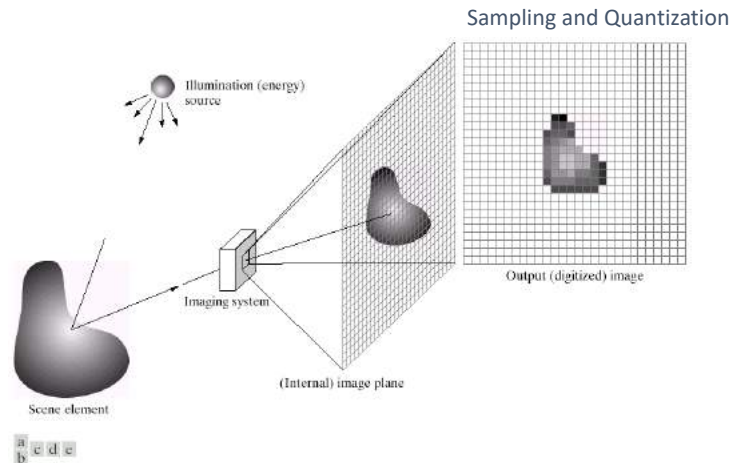
Common in Digital Camera  
 Charged-Couple Device (CCD)



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# Digital Image Acquisition



**FIGURE 2.15** An example of the digital image acquisition process (a) Energy ("illumination") source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

Introduction to the Mathematics of Image and Data Analysis by Gilad Lerman@umn.edu

## Problem: Effect of Compression

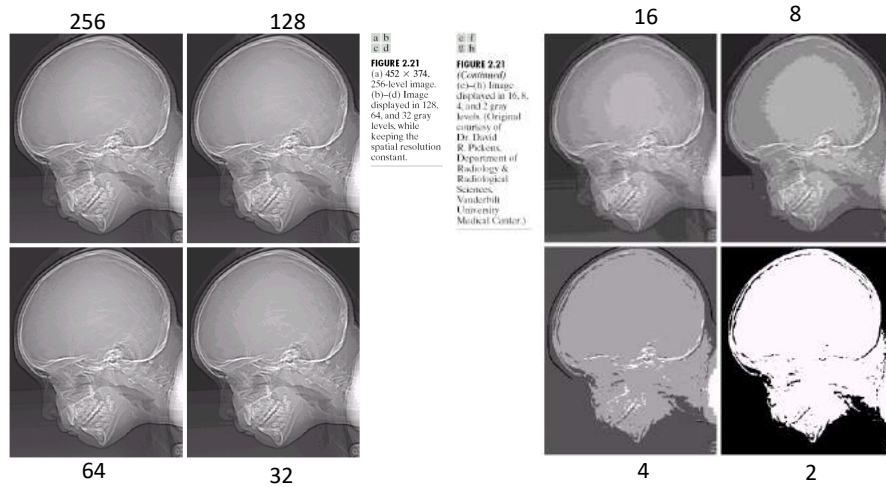
- Color image of 600x800 pixels
  - Without compression
    - $(600 \times 800 \text{ pixels}) \times (24 \text{ bits/pixel})$   
 $= 11.52 \text{M bits} = 1.44 \text{M bytes}$
  - After JPEG compression (popularly used on web)
    - only 89K bytes
    - compression ratio  $\sim 16:1$
- Movie
  - 720x480 per frame,
  - 30 frames/sec,
  - 24 bits/pixel
  - Raw video  $\sim 243 \text{M bits/sec}$
  - DVD  $\sim$  about 5M bits/sec
  - Compression ratio  $\sim 48:1$



"Library of Congress" by M. Wu (600x800)  
Based on slides by W. Trappe



## Problem: Effect of Quantization



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## Data Science and Social Impact Decision Making Biases



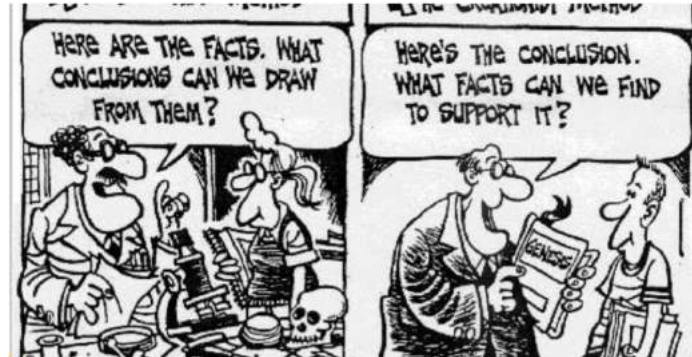
## Selective Perception & A specific case



### • Selective Perception

- See things from our own personal perspective
- Organize and interpret events/information based on this perception
- Influences what we pay attention to and the problems we identify, and the alternatives we develop or consider.

### Confirmation Bias:



Stacey Truex and Ling Liu. Countering Membership Inference Attacks with Differentially Private DNN Training

## Overconfidence Bias

- When we are given factual questions and asked to judge the probability that our answers are correct, we tend to be far too optimistic.

Target Confidence	✓ 99.9997%	✓ 65.810764%	✓ 72.56185%	✗ 62.29565%	✓ 99.99863%	✗ 99.63283%	✓ 98.37766%	
Attacker Confidence	✓ 86.100227%	✓ 50.491995%	✗ 61.852753%	✓ 72.06423%	✓ 56.403625%	✓ 99.88525%	✗ 53.290564%	
In Training Data?	✓	✗	✗	✗	✓	✗	✗	

Most Importantly...

**BE AWARE!**

Neither human nor machine can escape these biases but if you are **aware of them** and **challenge them**, you will become a **stronger critical thinker** and better decision maker overall!

**Mathematics + Social Impact**

***Two sides of the big data sword***