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```

3.19 MCMF

Basic

```
se rnu nu ai ts=4 sw=4 mouse=vi incsearch
sy on
ino ( ()<Esc>i
ino ' ''<Esc>i
ino " ""<Esc>i
ino [ []<Esc>i
ino { {}<Esc>i
ino {<CR> {<CR><Tab><CR>}<Esc>hxka
ino jj <Esc>
ino jk <Esc>
ino kk <Esc>
map <F5> :w<CR>:!
    g++ -g -fsanitize=undefined,address -Wall -Wextra
     -Wshadow %:r.cpp &&echo "Compiled" && ./a.out<CR>
```

1.1 Default [d4fb81]

```
#include <bits/stdc++.h>
using namespace std;
#define pb emplace_back
#define iter(x) (x).begin(), (x).end()
#define size(x) (int)(x).size()
ypedef long long ll;
signed main() {
    cin.tie(0)->sync_with_stdio(0);
setxkbmap -option caps:swapescape #caps to esc
cpp file.cpp -dD -P -fpreprocessed |
    tr -d '[:space:]' | md5sum | cut -c-6 #hash command
#!/usr/bin/bash
for ((i=0;;i++))
python gen.py > case.in
./A < case.in > aout
./B < case.in > bout
if ! (cmp -s aout bout);
then
cat case.in
fi
done
```

1.2 Default-extension [7a1c54]

```
#define lowbit(x) ((x) & -(x))
#define tmin(a, b) (a) = min((a), (b))
#define tmax(a, b) (a) = max((a), (b))
typedef pair<int, int> pii;
void db() { cerr << endl; }</pre>
template <class T, class... U>
void db(T a, U... b) { cerr << a << " ", db(b...); }</pre>
1.3 Pragma [Oca2dd]
#pragma GCC optimize("Ofast, no-stack-protector")
#pragma GCC optimize("no-math-errno,unroll-loops")
```

#pragma GCC target("popcnt, abm, mmx, avx, arch=skylake")

__builtin_ia32_ldmxcsr(__builtin_ia32_stmxcsr()|0x8040)

#pragma GCC target("sse,sse2,sse3,sse3,sse4")

1.4 FastIO [11a75d]

#define INF 0x3f3f3f3f3f

10

```
inline char gc() {
    const static int SZ = 1 << 16;</pre>
    static char buf[SZ], *p1, *p2;
    if (p1 == p2 && (p2 =
        buf + fread(p1 = buf, 1, SZ, stdin), p1 == p2))
        return -1;
    return *p1++;
}
void rd() {}
template <typename T, typename... U>
void rd(T &x, U &...y) {
    x = 0:
    bool f = 0;
    char c = gc();
    while (!isdigit(c))
        f = !(c ^ 45), c = gc();
    while (isdigit(c))
        x = (x << 1) + (x << 3) + (c ^ 48), c = gc();
    f \& (x = -x), rd(y...);
}
template <typename T>
void prt(T x) {
    if (x < 0)
        putchar('-'), x = -x;
    if (x > 9)
        prt(x / 10);
    putchar((x % 10) ^ 48);
```

Geometry

2.1 Template [47e2bd]

```
struct P {
#define eps 1e-9
    double x, y;
    P() \{ x = y = 0; \}
    P(double x, double y) : x(x), y(y) {}
    friend bool operator<(const P &a, const P &b)</pre>
         { return a.x == b.x ? a.y < b.y : a.x < b.x; }
    friend bool operator<=(const P &a, const P &b) {</pre>
         return a.x == b.x ? a.y <= b.y : a.x <= b.x; }
    friend bool operator==(const P &a, const
         P &b) { return a.x == b.x && a.y == b.y; }
    friend bool operator!=(const P &a, const
         P &b) { return a.x != b.x || a.y != b.y; }
    P operator+(const
         P &b) const { return P(x + b.x, y + b.y); }
    void operator+=(const P &b) { x += b.x, y += b.y; }
    P operator-(const
         P &b) const { return P(x - b.x, y - b.y); }
    void operator-=(const P &b) { x -= b.x, y -= b.y; }
    P operator
        *(double b) const { return P(x * b, y * b); }
    void operator*=(double b) { x *= b, y *= b; }
    P operator
        /(double b) const { return P(x / b, y / b); }
```

```
void operator/=(double b) { x /= b, y /= b; }
                                                                    return !ori(hl
    double operator*(
                                                                        [0], hl[1], a) && within(a, hl[0], hl[1]);
        const P &b) const { return x * b.x + y * b.y; }
    double operator^(
                                                                int l = 1, r = ln - 1, m;
        const P &b) const { return x * b.y - y * b.x; }
                                                                while (l < r - 1)  {
    double lth() const { return sqrt(x * x + y * y); }
                                                                    m = (l + r) >> 1;
    double lth2() const { return x * x + y * y; }
                                                                    if (ori(hl[0], a, hl[m]) < 0)</pre>
    inline void print
                                                                        l = m;
        () { cout << '(' << x << ' ' << y << ')'; }
                                                                    else
                                                                        r = m;
    friend istream &operator>>(
        istream &is, P &a) { return is >> a.x >> a.y; }
                                                                return ori(hl[0], hl[l], a) >= 0 && ori(hl[l
    friend ostream &operator<<(ostream &os,</pre>
                                                                    ], hl[r], a) >= 0 && ori(hl[r], hl[0], a) >= 0;
        const P &a) { return os << a.x << ' ' << a.y; }</pre>
                                                            2.2 Minimum Enclosing Circle [1f681e]
int ori(const P &a, const P &b, const P &c) {
    double k = (b - a) \wedge (c - a);
                                                            P perp(const P &a) {
    if (fabs(k) < eps)</pre>
                                                                return P(-a.y, a.x);
        return 0;
                                                            }
    return k > 0 ? 1 : -1;
                                                            struct Circle {
}
                                                                P o;
inline
                                                                double r;
     bool within(const P &a, const P &b, const P &c) {
                                                                inline bool in(const P
    return (b - a) * (c - a) < eps;
                                                                     &a) const { return (a - o).lth() <= r + eps; }
                                                            }:
bool intersects
                                                            Circle getcircle(const P &a, const P &b) {
    (const P &a, const P &b, const P &c, const P &d) {
                                                                return Circle{(a + b) / 2, (a - b).lth() / 2};
    int abc = ori(a, b, c);
    int abd = ori(a, b, d);
                                                            Circle getcircle(const P &a, const P &b, const P &c) {
    int cda = ori(c, d, a);
                                                                const P p1 = (a + b) / 2, p2 = (a + c) / 2;
    int cdb = ori(c, d, b);
                                                                Circle res;
    if (!abc && !abd)
                                                                res.o = intersection
        return within(a, c, d) || within(b, c, d) ||
                                                                    (p1, p1 + perp(a - b), p2, p2 + perp(a - c));
               within(c, a, b) || within(d, a, b);
                                                                res.r = (res.o - a).lth();
    return abc * abd <= 0 && cda * cdb <= 0;
                                                                return res;
P intersection
                                                            Circle findcircle(vector<P> &ar) {
    (const P &a, const P &b, const P &c, const P &d) {
                                                                int n = size(ar);
    double abc = (b - a) ^ (c - a);
                                                                shuffle(iter(ar), mt19937(time(NULL)));
    double abd = (b - a) ^ (d - a);
                                                                Circle res = \{ar[0], 0\};
    return (d * abc - c * abd) / (abc - abd);
                                                                for (int i = 0; i < n; i++) {
                                                                    if (res.in(ar[i]))
P BASE(0, 0);
                                                                        continue;
inline bool updown(const P &a) {
                                                                    res = {ar[i], 0};
    if (fabs(a.y) < eps)</pre>
                                                                    for (int j = 0; j < i; j++) {</pre>
        return a.x > eps;
                                                                        if (res.in(ar[j]))
    return a.y > eps;
                                                                            continue;
                                                                        res = getcircle(ar[i], ar[j]);
bool cmp(const P &a, const P &b) {
                                                                        for (int k = 0; k < j; k++) {
    bool ba = updown(a - BASE), bb = updown(b - BASE);
                                                                            if (res.in(ar[k]))
    if (ba ^ bb)
                                                                                continue:
        return ba;
                                                                            res = getcircle(ar[i], ar[j], ar[k]);
    return ori(BASE, a, b) > 0;
                                                                        }
                                                                    }
void fdhl(vector<P> &ar, vector<P> &hl) {
    sort(iter(ar));
                                                                return res;
    for (int i = 0; i < 2; i++) {</pre>
        int prln = size(hl);
                                                            2.3 Convex Hull [61610f]
        for (int j = 0; j < size(ar); j++) {</pre>
            while
                                                            void fdhl(vector<P> &ar, vector<P> &hl) {
                  (size(hl) - prln > 1 && ori(hl[size(hl
                                                                sort(iter(ar));
                ) - 1], hl[size(hl) - 2], ar[j]) >= 0)
                                                                for (int i = 0; i < 2; i++) {</pre>
                hl.pop_back();
                                                                    int prln = size(hl);
            hl.push_back(ar[j]);
                                                                    for (int j = 0; j < size(ar); j++) {</pre>
                                                                        while
        if (size(hl) > 1)
                                                                              (size(hl) - prln > 1 && ori(hl[size(hl
            hl.pop back():
                                                                            ) - 1], hl[size(hl) - 2], ar[j]) >= 0)
        reverse(ar.begin(), ar.end());
                                                                            hl.pop_back();
                                                                        hl.push_back(ar[j]);
    if (size(hl) > 1 && hl.front() == hl.back())
        hl.pop_back();
                                                                    if (size(hl) > 1)
                                                                        hl.pop_back();
bool in(const P &a, const vector<P> &hl) {
                                                                    reverse(ar.begin(), ar.end());
    int ln = size(hl);
    if (ln == 1)
                                                                if (size(hl) > 1 && hl.front() == hl.back())
        return a == hl[0];
                                                                    hl.pop_back();
    if (ln == 2) {
                                                           | }
```

2.4 Polar Angle Vector [56401e]

```
| P BASE(0, 0), BASEV(1, 0);
| inline bool updown(const P &a) {
| int tmp = ori(BASE, BASE + BASEV, a);
| if (!tmp)
| return BASEV * (a - BASE) > 0;
| return tmp > 0;
|}
| bool cmp(const P &a, const P &b) {
| bool ba = updown(a), bb = updown(b);
| if (ba ^ bb)
| return ba;
| return ori(BASE, a, b) > 0;
|}
```

2.5 In Convex Hull [513844]

```
bool in(const P &a, const vector<P> &hl) {
    int ln = size(hl);
    if (ln == 1)
        return a == hl[0];
    if (ln == 2) {
        return !ori(hl
            [0], hl[1], a) && within(a, hl[0], hl[1]);
    int l = 1, r = ln - 1, m;
    while (l < r - 1)  {
        m = (l + r) >> 1;
        if (ori(hl[0], a, hl[m]) < 0)
            l = m;
        else
            r = m;
    return ori(hl[0], hl[1], a) >= 0 && ori(hl[1
        ], hl[r], a) >= 0 && ori(hl[r], hl[0], a) >= 0;
}
```

2.6 Intersectsion [c5adb9]

```
bool within(const P &a, const P &b, const P &c) {
    return (b - a) * (c - a) < eps;
bool intersects
    (const P &a, const P &b, const P &c, const P &d) {
    int abc = ori(a, b, c);
    int abd = ori(a, b, d);
    int cda = ori(c, d, a);
    int cdb = ori(c, d, b);
    if (!abc && !abd)
         return within(a, c, d) || within(b, c, d) ||
    within(c, a, b) || within(d, a, b); return abc * abd <= \theta && cda * cdb <= \theta;
P intersection
    (const P &a, const P &b, const P &c, const P &d) {
    double abc = (b - a) ^ (c - a);
    double abd = (b - a) \wedge (d - a);
    return (d * abc - c * abd) / (abc - abd);
```

2.7 Minkowski [542fed]

```
//need Geometry template
void reorder_polygon(vector<P> & pt){
   int pos = 0;
   for(int i = 1; i < size(pt); i++){
      if(pt[i].y < pt[pos].y || (pt
        [i].y == pt[pos].y && pt[i].x < pt[pos].x))
      pos = i;
   }
   rotate(pt.begin(), pt.begin() + pos, pt.end());
}
vector<P> minkowski(vector<P> A, vector<P> B){
   reorder_polygon(A);
   reorder_polygon(B);
   A.push_back(A[0]);A.push_back(A[1]);
   B.push_back(B[0]);B.push_back(B[1]);
```

```
inline bool updown(const P &a) {
   if (fabs(a.y) < eps)
      return a.x > eps;
   return a.y > eps;
}
bool cmp(const P &a, const P &b) {
   bool ba = updown(a - BASE), bb = updown(b - BASE);
   if (ba ^ bb)
      return ba;
```

2.9 Rotation Sweep Line [9fd768]

return ori(BASE, a, b) > 0;

}

```
|// int cmp1(const P &a, const P &b) {
     bool ba = updown(a - BASE), bb = updown(b - BASE);
//
        if (ba ^ bb)
//
            return ba - !ba;
|//
        return ori(BASE, a, b);
// }
// Collinear
void sweep(int n, vector<P> ar) {
     static const int N = 2005;
     static int id[N], po[N];
     static pii lr[N * N];
     int m = 0;
     for (int i = 0; i < n; i++)</pre>
         for (int j = 0; j < n; j++)</pre>
             if (i != j)
                 lr[m++] = pii(i, j);
     sort(lr, lr + m, [&](const pii
          &a, const pii &b) { return cmp(ar[a.first] -
          ar[a.second], ar[b.first] - ar[b.second]); });
         (lr, lr + m, [&](const pii &a, const pii &b) {
           int tmp = cmp1(ar[a.first
         ] - ar[a.second], ar[b.first] - ar[b.second]);
     //
            if (tmp)
     //
                return tmp > 0;
     //
            if (ar[a.first] != ar[b.first])
     //
                return ar[a.first] < ar[b.first];</pre>
     //
            return ar[a.second] < ar[b.second];</pre>
     // });
     iota(id, id + n, 0);
     sort(id, id +
         n, [&](int a, int b) { return ar[a].y == ar[b].
         y ? ar[a].x < ar[b].x : ar[a].y < ar[b].y; });
     for (int i = 0; i < n; i++)</pre>
         po[id[i]] = i;
     for (int i = 0; i < m; i++) {</pre>
         swap(id[po[lr[i].first]], id[po[lr[i].second]])
              , swap(po[lr[i].first], po[lr[i].second]);
```

