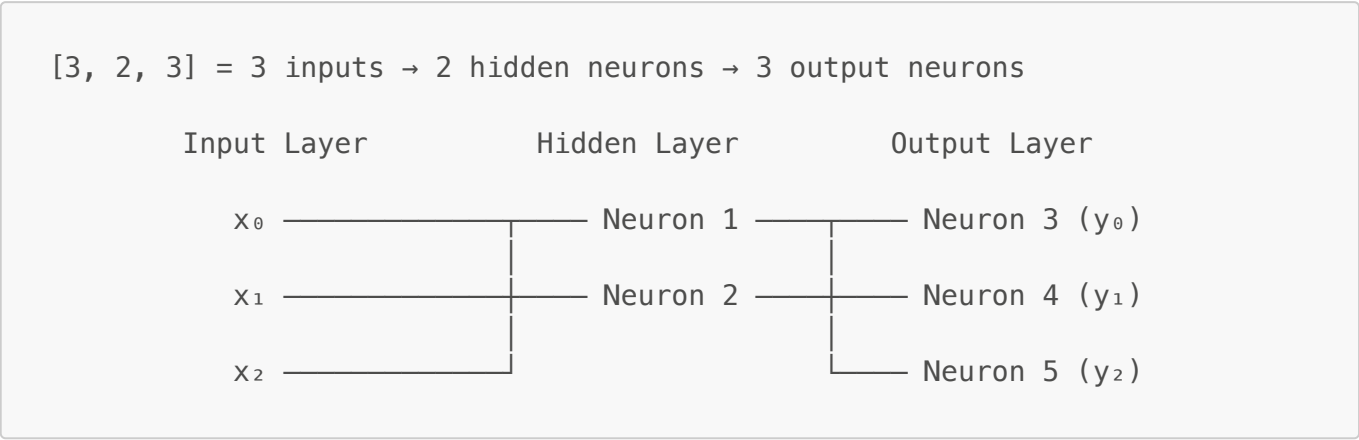


Backpropagation - Övning

Nätverksarkitektur



Träningsexempel

Värde	
Input	[0.0000, 0.4492, 0.1630]
Target	[0, 1, 0]
Learning rate	0.2

STEG 1: Forward Pass

Formel: $\text{Output} = \text{sigmoid}(\sum(\text{Input} \times \text{Vikt}) + \text{Bias})$

Sigmoid: $\sigma(x) = 1 / (1 + e^{-x})$

Lager 1 (Hidden)

Neuron 1

Input	Vikt	Input x Vikt
0.0000	0.1394	0.0000
0.4492	-0.4750	—
0.1630	-0.2250	-0.0367
Summa:		-0.2500
Värde		
Bias		-0.2768

Värde	
Total (Summa + Bias)	-0.5268
Output = sigmoid(-0.5268) 0.3713	

Neuron 2

Input	Vikt	Input × Vikt
0.0000	0.2365	0.0000
0.4492	0.1767	0.0794
0.1630	0.3922	0.0639
Summa:		0.1433
Värde		
Bias		-0.4131
Total (Summa + Bias)		___
Output = sigmoid(___)		___

Lager 2 (Output)

Neuron 3

Input (från Hidden)	Vikt	Input × Vikt
0.3713	-0.0781	-0.0290
0.4330	-0.4702	-0.2036
Summa:		-0.2326
Värde		
Bias		-0.2814
Total (Summa + Bias)		-0.5139
Output = sigmoid(-0.5139)		0.3743

Neuron 4

Input (från Hidden)	Vikt	Input × Vikt
0.3713	0.0054	0.0020
0.4330	-0.4735	___
Summa:		___

	Värde
Bias	-0.3012
Total (Summa + Bias)	-0.5042
Output = sigmoid(-0.5042)	0.3766

Neuron 5

Input (från Hidden)	Vikt	Input × Vikt
0.3713	0.1499	0.0556
0.4330	0.0449	0.0195
Summa:		0.0751
	Värde	
Bias	-0.2796	
Total (Summa + Bias)	-0.2045	
Output = sigmoid(-0.2045)	0.4491	

STEG 2: Backward Pass (Felberäkning)

Output-lagret (Lager 2)

Formel: $\Delta = (\text{Target} - \text{Output}) \times \text{Output} \times (1 - \text{Output})$

Neuron 3

Steg	Formel	Värde
Target		0
Output		0.3743
Error	Target - Output	-0.3743
Sigmoid derivata	Output × (1 - Output)	—
Delta	Error × Sigmoid derivata	-0.0877

Neuron 4

Steg	Formel	Värde
Target		1
Output		0.3766

Steg	Formel	Värde
Error	Target - Output	—
Sigmoid derivata	Output × (1 - Output)	0.2348
Delta	Error × Sigmoid derivata	—

