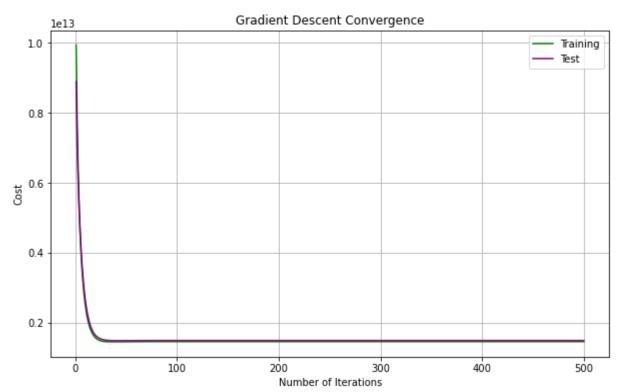
```
In [1]:
         import numpy as np
          import pandas as pd
          import matplotlib.pyplot as plt
          import seaborn as sns
In [2]:
         housing = pd.DataFrame(pd.read csv("Housing.csv"))
         housing.head()
Out[2]:
               price
                          bedrooms
                                    bathrooms stories mainroad guestroom basement hotwaterheating
           13300000
                     7420
                                  4
                                             2
                                                    3
                                                            yes
                                                                        no
                                                                                  no
                                                                                                  no
           12250000
                     8960
                                  4
                                                            yes
                                                                        no
                                                                                  no
                                                                                                 no
           12250000
                     9960
                                  3
                                             2
                                                    2
                                                            yes
                                                                        no
                                                                                 yes
                                                                                                 no
                                             2
           12215000
                     7500
                                  4
                                                    2
                                                            yes
                                                                        no
                                                                                 yes
                                                                                                  no
           11410000 7420
                                             1
                                  4
                                                    2
                                                            yes
                                                                       ves
                                                                                 yes
                                                                                                 no
In [3]:
         m = len(housing)
        545
Out[3]:
In [4]:
         housing.shape
        (545, 13)
Out[4]:
In [5]:
         housing.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 545 entries, 0 to 544
        Data columns (total 13 columns):
          #
              Column
                                Non-Null Count
                                                 Dtype
                                 _____
          0
              price
                                 545 non-null
                                                  int64
          1
              area
                                 545 non-null
                                                  int64
          2
                                 545 non-null
                                                  int64
              bedrooms
          3
              bathrooms
                                 545 non-null
                                                  int64
          4
              stories
                                 545 non-null
                                                  int64
          5
              mainroad
                                 545 non-null
                                                 object
          6
                                 545 non-null
                                                 object
              guestroom
          7
                                 545 non-null
              basement
                                                 object
          8
              hotwaterheating
                                 545 non-null
                                                 object
          9
              airconditioning
                                 545 non-null
                                                 object
          10
                                 545 non-null
                                                  int64
              parking
                                 545 non-null
          11
              prefarea
                                                  object
          12 furnishingstatus 545 non-null
                                                  object
        dtypes: int64(6), object(7)
        memory usage: 55.5+ KB
In [6]:
         housing.describe()
```

```
bathrooms
 Out[6]:
                         price
                                      area
                                            bedrooms
                                                                      stories
                                                                                 parking
          count 5.450000e+02
                                 545.000000
                                            545.000000
                                                       545.000000
                                                                  545.000000
                                                                              545.000000
           mean 4.766729e+06
                                5150.541284
                                              2.965138
                                                         1.286239
                                                                     1.805505
                                                                                0.693578
                1.870440e+06
                                2170.141023
                                              0.738064
                                                         0.502470
                                                                     0.867492
                                                                                0.861586
            std
            min
                 1.750000e+06
                                1650.000000
                                              1.000000
                                                         1.000000
                                                                     1.000000
                                                                                0.000000
            25%
                 3.430000e+06
                                3600.000000
                                              2.000000
                                                         1.000000
                                                                     1.000000
                                                                                0.000000
            50%
                4.340000e+06
                                4600.000000
                                              3.000000
                                                         1.000000
                                                                     2.000000
                                                                                0.000000
            75%
                 5.740000e+06
                                6360.000000
                                              3.000000
                                                         2.000000
                                                                     2.000000
                                                                                1.000000
            max 1.330000e+07
                              16200.000000
                                              6.000000
                                                         4.000000
                                                                     4.000000
                                                                                3.000000
 In [7]:
           varlist = ['mainroad', 'guestroom', 'basement', 'hotwaterheating', 'airconditioning',
           def binary map(x):
               return x.map({'yes' : 1, "no" : 0})
           housing[varlist] = housing[varlist].apply(binary map)
           housing.head()
 Out[7]:
                 price
                             bedrooms
                                       bathrooms stories mainroad guestroom basement hotwaterheating
                       area
                                                                                        0
          0 13300000 7420
                                     4
                                                2
                                                        3
                                                                  1
                                                                             0
                                                                                                        0
             12250000
                      8960
                                     4
                                                4
                                                                             0
                                                                                        0
                                                        4
                                                                  1
                                                                                                        0
             12250000 9960
                                     3
                                                2
                                                        2
                                                                             0
                                                                                                        0
                                                                  1
                                                2
             12215000 7500
                                     4
                                                        2
                                                                  1
                                                                             0
                                                                                                        0
             11410000 7420
                                     4
                                                1
                                                        2
                                                                                                        0
                                                                  1
                                                                             1
 In [8]:
           from sklearn.model_selection import train_test_split
           np.random.seed(0)
           df train, df test = train test split(housing, train size = 0.7, test size = 0.3, random
           df train.shape
 Out[8]: (381, 13)
 In [9]:
           df test.shape
 Out[9]: (164, 13)
In [10]:
           num_vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking', 'price']
           df_Newtrain = df_train[num_vars]
           df_Newtest = df_test[num_vars]
           df Newtrain.head()
Out[10]:
                area bedrooms bathrooms stories parking
                                                              price
```

```
area
                    bedrooms bathrooms stories parking
                                                           price
          454 4500
                            3
                                       1
                                              2
                                                        3143000
          392 3990
                            3
                                       1
                                              2
                                                         3500000
                                                      0
          231 4320
                            3
                                       1
                                              1
                                                         4690000
          271 1905
                            5
                                       1
                                              2
                                                        4340000
          250 3510
                            3
                                       1
                                              3
                                                      0 4515000
In [11]:
           df Newtest.head()
                     bedrooms bathrooms stories parking
Out[11]:
                area
                                                             price
          239
                4000
                             3
                                        1
                                               2
                                                       1 4585000
          113
                9620
                             3
                                        1
                                                          6083000
                                               1
          325
                3460
                             4
                                        1
                                               2
                                                          4007500
                             2
                                        1
           66
              13200
                                               1
                                                          6930000
          479
                3660
                             4
                                        1
                                               2
                                                          2940000
In [12]:
           def hypothesis(theta, X, n):
               h = np.ones((X.shape[0],1))
               theta = theta.reshape(1,n+1)
               for i in range(0, X.shape[0]):
                   h[i] = float(np.matmul(theta, X[i]))
               h = h.reshape(X.shape[0])
               return h
In [13]:
          def GD(theta, alpha, num_iter, h, X, y, n):
               cost = np.ones(num iter)
               for i in range(0,num_iter):
                   theta[0] = theta[0] - (alpha/X.shape[0]) * sum(h - y)
                   for j in range(1,n+1):
                       theta[j] = theta[j] - (alpha/X.shape[0]) * sum((h-y) * X.transpose()[j])
                   h = hypothesis(theta, X, n)
                   cost[i] = (1/X.shape[0]) * 0.5 * sum(np.square(h - y))
               theta = theta.reshape(1,n+1)
               return theta, cost
In [14]:
          def linear_regression(X, y, alpha, num_iter):
               n = X.shape[1]
               column = np.ones((X.shape[0],1))
               X = np.concatenate((column, X), axis = 1)
               theta = np.zeros(n+1)
               h = hypothesis(theta, X, n)
               theta, cost = GD(theta,alpha,num iter,h,X,y,n)
               return theta, cost
In [15]:
          X_t = df_Newtrain.values[:,[0,1,2,3,4]]
```

```
HW1
          Y t = df Newtrain.values[:,5]
          X v = df Newtest.values[:,[0,1,2,3,4]]
          Y v = df Newtest.values[:,5]
In [16]:
          mean = np.ones(X_t.shape[1])
          std = np.ones(X_t.shape[1])
          for i in range(0, X t.shape[1]):
              mean[i] = np.mean(X_t.transpose()[i])
              std[i] = np.std(X_t.transpose()[i])
              for j in range(0, X_t.shape[0]):
                   X t[j][i] = (X t[j][i] - mean[i])/std[i]
          mean = np.ones(X_v.shape[1])
          std = np.ones(X v.shape[1])
          for i in range(0, X_v.shape[1]):
              mean[i] = np.mean(X_v.transpose()[i])
              std[i] = np.std(X_v.transpose()[i])
              for j in range(0, X_v.shape[0]):
                   X \vee [j][i] = (X \vee [j][i] - mean[i])/std[i]
In [17]:
          df Newtrain.shape
Out[17]: (381, 6)
In [90]:
          theta, cost = linear_regression(X_t, Y_t, 0.1, 500)
          cost = list(cost)
          theta2, cost2 = linear regression(X v, Y v, 0.1, 500)
          cost2 = list(cost2)
          n iterations = [x \text{ for } x \text{ in } range(1,501)]
          n_iterations2 = [x for x in range(1,501)]
          plt.plot(n_iterations, cost, color = 'green', label = 'Training')
          plt.plot(n iterations2, cost2, color = 'purple', label = 'Test')
          plt.legend()
          plt.rcParams["figure.figsize"] = (10,6)
          plt.grid()
          plt.xlabel('Number of Iterations')
          plt.ylabel('Cost')
          plt.title('Gradient Descent Convergence')
Out[90]: Text(0.5, 1.0, 'Gradient Descent Convergence')
```



```
In [19]:
    num_vars = ['area', 'bedrooms', 'bathrooms', 'mainroad', 'guestroom', 'basement', 'hotw
    df_Newtrain = df_train[num_vars]
    df_Newtest = df_test[num_vars]
    df_Newtrain.head()
```