2.10 Half Plain Intersection [8f94b7]

```
struct Line{ P X,Y; };
pair<ll,ll> area_pair(Line a, Line b)
{ return pair<ll,ll>((
        a.Y - a.X)^(b.X - a.X), (a.Y - a.X)^(b.Y - a.X)); }
```

```
bool isin(Line l0, Line l1, Line l2) {
  // Check inter(l1, l2) strictly in l0
  auto [a02X, a02Y] = area_pair(l0, l2);
  auto [a12X, a12Y] = area_pair(l1, l2);
  if (a12X - a12Y < 0) a12X *= -1, a12Y *= -1;
  return (__int128)
       a02Y * a12X - (_int128) a02X * a12Y > 0; // C^4
/* Having solution, check size > 2 */
/* --^-- Line.X --^-- Line.Y --^-- */
/* add polar angle sort below:*/
/* add polar angle sort above:*/
vector<Line> halfPlaneInter(vector<Line> arr) {
  sort(iter(arr), [&](Line a, Line b) -> int {
    return cmp(a.Y - a.X, b.Y - b.X);
  }):
  deque<Line> dq(1, arr[0]);
  for (auto p : arr) {
    if (((
         dq.back().Y - dq.back().X) \wedge (p.Y - p.X)) == 0)
      continue:
    while (size(dq)
         >= 2 \& !isin(p, dq[size(dq) - 2], dq.back()))
      dq.pop_back();
    while (size(dq) >= 2 \&\& !isin(p, dq[0], dq[1]))
      dq.pop_front();
    dq.pb(p);
  }
  while (size(dq) >=
       3 && !isin(dq[0], dq[size(dq) - 2], dq.back()))
    dq.pop_back();
  while
      (size(dq) >= 3 \& !isin(dq.back(), dq[0], dq[1]))
    dq.pop_front();
  return vector<Line>(iter(dq));
| }
     Graph
```

```
3.1 BellmonFord [8c4cd9]
struct BellmonFord {
    struct E {
         int u, v;
         ll w;
         int s() { return u < v ? u : -u; }</pre>
    int n;
ll inf = LONG_LONG_MAX;
    vector<ll> d;
    vector<E> e:
    BellmonFord(int _n) : n(_n), e(0) {}
    void add_edge
         (int u, int v, ll w) { e.pb(E{u, v, w}); }
     void go(int s) {
         d.assign(n, inf);
         vector<int> p(n, -1);
         d[s] = 0;
         sort(iter(e
             ), [](E a, E b) { return a.s() < b.s(); });
         int lim = n / 2 + 2;
         for (int i = 0; i < lim; ++i)</pre>
             for (auto [u, v, w] : e) {
                 if (abs(d[u]) == inf)
                     continue;
                 if (d[v] > d[u] + w) {
                     p[v] = u;
                     d[v] = (
                          i < \lim -1 ? d[v] + w : -inf);
                 }
         for (int i = θ; i < lim; ++i)</pre>
             for (auto [u, v, w] : e)
                 if (d[u] == -inf)
                     d[v] = -inf;
|};
```

3.2 Block Cut [ac5ea2]

```
struct BCT {
     static const int N = 1e6 + 5; // change
     vector<int> e1[N], e2[N], sk; // e2 is the new tree
     int low[N], dfn[N], ctd = 0, ctn = 0;
     bool vs[N];
     void dfs(int u, int fa) {
         dfn[u] = low[u] = ++ctd;
         sk.pb(u), vs[u] = 1;
         for (int v : e1[u]) {
             if (v == fa)
                 continue;
             if (dfn[v]) {
                 if (vs[v])
                     tmin(low[u], dfn[v]);
                 continue;
             dfs(v, u), tmin(low[u], low[v]);
             if (low[v] >= dfn[u]) {
                 e2[u].pb(++ctn);
                 int x;
                 do {
                     x = sk.back();
                     sk.pop_back();
                     e2[ctn].pb(x);
                 } while (x != v);
         }
         vs[u] = 0;
     inline void addedge
         (int x, int y) { e1[x].pb(y), e1[y].pb(x); }
     inline void ini(int n, int rt) {
         for (int i = 1; i <= ctn; i++)</pre>
             e1[i].clear(), e2[i].clear();
         ctn = n, ctd = 0;
         memset(dfn + 1, 0, n << 2);
         memset(vs + 1, 0, n);
         sk.clear();
         dfs(rt, -1);
};
```

3.3 Vertex BCC [3faed3]

```
struct VertexBCC { // !simple affect BCCofE
  int n, m, dft, nbcc;
  vector<int> low, dfn, bln, is_ap, st1, st2, BCCofE;
  vector<vector<pii>>> G;
  vector<vector<int>> bcc, nG;
  void dfs(int u, int f) {
    int child = 0;
    low[u] = dfn[u] = ++dft, st1.pb(u);
    for (auto [v, id] : G[u])
      if (!dfn[v]) {
        st2.pb(id);
        dfs(v, u), ++child;
        tmin(low[u], low[v]);
        if (dfn[u] <= low[v]) {</pre>
          is_ap[u] = 1, bln[u] = bln[v] = nbcc++;
          bcc.pb(vector<int>(1, u)), bcc.back().pb(v);
          for (; st1.back() != v; st1.pop_back())
            bcc[bln[u]].pb
                 (st1.back()), bln[st1.back()] = bln[u];
          st1.pop_back();
          while (st2.back() != id)
            BCCofE
                 [st2.back()] = bln[u], st2.pop_back();
          BCCofE[id] = bln[u], st2.pop_back();
        }
      else if (v != f) {
        tmin(low[u], dfn[v]);
        if (dfn[v] < dfn[u])</pre>
          st2.pb(id);
      }
```

```
if (f == -1 && child < 2)
       is_ap[v] = 0;
     if (f == -1 && child == 0)
       bcc.pb(vector<int>(1, u)), bln[u] = nbcc++;
       (int _n) : n(_n), m(0), low(n), bln(n), G(n) {}
   void add_edge(int u, int v) {
     G[u].pb(v, m), G[v].pb(u, m++);
  void slv() {
    is_ap.assign(n, \theta), dfn = is_ap, dft = nbcc = \theta;
     st1.clear(), st2.clear(), BCCofE.assign(m, -1);
     for (int i = 0; i < n; ++i)</pre>
       if (!dfn[i])
         dfs(i, -1);
  }
  void block_cut_tree() {
     int tmp = nbcc;
     for (int i = 0; i < n; ++i)</pre>
       if (is_ap[i])
         bln[i] = tmp++;
     nG.assign(tmp, vector<int>(0));
     for (int i = 0; i < nbcc; ++i)</pre>
       for (int j : bcc[i])
         if (is_ap[j])
           nG[i].pb(bln[j]), nG[bln[j]].pb(i);
  } // up to 2 * n - 2 nodes!! bln[i] for id
};
```

3.4 Edge BCC [353c57]

```
struct EdgeBCC {
  int n, m, dft, necc;
  vector<int> low, dfn, bln, is_bridge, stk;
  vector<vector<pii>> G;
  void dfs(int u, int f) {
    dfn[u] = low[u] = ++dft, stk.pb(u);
    for (auto [v, id] : G[u])
      if (!dfn[v])
        dfs(v, id), tmin(low[u], low[v]);
      else if (id != f)
        tmin(low[u], dfn[v]);
    if (low[u] == dfn[u]) {
      if (f != -1) is_bridge[f] = 1;
      for (; stk.back() != u; stk.pop_back())
        bln[stk.back()] = necc;
      bln[u] = necc++, stk.pop_back();
   }
  EdgeBCC(int_n): n(_n), m(0), low(n), bln(n), G(n) {}
  void add_edge(int u, int v) {
   G[u].pb(v, m), G[v].pb(u, m++);
 void slv() {
    is_bridge.assign(m, 0), stk.clear();
    dfn.assign(n, 0), dft = necc = 0;
    for (int i = 0; i < n; ++i)</pre>
      if (!dfn[i]) dfs(i, -1);
}; // ecc_id(i): bln[i]
```

3.5 Centroid Decomp [314317]

```
struct CentroidDecomposition {
    vector<vector<int> > g;
    vector<int> sub;
    vector<bool> v;
    vector<vector<int>> tree;
    int root;
    void add_edge(int a, int b) {
        g[a].push_back(b);
        g[b].push_back(a);
    CentroidDecomposition(const vector<vector
        \langle int \rangle > \&g_{,} int isbuild = true) : g(g_{,}) {
        sub.resize(size(g), 0);
```

```
v.resize(size(q), false);
         if (isbuild) build();
    }
     void build() {
         tree.resize(size(q));
         root = build_dfs(0);
     int get_size(int cur, int par) {
         sub[cur] = 1;
         for (auto &dst : g[cur]) {
             if (dst == par || v[dst]) continue;
             sub[cur] += get_size(dst, cur);
         return sub[cur];
     int get_centroid(int cur, int par, int mid) {
         for (auto &dst : g[cur]) {
             if (dst == par || v[dst]) continue;
             if (sub[dst] > mid
                 ) return get_centroid(dst, cur, mid);
         return cur;
     int build_dfs(int cur) {
         int centroid = get_centroid
             (cur, -1, get_size(cur, -1) / 2);
         v[centroid] = true;
         for (auto &dst : g[centroid]) {
             if (!v[dst]) {
                 int nxt = build_dfs(dst);
                 if (centroid != nxt
                     ) tree[centroid].emplace_back(nxt);
             }
         v[centroid] = false;
         return centroid;
    }
};
3.6 C3 [e348b4]
namespace C3 {
```

```
const int N = 1e5 + 5; // change
vector<int> eg[N], to[N];
int pl[N], ln, pd[N], id[N], cnt[N];
inline void addedge(int x, int y) {
    eg[x].pb(y), eg[y].pb(x);
ll blt(int n) {
    priority_queue<pii> pq;
    for (int i = 1; i <= n; i++)</pre>
        pq.push(pii(pd[i] = -size(eg[i]), i));
    while (!pq.empty()) {
        pii tp = pq.top();
        pq.pop();
        if (id[tp.second])
            continue;
        pl[++ln] = tp.second;
        id[tp.second] = ln;
        for (int v : eg[tp.second])
            if (!id[v])
                to[v].pb(tp.second
                     ), pq.push(pii(++pd[v], v));
    ans = 0;
   for (int p = 1; p <= n; p++) {</pre>
        for (int u : to[pl[p]])
            cnt[u]++;
        for (int u : to[pl[p]])
            for (int v : to[u])
                ans += cnt[v];
        for (int u : to[pl[p]])
```

```
cnt[u] = 0;
        return ans;
    }
}
3.7 C4 [f966c6]
namespace C4 {
    const int N = 1e5 + 5; // change
    vector<int> eg[N], to[N];
    int pl[N], ln, pd[N], id[N], cnt[N];
    ll ans;
    inline void addedge(int x, int y) {
        eg[x].pb(y), eg[y].pb(x);
    ll blt(int n) {
        priority_queue<pii> pq;
        for (int i = 1; i <= n; i++)</pre>
             pq.push(pii(pd[i] = -size(eg[i]), i));
        while (!pq.empty()) {
             pii tp = pq.top();
             pq.pop();
             if (id[tp.second])
                 continue;
             pl[++ln] = tp.second;
             id[tp.second] = ln;
             for (int v : eg[tp.second])
                 if (!id[v])
                     to[v].pb(tp.second
                         ), pq.push(pii(++pd[v], v));
        ans = 0;
        for (int p = 1; p <= n; p++) {</pre>
             for (int u : to[pl[p]])
                 for (int v : eg[u])
                     if (id[v] < p)
                         ans += cnt[v]++;
             for (int u : to[pl[p]])
                 for (int v : eq[u])
                     cnt[v] = 0;
        return ans;
    }
| }-
       Directed MST [de79a2]
3.8
struct DirectedMST { // O(m+nlgn)
    struct edge {
        int u, v;
        ll w;
    };
    int n;
    vector<edge> e;
    DirectedMST(int_n) : n(_n), e(0) {}
    void add edge
         (int u, int v, ll w) { e.pb(edge{u, v, w}); }
    vector<int>
         slv(int root) { // O-based, return idx of edges
        using T = pair<ll, int>;
        using PQ = pair<pri>priority_queue
             <T, vector<T>, greater<T>>, ll>;
        auto push = [](PQ \&pq, T v) {
             pq.first.
                 emplace(v.first - pq.second, v.second);
        auto top = [](const PQ &pq) -> T {
```

auto r = pq.first.top();

while (!b.first.empty())

swap(a, b);

vector<PQ> h(n * 2);

};

return {r.first + pq.second, r.second};

push(a, top(b)), b.first.pop();

auto join = [&push, &top](PQ &a, PQ &b) {

if (size(a.first) < size(b.first))</pre>

```
for (int i = 0; i < size(e); ++i)</pre>
            push(h[e[i].v], {e[i].w, i});
        vector<int> a(n *
             2), v(n * 2, -1), pa(n * 2, -1), r(n * 2);
        iota(iter(a), 0);
        auto 0 = [&](int x) {
            int y;
            for (y = x; a[y] != y; y = a[y])
            for (int ox = x; x != y; ox = x)
                x = a[x], a[ox] = y;
            return y;
        };
        v[root] = n + 1;
        int pc = n;
        for (int i = 0; i < n; ++i)</pre>
            if (v[i] == -1) {
                for (int p = i; v[p] == -1
                      || v[p] == i; p = o(e[r[p]].u)) {
                    if (v[p] == i) {
                         int q = p;
                         p = pc++;
                         do {
                             h[q].second = -
                                 h[q].first.top().first;
                             join(h[pa
                                 [q] = a[q] = p], h[q]);
                         } while
                              ((q = o(e[r[q]].u)) != p);
                    v[p] = i;
                    while (!h[p].first.empty() &&
                          o(e[top(h[p]).second].u) == p)
                         h[p].first.pop();
                    r[p] = top(h[p]).second;
                }
            }
        vector<int> ans;
        for (int i = pc - 1; i >= 0; i--)
            if (i != root && v[i] != n) {
                for (int f = e[r[i]].
                    v; f != -1 \&\& v[f] != n; f = pa[f])
                    v[f] = n;
                ans.pb(r[i]);
        return ans;
    }
3.9 Dominator Tree [602345]
```

|};

```
struct DOT {
    static const int N = 2e5 + 5; // change
        [N], id[N], dfc, fa[N], idm[N], sdm[N], bst[N];
    vector<int> G[N], rG[N];
    void ini(int n) { // remember to initialize
        for (int i = 1; i <= n; i++)</pre>
            G[i].clear(), rG[i].clear();
        fill(dfn, dfn + n + 1, 0);
    inline void addedge
        (int u, int v) { G[u].pb(v), rG[v].pb(u); }
    int f(int x, int lm) {
        if (x <= lm)
            return x;
        int cr = f(fa[x], lm);
        if (sdm[bst[fa[x]]] < sdm[bst[x]])</pre>
            bst[x] = bst[fa[x]];
        return fa[x] = cr;
    }
    void dfs(int u) {
        id[dfn[v] = ++dfc] = v;
        for (int v : G[u])
            if (!dfn[v])
                 dfs(v), fa[dfn[v]] = dfn[u];
    }
```

```
void tar(vector<int> *eg, int rt) {
        dfc = 0, dfs(rt);
        for (int i = 1; i <= dfc; i++)</pre>
             sdm[i] = bst[i] = i;
        for (int i = dfc; i > 1; i--) {
             int u = id[i];
             for (int v : rG[u])
                 if ((v = dfn[v]))
                     f(v, i), tmin(sdm[i], sdm[bst[v]]);
             eg[sdm[i]].pb(i), u = fa[i];
             for (int v : eq[u])
                 f(v, u), idm[v]
                      = (sdm[bst[v]] == u ? u : bst[v]);
             eq[u].clear();
        }
        for (int i = 2; i <= dfc; i++) {</pre>
             if (sdm[i] != idm[i])
                 idm[i] = idm[idm[i]];
             eg[id[idm[i]]].pb(id[i]);
        }
    }
};
```

