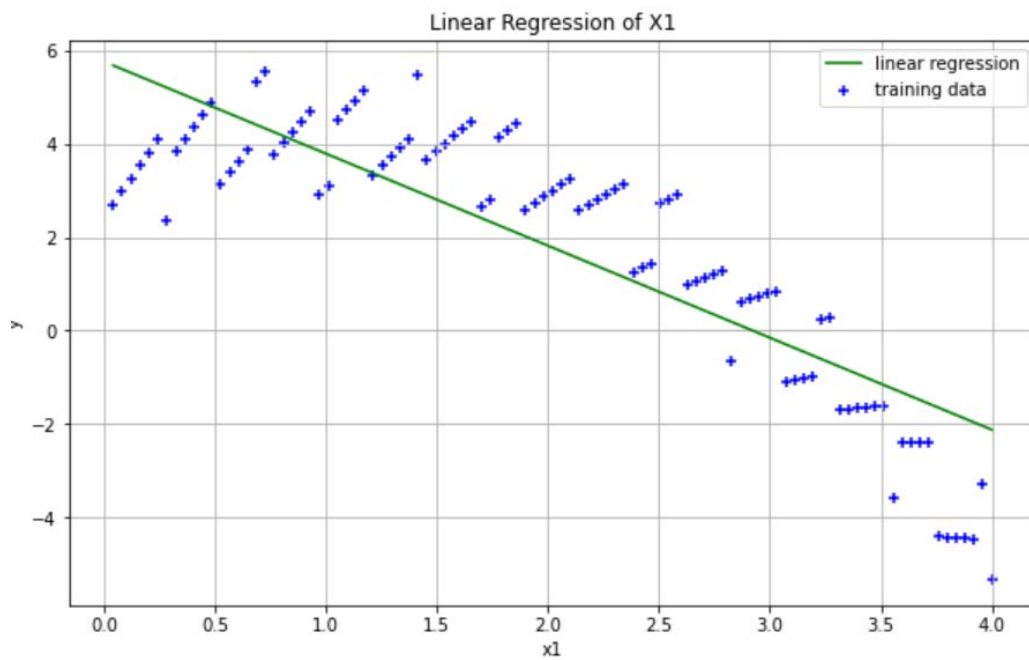


Homework 0 Report

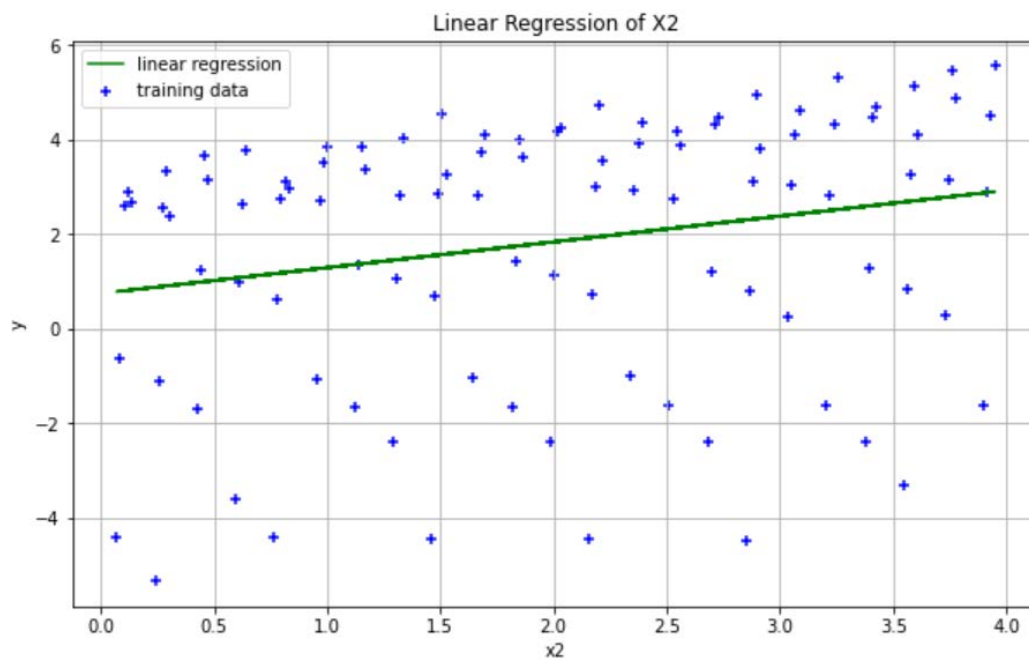
Problem 1

1.