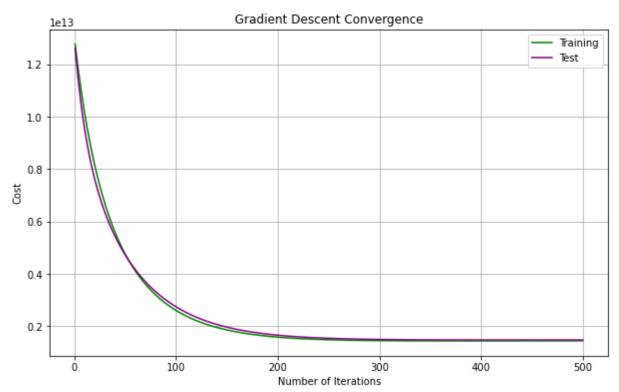
Out[19]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditioning	
	454	4500	3	1	1	0	0	0	1	
	392	3990	3	1	1	0	0	0	0	
	231	4320	3	1	1	0	0	0	0	
	271	1905	5	1	0	0	1	0	0	
	250	3510	3	1	1	0	0	0	0	

In [20]: df_Newtest.head()

Out[20]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditioning
	239	4000	3	1	1	0	0	0	0
	113	9620	3	1	1	0	1	0	0
	325	3460	4	1	1	0	0	0	1
	66	13200	2	1	1	0	1	1	0
	479	3660	4	1	0	0	0	0	0

```
X v = df Newtest.values[:,0:10]
In [21]:
           Y v = df Newtest.values[:,10]
In [22]:
          mean = np.ones(X_t.shape[1])
          std = np.ones(X_t.shape[1])
          for i in range(0, X_t.shape[1]):
               mean[i] = np.mean(X t.transpose()[i])
               std[i] = np.std(X_t.transpose()[i])
               for j in range(0, X_t.shape[0]):
                   X_t[j][i] = (X_t[j][i] - mean[i])/std[i]
          mean = np.ones(X v.shape[1])
           std = np.ones(X_v.shape[1])
          for i in range(0, X_v.shape[1]):
               mean[i] = np.mean(X_v.transpose()[i])
               std[i] = np.std(X_v.transpose()[i])
               for j in range(0, X_v.shape[0]):
                   X_v[j][i] = (X_v[j][i] - mean[i])/std[i]
In [92]:
          theta, cost = linear_regression(X_t, Y_t, 0.01, 500)
           cost = list(cost)
          theta2, cost2 = linear_regression(X_v, Y_v, 0.01, 500)
           cost2 = list(cost2)
          n_{iterations} = [x \text{ for } x \text{ in } range(1,501)]
          n iterations2 = [x \text{ for } x \text{ in } range(1,501)]
           plt.plot(n_iterations, cost, color = 'green', label = 'Training')
          plt.plot(n iterations2, cost2, color = 'purple', label = 'Test')
          plt.legend()
          plt.rcParams["figure.figsize"] = (10,6)
           plt.grid()
          plt.xlabel('Number of Iterations')
          plt.ylabel('Cost')
          plt.title('Gradient Descent Convergence')
```

Out[92]: Text(0.5, 1.0, 'Gradient Descent Convergence')



```
In [26]:
    num_vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking','price']
    df_Newtrain = df_train[num_vars]
    df_Newtest = df_test[num_vars]
    df_Normal = df_Newtrain
    df_Standard = df_Newtrain
    df_Newtrain.head()
```

```
Out[26]:
               area
                     bedrooms bathrooms stories parking
                                                             price
          454 4500
                             3
                                               2
                                                        0 3143000
                             3
                                               2
          392 3990
                                                        0 3500000
                             3
                                               1
          231 4320
                                                        0 4690000
                             5
                                               2
                                                        0 4340000
          271 1905
                                        1
          250 3510
                             3
                                        1
                                               3
                                                        0 4515000
```

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
```

```
scaler = MinMaxScaler()
df_Normal[num_vars] = scaler.fit_transform(df_Normal[num_vars])
df_Normal.head(20)
```