3.10 Eulerian Path [1628e1]

```
struct EulerianPath {
  int n, m;
  vector<vector<pii>> adi:
  vector<int> cur, vst;
  vector<pii> ans;
  EulerianPath
       (int _n) : n(_n), m(θ), adj(n, vector<pii>(θ)) {}
  void add_edge(int a, int b) { adj[a].pb(b, m++); }
  void dfs(int u) {
    for (; cur[u] < size(adj[u]); ++cur[u]) {</pre>
      auto [v, id] = adj[u][cur[u]];
       if (vst[id]) continue;
      vst[id] = 1, dfs(v);
       ans.pb(u, v);
    }
  }
  bool go() {
    vector<int> in(n, 0), out(n, 0);
    for (int i = 0; i < n; ++i) {</pre>
       out[i] = size(adj[i]);
      for (auto [j, id] : adj[i])
         ++in[j];
    int s = -1, t = -1, ss = -1;
    for (int i = 0; i < n; ++i) {</pre>
      if (out[i]) ss = i;
      if (in[i] == out[i]) continue;
      if (in[i] + 1 == out[i]) {
         if (s != -1) return 0;
         s = i;
         continue;
      if (in[i] - 1 == out[i]) {
         if (t != -1) return 0;
         t = i;
         continue;
      }
      return 0;
    if (s == -1) s = ss;
    cur.assign(n, 0), vst.assign(m, 0), ans.clear();
    dfs(s), reverse(iter(ans));
    return accumulate(iter(vst), 0) == m;
  }
|};
```

3.11 Gomory-Hu Tree [ba0b07]

```
| struct edge{
| int u,v,w;
|};
|vector<edge> result;
|vector<edge> ed;
```

```
void GomoryHu(int N){
   vector<int> par(N,0);
   for(int i=1;i<N;i++){
     FLOW din;
     for(const auto &[u,v,c]:ed){
        din.addedge(u,v,c,c);
     }
        din.s = i;
        din.t = par[i];
        result.push_back({i,par[i],din.getflow()});
        for(int j=i+1;j<N;++j){
            if(par[j]==par[i] && din.dp[j]<INF) par[j]=i;
        }
    }
}</pre>
```

3.12 HVL Decomp [5f618c]

```
namespace HLD {
     int in[N], ou[N], dfc, top[N], sz[N], fa[N], ch[N];
     vector<int> eg[N];
     inline void addedge(int u, int v) {
         eg[u].pb(v), eg[v].pb(u);
     inline void ini(int n) { // after using
         for (int i = 1; i <= n; i++)</pre>
             eg[i].clear();
         memset(ch + 1, 0, n << 2), dfc = 0;
     void dsz(int u) {
         sz[u] = 1;
         for (int v : eg[u]) {
             if (v == fa[u])
                 continue;
             fa[v] = u, dsz(v), sz[u] += sz[v];
             if (sz[v] > sz[ch[u]])
                 ch[u] = v;
         }
    }
     void dfs(int u) {
         in[u] = ++dfc;
         if (ch[u])
             top[ch[u]] = top[u], dfs(ch[u]);
         for (int v : eg[u])
             if (v != fa[u] && v != ch[u])
                 top[v] = v, dfs(v);
         ou[u] = dfc;
     inline void blt(int rt) {
         fa[rt] = 0, dsz(rt), top[rt] = rt, dfs(rt);
     void slv(int u, int v) {
         while (top[u] != top[v]) {
             if (in[top[v]] < in[top[v]])</pre>
                 swap(u, v);
             // [ in[top[u]], in[u] ];
             u = fa[top[u]];
         if (in[u] > in[v])
             swap(u, v);
         // [ in[u], in[v] ];
    }
}
```

3.13 Hopcroft-Karp [f6d745]

```
struct HK {
    static const
        int N = 1e5 + 5, M = N * 2; // change, 1-base
    int fr[N], pr[N], hd[N], m1
        [N], m2[N], to[M], nxt[M], ct = 1, n1, n2, ans;
    inline void ini(int _n1, int _n2) {
        n1 = _n1, n2 = _n2, ct = 1;
        memset(m1 + 1, 0, n1 << 2);
        memset(m2 + 1, 0, n2 << 2);
        memset(hd + 1, 0, n1 << 2);
}</pre>
```

```
inline void addedge(int u, int v) {
                                                                               lx[p] -= mn;
        to[ct] = v, nxt[ct] = hd[u], hd[u] = ct++;
                                                                               if (!m2[v])
                                                                                   break:
                                                                          }
    int getmatch() {
                                                                          while (v)
        ans = 0;
                                                                               u = pr[v], m2[v] = u, swap(v, m1[u]);
        for (bool ok = 1; ok;) {
             ok = 0, memset(fr + 1, 0, n1 << 2);
             queue<int> q;
                                                                      for (int i = 1; i <= n; i++)</pre>
             for (int i = 1; i <= n1; i++)</pre>
                                                                          ans += eg[i][m1[i]];
                                                                      return ans;
                 if (!m1[i])
                     q.push(fr[i] = i);
             while (!q.empty()) {
                                                             };
                 int u = q.front();
                                                              3.15
                                                                      Matching [becd87]
                 q.pop();
                 if (m1[fr[u]])
                                                             struct Matching {
                     continue;
                                                                  static const int maxn
                 for (int i = hd[u]; i; i = nxt[i]) {
                                                                       = 505, p = (int)1e9 + 7;// change this, 1-base
                     int v = to[i];
                                                                  int sizen = 0;
                     if (!m2[v]) {
                                                                  int sub_n=0;
                         while (v)
                                                                  int id[maxn], vertices[maxn], matches[maxn];
                              m2[v] = u, swap
                                                                  bool row_marked
                                  (m1[u], v), u = pr[u];
                                                                      [maxn] = {false}, col_marked[maxn] = {false};
                          ok = 1, ans++;
                                                                  int A[maxn][maxn], B[maxn][maxn], t[maxn][maxn];
                         break;
                                                                  vector<pair<int,int> > sidearr;
                     } else if (!fr[m2[v]])
                                                                  void init(int _n) {
                         q.push(v = m2[v])
                                                                      sizen = _n;
                                                                      sub_n = 0;
                              , fr[v] = fr[u], pr[v] = u;
                                                                      fill(id,id+_n+1,0);
                 }
             }
                                                                      fill(vertices, vertices+_n+1,0);
                                                                      fill(matches, matches+_n+1,0);
        return ans;
                                                                      fill(row_marked,row_marked+_n+1,0);
    }
                                                                      fill(col_marked,col_marked+_n+1,0);
};
                                                                      for(int i=0; i<=_n; i++) {</pre>
                                                                          fill(A[i], A[i]+_n+1,0);
3.14
        KM [6aefd7]
                                                                          fill(B[i],B[i]+_n+1,0);
                                                                          fill(t[i],t[i]+_n+1,0);
struct KM {
    static const int N = 505;
                                                                      sidearr.clear();
    int pr[N], eg[N][N], m1[N], m2[N], n;
    ll lx[N], ly[N], sl[N];
                                                                  Matching(int _n) {
    bool vy[N];
                                                                      init(_n);
    ll ans;
    inline void ini(int _n) {
                                                                  int qpow(int a, int b) {
        n = _n;
        memset(lx + 1, \sim INF, n << 3);
                                                                      int ans = 1;
        memset(ly + 1, 0, n \ll 3);
                                                                      while (b) {
        memset(m1 + 1, 0, n << 2);
                                                                          if (b \& 1) ans = (long long)ans * a % p;
        memset(m2 + 1, 0, n << 2);
                                                                          a = (long long)a * a % p;
                                                                          b >>= 1;
        for (int i = 1; i <= n; i++)</pre>
             memset(eg[i] + 1, \sim INF, n << 2);
                                                                      return ans;
    inline void addedge(int u, int v, int w) {
                                                                  void Gauss(int A[][maxn], int B[][maxn], int n) {
        tmax(eg[u][v], w), tmax(lx[u], (ll)w);
                                                                      if (B) {
                                                                          memset(B, 0, sizeof(t));
    ll getmatch() {
                                                                          for (int i = 1; i <= n; i++) B[i][i] = 1;</pre>
        ans = 0;
        for (int p = 1, u, v; p <= n; p++) {</pre>
                                                                      for (int i = 1; i <= n; i++) {</pre>
             memset(sl + 1, INF, n << 3);
                                                                          if (!A[i][i]) {
             memset(vy + 1, 0, n);
             for (u = p;; u = m2[v], vy[v] = 1) {
    ll mn = 1ll << 60;</pre>
                                                                               for (int j = i + 1; j <= n; j++) {</pre>
                                                                                   if (A[j][i]) {
                 for (int i = 1; i <= n; i++) {</pre>
                                                                                       swap(id[i], id[j]);
                     if (vy[i])
                                                                                       for (int k = i; k <= n; k</pre>
                         continue;
                                                                                            ++) swap(A[i][k], A[j][k]);
                     if (eg[u][i] != ~INF && lx
                                                                                       if (B
                          [v] + ly[i] - eg[v][i] < sl[i]
                                                                                            ) for (int k = 1; k <= n; k
                          sl[i] = lx[u] + ly
                                                                                            ++) swap(B[i][k], B[j][k]);
                                                                                       break;
                              [i] - eg[v][i], pr[i] = v;
                                                                                   }
                     if (sl[i] < mn)
                                                                               }
                         mn = sl[i], v = i;
                                                                               if (!A[i][i]) continue;
                 for (int i = 1; i <= n; i++) {</pre>
                     if (vy[i])
                                                                          int inv = qpow(A[i][i], p - 2);
                         ly[i] += mn, lx[m2[i]] -= mn;
                                                                          for (int j = 1; j <= n; j++) {</pre>
```

sl[i] -= mn;

}

if (i != j && A[j][i]) {

= (long long)A[j][i] * inv % p;