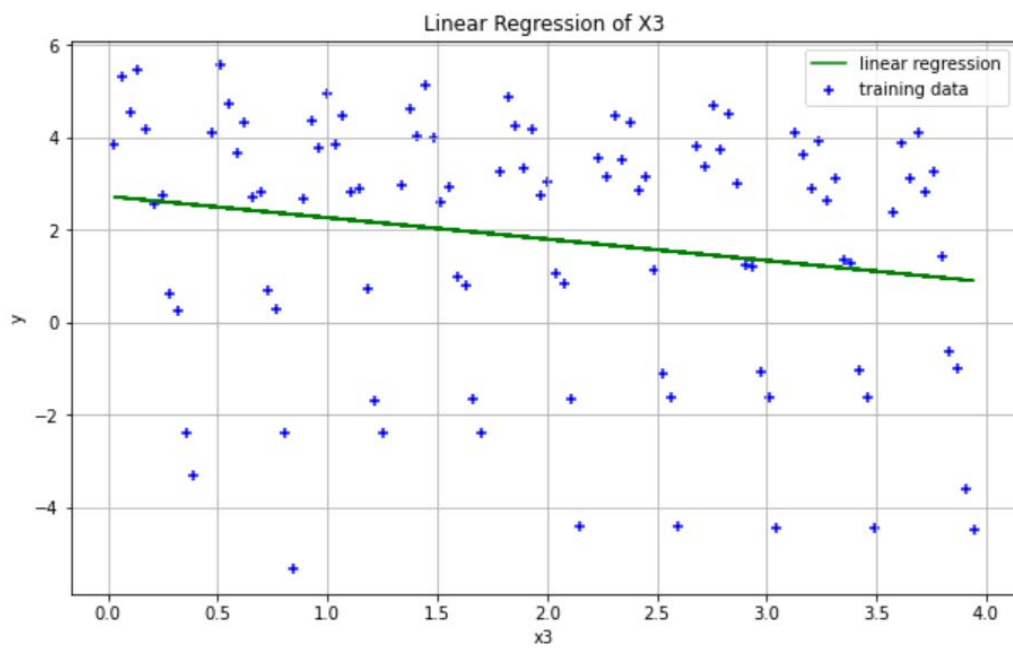
X1:



X2:

