# ECE 20100 – Spring 2017 Final Exam

May 2, 2017

#### **Section (circle below)**

Qi (12:30) – 0001 Tan (10:30) – 0004 Hosseini (7:30) – 0005

Cui (1:30) – 0006 Jung (11:30) – 0007

Lin (9:30) – 0008 Peleato-Inarrea (2:30) – 0009

Name PUID

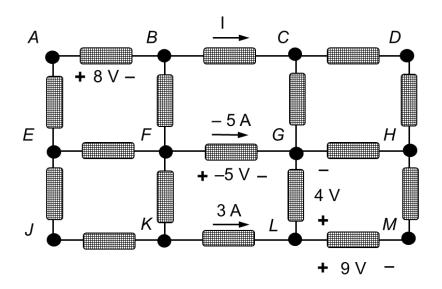
#### **Instructions**

- 1. DO NOT START UNTIL TOLD TO DO SO.
- 2. Write your name, section, professor, and student ID# on your **Scantron** sheet. We may check PUIDs.
- 3. This is a CLOSED BOOKS and CLOSED NOTES exam.
- 4. The use of a TI-30X IIS calculator is allowed.
- 5. If extra paper is needed, use the back of test pages.
- 6. Cheating will not be tolerated. Cheating in this exam will result in, at the minimum, an F grade for the course. In particular, **continuing to write after the exam time is up is regarded as cheating**.
- 7. If you cannot solve a question, be sure to look at the other ones, and come back to it if time permits.

By signing the scantron sheet, you affirm you have not received or provided assistance on this exam.

## **Question 1:**

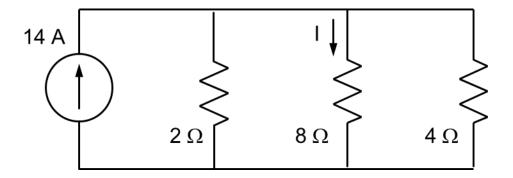
In the circuit shown, rectangular shapes represent general circuit elements (either resistors or sources). Find the current (I) between nodes B and C (in A).



- (1) 4
- (2) 3
- (3) 2
- (4) 1
- (5) 1
- (6) 2
- (7) 3
- (8) 4
- (9) None of the above

## **Question 2:**

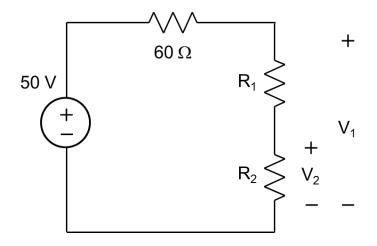
Find the value of the current (I) in the circuit below (in A).



- (1) 1
- (2) 2
- (3) 3
- (4) 4
- (5) 5
- (6) 6
- (7) 7
- (8) 8
- (9) None of the above

#### **Question 3:**

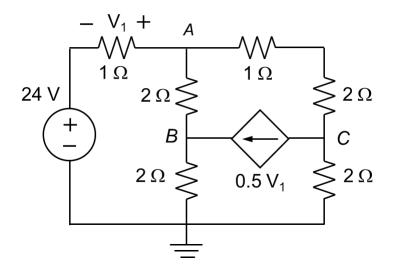
In the circuit below,  $V_1 = 35$  V and  $V_2 = 10$  V. Find the value of  $R_1$  (in Ohm) to achieve these voltages.



- (1) 10
- (2) 20
- (3) 40
- (4) 50
- (5) 60
- (6) 75
- (7) 80
- (8) 100
- (9) None of the above

## **Question 4:**

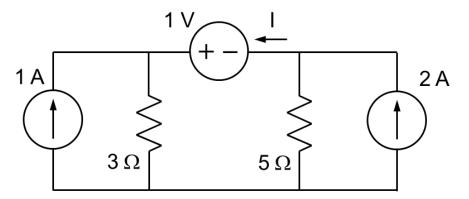
In the circuit below, find nodal voltage  $V_B$  (in Volts) when nodal voltage  $V_A$  equals 16 V.