```
Out[27]:
                  area
                       bedrooms bathrooms
                                              stories
                                                     parking
                                                                 price
          454 0.193548
                             0.50
                                        0.0
                                            0.333333
                                                     0.000000
                                                             0.120606
          392 0.156495
                             0.50
                                        0.0
                                            0.333333  0.000000  0.151515
          231 0.180471
                             0.50
                                        0.0
                                            0.000000
                                                     0.000000
                                                            0.254545
          271 0.005013
                             1.00
                                        0.0
                                            0.333333  0.000000  0.224242
          250 0.121622
                             0.50
                                        0.0
                                            0.666667
                                                     0.000000 0.239394
          541 0.040976
                             0.50
                                        0.0
                                            0.000000
                                                    0.000000 0.001485
          461 0.226969
                             0.25
                                            0.000000 0.000000 0.115152
                                        0.0
          124 0.340671
                             0.50
                                            1.000000 0.333333 0.363636
                                        0.5
          154 0.131793
                             0.50
                                            0.5
          451 0.357018
                             0.25
                                        0.0
                                            0.000000 0.000000 0.121212
             0.302528
                             0.50
                                        0.5
                                            1.000000 0.333333 0.472727
                                            0.000000
          493 0.154316
                             0.50
                                        0.0
                                                     0.000000 0.090909
                             0.25
                                            0.000000 0.000000
          465 0.142691
                                        0.0
                                                             0.112121
                             0.50
                                            490 0.182650
                                        0.0
          540 0.084568
                             0.25
                                            0.000000 0.666667
                                        0.0
                                                             0.006061
          406 0.253124
                             0.25
                                        0.0
                                            0.000000 0.333333 0.148485
          289
             0.291630
                             0.25
                                        0.0
                                            0.000000 0.666667 0.212121
          190 0.418774
                             0.75
                                        0.0
                                            0.302528
                             0.50
                                        0.0
                                            171 0.612685
                             0.50
                                            0.000000 0.333333 0.303030
                                        0.0
In [28]:
           import warnings
          warnings.filterwarnings('ignore')
```

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
scaler = StandardScaler()
df_Standard[num_vars] = scaler.fit_transform(df_Standard[num_vars])
df_Standard.head(20)
```

[28]:		area	bedrooms	bathrooms	stories	parking	price
	454	-0.286366	0.073764	-0.581230	0.207401	-0.822960	-0.868394
	392	-0.544762	0.073764	-0.581230	0.207401	-0.822960	-0.677628
	231	-0.377564	0.073764	-0.581230	-0.937813	-0.822960	-0.041744
	271	-1.601145	2.884176	-0.581230	0.207401	-0.822960	-0.228768
	250	-0.787958	0.073764	-0.581230	1.352614	-0.822960	-0.135256

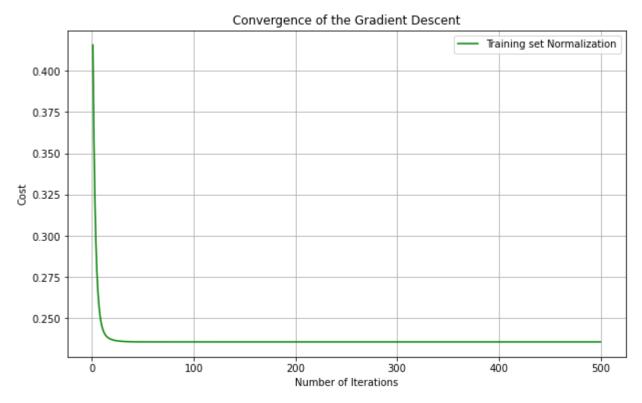
Out[

```
area bedrooms bathrooms
                                                   stories
                                                            parking
                                                                         price
           541 -1.350349
                           0.073764
                                      -0.581230
                                                -0.937813
                                                           -0.822960
                                                                     -1.603589
           461
               -0.053303
                           -1.331442
                                      -0.581230
                                                -0.937813
                                                           -0.822960
                                                                     -0.902058
           124
                0.739618
                           0.073764
                                       1.488383
                                                 2.497828
                                                           0.321375
                                                                      0.631546
           154
               -0.717026
                           0.073764
                                       1.488383
                                                 0.207401
                                                           1.465710
                                                                      0.407116
           451
                0.853616
                           -1.331442
                                      -0.581230
                                                 -0.937813
                                                           -0.822960
                                                                     -0.864653
            59
                0.473622
                           0.073764
                                       1.488383
                                                 2.497828
                                                           0.321375
                                                                      1.304836
           493
               -0.559962
                           0.073764
                                      -0.581230
                                                -0.937813
                                                           -0.822960
                                                                     -1.051678
           465
               -0.641027
                           -1.331442
                                      -0.581230
                                                -0.937813
                                                           -0.822960
                                                                     -0.920761
           490
               -0.362365
                           0.073764
                                      -0.581230
                                                 0.207401
                                                           0.321375 -1.032976
           540
               -1.046354
                           -1.331442
                                      -0.581230
                                                -0.937813
                                                           1.465710 -1.575348
           406
                0.129094
                           -1.331442
                                      -0.581230 -0.937813
                                                           0.321375 -0.696331
           289
                0.397623
                           -1.331442
                                      -0.581230
                                                -0.937813
                                                           1.465710 -0.303578
           190
                1.284276
                           1.478970
                                      -0.581230
                                                 0.207401
                                                           1.465710
                                                                     0.145281
           55
                0.473622
                           0.073764
                                      -0.581230
                                                 0.207401
                                                           0.321375
                                                                      1.379646
           171
                2.636548
                           0.073764
                                      -0.581230 -0.937813
                                                           0.321375
                                                                      0.257496
In [29]:
           Xn = df Normal.values[:,[0,1,2,3,4]]
           Yn = df Normal.values[:,5]
           Xtest = df_Newtest.values[:,[0,1,2,3,4]]
           Ytest = df_Newtest.values[:,5]
           Xs = df_Standard.values[:,[0,1,2,3,4]]
           Ys = df Standard.values[:,5]
In [30]:
           mean = np.ones(Xn.shape[1])
           std = np.ones(Xn.shape[1])
           for i in range(0, Xn.shape[1]):
                mean[i] = np.mean(Xn.transpose()[i])
                std[i] = np.std(Xn.transpose()[i])
                for j in range(0, Xn.shape[0]):
                    Xn[j][i] = (Xn[j][i] - mean[i])/std[i]
In [31]:
           mean = np.ones(Xs.shape[1])
           std = np.ones(Xs.shape[1])
           for i in range(0, Xs.shape[1]):
                mean[i] = np.mean(Xs.transpose()[i])
                std[i] = np.std(Xs.transpose()[i])
                for j in range(0, Xs.shape[0]):
                    Xs[j][i] = (Xs[j][i] - mean[i])/std[i]
In [32]:
           mean = np.ones(Xtest.shape[1])
           std = np.ones(Xtest.shape[1])
           for i in range(0, Xtest.shape[1]):
```

```
mean[i] = np.mean(Xtest.transpose()[i])
              std[i] = np.std(Xtest.transpose()[i])
              for j in range(0, Xtest.shape[0]):
                  Xtest[j][i] = (Xtest[j][i] - mean[i])/std[i]
In [33]:
          def compute_cost(X, n, theta):
              h = np.ones((X.shape[0],1))
              theta = theta.reshape(1,n+1)
              for i in range(0, X.shape[0]):
                  h[i] = float(np.matmul(theta, X[i]))
              h = h.reshape(X.shape[0])
              return h
In [34]:
          def gradient descent(X, Y, theta, alpha, iterations, n, h):
              cost = np.ones(iterations)
              for i in range(0,iterations):
                  theta[0] = theta[0] - (alpha/X.shape[0]) * sum(h - Y)
                  for j in range(1,n+1):
                      theta[j] = theta[j] - (alpha/X.shape[0]) * sum((h-Y) * X.transpose()[j])
                  h = compute_cost(X, n, theta)
                  cost[i] = (1/X.shape[0]) * 0.5 * sum(np.square(h - Y))
              theta = theta.reshape(1,n+1)
              return theta, cost
In [35]:
          def linear_regression(X, Y, alpha, iterations):
              n = X.shape[1]
              one_column = np.ones((X.shape[0],1))
              X = np.concatenate((one column, X), axis = 1)
              theta = np.zeros(n+1)
              h = compute cost(X, n, theta)
              theta, cost = gradient_descent(X, Y, theta, alpha, iterations, n, h)
              return theta, cost
In [36]:
          iterations = 500;
In [37]:
          theta, cost = linear_regression(Xn, Yn, 0.1, iterations)
          print('Final Theta Value with Normalization =', theta)
          cost = list(cost)
          n iterations = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Normalization = [[1.24535844e-16 3.83653304e-01 1.04343457e-01 2.
         98541735e-01
           2.34542828e-01 1.49757135e-01]]
In [38]:
          theta2, cost2 = linear regression(Xs, Ys, 0.1, iterations)
          print('Final Theta Value with Standardization =', theta2)
          cost2 = list(cost2)
          n_iterations2 = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Standardization = [[1.24535844e-16 3.83653304e-01 1.04343457e-01
         2.98541735e-01
           2.34542828e-01 1.49757135e-01]]
```