int t

```
for (int k = i; k <= n
                     ; k++) if (A[i][k]) A[j][k] = (
                                                            int matched(int x) {
                                                                 return matches[x];
                     A[j][k] - (ll)t * A[i][k]) % p;
                if (B) {
                    for (int k = 1; k <= n; k++) if</pre>
                          (B[i][k]) B[j][k] = (B[j][
                                                        3.16 Max Clique [2b1496]
                         k] - (ll)t * B[i][k]) % p;
                }
                                                        struct MaxClique { // fast
            }
                                                              when N <= 100, O-base, output sol[N] to get node;
        }
                                                          static const int N = 105;
                                                          bitset<N> G[N], cs[N];
    if (B) {
                                                          int ans, sol[N], q, cur[N], d[N], n;
        for (int i = 1; i <= n; i++) {</pre>
                                                          MaxClique(int _n) {
            int inv = qpow(A[i][i], p - 2);
                                                            n = _n;
            for (int j = 1; j <= n; j++) {</pre>
                                                            for (int i = 0; i < n; ++i) G[i].reset();</pre>
                if (B[i][j]) B[i][j]
                     = (long long)B[i][j] * inv % p;
                                                          void add_edge(int u, int v) {
            }
                                                            G[v][v] = G[v][v] = 1;
        }
   }
                                                          void pre_dfs(vector<int> &r, int l, bitset<N> mask) {
                                                            if (l < 4) {
void eliminate(int r, int c) {
                                                              for (int i : r) d[i] = (G[i] & mask).count();
    row_marked[r] = col_marked[c] = true;
                                                              sort(r.begin(),r.end()
                                                                   , [&](int x, int y) { return d[x] > d[y]; });
    int inv = qpow(B[r][c], p - 2);
    for (int i = 1; i <= sub_n; i++) {</pre>
        if (!row_marked[i] && B[i][c]) {
                                                            vector<int> c(size(r));
            int t = (long long)B[i][c] * inv % p;
                                                            int lft = max(ans - q + 1, 1), rgt = 1, tp = 0;
                                                            cs[1].reset(), cs[2].reset();
            for (int j = 1; j <= sub_n; j++)</pre>
                                                            for (int p : r) {
                if (!col_marked[j] && B[r][j])
                                                              int k = 1;
                    B[i][j] = (B[i][j] - (
                                                              while ((cs[k] \& G[p]).any()) ++k;
                         long long)t * B[r][j]) % p;
                                                              if (k > rgt) cs[++rgt + 1].reset();
        }
                                                              cs[k][p] = 1;
    }
                                                              if (k < lft) r[tp++] = p;
void add_edge(int a,int b) {
                                                            for (int k = lft; k <= rgt; ++k)</pre>
    sidearr.pb(min(a,b),max(a,b));
                                                              for (int p = cs[k]._Find_first
                                                                   (); p < N; p = cs[k]._Find_next(p))
void build_matching() {
                                                                 r[tp] = p, c[tp] = k, ++tp;
    auto rng = mt19937(chrono::steady_clock
                                                            dfs(r, c, l + 1, mask);
        ::now().time_since_epoch().count());
    for(auto e : sidearr) {
                                                          void dfs(vector<</pre>
        int x = e.first;
                                                              int> &r, vector<int> &c, int l, bitset<N> mask) {
        int y = e.second;
                                                            while (!r.empty()) {
        A[x][y] = rng() % p;
                                                              int p = r.back();
        A[y][x] = -A[x][y];
                                                              r.pop_back(), mask[p] = 0;
                                                              if (q + c.back() <= ans) return;</pre>
    for (int i = 1; i <= sizen; i++) id[i] = i;</pre>
                                                              cur[q++] = p;
    memcpy(t, A, sizeof(t));
                                                              vector<int> nr;
    Gauss(A, nullptr, sizen);
                                                              for (int i : r) if (G[p][i]) nr.pb(i);
    for (int i = 1; i <= sizen; i++) {</pre>
                                                              if (!nr.empty()) pre_dfs(nr, l, mask & G[p]);
        if (A[id[i]][id[i]]) vertices[++sub_n] = i;
                                                              else if (q > ans) ans = q, copy_n(cur, q, sol);
                                                              c.pop_back(), --q;
    for (int i = 1; i <= sub_n; i++) {</pre>
                                                            }
        for (int j = 1; j <= sub_n; j++)</pre>
             A[i][j] = t[vertices[i]][vertices[j]];
                                                          int solve() {
                                                            vector<int> r(n);
    Gauss(A, B, sub_n);
                                                            ans = q = 0, iota(r.begin(),r.end(), 0);
    for (int i = 1; i <= sub_n; i++) {</pre>
                                                            pre_dfs(r, 0, bitset<N>(string(n, '1')));
        if (!matches[vertices[i]]) {
                                                            return ans;
            for (int j = i + 1; j <= sub_n; j++) {</pre>
                                                          }
                if (!matches
                                                       |};
                     [vertices[j]] && t[vertices
                                                        3.17 Max Flow [b0a4f0]
                     [i]][vertices[j]] && B[j][i]) {
                    matches[
                                                        struct FLOW {
                         vertices[i]] = vertices[j];
                                                            static const int N = 1e3 + 5, M = N * 10; // change
                    matches[
                                                            int dp[N
                         vertices[j]] = vertices[i];
                                                                 ], cr[N], hd[N], ct = 2, s = 0, t = 1, n, flow;
                     eliminate(i, j);
                                                          FLOW(int _n):n(_n){}
                     eliminate(j, i);
                                                            struct E {
                    break;
                                                                 int to, cap, nxt;
                }
                                                            } eg[M];
            }
                                                            inline void addedge(int u, int v, int w,int d=0) {
        }
                                                                 eg[ct] = \{v, w, hd[u]\};
                                                                hd[v] = ct++;
```

```
eg[ct] = \{u, d, hd[v]\};
        hd[v] = ct++;
    bool bfs() {
        memset(dp, INF, (n + 1) << 2);
        queue<int> q;
        q.push(s), dp[s] = 0;
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (int i = hd[v]; i; i = eg[i].nxt) {
                 const int v = eg[i].to;
                 if (!eg[i].cap || dp[u] + 1 >= dp[v])
                 dp[v] = dp[u] + 1, q.push(v);
            }
        }
        return dp[t] != INF;
    int dfs(int u, int fl) {
        if (u == t)
            return fl;
        int sm = 0;
        for (int &i = cr[u]; i; i = eg[i].nxt) {
            int v = eg[i].to, &w = eg[i].cap;
            if (!w || dp[v] + 1 != dp[v])
                continue
            int tp = dfs(v, min(w, fl - sm));
            w -= tp, sm += tp, eg[i ^ 1].cap += tp;
            if (sm == fl)
                return fl;
        return sm;
    int getflow() {
        flow = 0;
        while (bfs())
            memcpy(cr
                 hd, (n + 1) << 2), flow += dfs(s, INF);
        return flow;
    }
};
        Flow With Demand [160a76]
3.18
struct DMFLOW {
    struct FLOW {
        static const
              int N = 305, M = N \star N \star 12; // change
```

```
int dp[N], cr
    [N], hd[N], ct = 2, s = 0, t = 1, n, flow;
inline void ini(int _n) { n = _n; }
struct E {
    int to, cap, nxt;
} eg[M];
inline void addedge(int u, int v, int w) {
    eg[ct] = \{v, w, hd[u]\};
    hd[v] = ct++;
    eg[ct] = \{u, \theta, hd[v]\};
    hd[v] = ct++;
bool bfs() {
    memset(dp, INF, (n + 1) << 2);
    queue<int> q;
    q.push(s), dp[s] = 0;
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        for (int i = hd[v]; i; i = eq[i].nxt) {
            const int v = eg[i].to;
            if (!eq
                 [i].cap || dp[u] + 1 >= dp[v])
                continue;
            dp[v] = dp[u] + 1, q.push(v);
        }
    return dp[t] != INF;
```

```
int dfs(int u, int fl) {
             if (u == t)
                 return fl;
             int sm = 0:
             for (int &i = cr[u]; i; i = eg[i].nxt) {
                 int v = eg[i].to, &w = eg[i].cap;
                 if (!w || dp[v] + 1 != dp[v])
                     continue;
                 int tp = dfs(v, min(w, fl - sm));
                 w -= tp, sm += tp, eg[i ^ 1].cap += tp;
                 if (sm == fl)
                     return fl;
             return sm;
         int getflow() {
             flow = 0;
             while (bfs())
                 memcpy(cr, hd,
                     (n + 1) << 2), flow += dfs(s, INF);
             return flow:
        }
     } fw;
     int n, sum, s, t;
     inline void ini(int _n) {
         n = _n, fw.ini(fw.t = n + 1), sum = fw.s = 0; }
     inline void addlr(int u, int v, int l, int r) {
         if (l) {
             fw.addedge(u, fw.t, l);
             fw.addedge(fw.s, v, l);
             sum += l:
         if (r - l)
             fw.addedge(u, v, r - l);
     int slv() {
         fw.addedge(t, s, INF);
         int res = fw.getflow();
         if (res != sum)
             return -1;
         fw.s = s, fw.t = t;
         res = fw.getflow();
         // maximum
         // fw.s = t, fw.t = s;
         // res = INF - fw.getflow();
         // minimum
         return sum = res;
    }
|} dmfw;
        MCMF [5190af]
```

3.19

```
struct MCMF {
    static const int N = 5005, M = N * 20;
    struct E {
        int to, cap, co, nxt;
    } eg[M];
    int dp[N], hd[
        N], cr[N], ct = 2, s = 0, t = 1, n, flow, cost;
    bool vd[N];
    inline void ini(int _n) { n = _n; }
    inline void addedge(int u, int v, int w, int c) {
        eg[ct] = \{v, w, c, hd[u]\};
        hd[v] = ct++;
        eg[ct] = \{u, 0, -c, hd[v]\};
        hd[v] = ct++;
    bool spfa() {
        queue<int> q;
        memset(dp, INF, (n + 1) << 2);
        q.push(s), vd[s] = 1, dp[s] = 0;
        while (!q.empty()) {
            int u = q.front();
            q.pop(), vd[u] = 0;
            for (int i = hd[v]; i; i = eg[i].nxt) {
                const int v = eg[i].to, c = eg[i].co;
```

if (u == t)
 return fl;

```
if (!eg[i].cap \mid\mid dp[v] + c >= dp[v])
                                                                        int sm = 0;
                     continue;
                                                                        vd[v] = 1;
                 dp[v] = dp[u] + c;
                                                                        for (int &i = cr[u]; i; i = eg[i].nxt) {
                 if (!vd[v])
                                                                            int &w = eq[
                     vd[v] = 1, q.push(v);
                                                                                 i].cap, v = eg[i].to, c = eg[i].co;
            }
                                                                            if (!w || vd[v] || dp[u] + c != dp[v])
                                                                                continue;
        return dp[t] != INF;
                                                                            int tp = dfs(v, min(fl - sm, w));
                                                                            w -= tp, eg[i ^ 1].cap
                                                                                 += tp, sm += tp, cost += tp * c;
    int dfs(int u, int fl) {
                                                                        }
        if (u == t)
            return fl;
                                                                        vd[u] = 0;
                                                                        return sm;
        int sm = 0;
        vd[v] = 1;
                                                                    pii getflow() {
        for (int &i = cr[u]; i; i = eg[i].nxt) {
                                                                        flow = cost = 0;
            int &w =
                                                                        while (spfa())
                  eg[i].cap, v = eg[i].to, c = eg[i].co;
                                                                            memcpy(cr, hd,
            if (!w || vd[v] || dp[u] + c != dp[v])
                                                                                 (n + 1) << 2), flow += dfs(s, INF);
                 continue
                                                                        return pii(flow, cost);
            int tp = dfs(v, min(fl - sm, w));
                                                                    }
            w -= tp, eg[i ^
                                                                } fw;
                 1].cap += tp, sm += tp, cost += tp * c;
                                                                int n, sfl, sco, s, t;
                                                                void ini(int _n) { n = _n
        vd[u] = 0;
                                                                     , fw.ini(fw.t = n + 1), fw.s = sfl = sco = 0; }
        return sm;
    }
                                                                inline
                                                                    void addlr(int u, int v, int l, int r, int c) {
    pii getflow() {
        flow = cost = 0;
                                                                    if (l) {
        while (spfa())
                                                                        fw.addedge(u, fw.t, l, 0);
            memcpy(cr,
                                                                        fw.addedge(fw.s, v, l, Θ);
                                                                        sco += l * c, sfl += l;
                 hd, (n + 1) << 2), flow += dfs(s, INF);
        return pii(flow, cost);
    }
                                                                    if (r - l)
                                                                        fw.addedge(u, v, r - l, c);
|};
        MCMF With Demand [4c3d71]
3.20
                                                                int slv() {
                                                                    fw.addedge(t, s, INF, 0);
struct DMMCMF {
                                                                    if (sfl != fw.getflow().first)
    struct MCMF {
                                                                        return -1;
        static const int N = 315, M = N * N;
                                                                    return sco += fw.cost;
        struct E {
                                                                }
            int to, cap, co, nxt;
                                                            } dmfw;
        } eg[M];
        int dp[N], hd[N],
                                                            3.21 SCC [ff24f9]
            cr[N], ct = 2, s = 0, t = 1, n, flow, cost;
                                                            struct SCC {
        bool vd[N];
                                                              int n, dft, nscc;
        inline void ini(int _n) { n = _n; }
                                                              vector<int> low, dfn, bln, instk, stk;
        inline
                                                              vector<vector<int>> G;
              void addedge(int u, int v, int w, int c) {
                                                              void dfs(int u) {
            eg[ct] = \{v, w, c, hd[u]\};
                                                                low[u] = dfn[u] = ++dft;
            hd[u] = ct++;
                                                                instk[v] = 1, stk.pb(v);
            eg[ct] = \{u, 0, -c, hd[v]\};
                                                                for (int v : G[u])
            hd[v] = ct++;
                                                                  if (!dfn[v])
                                                                    dfs(v), tmin(low[u], low[v]);
        bool spfa() {
                                                                  else if (instk[v] && dfn[v] < dfn[u])
            queue<int> q;
                                                                    tmin(low[u], dfn[v]);
            memset(dp, INF, (n + 1) << 2);
                                                                if (low[u] == dfn[u]) {
            q.push(s), vd[s] = 1, dp[s] = 0;
                                                                  for (; stk.back() != u; stk.pop_back())
            while (!q.empty()) {
                                                                    bln[stk.back()] = nscc, instk[stk.back()] = 0;
                 int u = q.front();
                                                                  instk[u] = 0, bln[u] = nscc++, stk.pop_back();
                 q.pop(), vd[v] = 0;
                 for (int i = hd[v]; i; i = eg[i].nxt) {
                                                                }
                     const
                                                              SCC(int _n): n(_n), low(n), bln(n), G(n) {}
                         int v = eg[i].to, c = eg[i].co;
                                                              void add_edge(int u, int v) { G[u].pb(v); }
                     if (!eg
                                                              void slv() {
                         [i].cap || dp[u] + c >= dp[v])
                                                                dfn.assign(n, 0), instk = dfn, dft = nscc = 0;
                         continue;
                     dp[v] = dp[u] + c;
                                                                for (int i = 0; i < n; ++i)</pre>
                                                                  if (!dfn[i]) dfs(i);
                     if (!vd[v])
                         vd[v] = 1, q.push(v);
                                                           |}; // scc_id(i): bln[i]
                 }
            }
                                                            3.22 SPFA [Oad2fd]
            return dp[t] != INF;
                                                           | struct SPFA {
        int dfs(int u, int fl) {
                                                                int n;
```

vector<ll> d;

vector<vector<pair<int, ll>>> adj;

```
SPFA(int _n
        ) : n(_n), adj(_n, vector<pair<int, ll>>(0)) {}
    void add_edge
        (int u, int v, ll w) { adj[u].pb(v, w); }
    bool go(int s) {
        vector<int> cnt(n, 0), inq(n, 0);
        queue<int> q;
        d.assign(n, LONG_LONG_MAX);
        d[s] = 0, inq[s] = 1, q.emplace(s);
        while (!q.empty()) {
            int u = q.front();
            q.pop(), inq[v] = 0;
            for (auto [v, w] : adj[u]) {
                if (d[v] > d[u] + w) {
                    if (++cnt[v] >= n)
                        return 0; // negative cycle
                    d[v] = d[u] + w;
                    if (!inq[v])
                         q.emplace(v), inq[v] = 1;
                }
            }
        return 1:
    }
};
```

3.23 2-SAT [710518]

```
struct TwoSAT { // SCC needed
  vector<bool> istrue;
  SCC scc:
  TwoSAT(int _n) : n(_n), scc(n + n) { }
  int rv(int a) { return a >= n ? a - n : a + n; }
  void add_clause(int a, int b) {
    scc.add_edge(rv(a), b);
    scc.add_edge(rv(b), a);
  }
  bool slv() {
    scc.slv(), istrue.assign(n + n, 0);
    for (int i = 0; i < n; ++i) {</pre>
      if (scc.bln[i] == scc.bln[i + n]) return 0;
       istrue[i] = scc.bln[i] < scc.bln[i + n];</pre>
      istrue[i + n] = !istrue[i];
    return 1;
  }
|};
```