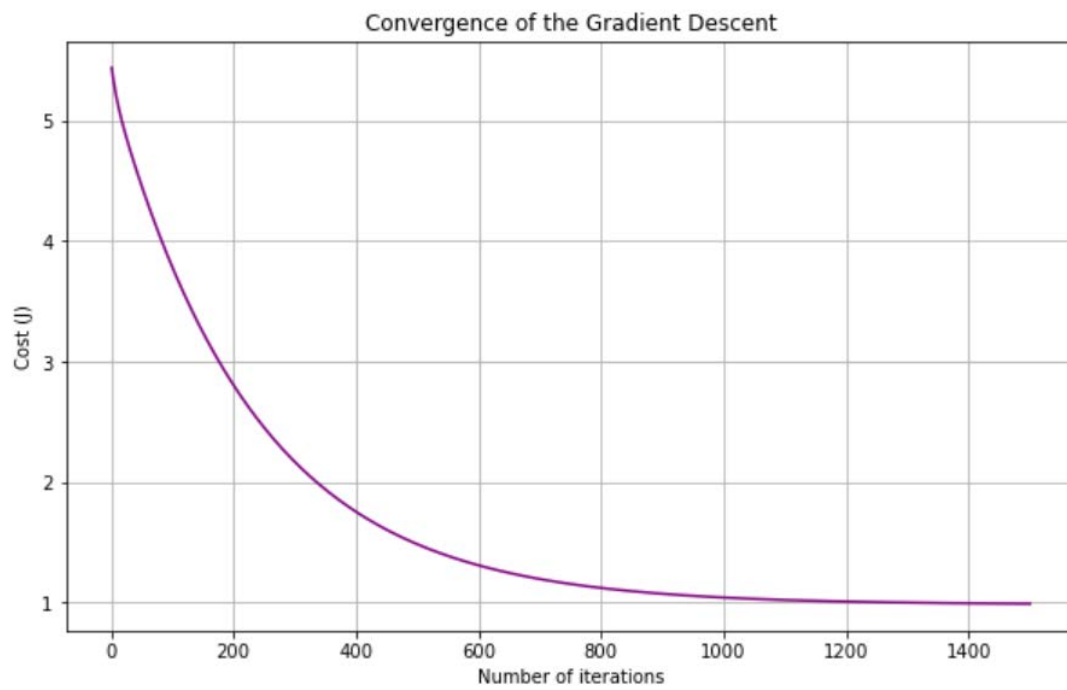


X3:

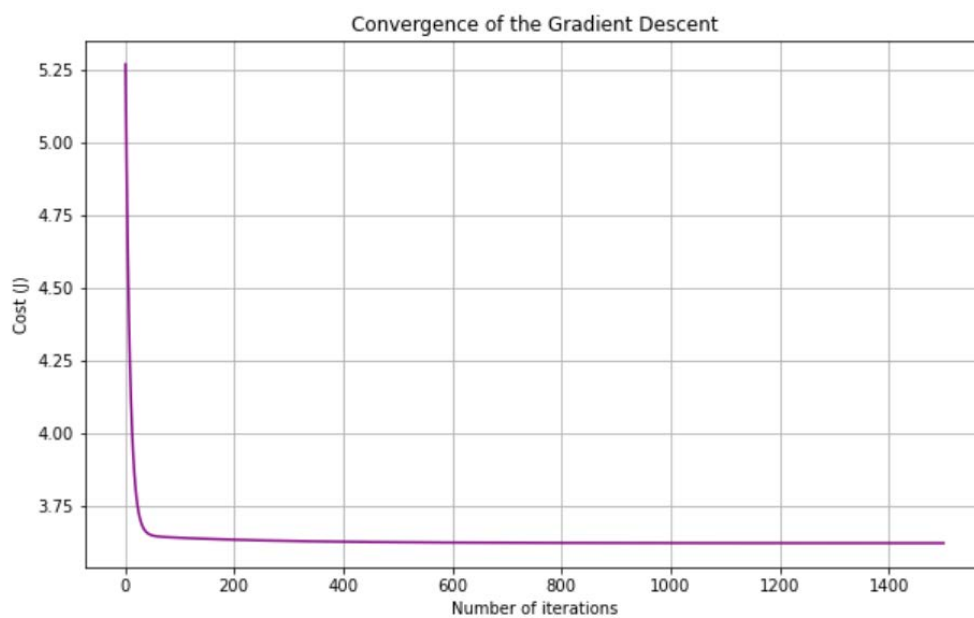


2.