- (1) 1
- (2) 2
- $(3) \ 3$
- (4) 4
- (5) 8
- (6) 12
- (7) 16
- (8) 20
- (9) None of the above

## **Question 5:**

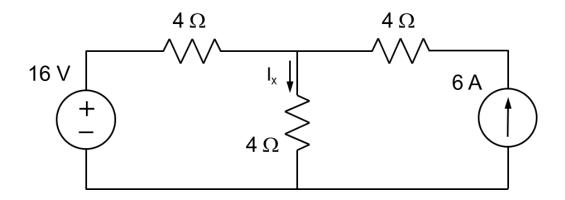
Use source transformation to determine the current I in the circuit below. Find the current I (in A).



- (1) 1
- (2) 2
- (3) 3
- (4) 5
- (5) 1
- (6) 2
- (7) 3
- (8) 5
- (9) None of the above

#### **Question 6:**

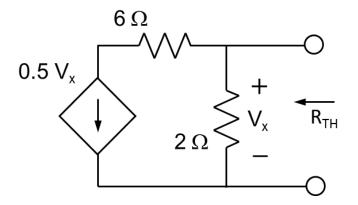
Using superposition, find the contributions to the current  $I_x$  (in A) from each source (VS – voltage source active only; CS – current source active only).



- (1)  $i_x(VS) = 0.5$ ;  $i_x(CS) = 2$
- (2)  $i_x(VS) = 1;$   $i_x(CS) = 2$
- (3)  $i_x(VS) = 1.5;$   $i_x(CS) = 4$
- (4)  $i_x(VS) = 16$   $i_x(CS) = 1.5$
- (5)  $i_x(VS) = 0.3$ ;  $i_x(CS) = 0.75$
- (6)  $i_x(VS) = 4;$   $i_x(CS) = 1$
- (7)  $i_x(VS) = 2;$   $i_x(CS) = 3$
- (8)  $i_x(VS) = 2;$   $i_x(CS) = 1.5$
- (9) None of the above

## **Question 7:**

Find the Thévenin equivalent resistance,  $R_{th}$  for the circuit below (in  $\Omega$ ).



- (1) 1
- (2) 2
- (3) 3
- (4) 4
- (5) 5
- (6) 6
- (7) 7
- (8) 8
- (9) None of the above

#### **Question 8:**

In a first-order RC circuit, the capacitor voltage is represented as,

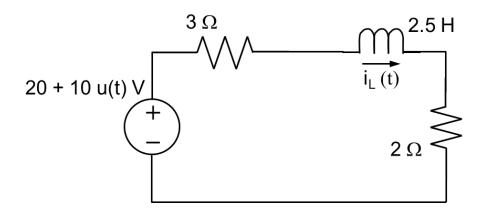
$$v_C(t) = 10 (1 - e^{-t/3}) V$$

Find the time (in s) required for the capacitor voltage to change from 2 V to 8 V.

- $(1) 1 \ln(5/2)$
- $(2) 1 \ln(3)$
- (3) 1 ln(4)
- (4) 1 ln(10)
- $(5) 3 \ln(5/2)$
- $(6) 3 \ln(3)$
- $(7) 3 \ln(4)$
- (8) 3 ln(10)
- (9) None of the above

## **Question 9:**

In the circuit shown, find the inductor current  $i_L(t)$  for  $t \ge 0$  s (in A).



(1) 
$$7.5 - 2.5 e^{-2t}$$

(2) 
$$7.5 - 2.5 e^{-0.5t}$$

(3) 
$$5 e^{-2t}$$

(4) 
$$5 e^{-0.51}$$

(5) 
$$6-2e^{-2t}$$

(6) 
$$6-2e^{-0.5t}$$

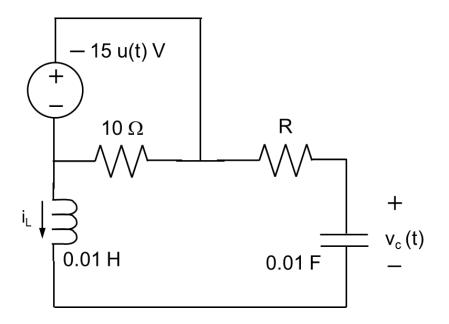
(7) 
$$4.5 - 2.5 e^{-2t}$$

(8) 
$$4.5 - 2.5 e^{-0.5t}$$

(9) None of the above

## **Question 10:**

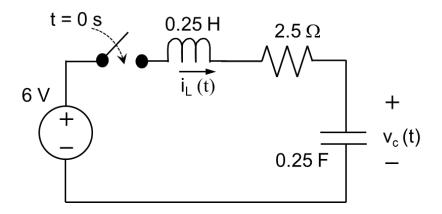
Find the range for resistance R (in Ohm) that makes the circuit *underdamped*.