4 Math

4.1 Big Interger [4347d6]

```
#undef size
template<typename T>
inline string to_string(const T& x){
 stringstream ss;
 return ss<<x,ss.str();</pre>
struct bigN:vector<ll>{
 const static int base=1000000000, width=log10(base);
  bool negative;
 bigN(const_iterator
       a,const_iterator b):vector<ll>(a,b){}
 bigN(string s){
    if(s.empty())return;
    if(s[0]=='-')negative=1,s=s.substr(1);
    else negative=0;
    for(int i=int(s.size())-1;i>=0;i-=width){
      ll t=0;
      for(int j=max(0,i-width+1);j<=i;++j)</pre>
        t=t*10+s[j]-'0';
      push_back(t);
    }
    trim();
  template<typename T>
    bigN(const T &x):bigN(to_string(x)){}
```

```
bigN():negative(0){}
void trim(){
  while(size()&&!back())pop_back();
  if(empty())negative=0;
void carry(int _base=base){
  for(size_t i=0;i<size();++i){</pre>
    if(at(i)>=0&&at(i)<_base)continue;</pre>
    if(i+1u==size())push_back(0);
    int r=at(i)%_base;
    if(r<0)r+=_base;</pre>
    at(i+1)+=(at(i)-r)/_base,at(i)=r;
  }
}
int abscmp(const bigN &b)const{
  if(size()>b.size())return 1;
  if(size()<b.size())return -1;</pre>
  for(int i=int(size())-1;i>=0;--i){
    if(at(i)>b[i])return 1;
    if(at(i)<b[i])return -1;</pre>
  return 0;
}
int cmp(const bigN &b)const{
  if(negative!=b.negative)return negative?-1:1;
  return negative?-abscmp(b):abscmp(b);
bool operator<(const bigN&b)const{return cmp(b)<0;}</pre>
bool operator>(const bigN&b)const{return cmp(b)>0;}
bool operator<=(const bigN&b)const{return cmp(b)<=0;}</pre>
bool operator>=(const bigN&b)const{return cmp(b)>=0;}
bool operator==(const bigN&b)const{return !cmp(b);}
bool operator!=(const bigN&b)const{return cmp(b)!=0;}
bigN abs()const{
  bigN res=*this;
  return res.negative=0, res;
bigN operator-()const{
  bigN res=*this;
  return res.negative=!negative,res.trim(),res;
bigN operator+(const bigN &b)const{
  if(negative)return -(-(*this)+(-b));
  if(b.negative)return *this-(-b);
  bigN res=*this;
  if(b.size()>size())res.resize(b.size());
  for(size_t i=0;i<b.size();++i)res[i]+=b[i];</pre>
  return res.carry(),res.trim(),res;
bigN operator-(const bigN &b)const{
  if(negative)return -(-(*this)-(-b));
  if(b.negative)return *this+(-b);
  if(abscmp(b)<0)return -(b-(*this));</pre>
  bigN res=*this;
  if(b.size()>size())res.resize(b.size());
  for(size_t i=0;i<b.size();++i)res[i]-=b[i];</pre>
  return res.carry(),res.trim(),res;
bigN operator*(const bigN &b)const{
  bigN res;
  res.negative=negative!=b.negative;
  res.resize(size()+b.size());
  for(size_t i=0;i<size();++i)</pre>
    for(size_t j=0;j<b.size();++j)</pre>
      if((res[i+j]+=at(i)*b[j])>=base){
        res[i+j+1]+=res[i+j]/base;
        res[i+j]%=base;
      }
  return res.trim(),res;
bigN operator/(const bigN &b)const{
  int norm=base/(b.back()+1);
  bigN x=abs()*norm;
  bigN y=b.abs()*norm;
  bigN q,r;
```

```
q.resize(x.size());
                                                                }
    for(int i=int(x.size())-1;i>=0;--i){
                                                                 friend
                                                                     mint operator/(mint const &a, mint const &b) {
      r=r*base+x[i];
      int s1=r.size()<=y.size()?0:r[y.size()];</pre>
                                                                    return mint(a) /= b;
      int s2=r.size()<y.size()?0:r[y.size()-1];</pre>
                                                                 friend ostream
      int d=(ll(base)*s1+s2)/y.back();
      r=r-y*d;
                                                                      &operator<<(ostream &os, mint const &m) {
      while(r.negative)r=r+y,--d;
                                                                    return os << m.v;</pre>
      q[i]=d;
                                                                 friend istream &operator>>(istream &is, mint &m) {
    q.negative=negative!=b.negative;
                                                                    return is >> m.v;
   return q.trim(),q;
                                                           };
 bigN operator%(const bigN &b)const{
                                                           4.3 Fraction [9c92bf]
    return *this-(*this/b)*b;
                                                           struct frac {
                                                                ll n, d;
 friend istream& operator>>(istream &ss,biqN &b){
                                                                frac(const
   string s:
   return ss>>s, b=s, ss;
                                                                     ll &_n = 0, const ll &_d = 1) : n(_n), d(_d) {
 }
                                                                    ll t = \_gcd(n, d);
 friend
                                                                    n /= t, d /= t;
       ostream& operator<<(ostream &ss,const bigN &b){</pre>
                                                                    if (d < 0)
    if(b.negative)ss<<'-';</pre>
                                                                        n = -n, d = -d;
    ss<<(b.empty()?0:b.back());
    for(int i=int(b.size())-2;i>=0;--i)
                                                                frac operator-() const {
      ss<<setw(width)<<setfill('0')<<b[i];</pre>
                                                                    return frac(-n, d);
    return ss;
                                                                frac operator+(const frac &b) const {
 template<typename T>
                                                                    return frac(n * b.d + b.n * d, d * b.d);
   operator T(){
     stringstream ss;
                                                                void operator+=(const frac &b) {
      ss<<*this;
                                                                    *this = frac(n * b.d + b.n * d, d * b.d);
      T res;
      return ss>>res,res;
                                                                frac operator-(const frac &b) const {
                                                                    return frac(n * b.d - b.n * d, d * b.d);
                                                                }
#define size(x) (int)(x).size()
                                                                void operator-=(const frac &b) {
4.2 Mod Int [c34f76]
                                                                    *this = frac(n * b.d - b.n * d, d * b.d);
                                                                }
template <unsigned P>
                                                                frac operator*(const frac &b) const {
struct mint { // P not prime break /=
                                                                    return frac(n * b.n, d * b.d);
    unsigned v;
                                                                }
     mint(ll v = 0) : v((v%P+P) % P) {}
                                                                void operator*=(const frac &b) {
     mint &operator+=(mint const &o) {
                                                                    *this = frac(n * b.n, d * b.d);
        V = (V += 0.V) >= P ? V - P : V;
                                                                }
        return *this;
                                                                frac operator/(const frac &b) const {
                                                                    return frac(n * b.d, d * b.n);
     mint & operator -= (mint const & o) {
        v = (v < o.v) ? v + P - o.v : v - o.v;
                                                                void operator/=(const frac &b) {
        return *this;
                                                                    *this = frac(n * b.d, d * b.n);
    mint &operator*=(mint const &o) {
        v = 111 * v * o.v % P;
                                                                friend ostream
        return *this;
                                                                     &operator<<(ostream &os, frac const &f) {
                                                                    if (f.d == 1)
                                                                        return os << f.n;
                                                                    return os << f.n << '/' << f.d;
         mint operator+(mint const &a, mint const &b) {
        return mint(a) += b;
   }
                                                                friend istream &operator>>(istream &is, frac &f) {
                                                                    istream &tp = is >> f.n >> f.d;
                                                                    f = frac(f.n, f.d);
         mint operator-(mint const &a, mint const &b) {
                                                                    return tp;
        return mint(a) -= b;
                                                                }
                                                           };
     friend
         mint operator*(mint const &a, mint const &b) {
                                                           4.4 FWT [02d887]
        return mint(a) *= b;
                                                           struct Fast_Walsh_Transform { // Modint needed
                                                                string op; // and, or, xor
     inline mint pow(ll n) const {
                                                                void fwt(vector<mint> &v, bool ifwt) {
        mint r(1);
                                                                    int n = __lg(size(v));
        mint a = v:
                                                                    mint iv2 = mint(1) / 2;
        for (; n; a *= a, n >>= 1)
                                                                    for (int i = 0; i < n; ++i)</pre>
           r *= (n & 1) ? (a) : (mint(1));
        return r;
                                                                        for (int j = 0; j < 1 << n; ++j)</pre>
                                                                            if (op == "and" && (~j >> i &
    }
     mint &operator/=(mint const &o) {
                                                                                1) || op == "or" && (j >> i & 1)) {
        *this *= o.pow(P - 2);
                                                                                if (!ifwt)
                                                                                    v[j] += v[j ^ (1 << i)];
        return *this;
```

```
else
                         v[j] -= v[j ^ (1 << i)];
                 } else
                      if (op == "xor" && (j >> i & 1)) {
                     mint x = v[j ^ (1 << i)], y = v[j];
                     if (!ifwt)
                         v[j ^ (1 <<
                              i)] = x + y, v[j] = x - y;
                     else
                         v[j ^ (1 << i)] = (x + y) *
                              iv2, v[j] = (x - y) * iv2;
                 }
    vector<mint> v1, v2; // size(v1) = size(v2) = 2^k
    Fast_Walsh_Transform(const vector
         <mint> &_v1, const vector<mint> &_v2, const
          string &_op) : v1(_v1), v2(_v2), op(_op) {}
    vector<mint> solve
         () { // ans_k = \sum_{i=0}^{k} a_i * b_j
        fwt(v1, 0), fwt(v2, 0);
        for (int i = 0; i < size(v1); ++i)</pre>
             v1[i] *= v2[i];
         fwt(v1, 1);
        return v1;
    }
|};
```

4.5 FFT [c93fdc]

```
typedef complex<double> cd;
struct FFT {
#define M_PI 3.14159265358979323846264338327950288
    static const int K = 19, N = 1 << K; // change
    cd pl[N];
    int rv[N];
    void dft(vector<cd> &ar) {
        int n = size(ar), k = log2(n);
        if (n <= 1)
            return;
        for (int i = 1; i < n; i++)</pre>
            if (i < rv[i] >> (K - k))
                 swap(ar[i], ar[rv[i] >> (K - k)]);
        cd a, b;
        for (int l = 1; l < n; l <<= 1) {</pre>
            for (int i = 0; i < n; i += l << 1) {</pre>
                 for (int j = 0; j < l; j++) {</pre>
                     a = ar[i + j],
                          b = ar[i + j + l] * pl[j + l];
                     ar[i + j] = a + b;
                     ar[i + j + l] = a - b;
                 }
            }
        }
    void idft(vector<cd> &ar) {
        double n = size(ar);
        reverse(ar.begin() + 1, ar.end());
        for (cd &i : ar)
            i /= n;
        dft(ar);
    vector<cd> pmul(vector<cd> a, vector<cd> b) {
        int n = size(a) + size(b) - 1;
        while (n & (n - 1))
            n += lowbit(n);
        a.resize(n), b.resize(n);
        dft(a), dft(b);
        for (int i = 0; i < n; i++)</pre>
            a[i] *= b[i];
        idft(a), a.resize(n);
        return a;
    FFT() {
        pl[1] = polar(1.0, 0.0);
        for (int k = 2; k < N; k <<= 1)</pre>
            for (int i = k; i < k << 1; i++)</pre>
```

};

```
14
                  pl[i] = polar(1.0,
                       2.0 * M_PI * (i - k) / (k * 2.0));
         for (int i = 1, hb = -1; i < N; i++) {</pre>
             if (!(i & (i - 1)))
                  hb++;
             rv[i] =
                   rv[i ^ (1 << hb)] | 1 << (K - 1 - hb);
         }
     }
|};
 4.6
       NTT [5af390]
const int M = 998244353;
 typedef mint<M> mi;
 struct NTT {
     static const int K = 20, N = 1 << K;
     mi pl[N];
     int rv[N];
     void dft(vector<mi> &ar) {
         static int n, k;
         n = size(ar), k = log2(n);
         if (n <= 1)
             return;
         for (int i = 1; i < n; i++)</pre>
             if (i < rv[i] >> (K - k))
                  swap(ar[i], ar[rv[i] >> (K - k)]);
         static mi a, b;
         for (int l = 1; l < n; l <<= 1) {</pre>
             for (int i = 0; i < n; i += l << 1) {</pre>
                  for (int j = 0; j < l; j++) {</pre>
                      a = ar[i + j],
                           b = ar[i + j + l] * pl[j + l];
                      ar[i + j] = a + b;
                      ar[i + j + l] = a - b;
                  }
             }
         }
     }
     void idft(vector<mi> &ar) {
         static mi ivn;
         ivn.v = 1, ivn /= size(ar);
         reverse(ar.begin() + 1, ar.end());
         for (mi &i : ar)
             i *= ivn;
         dft(ar);
     }
   template<typename T>
     T pmul(T a, T b) {
         static int n;
         n = size(a) + size(b) - 1;
         while (n & (n - 1))
             n += lowbit(n);
         a.resize(n), b.resize(n);
         dft(a), dft(b);
         for (int i = 0; i < n; i++)</pre>
             a[i] *= b[i];
         idft(a), a.resize(n);
         return a;
     }
     NTT() {
         pl[1] = 1;
         for (int k = 1; k < K; k++) {</pre>
             mi \ omega = mi(3).pow((M - 1) >> (k + 1));
             for (int i = 1 << (k - 1); i < 1 << k; i++)</pre>
                  pl[i * 2] = pl
                      [i], pl[i * 2 + 1] = pl[i] * omega;
         for (int i = 1, hb = -1; i < N; i++) {
             if (!(i & (i - 1)))
                  hb++;
             rv[i] =
                   rv[i ^ (1 << hb)] | 1 << (K - 1 - hb);
         }
     }
```