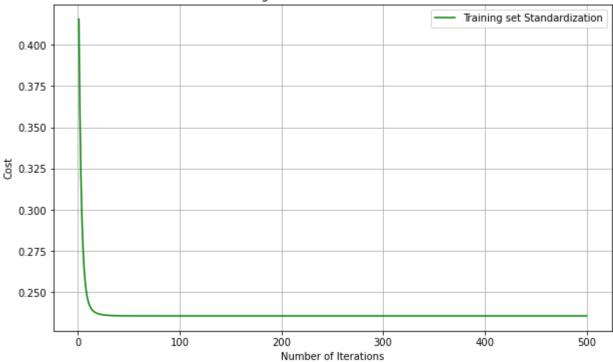
```
theta_t, cost_t = linear_regression(Xtest, Ytest, 0.1, iterations)
In [39]:
          print('Final Theta Value of the Test Set =', theta t)
          cost_t = list(cost_t)
          n_iterations_t = [x for x in range(1,(iterations + 1))]
         Final Theta Value of the Test Set = [[4009323.46427773 844638.61768703 225437.77741561
         911745.77297157
            885446.81234427 751101.29064712]]
In [40]:
          plt.plot(n_iterations, cost, color = 'green', label='Training set Normalization')
          plt.legend()
          plt.rcParams["figure.figsize"]=(10,6)
          plt.grid()
          plt.xlabel('Number of Iterations')
          plt.ylabel('Cost')
          plt.title('Convergence of the Gradient Descent')
```

Out[40]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')

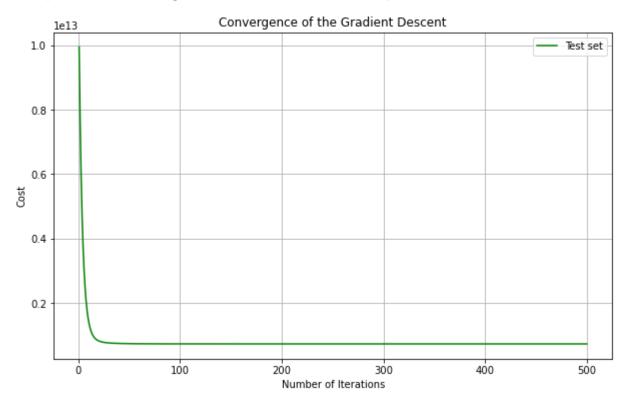


```
In [41]:
    plt.plot(n_iterations2, cost2, color = 'green', label='Training set Standardization')
    plt.legend()
    plt.rcParams["figure.figsize"]=(10,6)
    plt.grid()
    plt.xlabel('Number of Iterations')
    plt.ylabel('Cost')
    plt.title('Convergence of the Gradient Descent')
```

Out[41]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



Out[42]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



Out[43]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditioning
	454	4500	3	1	1	0	0	0	1
	392	3990	3	1	1	0	0	0	0
	231	4320	3	1	1	0	0	0	0
	271	1905	5	1	0	0	1	0	0
	250	3510	3	1	1	0	0	0	0

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
scaler = MinMaxScaler()
df_Normal[num_vars] = scaler.fit_transform(df_Normal[num_vars])
df_Normal.head(20)
```

Out[44]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditionin
	454	0.193548	0.50	0.0	1.0	0.0	0.0	0.0	1
	392	0.156495	0.50	0.0	1.0	0.0	0.0	0.0	0
	231	0.180471	0.50	0.0	1.0	0.0	0.0	0.0	0
	271	0.005013	1.00	0.0	0.0	0.0	1.0	0.0	0
	250	0.121622	0.50	0.0	1.0	0.0	0.0	0.0	0
	541	0.040976	0.50	0.0	0.0	0.0	0.0	0.0	0
	461	0.226969	0.25	0.0	1.0	0.0	1.0	0.0	1
	124	0.340671	0.50	0.5	1.0	0.0	0.0	0.0	0
	154	0.131793	0.50	0.5	1.0	0.0	0.0	0.0	0
	451	0.357018	0.25	0.0	1.0	0.0	0.0	0.0	0
	59	0.302528	0.50	0.5	1.0	1.0	0.0	0.0	1
	493	0.154316	0.50	0.0	1.0	0.0	0.0	0.0	0
	465	0.142691	0.25	0.0	1.0	0.0	0.0	0.0	0
	490	0.182650	0.50	0.0	0.0	0.0	0.0	1.0	0
	540	0.084568	0.25	0.0	1.0	0.0	1.0	0.0	0
	406	0.253124	0.25	0.0	1.0	0.0	0.0	0.0	0
	289	0.291630	0.25	0.0	1.0	1.0	1.0	0.0	0

	area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditionin
190	0.418774	0.75	0.0	1.0	0.0	0.0	0.0	1
55	0.302528	0.50	0.0	1.0	0.0	0.0	0.0	1
171	0.612685	0.50	0.0	1.0	0.0	0.0	0.0	0

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
scaler = StandardScaler()
df_Standard[num_vars] = scaler.fit_transform(df_Standard[num_vars])
df_Standard.head(20)
```