- (1)  $0 \le R \le 2$
- (2)  $0 \le R \le 4$
- (3)  $0 \le R \le 5$
- (4)  $0 \le R \le 10$
- (5)  $2 \le R \le \infty$
- (6)  $4 \le R \le \infty$
- $(7) \ 5 \le R \le \infty$
- (8)  $10 \le R \le \infty$
- (9) None of the above

#### **Question 11:**

In the following circuit, the switch has been open for a long time and it closes at t = 0 s. The capacitor voltage  $v_C(t)$  was 0 V at  $t = 0^-$  s. Find the capacitor voltage  $v_C(t)$  for  $t \ge 0$  s (in Volts).



(1) 
$$6-6(1+t)e^{-2t}$$

(2) 
$$6 - (6\cos 8t + 8\sin 8t) e^{-2t}$$

(3) 
$$6 + 2 e^{-8t} - 8 e^{-2t}$$

(4) 
$$8e^{-8t} - 8e^{-2t}$$

(5) 
$$6-6(1+t)e^{-8t}$$

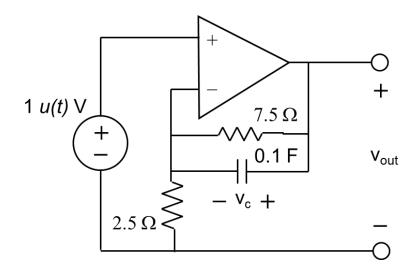
(6) 
$$6 + (-8\cos 8t + 6\sin 8t) e^{-2t}$$

(7) 
$$6+8e^{-8t}-6e^{-2t}$$

(8) None of the above

## **Question 12:**

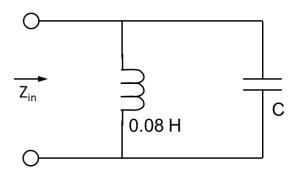
In the ideal op amp circuit below, find  $v_{out}$  ( $\infty$ ) (in Volts).



- (1) 1
- (2) 2
- (3) 3
- (4) 4
- (5) 5
- (6) 6
- (7) 7
- (8) 8
- (9) None of the above

#### **Question 13:**

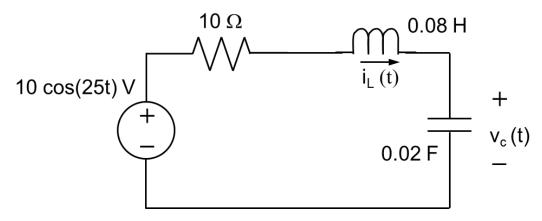
The circuit shown is to have an input impedance of  $Z_{in}(j\omega)=25j$  Ohm at  $\omega=100$  rads/sec. Find the capacitance C to achieve this impedance (in mF).



- (1) 0.10
- (2) 0.23
- (3) 0.37
- (4) 0.44
- (5) 0.50
- (6) 0.66
- (7) 0.85
- (8) 1.0
- (9) None of the above

#### **Question 14:**

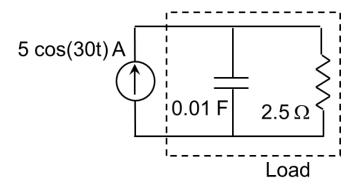
In the following circuit, find the sinusoidal steady state capacitor voltage  $v_C(t)$  (in Volts).



- $(1) \cos(25t)$
- (2)  $2\cos(25t + 90^\circ)$
- (3)  $2\cos(25t 90^\circ)$
- (4)  $2\cos(25t)$
- $(5) \ 0.2 \cos(25t 90^{\circ})$
- (6)  $0.2\cos(25t + 90^\circ)$
- $(7) \ 0.2 \cos(25t)$
- (8) 0
- (9) None of the above

#### **Question 15:**

Find the instantaneous power (in W) absorbed by the load.