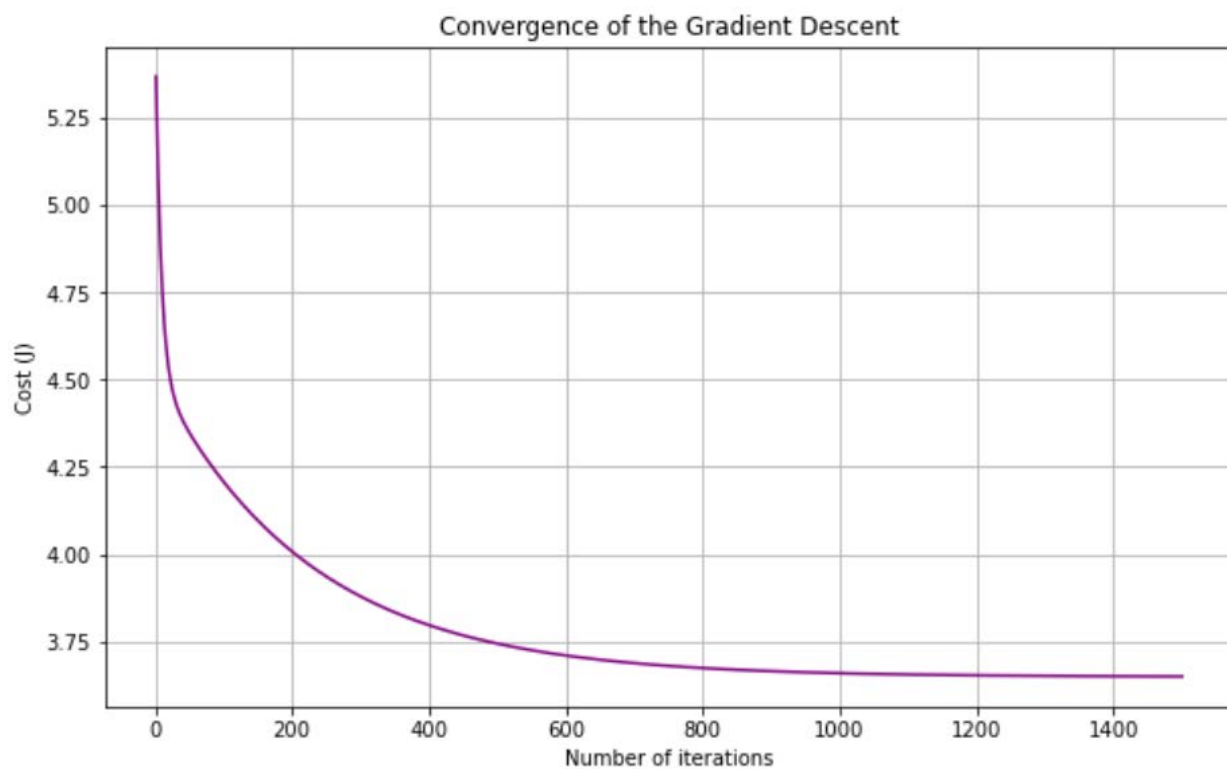
X1:



X2:



X3:



- Variable x2 has the lowest loss cost for explaining the output y as it regresses the quickest. It can be seen from the convergence graphs that variable x2 has the steepest drop.