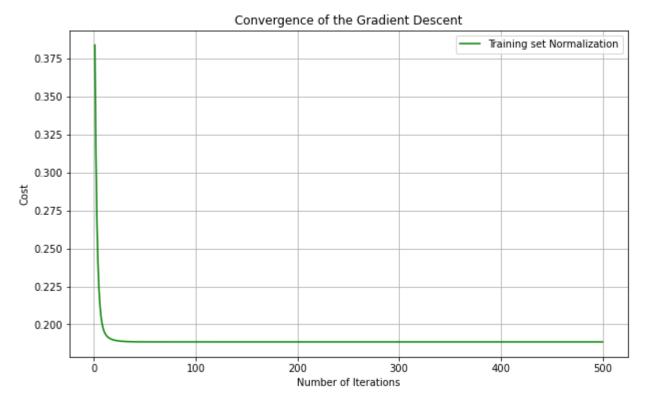
basement hotwaterheating airconditioni Out[45]: bedrooms bathrooms area mainroad guestroom -0.286366 454 0.073764 -0.581230 0.393123 -0.457738 -0.711287-0.216109 1.4226 -0.544762 -0.7029 392 0.073764 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 -0.377564 -0.581230 -0.711287 -0.7029 231 0.073764 0.393123 -0.457738 -0.216109 271 -1.601145 2.884176 -0.581230 -2.543735 -0.457738 1.405903 -0.216109 -0.7029 250 -0.787958 0.073764 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 -1.350349 0.073764 -0.581230 -2.543735 -0.457738 -0.711287 -0.216109 -0.7029541 461 -0.053303 -1.331442 -0.581230 0.393123 -0.457738 1.405903 -0.216109 1.4226 124 0.739618 0.073764 1.488383 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 154 -0.717026 0.073764 1.488383 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 451 0.853616 -1.331442 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 59 0.473622 0.073764 1.488383 0.393123 2.184657 -0.711287 -0.216109 1.4226 493 -0.559962 0.073764 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 -0.641027 -1.331442 -0.581230 0.393123 -0.457738 -0.711287 -0.7029465 -0.216109 490 -0.362365 0.073764 -0.581230 -2.543735 -0.457738 -0.711287 4.627285 -0.7029 -1.046354 540 -1.331442 -0.581230 0.393123 -0.457738 1.405903 -0.216109 -0.7029 406 0.129094 -1.331442 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 -0.7029 0.397623 -0.581230 0.393123 289 -1.331442 2.184657 1.405903 -0.216109 -0.7029190 1.284276 1.478970 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 1.4226 0.473622 55 0.073764 -0.581230 0.393123 -0.457738 -0.711287 -0.216109 1.4226 171 2.636548 0.073764 -0.581230 -0.457738 -0.711287 -0.7029 0.393123 -0.216109

```
Xtest = df Newtest.values[:,0:10]
          Ytest = df Newtest.values[:,10]
          Xs = df_Standard.values[:,0:10]
          Ys = df Standard.values[:,10]
In [47]:
          mean = np.ones(Xn.shape[1])
          std = np.ones(Xn.shape[1])
          for i in range(0, Xn.shape[1]):
              mean[i] = np.mean(Xn.transpose()[i])
              std[i] = np.std(Xn.transpose()[i])
              for j in range(0, Xn.shape[0]):
                  Xn[j][i] = (Xn[j][i] - mean[i])/std[i]
In [48]:
          mean = np.ones(Xs.shape[1])
          std = np.ones(Xs.shape[1])
          for i in range(0, Xs.shape[1]):
              mean[i] = np.mean(Xs.transpose()[i])
              std[i] = np.std(Xs.transpose()[i])
              for j in range(0, Xs.shape[0]):
                  Xs[j][i] = (Xs[j][i] - mean[i])/std[i]
In [49]:
          mean = np.ones(Xtest.shape[1])
          std = np.ones(Xtest.shape[1])
          for i in range(0, Xtest.shape[1]):
              mean[i] = np.mean(Xtest.transpose()[i])
              std[i] = np.std(Xtest.transpose()[i])
              for j in range(0, Xtest.shape[0]):
                  Xtest[j][i] = (Xtest[j][i] - mean[i])/std[i]
In [50]:
          theta, cost = linear_regression(Xn, Yn, 0.1, iterations)
          print('Final Theta Value with Normalization =', theta)
          cost = list(cost)
          n iterations = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Normalization = [1.24885520e-16\ 2.64108625e-01\ 1.27168543e-01\ 2.
         88652311e-01
           1.21315783e-01 9.99334571e-02 3.90689188e-02 1.43965719e-01
           2.70513007e-01 9.08846334e-02 1.67876986e-01]]
In [51]:
          theta2, cost2 = linear regression(Xs, Ys, 0.1, iterations)
          print('Final Theta Value with Standardization =', theta2)
          cost2 = list(cost2)
          n_iterations2 = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Standardization = [[1.24885520e-16 2.64108625e-01 1.27168543e-01
         2.88652311e-01
           1.21315783e-01 9.99334571e-02 3.90689188e-02 1.43965719e-01
           2.70513007e-01 9.08846334e-02 1.67876986e-01]]
In [52]:
          theta t, cost t = linear regression(Xtest, Ytest, 0.1, iterations)
          print('Final Theta Value of the Test Set =', theta t)
          cost t = list(cost t)
          n_iterations_t = [x for x in range(1,(iterations + 1))]
```

Final Theta Value of the Test Set = [[3665283.80998753 741402.85068115 264657.01674763 992948.00356364 305680.32344454 126509.594599 265573.12956302 96887.61766261 1318395.63714537 574221.3020385 498783.75949985]]

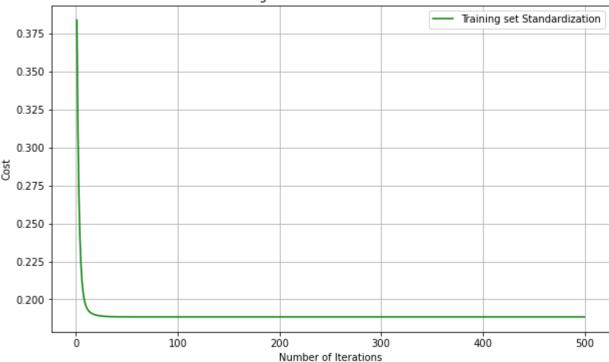
```
plt.plot(n_iterations, cost, color = 'green', label='Training set Normalization')
plt.legend()
plt.rcParams["figure.figsize"]=(10,6)
plt.grid()
plt.xlabel('Number of Iterations')
plt.ylabel('Cost')
plt.title('Convergence of the Gradient Descent')
```

Out[53]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



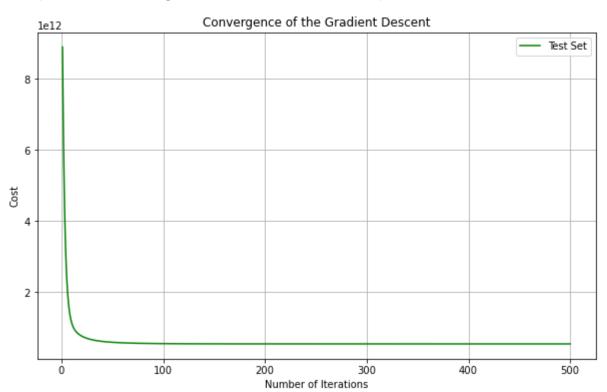
```
In [54]:
    plt.plot(n_iterations2, cost2, color = 'green', label='Training set Standardization')
    plt.legend()
    plt.rcParams["figure.figsize"]=(10,6)
    plt.grid()
    plt.xlabel('Number of Iterations')
    plt.ylabel('Cost')
    plt.title('Convergence of the Gradient Descent')
```

Out[54]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



```
In [55]:
    plt.plot(n_iterations_t, cost_t, color = 'green', label='Test Set')
    plt.legend()
    plt.rcParams["figure.figsize"]=(10,6)
    plt.grid()
    plt.xlabel('Number of Iterations')
    plt.ylabel('Cost')
    plt.title('Convergence of the Gradient Descent')
```

Out[55]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



```
## Problem 3 ##
In [56]:
In [57]:
          from sklearn.model_selection import train_test_split
           np.random.seed(0)
          df_train, df_test = train_test_split(housing, train_size = 0.7, test_size = 0.3, random)
          df train.shape
Out[57]: (381, 13)
In [58]:
           num_vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking','price']
          df Newtrain = df train[num vars]
          df_Newtest = df_test[num_vars]
          df Normal = df Newtrain
          df_Standard = df_Newtrain
           df Newtrain.head()
Out[58]:
                    bedrooms bathrooms stories
                                                parking
                                                           price
          454 4500
                           3
                                             2
                                                      0 3143000
          392 3990
                            3
                                             2
                                                        3500000
          231 4320
                            3
                                                        4690000
          271 1905
                                             2
                                                        4340000
          250 3510
                            3
                                      1
                                             3
                                                      0 4515000
In [59]:
           import warnings
          warnings.filterwarnings('ignore')
          from sklearn.preprocessing import MinMaxScaler, StandardScaler
           scaler = MinMaxScaler()
          df_Normal[num_vars] = scaler.fit_transform(df_Normal[num_vars])
          df Normal.head(20)
Out[59]:
                  area
                       bedrooms bathrooms
                                              stories
                                                     parking
                                                                price
          454 0.193548
                            0.50
                                            392 0.156495
                            0.50
                                        0.0
                                            0.333333  0.000000  0.151515
          231 0.180471
                            0.50
                                        0.0
                                            0.000000 0.000000 0.254545
          271 0.005013
                            1.00
                                        0.0
                                            0.333333  0.000000  0.224242
          250 0.121622
                            0.50
                                        0.0
                                            0.666667 0.000000 0.239394
          541 0.040976
                                            0.000000 0.000000 0.001485
                            0.50
                                        0.0
          461 0.226969
                            0.25
                                            0.000000 0.000000 0.115152
                                        0.0
          124 0.340671
                            0.50
                                        0.5
                                           1.000000 0.333333 0.363636
          154 0.131793
                            0.50
                                        0.5
                                           451 0.357018
                            0.25
                                        0.0
                                            0.000000 0.000000 0.121212
```