- (1)  $5\cos(53.13^\circ) + 5\cos(60t + 53.13^\circ)$
- (2)  $25\cos(53.13^\circ) + 25\cos(60t + 53.13^\circ)$
- (3)  $12.5\cos(53.13^\circ) + 12.5\cos(60t + 53.13^\circ)$
- (4)  $25\cos(53.13^\circ) + 5\cos(30t + 53.13^\circ)$
- $(5) 5 \cos(-36.87^{\circ}) + 5 \cos(60t 36.87^{\circ})$
- (6)  $25 \cos(-36.87^{\circ}) + 25 \cos(30t 36.87^{\circ})$
- (7)  $12.5 \cos(-36.87^{\circ}) + 12.5 \cos(60t 36.87^{\circ})$
- (8)  $25 \cos(-36.87^{\circ}) + 25 \cos(60t 36.87^{\circ})$
- (9) None of the above

## **Question 16:**

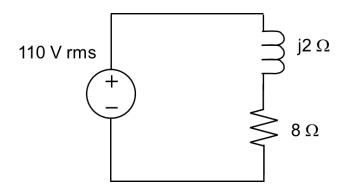
Find the effective (rms) value (in V rms) of the voltage waveform,

$$v(t) = 5(1 + \cos(\omega t)) V$$

- (1) 5
- (2)  $2.5\sqrt{2}$
- (3)  $5\sqrt{2}$
- (4)  $5\sqrt{3/2}$
- (5)  $5 + 2.5\sqrt{2}$
- (6)  $5 + 5\sqrt{2}$
- (7)  $5 + 5\sqrt{3/2}$
- (8) 7.5
- (9) None of the above

## **Question 17:**

Find the apparent power (in VA) supplied by the 110 V rms source.



- (1) 875.6
- (2) 1023.9
- (3) 1237.1
- (4) 1467.3
- (5) 1612.5
- (6) 1866.2
- (7) 2085.2
- (8) 3025.0

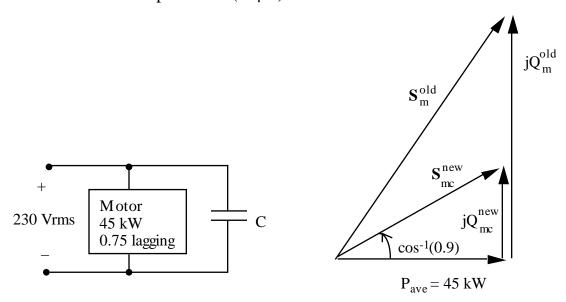
#### **Question 18:**

Find the complex power delivered to a load that absorbs 1 kW average power with a power factor (pf) equal to 0.91 *leading* (in VA):

- (1) 1,000 + j118.4
- (2) 1,000 + j237.1
- (3) 1,000 + j314.5
- (4) 1,000 + j455.6
- (5) 1,000 j118.4
- (6) 1,000 j237.1
- (7) 1,000 j314.5
- (8) 1,000 j455.6
- (9) None of the above

#### **Question 19:**

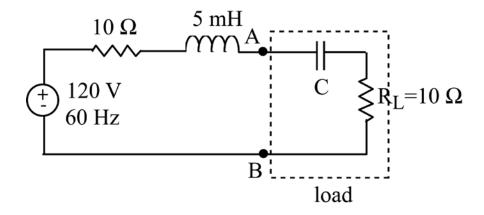
The motor in the circuit below consumes 45 kW at a power factor of 0.75 lagging. The effective voltage across the motor is 230 V at  $\omega=120\pi$ . A capacitor is put in parallel with the motor to increase the power factor to 0.9 lagging. It is already known that with compensation,  $Q_{mc}^{new}=21.8$  kVAR, and without compensation,  $Q_{mc}^{old}=39.7$  kVAR. The capacitance (in  $\mu F$ ) is:



- (1) 7801.7
- (2) 1994.4
- (3) 897.6
- (4) 472.0
- (5) 99.0
- (6) 26.5
- (7) 21.2
- (8) 15.4

## **Question 20:**

Find the value of C (in mF) that will deliver maximum power to  $R_{\rm L}$ .



