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CNC - Formal Languages
Homework 5

9. Construct a grammar over $\{a, b, c\}$ whose language is $\{a^n b^m c^i \mid 0 \leq n + m \leq i\}$.

$S \rightarrow aSc \mid A \mid \lambda$
 $A \rightarrow bAc \mid B$
 $B \rightarrow cC \mid \lambda$

11. Construct a grammar over $\{a, b\}$ whose language is $\{a^m b^n a^i \mid i = m + n\}$.

$S \rightarrow LS \mid LSR \mid SR \mid \lambda$
 $L \rightarrow ab \mid aLb$
 $R \rightarrow ba \mid bRa$

Find a CFG over $\{a,b\}$ that generates the language consisting of strings that have twice as many a's as b's and prove your grammar correct.

$S \rightarrow Bbaa \mid bBaa \mid baBa \mid baaB \mid Baba \mid aBba \mid abBa \mid abaB \mid Baab \mid aBab \mid aaBb \mid aabB$
 $B \rightarrow S \mid \lambda$