Neuron 5

Steg	Formel	Värde
Target		0
Output		0.4491
Error	Target - Output	-0.4491
Sigmoid derivata	Output × (1 - Output)	0.2474
Delta	Error × Sigmoid derivata	-0.1111

Hidden-lagret (Lager 1)

Formel: $\Delta = (\sum \Delta_{\text{next}} \times \text{Vikt}_{\text{till_next}}) \times \text{Output} \times (1 - \text{Output})$

Neuron 1

Steg 1: Beräkna error contribution från output-lagret

Nästa Neuron	Delta	Vikt till Neuron 1	Bidrag
Neuron 3	-0.0877	-0.0781	0.0068
Neuron 4	0.1464	0.0054	0.0008
Neuron 5	-0.1111	0.1499	—
Summa:			-0.0090

Steg 2: Beräkna delta

Steg	Formel	Värde
Output		0.3713
Error contribution	Summa från ovan	-0.0090
Sigmoid derivata	Output × (1 - Output)	0.2334
Delta	Error contrib × Sigmoid derivata	-0.0021

Neuron 2

Steg 1: Beräkna error contribution från output-lagret

Nästa Neuron	Delta	Vikt till Neuron 2	Bidrag
Neuron 3	-0.0877	-0.4702	___
Neuron 4	0.1464	-0.4735	-0.0693
Neuron 5	-0.1111	0.0449	-0.0050
		Summa:	___

Steg 2: Beräkna delta

Steg	Formel	Värde
Output		0.4330
Error contribution	Summa från ovan	___
Sigmoid derivata	Output × (1 - Output)	0.2455
Delta	Error contrib × Sigmoid derivata	-0.0081

STEG 3: Viktuppdatering

Formel: Ny vikt = Gammal vikt + Learning rate × Delta × Input

Learning rate = 0.2

Lager 1 (Hidden)

Neuron 1 (δ = -0.0021)

Vikt	Gammal	Input	Ändring	Ny
w ₀	0.1394	0.0000	0.2 × -0.0021 × 0.0000 = -0.0000	0.1394
w ₁	-0.4750	0.4492	0.2 × -0.0021 × 0.4492 = ___	___
w ₂	-0.2250	0.1630	0.2 × -0.0021 × 0.1630 = -0.0001	-0.2250
bias	-0.2768	1	0.2 × -0.0021 = -0.0004	-0.2772

Neuron 2 (δ = -0.0081)

Vikt	Gammal	Input	Ändring	Ny
w ₀	0.2365	0.0000	0.2 × -0.0081 × 0.0000 = -0.0000	0.2365
w ₁	0.1767	0.4492	0.2 × -0.0081 × 0.4492 = -0.0007	0.1760
w ₂	0.3922	0.1630	0.2 × -0.0081 × 0.1630 = -0.0003	0.3919

Vikt	Gammal	Input	Ändring	Ny
bias	-0.4131	1	$0.2 \times -0.0081 = -0.0016$	-0.4147

Lager 2 (Output)

Neuron 3 ($\delta = -0.0877$)

Vikt	Gammal	Input (från Hidden)	Ändring	Ny
w_0	-0.0781	0.3713	$0.2 \times -0.0877 \times 0.3713 = -0.0065$	-0.0846
w_1	-0.4702	0.4330	$0.2 \times -0.0877 \times 0.4330 = -0.0076$	-0.4778
bias	-0.2814	1	$0.2 \times -0.0877 = -0.0175$	-0.2989

Neuron 4 ($\delta = 0.1464$)

Vikt	Gammal	Input (från Hidden)	Ändring	Ny
w_0	0.0054	0.3713	$0.2 \times 0.1464 \times 0.3713 = \underline{\hspace{1cm}}$	$\underline{\hspace{1cm}}$
w_1	-0.4735	0.4330	$0.2 \times 0.1464 \times 0.4330 = 0.0127$	-0.4608
bias	-0.3012	1	$0.2 \times 0.1464 = 0.0293$	-0.2719

Neuron 5 ($\delta = -0.1111$)

Vikt	Gammal	Input (från Hidden)	Ändring	Ny
w_0	0.1499	0.3713	$0.2 \times -0.1111 \times 0.3713 = -0.0082$	0.1416
w_1	0.0449	0.4330	$0.2 \times -0.1111 \times 0.4330 = -0.0096$	0.0353
bias	-0.2796	1	$0.2 \times -0.1111 = -0.0222$	-0.3018

Sammanfattning

Neuron	Output (före)	Delta	Funktion
1	0.3713	-0.0021	Hidden
2	$\underline{\hspace{1cm}}$	-0.0081	Hidden
3	0.3743	-0.0877	Output (y_0)
4	0.3766	$\underline{\hspace{1cm}}$	Output (y_1)
5	0.4491	-0.1111	Output (y_2)