- (1) 0.0014
- (2) 0.055
- (3) 0.53
- (4) 1.41
- (5) 14.1
- (6) 55.6
- (7) 251.6
- (8) 530.5

## Potentially Useful Formulas (2<sup>nd</sup> Midterm)

$$x(t) = x(\infty) + \left[x(t_0^+) - x(\infty)\right]e^{-(t-t_0)/\tau}$$
, where  $\tau = R_{TH}C$  or  $\tau = \frac{L}{R_{TH}}$ 

$$\begin{aligned} v_L(t) &= L \frac{di_L(t)}{dt} & i_C(t) &= C \frac{dv_C(t)}{dt} \\ i_L(t) &= i_L(t_0) + \frac{1}{L} \int_{t_0}^t v_L(t') dt' & v_C(t) &= v_C(t_0) + \frac{1}{C} \int_{t_0}^t i_C(t') dt' \\ W_L(t_0, t_1) &= \frac{L}{2} \Big[ \Big( i_L(t_1) \Big)^2 - \Big( i_L(t_0) \Big)^2 \Big] & W_C(t_0, t_1) &= \frac{C}{2} \Big[ \Big( v_C(t_1) \Big)^2 - \Big( v_C(t_0) \Big)^2 \Big] \end{aligned}$$

$$-\ln x = \ln \frac{1}{x}$$

Elapsed time formula:  $t_2$  -  $t_1$  =  $\tau$  ln[( $X_1$  -  $x(\infty)$ )/( $X_2$  -  $x(\infty)$ )]

## Potentially Useful Formulas (3<sup>rd</sup> midterm)

 $First \ order \ circuit: \ x(t) = x(\infty) + \left[ x(t_{_{o}}^{^{+}}) - x(\infty) \right] e^{-\left(t - t_{_{o}}^{^{+}}\right)/\tau}, \ \tau = L/R \ \ or \ \ \tau = RC$ 

Series RLC: 
$$s^2 + \frac{R}{L}s + \frac{1}{LC} = 0$$

Parallel RLC: 
$$s^2 + \frac{1}{RC}s + \frac{1}{LC} = 0$$

$$x(t) = x(\infty) + (A\cos\omega_d t + B\sin\omega_d t)e^{-\sigma t}$$

$$x(t) = x(\infty) + (A + Bt)e^{-\sigma t}$$

$$x(t) = x(\infty) + \left(Ae^{s_1t} + Be^{s_2t}\right)$$

$$s_1, s_2 = \frac{-b \pm \sqrt{b^2 - 4c}}{2}$$
 for  $s^2 + bs + c = 0$ , where  $c = (LC)^{-1}$ 

$$\sigma = \frac{b}{2} = \begin{cases} R/2L & \text{(series)} \\ \frac{1}{2RC} & \text{(parallel)} \end{cases}$$

$$\omega_{o} = \sqrt[4]{\text{LC}}$$

$$s_{1,2} = -\sigma \pm \sqrt{\sigma^2 - \omega_o^2}$$

$$\omega_d = \frac{\sqrt{4c - b^2}}{2} = \sqrt{\omega_o^2 - \sigma^2}$$

#### Potentially Useful Formulas (since Exam 3)

$$P_{ave} = \frac{1}{T} \int_{0}^{T} p(t)dt = \frac{V_{m}I_{m}}{2} \cos(\theta_{V} - \theta_{I}) = V_{eff}I_{eff} \cos(\theta_{V} - \theta_{I}) = V_{rms}I_{rms} \cos(\theta_{V} - \theta_{I})$$

$$\mathbf{S} = \frac{1}{2} \mathbf{V}_m \mathbf{I}_m^* = \mathbf{V}_{eff} \mathbf{I}_{eff}^* = \mathbf{V}_{rms} \mathbf{I}_{rms}^* = P + jQ \text{ VA}$$

$$pf = \frac{P}{|\mathbf{S}|} = \frac{P}{\sqrt{P^2 + Q^2}} = \cos(\theta_V - \theta_I)$$
,  $pfa = (\theta_V - \theta_I)$ 

$$\cos \alpha \cos \beta = \frac{1}{2} \cos (\alpha - \beta) + \frac{1}{2} \cos (\alpha + \beta)$$

Item		Α		В		С		D		Е		F		G		Н	1
1.											Χ	10.00					
2.			X	10.00													
3.															Χ	10.00	
4.							X	10.00									
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