4.7 Polynomial [048b32]

```
template<typename T>
struct Poly:vector<T>{
 using vector<T>::vector;
  static NTT con;
 Poly(const Poly &p,int m): vector<T>(m){
    copy_n(p.data(),min(size(p),m),this->data());
 Poly& isz(int m) { return this->resize(m), *this; }
 Poly operator+(T const &b){
   Poly ret = Poly(*this, size(*this));
    ret[0]+=b;
   return ret;
 }-
 Poly operator*(T const &b){
   Poly ret = Poly(*this, size(*this));
    for(int i=0;i<size(ret);i++) ret[i]*=b;</pre>
    return ret;
 Poly operator+(Poly &b){
    Poly ret = Poly(*this, max(size(b), size(*this)));
    for(int i=0;i<size(ret);i++) ret[i]+=b[i];</pre>
    return ret;
 Poly operator*(Poly b){
   return con.pmul(*this,b);
 Poly dx() {
   Poly ret(size(*this)-1);
        =0;i<size(ret);i++) ret[i]=T(i+1)*(*this)[i+1];
    ret.resize(max(1,size(ret)));
    return ret;
 Poly ix() {
   Poly ret(size(*this) + 1);
    for(int i=1;i<size</pre>
        (ret); i++) ret[i] = T(1)/T(i) * (*this)[i-1];
   return ret;
 }
 Poly inv() {
    int n = size(*this);
    if(n==1) return {T(1)/(*this)[0]};
    int m = n<<1;
    while(m^lowbit(m)) m+=lowbit(m);
   Poly xi = Poly(*this,(n+1)/2).inv().isz(m);
   Poly yi(*this,m);
   con.dft(xi);con.dft(yi);
    for(int i=0;i<m;i++){</pre>
      xi[i] = xi[i]*(mi(2)-yi[i]*xi[i]);
    con.idft(xi);
   return xi.isz(n);
 Poly ln(){
    int n = size(*this);
   Poly ret = (*this).dx();
    Poly inv = (*this).inv();
   ret = ret*inv;
    ret.resize(n);
    return ret.ix().isz(n);
 }
 Poly exp(){
    int n = size(*this);
    if(n==1) return {T(1)};
    Poly xi = Poly(*this,(n+1)/2).exp().isz(n);
   Poly yi = xi.ln();yi[0]=T(-1);
    for(int i=0;i<n;i++) yi[i] = (*this)[i]-yi[i];</pre>
   return (xi*yi).isz(n);
 Poly pow(T k){
   Poly d = (*this).ln();
    d = d*k;
    d = d.exp();
   return d;
```

```
}
};
template<typename T>
NTT Poly<T>::con;
4.8 Bit Conv [f7735d]
template <typename T>
inline void tozero(vector<T> &a, int n, int d) {
     d = 1 << d;
    for (int i = 0; i < 1 << n; i += d << 1) {</pre>
         for (int j = 0; j < d; j++) {</pre>
             a[i + j] += a[i + j + d];
             a[i + j + d] = 0;
         }
    }
template <typename T>
inline void flip(vector<T> &a, int n, int d) {
     d = 1 << d;
     for (int i = 0; i < 1 << n; i += d << 1) {</pre>
         for (int j = 0; j < d; j++) {</pre>
             swap(a[i + j], a[i + j + d]);
    }
}
template <typename T>
vector<T> GCONV
     (vector<T> ar, vector<T> br, vector<string> ops) {
     int n = size(ops);
     ar.resize(1 << n), br.resize(1 << n);
     vector<int> op(n, 0);
     int fg = 0;
     for (int d = 0; d < n; d++) {</pre>
         if (ops[d][0] == '1') {
             fg ^= (1 << d);
             for (int i = 0; i < 4; i++)</pre>
                 ops[d][i] = '0' + '1' - ops[d][i];
         if (ops[d] == "0000")
             tozero(
                 ar, n, d), tozero(br, n, d), op[d] = 0;
         else if (ops[d] == "0001")
             op[d] = 1;
         else if (ops[d] == "0010")
             flip(br, n, d), op[d] = 1;
         else if (ops[d] == "0011")
             tozero(br, n, d), op[d] = 2;
         else if (ops[d] == "0100")
             flip(ar, n, d), op[d] = 1;
         else if (ops[d] == "0101")
             tozero(ar, n, d), op[d] = 2;
         else if (ops[d] == "0110")
             op[d] = 3;
         else
             op[d] = 2;
         FWT(ar
             , n, d, op[d], 0), FWT(br, n, d, op[d], 0);
     for (int i = 0; i < 1 << n; i++)</pre>
         ar[i] *= br[i];
     for (int d = n - 1; d >= 0; d--)
         FWT(ar, n, d, op[d], 1);
     for (int i = 0; i < 1 << n; i++)</pre>
         if (i < (i ^ fg))
             swap(ar[i], ar[i ^ fg]);
     return ar:
}
       Miller Rabin [67a711]
| bool isPrime(const uint64_t n) {
  if (n < 2 || n % 6 % 4 != 1) return (n | 1) == 3;
  uint64_t A[] = \{2,
        325, 9375, 28178, 450775, 9780504, 1795265022},
  s = __builtin_ctzll(n-1), D = n >> s;
  for (auto a : A) {
```

4.10 Pollard' s Rho [938b8b]

```
|ll PollardRho(
     ll x) \{//\text{ get a factor of } x(\text{not prime}) \text{ in } 0(x^0.25)
   if(x%2==0) return 2;
   if(x%3==0) return 3;
     ll s = 0, t = 0;
     ll c = (ll) rand() % (x - 1) + 1;
     int step = 0, g = 1;
     ll\ val = 1;
     for (g = 1;; g <<= 1, s = t, val = 1) {</pre>
         for (step = 1; step <= g; ++step) {</pre>
              t = (__int128(t)*t+c)%x;
              val = \__int128(val) * abs(t - s) % x;
              if ((step % 127) == 0) {
                  ll d = \_gcd(val, x);
                  if (d > 1) return d;
              }
         ll d = \_gcd(val, x);
         if (d > 1) return d;
     }
}
```

4.11 Discrete Log [78c47f]

```
int mod_log(int a, int b, int m) {
  if(b==1%m) return 0;
    int n = int(ceil(sqrt(m)));
    int e = 0;
    int k = 1:
     for (int g; (g = gcd(a, m)) != 1;) {
         if (b % g != 0) return -1;
         b /= g; m /= g;
         e++:
    k = (1LL*k*(a/g))%m;
         if (b == k) return e;
    }
    int x = 1:
    unordered_map<int, int> map_;
    for (int q = 0; q < n; q++, x = (1LL*x*a)%m) {
         map_{[(1LL*x*b)%m]} = q;
    int y = x;
    for (int p = 1; p <= n; p++, y = (1LL*y*x)%m) {</pre>
         if (auto it =
              map_.find((1LL*y*k)%m); it != end(map_)) {
             return int(p) * n - it->second + e;
         }
    return -1;
| }
```

4.12 Exgcd/CRT [f45f4d]

```
// find x,y such that ax+by=gcd(a,b)
|ll exgcd(ll a, ll b, ll &x, ll &y) {
    if (!b) return x = 1, y = 0, a;
    ll d = exgcd(b, a % b, y, x);
    return y -= a/b * x, d;
|}
|ll CRT(int k, ll* a, ll* r) {
    ll n = 1, ans = 0;
    for (int i = 1; i <= k; i++) n = n * r[i];
    for (int i = 1; i <= k; i++) {
        ll m = n / r[i], b, y;
        exgcd(m, r[i], b, y); // b * m mod r[i] = 1
        ans = (ans + a[i] * m * b % n) % n;</pre>
```

4.13 Semi-Euclid [e7979f]

```
|//0~(n-1)!!!! sum floor((ax+b)/m)
|ll semiEuclid(ll a,ll b,ll m,ll n){
| if(a==0) return (b/m)*(n);
| if(a >= m or b >= m) return n*(
| n-1)/2*(a/m) + n*(b/m) + semiEuclid(a%m,b%m,m,n);
| ll l = (a*(n-1)+b)/m;
| return l*(n-1) - semiEuclid(m,m-b-1,a,l);
|}
```

4.14 LP

Primal	Dual
Maximize $c^{T}x$ s.t. $Ax \leq b$, $x \geq 0$	Minimize $b^{T}y$ s.t. $A^{T}y \ge c, y \ge 0$
Maximize $c^{T}x$ s.t. $Ax \leq b$	Minimize $b^{T}y$ s.t. $A^{T}y = c, y \ge 0$
Maximize $c^{T}x$ s.t. $Ax = b, x \ge 0$	Minimize $b^{T}y$ s.t. $A^{T}y \ge c$

 $\overline{\mathbf{x}}$ and $\overline{\mathbf{y}}$ are optimal if and only if for all $i \in [1,n]$, either $\overline{x}_i = 0$ or $\sum_{j=1}^m A_{ji} \overline{y}_j = c_i$ holds and for all $i \in [1,m]$ either $\overline{y}_i = 0$ or $\sum_{j=1}^n A_{ij} \overline{x}_j = b_j$ holds.

```
1. In case of minimization, let c_i' = -c_i
2. \sum_{1 \leq i \leq n} A_{ji} x_i \geq b_j \rightarrow \sum_{1 \leq i \leq n} -A_{ji} x_i \leq -b_j
```

- 3. $\sum_{1 \leq i \leq n} A_{ji} x_i = b_j$
- 4. If x_i has no lower bound, replace x_i with $x_i x_i'$

4.15 Simplex [6b4566]

```
const int MAXN = 11000, MAXM = 405;
const double eps = 1E-10;
double a[MAXN][MAXM], b[MAXN], c[MAXM];
double d[MAXN][MAXM], x[MAXM];
int ix[MAXN + MAXM]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
// usage :
// value = simplex(a, b, c, N, M);
double simplex(int n, int m){
  ++m;
  fill_n(d[n], m + 1, 0);
  fill_n(d[n + 1], m + 1, 0);
  iota(ix, ix + n + m, \theta);
  int r = n, s = m - 1;
  for (int i = 0; i < n; ++i) {</pre>
    for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i][j];</pre>
    d[i][m - 1] = 1;
    d[i][m] = b[i];
    if (d[r][m] > d[i][m]) r = i;
  copy_n(c, m - 1, d[n]);
  d[n + 1][m - 1] = -1;
  for (double dd;; ) {
    if (r < n) {
      swap(ix[s], ix[r + m]);
       d[r][s] = 1.0 / d[r][s];
      for (int j = 0; j <= m; ++j)</pre>
         if (j != s) d[r][j] *= -d[r][s];
      for (int i = 0; i <= n + 1; ++i) if (i != r) {</pre>
         for (int j = 0; j <= m; ++j) if (j != s)</pre>
           d[i][j] += d[r][j] * d[i][s];
         d[i][s] *= d[r][s];
      }
    r = s = -1;
    for (int j = 0; j < m; ++j)</pre>
      if (s < 0 || ix[s] > ix[j]) {
         if (d[n + 1][j] > eps ||
             (d[n + 1][j] > -eps \&\& d[n][j] > eps))
           s = j;
    if (s < 0) break;
```

```
for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {</pre>
       if (r < 0 ||
           (dd = d[r][m]
                 / d[r][s] - d[i][m] / d[i][s]) < -eps ||
           (dd < eps \&\& ix[r + m] > ix[i + m]))
     if (r < 0) return -1; // not bounded
  }
   if (d[n + 1][m] < -eps) return -1; // not executable</pre>
   double ans = 0;
   fill_n(x, m, 0);
   for (int i = m; i <
        n + m; ++i) { // the missing enumerated x[i] = 0
     if (ix[i] < m - 1){</pre>
       ans += d[i - m][m] * c[ix[i]];
       x[ix[i]] = d[i-m][m];
     }
   return ans;
| }
```

4.16 Theorem

- LTE Lemma $\nu_p(x^n-y^n)=\nu_p(x-y)+\nu_p(n), \ \mbox{if} \ p|x-y.$ $\nu_2(x^n-y^n)=\nu_2(x-y)+\nu_2(n), \ \mbox{if} \ 4|x-y.$ $\nu_2(x^n-y^n)=\nu_2(x-y)+\nu_2(x+y)+\nu_2(n)-1, \ \mbox{if} \ 2|x-y \ \mbox{and} \ n \ \mbox{is even}.$ $\nu_p(x^n+y^n) = \nu_p(x+y) + \nu_p(n)$, if p|x+y and n is odd. $\nu_2(x^n+y^n) = 1$, if 2|x+y and n is even. $\nu_2(x^n+y^n)=\nu(x+y)$ if 2|x+y and n is odd.
- Cramer's rule

Vandermonde's Identity

$$C(n+m,k) = \sum_{i=0}^{k} C(n,i)C(m,k-i)$$

Kirchhoff's Theorem

Denote L be a $n \times n$ matrix as the Laplacian matrix of graph G, where $L_{ii} = d(i)$, $L_{ij} = -c$ where c is the number of edge (i,j) in G.

- The number of undirected spanning in G is $|\det(\tilde{L}_{11})|$.
- The number of directed spanning tree rooted at r in G is $|\det(\tilde{L}_{rr})|$.
- Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij} = x_{ij}$ (x_{ij} is chosen uniformly at random) if i < j and $(i,j) \in E$, otherwise $d_{ij} = -d_{ji}$. $\frac{rank(D)}{2}$ is the maximum matching on G.

- Cayley's Formula
 - Given a degree sequence d_1, d_2, \dots, d_n for each labeled vertices, there are $\frac{(n-2)!}{(d_1-1)!(d_2-1)!\cdots(d_n-1)!}$ spanning trees.
 - Let $T_{n,k}$ be the number of labeled forests on n vertices with k components, such that vertex 1,2,...,k belong to different components. Then $T_{n,k}=kn^{n-k-1}$.
- Erd⊠s–Gallaitheorem

A sequence of nonnegative integers $d_1 \ge \cdots \ge d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only

if
$$d_1+\cdots+d_n$$
 is even and $\sum_{i=1}^k d_i \leq k(k-1)+\sum_{i=k+1}^n \min(d_i,k)$ holds for

every $1 \le k \le n$.

A pair of sequences of nonnegative integers $a_1 \ge \cdots \ge a_n$ and b_1, \dots, b_n

is bigraphic if and only if $\sum_{i=1}^n a_i = \sum_{i=1}^n b_i$ and $\sum_{i=1}^k a_i \leq \sum_{i=1}^n \min(b_i,k)$ holds

for every $1 \le k \le n$. Fulkerson-Chen-Ansteetheorem

A sequence $(a_1, b_1), \ldots, (a_n, b_n)$ of nonnegative integer pairs with $a_1 \geq \cdots \geq a_n$ is digraphic if and only if $\sum_{i=1}^n a_i = \sum_{i=1}^n b_i$ and

$$\sum_{i=1}^k a_i \leq \sum_{i=1}^k \min(b_i,k-1) + \sum_{i=k+1}^n \min(b_i,k) \operatorname{holds} \operatorname{for \, every} 1 \leq k \leq n.$$

· Pick' stheorem

For simple polygon, when points are all integer, we have $A = \#\{\text{lattice points in the interior}\} + \frac{\#\{\text{lattice points on the boundary}\}}{2} - 1.$

- Möbius inversion formula
 - $f(n) = \sum_{d|n} g(d) \Leftrightarrow g(n) = \sum_{d|n} \mu(d) f(\frac{n}{d})$
 - $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

- Sphericalcap
 - Aportion of a sphere cut off by a plane.
 - r: sphere radius, a: radius of the base of the cap, h: height of the cap,
 - Volume = $\pi h^{2}(3r h)/3 = \pi h(3a^{2} + h^{2})/6 = \pi r^{3}(2 + \cos\theta)(1 \sin\theta)$ $\cos\theta)^2/3$.
 - Area = $2\pi rh = \pi(a^2 + h^2) = 2\pi r^2(1 \cos\theta)$.
- Lagrange multiplier
 - Optimize $f(x_1,...,x_n)$ when k constraints $g_i(x_1,...,x_n) = 0$.
 - Lagrangian function $\mathcal{L}(x_1, \dots, x_n, \lambda_1, \dots, \lambda_k) = f(x_1, \dots, x_n)$
 - $\sum_{i=1}^{\bar{k}} \lambda_i g_i(x_1,...,x_n)$. The solution corresponding to the original constrained optimization. tion is always a saddle point of the Lagrangian function.
- Nearest points of two skew lines
 - Line 1: $v_1 = p_1 + t_1 d_1$
 - Line 2: $v_2 = p_2 + t_2 d_2$
 - $\boldsymbol{n} = \boldsymbol{d}_1 \times \boldsymbol{d}_2$
 - $\boldsymbol{n}_1 = \boldsymbol{d}_1 \times \boldsymbol{n}$
 - $\boldsymbol{n}_2 = \boldsymbol{d}_2 \times \boldsymbol{n}$
 - $c_1 = p_1 + \frac{(p_2 p_1) \cdot n_2}{d_1 \cdot n_2} d_1$
 - $-c_2 = p_2 + \frac{(p_1 p_2) \cdot n_1}{d_2 \cdot n_1} d_2$
- Derivatives/Integrals