0.50

0.5

1.000000 0.333333 0.472727

59 0.302528

	area	bedrooms	bathrooms	stories	parking	price
493	0.154316	0.50	0.0	0.000000	0.000000	0.090909
465	0.142691	0.25	0.0	0.000000	0.000000	0.112121
490	0.182650	0.50	0.0	0.333333	0.333333	0.093939
540	0.084568	0.25	0.0	0.000000	0.666667	0.006061
406	0.253124	0.25	0.0	0.000000	0.333333	0.148485
289	0.291630	0.25	0.0	0.000000	0.666667	0.212121
190	0.418774	0.75	0.0	0.333333	0.666667	0.284848
55	0.302528	0.50	0.0	0.333333	0.333333	0.484848
171	0.612685	0.50	0.0	0.000000	0.333333	0.303030

```
In [60]:
```

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
scaler = StandardScaler()
df_Standard[num_vars] = scaler.fit_transform(df_Standard[num_vars])
df_Standard.head(20)
```

Out[60]:

	area	bedrooms	bathrooms	stories	parking	price
454	-0.286366	0.073764	-0.581230	0.207401	-0.822960	-0.868394
392	-0.544762	0.073764	-0.581230	0.207401	-0.822960	-0.677628
231	-0.377564	0.073764	-0.581230	-0.937813	-0.822960	-0.041744
271	-1.601145	2.884176	-0.581230	0.207401	-0.822960	-0.228768
250	-0.787958	0.073764	-0.581230	1.352614	-0.822960	-0.135256
541	-1.350349	0.073764	-0.581230	-0.937813	-0.822960	-1.603589
461	-0.053303	-1.331442	-0.581230	-0.937813	-0.822960	-0.902058
124	0.739618	0.073764	1.488383	2.497828	0.321375	0.631546
154	-0.717026	0.073764	1.488383	0.207401	1.465710	0.407116
451	0.853616	-1.331442	-0.581230	-0.937813	-0.822960	-0.864653
59	0.473622	0.073764	1.488383	2.497828	0.321375	1.304836
493	-0.559962	0.073764	-0.581230	-0.937813	-0.822960	-1.051678
465	-0.641027	-1.331442	-0.581230	-0.937813	-0.822960	-0.920761
490	-0.362365	0.073764	-0.581230	0.207401	0.321375	-1.032976
540	-1.046354	-1.331442	-0.581230	-0.937813	1.465710	-1.575348
406	0.129094	-1.331442	-0.581230	-0.937813	0.321375	-0.696331
289	0.397623	-1.331442	-0.581230	-0.937813	1.465710	-0.303578
190	1.284276	1.478970	-0.581230	0.207401	1.465710	0.145281

area bedrooms bathrooms

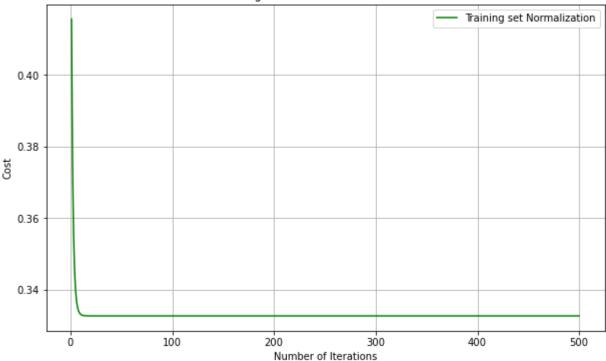
```
0.473622
                         0.073764
                                   -0.581230
                                             0.207401
           55
                                                       0.321375
                                                                1.379646
          171
               2.636548
                         0.073764
                                   -0.581230 -0.937813
                                                       0.321375
                                                                0.257496
In [61]:
          Xn = df_Normal.values[:,[0,1,2,3,4]]
          Yn = df Normal.values[:,5]
          Xtest = df_Newtest.values[:,[0,1,2,3,4]]
          Ytest = df Newtest.values[:,5]
          Xs = df Standard.values[:,[0,1,2,3,4]]
          Ys = df Standard.values[:,5]
In [62]:
          mean = np.ones(Xn.shape[1])
          std = np.ones(Xn.shape[1])
          for i in range(0, Xn.shape[1]):
              mean[i] = np.mean(Xn.transpose()[i])
              std[i] = np.std(Xn.transpose()[i])
              for j in range(0, Xn.shape[0]):
                  Xn[j][i] = (Xn[j][i] - mean[i])/std[i]
In [63]:
          mean = np.ones(Xs.shape[1])
          std = np.ones(Xs.shape[1])
          for i in range(0, Xs.shape[1]):
              mean[i] = np.mean(Xs.transpose()[i])
              std[i] = np.std(Xs.transpose()[i])
              for j in range(0, Xs.shape[0]):
                  Xs[j][i] = (Xs[j][i] - mean[i])/std[i]
In [64]:
          mean = np.ones(Xtest.shape[1])
          std = np.ones(Xtest.shape[1])
          for i in range(0, Xtest.shape[1]):
              mean[i] = np.mean(Xtest.transpose()[i])
              std[i] = np.std(Xtest.transpose()[i])
              for j in range(0, Xtest.shape[0]):
                  Xtest[j][i] = (Xtest[j][i] - mean[i])/std[i]
In [65]:
          def compute_cost(X, n, theta):
              h = np.ones((X.shape[0],1))
              theta = theta.reshape(1,n+1)
              for i in range(0, X.shape[0]):
                  h[i] = float(np.matmul(theta, X[i]))
              h = h.reshape(X.shape[0])
              return h
In [66]:
          def gradient_descent(X, Y, theta, alpha, iterations, n, h):
              lam = 1000
              cost = np.ones(iterations)
              for i in range(0,iterations):
                   theta[0] = theta[0] - (alpha/X.shape[0]) * sum(h - Y)
                   for j in range(1,n+1):
                       theta[j] = (theta[j]*(1-(alpha*(lam/X.shape[0])))) - (alpha/X.shape[0]) * s
```

stories

parking

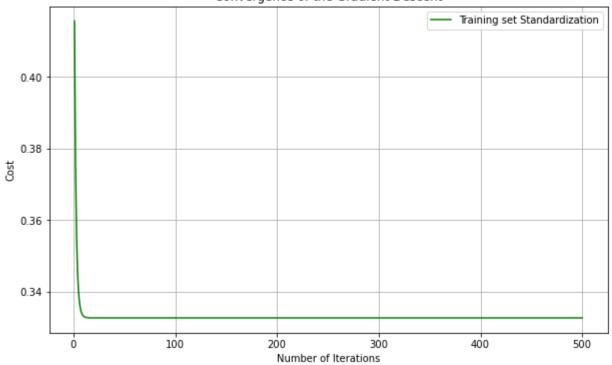
price