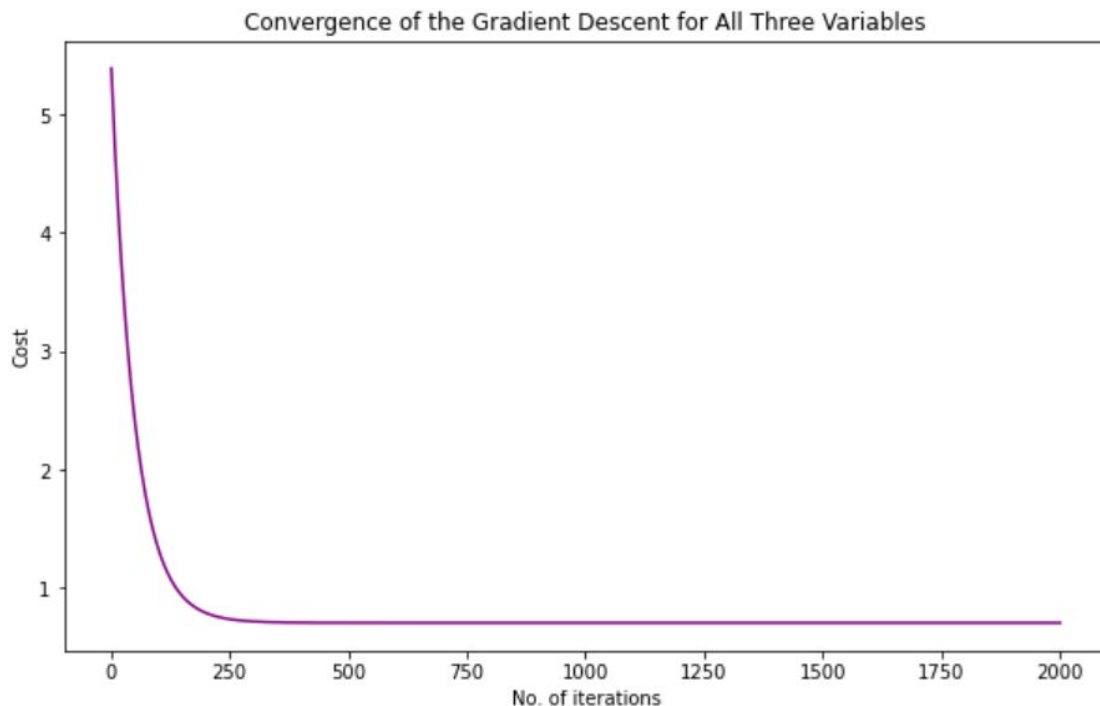
- For x_1 when the learning rate, α , was set to 0.01 the values of θ were 5.75752967 for θ_0 and -1.97114532 for θ_1 . When α was increased to 0.015, θ_0 increased to 5.94478172 and θ_1 decreased to -2.04390178. When α was increased again to 0.1, θ_0 increased to 5.99114009 and θ_1 decreased to -2.06191424. Therefore, as the learning rate is increased the value of θ_0 increases while θ_1 decreases.

For x_2 when α was set to 0.01, θ_0 was 0.7392744 and θ_1 was 0.5453018. After α was increased to 0.015, θ_0 was increased to 0.75281115 and θ_1 decreased 0.54000281. When α was increased again to 0.1, θ_0 was increased to 0.75592882 and θ_1 was decreased to 0.53878239. So therefore, as α is increased, θ_0 will increase and θ_1 will decrease.

For x_3 when α was set to 0.01, θ_0 was 2.71943299 and θ_1 was -0.46300206. After α was increased to 0.015, θ_0 was increased to 2.79572447 and θ_1 was decreased to -0.49308308. After α was increased again to 0.1, θ_0 was increased to 2.81356727 and θ_1 was decreased to -0.50011833. So therefore, as α increases, θ_0 will increase and θ_1 will decrease.

Problem 2

- The linear model for X_2 is the best because it regresses the quickest to the lowest cost.
-



- For α equals 0.01, $\theta = [1.82565676 \ -2.3578133 \ 0.65275329 \ -0.33677367]$. When α was increased to 0.015, $\theta = [1.82565677 \ -2.35781332 \ 0.65275329 \ -0.33677366]$. Then when α was increased again to 0.1, $\theta = [1.82565677$

-2.35781332 0.65275329 -0.33677366]. The number of iterations does not change as it is a set value, and the value of theta doesn't seem to change much with the change of learn rate.

4. For $(X_1, X_2, X_3) = (1, 1, 1)$, the value of Y could be estimated to be 11.96021843. As,
 $Y = 1 * 1.82565676^3 + 1 * -2.3578133^2 + 1 * 0.65275329 - 0.33677367$.

For $(X_1, X_2, X_3) = (2, 0, 4)$, the value of Y could be estimated to be 14.44414999. As,
 $Y = 2 * 1.82565676^3 + 0 * -2.3578133^2 + 4 * 0.65275329 - 0.33677367$

For $(X_1, X_2, X_3) = (3, 2, 1)$, the value of Y could be estimated to be 29.68941249. As,
 $Y = 3 * 1.82565676^3 + 2 * -2.3578133^2 + 1 * 0.65275329 - 0.33677367$

GitHub: <https://github.com/willwoodard16/Intro-to-MI-4105>