Integration by parts:
$$\int_{a}^{b} f(x)g(x)dx = [F(x)g(x)]_{a}^{b} - \int_{a}^{b} F(x)g'(x)dx \\ \left| \frac{d}{dx} \sin^{-1}x = \frac{1}{\sqrt{1-x^{2}}} \right| \frac{d}{dx} \cos^{-1}x = -\frac{1}{\sqrt{1-x^{2}}} \left| \frac{d}{dx} \tan^{-1}x = \frac{1}{1+x^{2}} \right| \\ \frac{d}{dx} \tan x = 1 + \tan^{2}x \qquad \int \tan ax = -\frac{\ln|\cos ax|}{a} \\ \int e^{-x^{2}} = \frac{\sqrt{\pi}}{2} \operatorname{erf}(x) \left| \int xe^{ax}dx = \frac{e^{ax}}{a^{2}} (ax - 1) \right| \\ \int \sqrt{a^{2} + x^{2}} = \frac{1}{2} \left(x\sqrt{a^{2} + x^{2}} + a^{2} \operatorname{asinh}(x/a) \right)$$

Spherical Coordinate

$$(x,y,z) = (r\sin\theta\cos\phi, r\sin\theta\sin\phi, r\cos\theta)$$

$$(r,\theta,\phi) = (\sqrt{x^2 + y^2 + z^2}, a\cos(z/\sqrt{x^2 + y^2 + z^2}), a\tan(y,x))$$

Rotation Matrix

$$M(\theta)\!=\!\begin{bmatrix}\!\cos\!\theta & -\!\sin\!\theta \\ \!\sin\!\theta & \!\cos\!\theta \end{bmatrix}\!,\!R_x(\theta_x)\!=\!\begin{bmatrix} 1 & 0 & 0 \\ 0 & \!\cos\!\theta_x & -\!\sin\!\theta_x \\ 0 & \!\sin\!\theta & \!\cos\!\theta \end{bmatrix}$$

- Pell' s equation $x^2 ny^2 = 1 \Rightarrow \text{let } x_1, y_1 \text{ be the smallest solution: the}$ other solution has the form $x_i+y_i\sqrt{n}=(x_1+y_1\sqrt{n})^i$ $(x_1,y_1$ can be found by continuous fraction expansion of \sqrt{n}
- Lucas' Theorem

$$\binom{n}{i} \equiv \prod_{i=0}^{m} \binom{n_j}{i_j} \pmod{p}$$

where a_j is a 's representation in p-base

Cipolla's algorithm find $a \Rightarrow (\frac{a^2-n}{p}) = -1$ (legendre symbol) and calculate $(a+\sqrt{a^2-n})^{(p+1)/2}$ in the field $(F)_p(\sqrt{a^2-n})$, that will be a solution.(note: p=2 need to be seperate out)

String

5.1 AC auto [0852a8]

```
struct ACauto {
    const static int N = 2e5 + 5; // change
    int tr
        [26][N], fail[N], ctn = 1, cnt[N], endat[N], n;
    vector<int> top; // fail tree topological order
    inline void clr(int p) {
        fail[p] = cnt[p] = 0;
        for (int i = 0; i < 26; i++)</pre>
            tr[i][p] = 0;
    inline int add(const string &s) {
        int cr = 1;
        for (int c : s) {
            c -= 'a';
            if (!tr[c][cr])
                clr(tr[c][cr] = ++ctn);
            cr = tr[c][cr];
        return cr;
    void blt(const vector<string> &ar) {
```

if (rk[i] == n)

continue;

int j = sa[rk[i]];

```
for (int i = 0; i < 26; i++)
                                                                          while (i + k <</pre>
             tr[i][0] = 1;
                                                                               n \& j + k < n \& s[i + k] == s[j + k]
                                                                               k++:
        clr(ctn = 1), n = size(ar);
                                                                          lcp[rk[i]] = k;
        for (int i = 0; i < n; i++)</pre>
                                                                      } // lcp[1~n-1],sα[0~n-1]
             endat[i] = add(ar[i]);
        queue<int> q;
                                                             |};
        q.push(1);
        while (!q.empty()) {
                                                             5.3 KMP [2b5dca]
             int pr = q.front();
                                                             |vector<int> kmp(string &s) {
             q.pop();
             top.pb(pr);
                                                                  int n = size(s);
             for (int i = 0; i < 26; i++) {
                                                                  vector<int> pi(n, 0);
                 int &cr = tr[i][pr];
                                                                  for (int i = 1; i < n; i++) {</pre>
                 if (cr)
                                                                      int j = pi[i - 1];
                     fail[cr]
                                                                      while (j > 0 && s[i] != s[j])
                           = tr[i][fail[pr]], q.push(cr);
                                                                          j = pi[j - 1];
                 else
                                                                      if (s[i] == s[j])
                     cr = tr[i][fail[pr]];
                                                                          j++;
             }
                                                                      pi[i] = j;
        }
                                                                  return pi;
        reverse(iter(top));
                                                             | }
    void qry(const string &s) {
                                                             5.4 Z [29dad4]
        int cr = 1;
        for (char c : s) // ways to walk
                                                             vector<int> z_algo(string &s) { // 0-base
             cr = tr[c - 'a'][cr], cnt[cr]++;
                                                                  int n = size(s);
        for (int i : top)
                                                                  vector<int> z(n, 0);
            cnt[fail[i]] += cnt[i];
                                                                  for (int i = 1, l = 0, r = 0; i < n; i++) {
    }
                                                                      if (i <= r)
};
                                                                          z[i] = min(z[i - l], r - i + 1);
                                                                      while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]])
5.2 SA [e051ae]
                                                                          z[i]++
                                                                      if (i + z[i] - 1 > r)
struct SA {
                                                                          l = i, r = i + z[i] - 1;
    static const int N = 5e5 + 5; // change
    int sa[N], rk[N], cnt[N], lcp[N], tmp[N], n;
                                                                  z[0] = n;
    void blt(const string &s) {
                                                                  return z;
        n = s.length();
                                                             }
        int m = 128;
                                                             5.5 Manacher [947d5b]
        memset(cnt + 1, 0, m << 2);
        for (int i = 0; i < n; i++)</pre>
                                                             vector<int> manacher(string
             cnt[rk[i] = s[i]]++;
                                                                  &s) {//pad \ s \ with \ $->$a$b$c....z$, realans = ans-1.}
        for (int i = 1; i <= m; i++)</pre>
                                                                string t(size(s) * 2 + 1, '$');
             cnt[i] += cnt[i - 1];
                                                                for(int i=0;i<size(s);i++) t[i * 2 + 1] = s[i];</pre>
        for (int i = n - 1; i >= 0; i--)
                                                                int n = size(t), m = 0, r = 0;
             sa[--cnt[rk[i]]] = i;
                                                               vector<int> p(n);
        for (int k = 1;; k <<= 1) {
                                                                for(int i=0;i<n;i++) {</pre>
             int ln = 0;
                                                                  p[i] = (r > i ? min(r - i, p[m - (i - m)]) : 1);
             for (int i = n - k; i < n; i++)</pre>
                                                                  while (i-p[i] \ge 0 \& i + p[i] < n \& \&
                 tmp[ln++] = i;
                                                                      t[i - p[i]] == t[i + p[i]]) ++p[i];
             for (int i = 0; i < n; i++)</pre>
                                                                  if (i + p[i] > r) m = i, r = i + p[i];
                 if (sa[i] >= k)
                     tmp[ln++] = sa[i] - k;
                                                                return p;
             memset(cnt + 1, 0, m << 2);
                                                             }
             for (int i = 0; i < n; i++)</pre>
                 cnt[rk[i]]++;
                                                             5.6 SAM [96a460]
             for (int i = 1; i <= m; i++)</pre>
                                                             struct SAM {
                 cnt[i] += cnt[i - 1];
             for (int i = n - 1; i >= 0; i--)
                                                                      const int N = 2e5 + 6; // node < 2n ; edge < 3n</pre>
                 sa[--cnt[rk[tmp[i]]]] = tmp[i];
                                                                  int tr[26][
             memcpy(tmp, rk, n << 2), rk[sa[0]] = m = 1;
                                                                      N], len[N], lnk[N], tmp[N], pl[N], ctn, lst;
             for (int i = 1; i < n; i++) {
                                                                  inline void ini(int x) {
                 if (tmp[sa[i]] != tmp[sa[i - 1]] ||
                                                                      for (int i = 0; i < 26; i++)</pre>
                     sa[i - 1] + k >= n ||
                                                                          tr[i][x] = 0;
                     tmp[sa
                          [i] + k] != tmp[sa[i - 1] + k])
                                                                  inline void ini() {
                     m++:
                                                                      ini(ctn = lst = len[0] = 0), lnk[0] = -1;
                 rk[sa[i]] = m;
                                                                      memset(tmp, 0, sizeof(tmp));
             if (m == n)
                                                                  inline void cp(int x, int y) {
                 break;
                                                                      lnk[x] = lnk[y];
                                                                      for (int i = 0; i < 26; i++)</pre>
        for (int i = 0, k = 0; i < n; i++, k -= !!k) {</pre>
```

tr[i][x] = tr[i][y];

void ext(const char cc) {

```
static int c, cr, p, q; c = cc - 'a', p = lst;
                                                                        ext(c);
                                                                }
        ini(cr = ++ctn), len[cr] = len[p] + 1;
                                                           };
        while (~p && !tr[c][p])
                                                                 Data Sructure
                                                            6
            tr[c][p] = cr, p = lnk[p];
        if (~p) {
                                                            6.1 Li-Chao [f2885c]
            q = tr[c][p];
            if (len[q] == len[p] + 1)
                                                            struct LiChaoMin {
                lnk[cr] = q;
                                                                struct line {
            else {
                                                                    ll m, k, id;
                                                                    line(ll _{m} = 0, ll _{k}
                cp(++ctn, q), len[ctn] = len[p] + 1;
                while (~p && tr[c][p] == q)
                                                                        = 0, ll _id = 0) : m(_m), k(_k), id(_id) {}
                                                                    tr[c][p] = ctn, p = lnk[p];
                lnk[cr] = lnk[q] = ctn;
                                                                };
            }
                                                                struct node {
                                                                    node *l, *r;
        } else
                                                                    line f;
            lnk[cr] = 0;
                                                                    node(line v) : f(v), l(NULL), r(NULL) {}
        lst = cr;
                                                                node *root;
    void blt(const string &s) {
                                                                int sz;
        ini();
                                                                void insert(node *&x, int l, int r, line &ln) {
        for (const char &c : s)
                                                                    if (!x) {
            ext(c);
                                                                        x = new node(ln);
        for (int i = 0; i <= ctn; i++)</pre>
                                                                        return;
            tmp[len[i]]++;
        for (int i = 1; i <= ctn; i++)</pre>
                                                                    ll trl = x->f.at(l), trr = x->f.at(r);
            tmp[i] += tmp[i - 1];
                                                                    ll vl = ln.at(l), vr = ln.at(r);
        for (int i = ctn; i >= 0; i--)
                                                                    if (trl <= vl && trr <= vr)
            pl[--tmp[len[i]]] = i;
                                                                        return;
                                                                    if (trl > vl && trr > vr) {
};
                                                                        x->f = ln;
                                                                        return;
5.7 exSAM [98e565]
struct exSAM {
                                                                    if (trl > vl)
    static const int N = 2e6 + 6;
                                                                        swap(x->f, ln);
    int tr[26][
                                                                    int mid = (l + r) >> 1;
        N], len[N], lnk[N], tmp[N], pl[N], ctn, lst;
                                                                    if (x->f.at(mid) < ln.at(mid))</pre>
    inline void ini(int x) {
                                                                        insert(x->r, mid + 1, r, ln);
        for (int i = 0; i < 26; i++)
            tr[i][x] = 0;
                                                                        swap(x->f, ln), insert(x->l, l, mid, ln);
    inline void ini() {
                                                                ll query(node *&x, int l, int r, ll idx) {
        ini(ctn = lst = len[0] = 0), lnk[0] = -1;
                                                                    if (!x)
    memset(tmp,0,sizeof(tmp));
                                                                        return LONG_LONG_MAX;
                                                                    if (l == r)
                                                                        return x->f.at(idx);
    inline void cp(int x, int y) {
        lnk[x] = lnk[y];
                                                                    int mid = (l + r) >> 1;
        for (int i = 0; i < 26; i++)</pre>
                                                                    if (mid >= idx)
            tr[i][x] = tr[i][y];
                                                                        return min(x
                                                                             ->f.at(idx), query(x->l, l, mid, idx));
    void ext(const char cc) {
                                                                    return min(x
        static int c, cr, p, q,*x; c = cc - 'a', p = lst;
                                                                         ->f.at(idx), query(x->r, mid + 1, r, idx));
    if (!tr[c][p]){
                                                                LiChaoMin(int _sz) : sz(_sz + 1), root(NULL) {}
      ini(cr = ++ctn), len[cr] = len[p] + 1;
                                                                void add_line(ll m, ll k, ll id = \theta) {
          while (~p && !tr[c][p])
                                                                    auto ln = line(m, k, id);
              tr[c][p] = cr, p = lnk[p];
                                                                    insert(root, -sz, sz, ln);
      lst=cr,x=&lnk[cr];
                                                                } // -sz <= query_x <= sz
    }
                                                                ll query
    else x=&lst;
                                                                     (ll idx) { return query(root, -sz, sz, idx); }
        if (~p) {
                                                           };
            q = tr[c][p];
                                                            6.2 Treap [d7ba9f]
            if (len[q] == len[p] + 1)
                *x = q;
                                                            namespace Treap {
                                                                const int N = 2e5 + 5;
                cp(++ctn, q), len[ctn] = len[p] + 1;
                                                                struct node {
                while (~p && tr[c][p] == q)
                                                                    int ky, sz, mn, mx, ln, rn;
                    tr[c][p] = ctn, p = lnk[p];
                                                                    ll sum;
                *x = lnk[q] = ctn;
                                                                    bool tg;
            }
                                                                    static node *pl;
        } else
                                                                    node() \{ sum = sz = 0, mx = \sim INF, mn = INF; \}
            lnk[cr] = 0;
                                                                    inline void ini(int v) { sum = ky
                                                                         = mx = mn = v, sz = 1, ln = rn = tg = 0; }
    void blt(const string &s) {
                                                                    inline void upd(int v) {
        lst=0;
                                                                        ky = mx = mn = v;
        for (const char &c : s)
                                                                        sum = 111 * v * sz;
```

```
tq = 1:
        inline void up() {
            sz = 1 + pl[ln].sz + pl[rn].sz;
            sum = mx = mn = ky;
            sum += pl[ln].sum + pl[rn].sum;
            tmax(mx, max(pl[ln].mx, pl[rn].mx));
            tmin(mn, min(pl[ln].mn, pl[rn].mn));
        }
        inline
             void down() { tg && (ln && (pl[ln].upd(ky)
             0), rn && (pl[rn].upd(ky), 0)), tg = 0; }
    } pool[N];
    mt19937 rnd(time(0));
    node *node::pl = pool, *pl = pool;
    int ctp = 0;
    inline int nwnd(int v) {
        pl[++ctp].ini(v);
        return ctp;
    int mg(int a, int b) {
        if (!a || !b)
            return a ? a : b;
        if ((int
            )rnd() % (pl[a].sz + pl[b].sz) < pl[a].sz)</pre>
            return pl[a].down(), pl[
                a].rn = mg(pl[a].rn, b), pl[a].up(), a;
        else
            return pl[b].down(), pl[
                b].ln = mg(a, pl[b].ln), pl[b].up(), b;
    void splsz(int rt, int &a, int &b, int k) {
        if (!rt)
            return a = b = 0, void();
        pl[rt].down();
        if (pl[pl[rt].ln].sz < k)
            a = rt, splsz(pl[rt].rn,
                pl[a].rn, b, k - pl[pl[rt].ln].sz - 1);
            b = rt, splsz(pl[rt].ln, a, pl[b].ln, k);
        pl[rt].up();
    void splky(int rt, int &a, int &b, int v) {
        if (!rt)
            return a = b = 0, void();
        pl[rt].down();
        if (pl[rt].ky <= v)
            a = rt, splky(pl[rt].rn, pl[a].rn, b, v);
            b = rt, splky(pl[rt].ln, a, pl[b].ln, v);
        pl[rt].up();
}
6.3 Link Cut Tree [49d7e6]
struct LCT {
    static const int N = 4e5 + 5; // change
    int fa[N], ch[2][N], sz[N], sv[N];
#define gch(x) ((x) == ch[1][fa[x]])
#define nrt(x) ((x) == ch[gch(x)][fa[x]])
#define up
    (x) sz[x] = sz[ch[0][x]] + sz[ch[1][x]] + sv[x] + 1
    inline void rota(int x) {
        int f = fa[x], ff = fa[f], k = gch(x);
        if (nrt(f))
            ch[gch(f)][ff] = x;
        fa[x] = ff;
        if (ch[!k][x])
            fa[ch[!k][x]] = f;
        ch[k][f] = ch[!k][x];
        ch[!k][x] = f, fa[f] = x;
        up(f), up(x);
```