```
h = compute cost(X, n, theta)
                   cost[i] = (1/X.shape[0]) * 0.5 * sum(np.square(h - Y))
              theta = theta.reshape(1,n+1)
              return theta, cost
In [67]:
          def linear_regression(X, Y, alpha, iterations):
              n = X.shape[1]
              one_column = np.ones((X.shape[0],1))
              X = np.concatenate((one column, X), axis = 1)
              theta = np.zeros(n+1)
              h = compute cost(X, n, theta)
              theta, cost = gradient_descent(X, Y, theta, alpha, iterations, n, h)
               return theta, cost
In [68]:
          iterations = 500;
In [69]:
          theta, cost = linear regression(Xn, Yn, 0.1, iterations)
          print('Final Theta Value with Normalization =', theta)
          cost = list(cost)
          n_iterations = [x for x in range(1,(iterations + 1))]
          Final Theta Value with Normalization = [[1.42056096e-16 1.24270894e-01 7.53179957e-02 1.
          10985844e-01
           9.01203112e-02 7.75127501e-02]]
In [70]:
          theta2, cost2 = linear_regression(Xs, Ys, 0.1, iterations)
          print('Final Theta Value with Standardization =', theta2)
          cost = list(cost2)
          n iterations2 = [x \text{ for } x \text{ in } range(1,(iterations + 1))]
          Final Theta Value with Standardization = [[1.42056096e-16 1.24270894e-01 7.53179957e-02
          1.10985844e-01
           9.01203112e-02 7.75127501e-02]]
In [71]:
          theta_t, cost_t = linear_regression(Xtest, Ytest, 0.1, iterations)
          print('Final Theta Value of the Test Set =', theta)
          cost_t = list(cost_t)
          n iterations t = [x \text{ for } x \text{ in } range(1, (iterations + 1))]
          Final Theta Value of the Test Set = [[1.42056096e-16 1.24270894e-01 7.53179957e-02 1.109
          85844e-01
           9.01203112e-02 7.75127501e-02]]
In [72]:
          plt.plot(n_iterations, cost, color = 'green', label='Training set Normalization')
          plt.legend()
          plt.rcParams["figure.figsize"]=(10,6)
          plt.grid()
          plt.xlabel('Number of Iterations')
          plt.vlabel('Cost')
          plt.title('Convergence of the Gradient Descent')
Out[72]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')
```



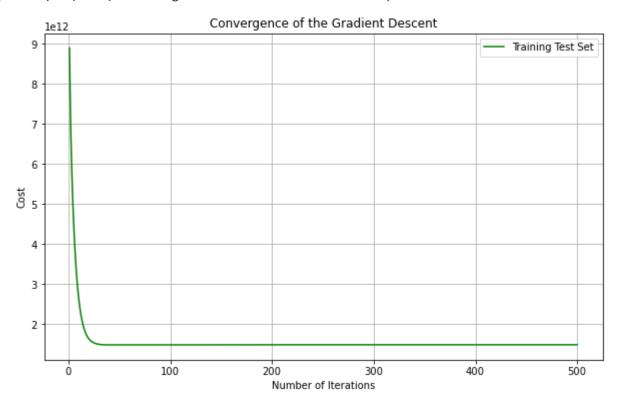
Out[73]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')





```
In [94]: plt.plot(n_iterations_t, cost_t, color = 'green', label='Training Test Set')
plt.legend()
plt.rcParams["figure.figsize"]=(10,6)
plt.grid()
plt.xlabel('Number of Iterations')
plt.ylabel('Cost')
plt.title('Convergence of the Gradient Descent')
```

Out[94]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



```
num_vars = ['area', 'bedrooms', 'bathrooms', 'mainroad', 'guestroom', 'basement', 'hotw
df_Newtrain = df_train[num_vars]
df_Newtest = df_test[num_vars]
df_Normal = df_Newtrain
df_Standard = df_Newtrain
df_Newtrain.head()
```

```
Out[75]:
                     bedrooms bathrooms mainroad guestroom basement hotwaterheating airconditioning
                area
                             3
                                                                        0
          454 4500
                                         1
                                                   1
                                                              0
                                                                                         0
                                                                                                        1
          392 3990
                             3
                                         1
                                                   1
                                                              0
                                                                        0
                                                                                         0
                                                                                                        0
          231 4320
                             3
                                         1
                                                   1
                                                              0
                                                                        0
                                                                                         0
                                                                                                        0
          271 1905
                             5
                                         1
                                                   0
                                                              0
                                                                        1
                                                                                         0
                                                                                                        0
          250 3510
                             3
                                         1
                                                   1
                                                              0
                                                                        0
                                                                                         0
                                                                                                        0
```

