

**CSF**  
**Hwk04**  
**For ever...**

**1.** Write method `sumTo()` that takes an integer and returns an integer. It should return the sum of all the integers between 1 and the number given.

Ex: `sumTo(1) ==> 1`, `sumTo(4) ==> 10`, `sumTo(10) ==> 55`, `sumTo(0) ==> 0`

**2.** Write a method `sumOfSums()` that takes an integer and returns an integer. It should return the sum of all the "sumTo's" of the integers between 1 and the number given. Use your `sumTo()` method to help.

Ex: `sumOfSums(1) ==> 1`, `sumTo(4) ==> 20`, `sumTo(7) ==> 84`, `sumTo(10) ==> 220`,  
`sumTo(0) ==> 0`

**3.** Write a method `sumOfEvenBetween()` that takes two integers and returns an integer. It should return the sum of all the integers between the first number and the second number that are even.

**Note:** Either number can be the largest.

Ex: `sumOfEvenBetween(2,5) ==> 6`, `sumOfEvenBetween(5,2) ==> 6`  
`sumOfEvenBetween(1,10) ==> 30`, `sumOfEvenBetween(5,5) ==> 0`

**4.** Write a method `sumPropDivisors()` that takes an integer (x) and returns an integer. It should return the sum of all the positive integers less than x that divide evenly into x.

Ex: `sumPropDivisors(0) ==> 0`, `sumPropDivisors(1) ==> 0`, `sumPropDivisors(6) ==> 6`,  
`sumPropDivisors(10) ==> 8`, `sumPropDivisors(13) ==> 1`

**5.** Write a method `isPerfect()` that takes an integer (greater than 0) and returns a boolean. It should return true if the number equals the sum of its proper divisors. Such a number is called a "perfect number". Use `sumPropDivisors()` as a helper method.

Ex: `isPerfect(1) ==> false`, `isPerfect(4) ==> false`, `isPerfect(6) ==> true`  
`isPerfect(10) ==> false`, `isPerfect(28) ==> true`, `isPerfect(496) ==> true`

**6.** Write a java method called `isPrime()` that takes an integer and returns a boolean. It should return true if the number is prime, and false otherwise. Note that one way to determine if a number is prime is to see if the sum of its proper divisors is 1. Use `sumPropDivisors()` as a helper method. Remember, 1 is not a prime and therefore it is again an exception.

Ex: `isPrime(1) ==> false`, `isPrime(2) ==> true`, `isPrime(5) ==> true`, `isPrime(9) ==> false`  
`isPrime(93) ==> false`, `isPrime(101) ==> true`

**7. EC)** Write a method that given integer *n*, will find the *n*th perfect number. Use it to find the 4<sup>th</sup> perfect number. The first 3 are 6, 28, and 496. Email me your code and the answer.

**8. EC)** Write a method that determines if two numbers are amicable. Two numbers x and y are amicable if they are not the same number and the sum of the proper divisors of x equals y and vice versa. Use your method to determine the first two amicable numbers. Email me your code.