inline void splay(int x) {

if (nrt(f))

for (int f = fa[x]; nrt(x); rota(x), f = fa[x])

```
rota(gch(x) ^ gch(f) ? x : f);
     inline int acc(int x) {
         int p;
         for (p = 0; x; p = x, x = fa[x])
              splay(x), sv[x] += sz[
                  ch[1][x]] - sz[p], ch[1][x] = p, up(x);
         return p;
     inline int findroot(int x) {
         int cr = acc(x);
         while (ch[0][cr])
             cr = ch[\theta][cr];
         splay(cr);
         return cr;
     }
     void link(int x, int y) {
         int rt = findroot(y);
         acc(x), acc(rt);
         acc(y), splay(y);
         sv[y] += sz[x];
         fa[x] = y, up(y);
         acc(rt);
     void cut(int x, int y) {
         int rt = findroot(y);
         acc(rt);
         acc(y), splay(y), splay(x);
         sv[y] -= sz[x];
         fa[x] = 0, up(y);
         acc(x), acc(rt);
| }:
6.4 Ultimate Segment Tree [6e7e86]
struct SegBeat {
     int n,n0;
     vector<ll> max_v,smax_v
          ,max_c,min_v,smin_v,min_c,sum,len,ladd,lval;
     void update_node_max(int k, ll x) {
         sum[k] += (x - max_v[k]) * max_c[k];
         if(max_v
             [k] == \min_{v[k]} \max_{v[k]} = \min_{v[k]} = x;
         else if(max_v
              [k] == smin_v[k]) max_v[k] = smin_v[k] = x;
         else max_v[k] = x;
         if(lval[k] != 1e18 && x < lval[k]) lval[k] = x;</pre>
     void update_node_min(int k, ll x) {
         sum[k] += (x - min_v[k]) * min_c[k];
         if(max_v
              [k] == min_v[k]) max_v[k] = min_v[k] = x;
         else if(smax_v
              [k] == \min_{v[k]} \min_{v[k]} = \max_{v[k]} = x;
         else min_v[k] = x;
         if(lval[k] != 1e18 && lval[k] < x) lval[k] = x;</pre>
     void push(int k) {
         if(n0-1 <= k) return;
         if(lval[k] != 1e18) {
             updateall(2*k+1, lval[k]);
             updateall(2*k+2, lval[k]);
             lval[k] = 1e18;
             return:
         if(ladd[k] != 0) {
             \begin{array}{ll} \text{addall(2*k+1, ladd[k]);} \\ \text{addall(2*k+2, ladd[k]);} \end{array}
             ladd[k] = 0;
         if(max_v[k] < max_v</pre>
              [2*k+1]) update_node_max(2*k+1, max_v[k]);
         if(min_v[2*k+1] <
              min_v[k]) update_node_min(2*k+1, min_v[k]);
         if(max_v[k] < max_v</pre>
              [2*k+2]) update_node_max(2*k+2, max_v[k]);
```

```
if(min_v[2*k+2] <
        min_v[k]) update_node_min(2*k+2, min_v[k]);
void update(int k) {
    sum[k] = sum[2*k+1] + sum[2*k+2];
    if(max_v[2*k+1] < max_v[2*k+2]) {
        \max_{v[k]} = \max_{v[2*k+2]};
        \max_{c[k]} = \max_{c[2*k+2]};
        smax_v
             [k] = \max(\max_{v[2*k+1]}, \max_{v[2*k+2]});
    } else if(\max_{v[2*k+1]} > \max_{v[2*k+2]}) {
        max_v[k] = max_v[2*k+1];
        \max_{c[k]} = \max_{c[2*k+1]};
        smax_v
             [k] = \max(\max_{v[2*k+1]}, \max_{v[2*k+2]});
    } else {
        \max_{v[k]} = \max_{v[2*k+1]};
        \max_{c[k]} = \max_{c[2*k+1]} + \max_{c[2*k+2]};
        smax_v[
             k] = max(smax_v[2*k+1], smax_v[2*k+2]);
    if(min_v[2*k+1] < min_v[2*k+2]) {</pre>
        min_v[k] = min_v[2*k+1];
        min_c[k] = min_c[2*k+1];
        smin_v
             [k] = min(smin_v[2*k+1], min_v[2*k+2]);
    } else if(min_v[2*k+1] > min_v[2*k+2]) {
        min_v[k] = min_v[2*k+2];
        min_c[k] = min_c[2*k+2];
        smin_v
             [k] = min(min_v[2*k+1], smin_v[2*k+2]);
    } else {
        min_v[k] = min_v[2*k+1];
        \min_{c[k]} = \min_{c[2*k+1]} + \min_{c[2*k+2]};
        smin_v[
             k] = min(smin_v[2*k+1], smin_v[2*k+2]);
    }
void _chmin
    (ll x, int a, int b, int k, int l, int r) {
    if(b <= l || r <= a || max_v[k] <= x) return;</pre>
    if(a <= l && r <= b && smax_v[k] < x) {</pre>
        update_node_max(k, x);
        return;
    }
    push(k):
    _{chmin}(x, a, b, 2*k+1, l, (l+r)/2);
    _{chmin}(x, a, b, 2*k+2, (l+r)/2, r);
    update(k);
void _chmax
    (ll x, int a, int b, int k, int l, int r) {
    if(b <= l || r <= a || x <= min_v[k]) return;
    if(a <= l && r <= b && x < smin_v[k]) {</pre>
        update_node_min(k, x);
    }
    push(k);
    _{chmax}(x, a, b, 2*k+1, l, (l+r)/2);
    _{chmax}(x, a, b, 2*k+2, (l+r)/2, r);
    update(k);
void addall(int k, ll x) {
    \max_{v[k]} += x;
    if(smax_v[k] != -1e18) smax_v[k] += x;
    min_v[k] += x;
    if(smin_v[k] != 1e18) smin_v[k] += x;
    sum[k] += len[k] * x;
    if(lval[k] != 1e18) lval[k] += x;
    else ladd[k] += x;
void updateall(int k, ll x) {
    \max_{v[k]} = x;
    smax_v[k] = -1e18;
    min_v[k] = x;
```

```
smin_v[k] = 1e18;
    \max_{c[k]} = \min_{c[k]} = \operatorname{len}[k];
    sum[k] = x * len[k];
    lval[k] = x;
    ladd[k] = 0;
void _add_val
    (ll x, int a, int b, int k, int l, int r) {
    if(b <= l || r <= a) return;
    if(a <= l && r <= b) {
        addall(k, x);
        return:
    push(k);
    _{add\_val(x, a, b, 2*k+1, l, (l+r)/2);}
    _{add\_val(x, a, b, 2*k+2, (l+r)/2, r);}
    update(k);
void _update_val
    (ll x, int a, int b, int k, int l, int r) {
    if(b <= l || r <= a) return;
    if(a <= l && r <= b) {
        updateall(k, x);
        return;
    }
    push(k);
    _{update_{val}(x, a, b, 2*k+1, l, (l+r)/2);}
    _{update_{val}(x, a, b, 2*k+2, (l+r)/2, r);}
    update(k);
ll _query_max(int a, int b, int k, int l, int r) {
    if(b <= l || r <= a) return -1e18;
    if(a <= l && r <= b) return max_v[k];
    push(k);
    ll lv = _query_max(a, b, 2*k+1, l, (l+r)/2);
    ll rv = _query_max(a, b, 2*k+2, (l+r)/2, r);
    return max(lv, rv);
ll _query_min(int a, int b, int k, int l, int r) {
    if(b <= l || r <= a) return 1e18;
    if(a <= 1 && r <= b) return min_v[k];
    push(k);
    ll lv = _query_min(a, b, 2*k+1, l, (l+r)/2);
ll rv = _query_min(a, b, 2*k+2, (l+r)/2, r);
    return min(lv, rv);
ll _query_sum(int a, int b, int k, int l, int r) {
    if(b <= l || r <= a) return Θ;
    if(a <= l && r <= b) return sum[k];</pre>
    push(k);
    ll lv = _query_sum(a, b, 2*k+1, l, (l+r)/2);
    ll rv = _query_sum(a, b, 2*k+2, (l+r)/2, r);
    return lv + rv;
SegBeat(int _n) : n(_n) {
    max_v.resize(4*_n+4,0);smax_v.resize
         (4*_n+4,-1e18); max_c.resize(4*_n+4,1);
    min_v.resize(4*_n+4,0);smin_v.
         resize(4*_n+4,1e18);min_c.resize(4*_n+4,1);
    sum.resize(4*_n+4,0);len.resize(4*_n+4,0);
    ladd.resize(4*_n+4,0);lval.resize(4*_n+4,1e18);
    n0 = 1:
    while(n0 < n) n0 <<= 1;</pre>
    len[0] = n0;
    for(int i=0; i<n0-1; ++</pre>
         i) len[2*i+1] = len[2*i+2] = (len[i] >> 1);
    for(int i=n; i<n0; ++i) {</pre>
        \max_{v[n0-1+i]} = \max_{v[n0-1+i]} = -1e18;
        \min_{v[n0-1+i]} = \min_{v[n0-1+i]} = 1e18;
        \max_{c[n0-1+i]} = \min_{c[n0-1+i]} = 0;
    for(int i=n0-2; i>=0; i--) update(i);
void chmin(int
     a, int b, ll x) {_{\text{chmin}}(x, a-1, b, 0, 0, n0);}
```

```
National Taiwan University QwQ_GG
    void chmax(int
          a, int b, ll x) \{ -chmax(x, a-1, b, 0, 0, n0); \}
    void add_val(int a
         , <mark>int</mark> b, ll x) {_add_val(x, a-1, b, 0, 0, n0);}
    void update_val(int a, int
          b, ll x) {_update_val(x, a-1, b, 0, 0, n0);}
    ll query_max(int a
         , int b) {return _query_max(a-1, b, 0, 0, n0);}
    ll query_min(int a
         , int b) {return _query_min(a-1, b, 0, 0, n0);}
    ll query_sum(int a
         , int b) {return _query_sum(a-1, b, 0, 0, n0);}
|};
7
     Misc
      Total Binary Search [ac23f3]
struct TotalBS {
    int Q;
    vector<int> ans;
    TotalBS(int _Q) {
        Q=_Q;
        ans.resize(Q);
    void split(vector<</pre>
         int> &qrys,vecotr<int> &ok,vector<int> &fail) {
        for(auto i :qrys) {
        vector<int>.swap(qrys);
        return;
    void do_things(int l,int mid) {
        return;
    }
    void undo_things(int l,int mid) {
        return;
    void total_BS(int l, int r, vector<int> &qrys) {
        if (l == r) {
             for(auto i : qrys) {
                 ans[i] = l;
             }
        int mid = (l + r) / 2;
        do_things(l, mid);
        vector<int> lft,rgt;
        split(qrys,lft,rgt);
        total_BS(mid + 1, r, rgt);
        undo_things(l, mid);
        total_BS(l, mid, lft);
};
7.2 CDQ [11f96f]
void CDQ(int l, int r) { // 三維偏序
    if (l == r)
        return;
    int mid = (l + r) / 2;
    CDQ(l, mid);
    CDQ(mid + 1, r);
    sort(arr + l, arr + mid + 1, cmpB);
    sort(arr + mid + 1, arr + r + 1, cmpB);
    int i = 1;
    int j = mid + 1;
    while (j <= r) {
        while (i <= mid && ue[i].b <= ue[j].b) {</pre>
```

BIT.Add(arr[i].c, arr[i].cnt);

ue[j].res += BIT.Ask(arr[j].c);

BIT.Add(arr[k].c, -arr[k].cnt);

i++;

for (int k = l; k < i; k++)</pre>

}

return;

į }-