```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
```

```
scaler = MinMaxScaler()
df_Normal[num_vars] = scaler.fit_transform(df_Normal[num_vars])
df_Normal.head(20)
```

Out[76]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditionin
	454	0.193548	0.50	0.0	1.0	0.0	0.0	0.0	1
	392	0.156495	0.50	0.0	1.0	0.0	0.0	0.0	0
	231	0.180471	0.50	0.0	1.0	0.0	0.0	0.0	0
	271	0.005013	1.00	0.0	0.0	0.0	1.0	0.0	0
	250	0.121622	0.50	0.0	1.0	0.0	0.0	0.0	0
	541	0.040976	0.50	0.0	0.0	0.0	0.0	0.0	0
	461	0.226969	0.25	0.0	1.0	0.0	1.0	0.0	1
	124	0.340671	0.50	0.5	1.0	0.0	0.0	0.0	0
	154	0.131793	0.50	0.5	1.0	0.0	0.0	0.0	0
	451	0.357018	0.25	0.0	1.0	0.0	0.0	0.0	0
	59	0.302528	0.50	0.5	1.0	1.0	0.0	0.0	1
	493	0.154316	0.50	0.0	1.0	0.0	0.0	0.0	0
	465	0.142691	0.25	0.0	1.0	0.0	0.0	0.0	0
	490	0.182650	0.50	0.0	0.0	0.0	0.0	1.0	0
	540	0.084568	0.25	0.0	1.0	0.0	1.0	0.0	0
	406	0.253124	0.25	0.0	1.0	0.0	0.0	0.0	0
	289	0.291630	0.25	0.0	1.0	1.0	1.0	0.0	0
	190	0.418774	0.75	0.0	1.0	0.0	0.0	0.0	1
	55	0.302528	0.50	0.0	1.0	0.0	0.0	0.0	1
	171	0.612685	0.50	0.0	1.0	0.0	0.0	0.0	0

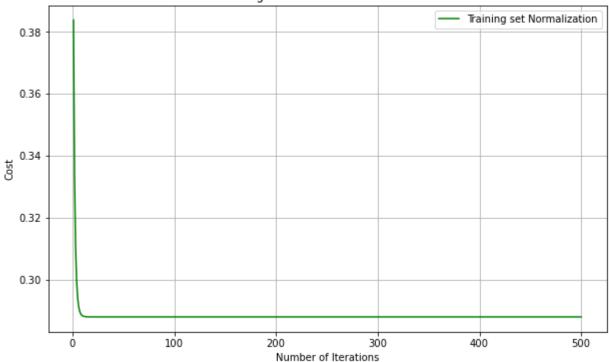
```
import warnings
warnings.filterwarnings('ignore')
from sklearn.preprocessing import MinMaxScaler, StandardScaler
scaler = StandardScaler()
df_Standard[num_vars] = scaler.fit_transform(df_Standard[num_vars])
df_Standard.head(20)
```

Out[77]:		area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditioni
	454	-0.286366	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	1.4226
	392	-0.544762	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
	231	-0.377564	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
	271	-1.601145	2.884176	-0.581230	-2.543735	-0.457738	1.405903	-0.216109	-0.7029

	area	bedrooms	bathrooms	mainroad	guestroom	basement	hotwaterheating	airconditioni
250	-0.787958	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
541	-1.350349	0.073764	-0.581230	-2.543735	-0.457738	-0.711287	-0.216109	-0.7029
461	-0.053303	-1.331442	-0.581230	0.393123	-0.457738	1.405903	-0.216109	1.4226
124	0.739618	0.073764	1.488383	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
154	-0.717026	0.073764	1.488383	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
451	0.853616	-1.331442	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
59	0.473622	0.073764	1.488383	0.393123	2.184657	-0.711287	-0.216109	1.4226
493	-0.559962	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
465	-0.641027	-1.331442	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
490	-0.362365	0.073764	-0.581230	-2.543735	-0.457738	-0.711287	4.627285	-0.7029
540	-1.046354	-1.331442	-0.581230	0.393123	-0.457738	1.405903	-0.216109	-0.7029
406	0.129094	-1.331442	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029
289	0.397623	-1.331442	-0.581230	0.393123	2.184657	1.405903	-0.216109	-0.7029
190	1.284276	1.478970	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	1.4226
55	0.473622	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	1.4226
171	2.636548	0.073764	-0.581230	0.393123	-0.457738	-0.711287	-0.216109	-0.7029

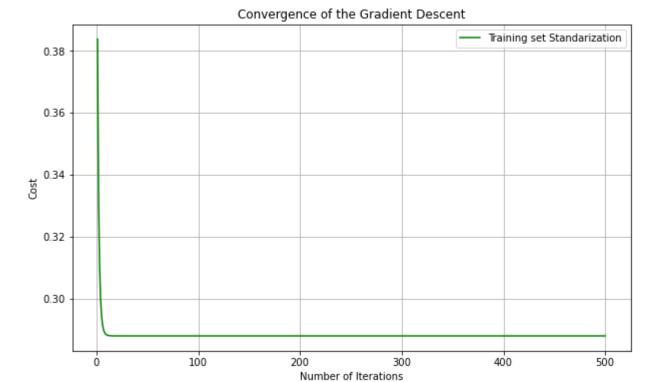
```
In [78]:
          Xn = df_Normal.values[:,0:10]
          Yn = df_Normal.values[:,10]
          Xtest = df_Newtest.values[:,0:10]
          Ytest = df_Newtest.values[:,10]
          Xs = df_Standard.values[:,0:10]
          Ys = df_Standard.values[:,10]
In [79]:
          mean = np.ones(Xn.shape[1])
          std = np.ones(Xn.shape[1])
          for i in range(0, Xn.shape[1]):
              mean[i] = np.mean(Xn.transpose()[i])
              std[i] = np.std(Xn.transpose()[i])
              for j in range(0, Xn.shape[0]):
                  Xn[j][i] = (Xn[j][i] - mean[i])/std[i]
In [80]:
          mean = np.ones(Xs.shape[1])
          std = np.ones(Xs.shape[1])
          for i in range(0, Xs.shape[1]):
              mean[i] = np.mean(Xs.transpose()[i])
              std[i] = np.std(Xs.transpose()[i])
              for j in range(0, Xs.shape[0]):
                  Xs[j][i] = (Xs[j][i] - mean[i])/std[i]
In [81]:
```

```
mean = np.ones(Xtest.shape[1])
          std = np.ones(Xtest.shape[1])
          for i in range(0, Xtest.shape[1]):
              mean[i] = np.mean(Xtest.transpose()[i])
              std[i] = np.std(Xtest.transpose()[i])
              for j in range(0, Xtest.shape[0]):
                  Xtest[j][i] = (Xtest[j][i] - mean[i])/std[i]
In [82]:
          theta, cost = linear regression(Xn, Yn, 0.1, iterations)
          print('Final Theta Value with Normalization =', theta)
          cost = list(cost)
          n iterations = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Normalization = [[1.38369922e-16 1.08337017e-01 7.58521283e-02 1.
         08013107e-01
           5.54076634e-02 5.32500668e-02 3.66508358e-02 3.65154719e-02
           9.68953820e-02 6.81505402e-02 7.57869446e-02]]
In [83]:
          theta2, cost2 = linear_regression(Xs, Ys, 0.1, iterations)
          print('Final Theta Value with Standardization =', theta2)
          cost2 = list(cost2)
          n_iterations2 = [x for x in range(1,(iterations + 1))]
         Final Theta Value with Standardization = [[1.38369922e-16 1.08337017e-01 7.58521283e-02
         1.08013107e-01
           5.54076634e-02 5.32500668e-02 3.66508358e-02 3.65154719e-02
           9.68953820e-02 6.81505402e-02 7.57869446e-02]]
In [84]:
          theta t, cost t = linear regression(Xtest, Ytest, 0.1, iterations)
          print('Final Theta Value of the Test Set =', theta_t)
          cost t = list(cost t)
          n_iterations_t = [x for x in range(1,(iterations + 1))]
         Final Theta Value of the Test Set = [[4.68135283e+06\ 9.14174376e+04\ 7.10541172e+04\ 1.030]
         91554e+05
           6.81362933e+04 4.24713613e+04 1.63927974e+04 8.78780977e+02
           6.38058529e+04 5.14196389e+04 2.74614616e+04]]
In [85]:
          plt.plot(n_iterations, cost, color = 'green', label='Training set Normalization')
          plt.legend()
          plt.rcParams["figure.figsize"]=(10,6)
          plt.grid()
          plt.xlabel('Number of Iterations')
          plt.ylabel('Cost')
          plt.title('Convergence of the Gradient Descent')
Out[85]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')
```



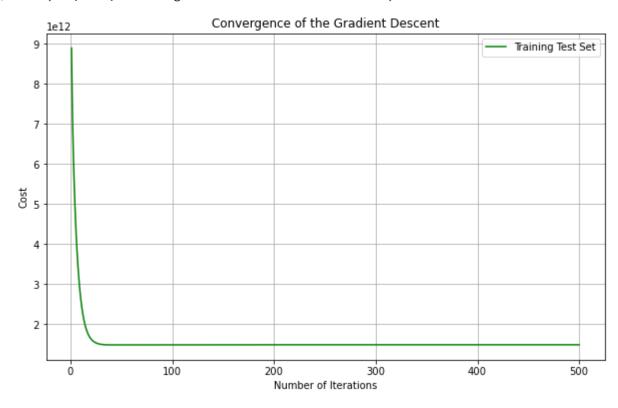
```
plt.plot(n_iterations2, cost2, color = 'green', label='Training set Standarization')
plt.legend()
plt.rcParams["figure.figsize"]=(10,6)
plt.grid()
plt.xlabel('Number of Iterations')
plt.ylabel('Cost')
plt.title('Convergence of the Gradient Descent')
```

Out[86]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



```
In [93]: plt.plot(n_iterations_t, cost_t, color = 'green', label='Training Test Set')
plt.legend()
plt.rcParams["figure.figsize"]=(10,6)
plt.grid()
plt.xlabel('Number of Iterations')
plt.ylabel('Cost')
plt.title('Convergence of the Gradient Descent')
```

Out[93]: Text(0.5, 1.0, 'Convergence of the Gradient Descent')



```
In [ ]:
```