

STUDY GUIDE

COMBINATIONS AND PERMUTATIONS

Key Terms & Definitions

- » **Counting Principle/Fundamental Theorem of Counting:** Formally states that if a job consists of k separate tasks and there are n_1 ways of doing the first task, n_2 ways of doing the second task, and so on, then there are $n_1 \times n_2 \times \dots \times n_k$ ways of completing the entire job.
- » **Factorial:** Denoted by an exclamation point!, this is the number of ways to list a set of n objects. It is found by multiplying a number by every number between itself and 1, such that $n! = n \times (n-1) \times \dots \times 2 \times 1$.
- » **Permutation:** An arrangement of objects without repetition in which order matters.
 - Formula: $P(n, k) = \frac{n!}{(n-k)!}$, where n is the number of possible options and k is the number of options we want to choose.
- » **Combination:** An arrangement of objects without repetition in which order *does not* matter and therefore all possible cases must be taken into account.
 - Formula: $C(n, k) = \frac{n!}{k!(n-k)!}$, where n is the number of possible options and k is the number of options we want to choose.

Guiding Questions

- 1) Name a few situations in which order would matter — and a few in which it wouldn't — in choosing sets of objects or outcomes.
- 2) Why is it more complicated to calculate arrangements in which order does not matter?
- 3) Why do we need combinations and permutations to calculate probability? Why can't we just take the ratio of that type of event/object on its own?

Additional Resources

1. [Easy Permutations and Combinations](#)

- » A straightforward, simple explanation of the differences between permutations and combinations.

2. [Combinations and Permutations](#)

- » Another simple explanation of the difference with more mathematical emphasis.

3. [Khan Academy](#)

- » Khan Academy's unit on probability using combinations and permutations.