1. 1

First, we find the partials:

$$\begin{split} \frac{\partial x_i}{\partial u_j} &= \frac{1}{u_{d+1}} \\ \frac{\partial x_i}{\partial j_i} &= \frac{1}{u_i} + \frac{1}{u_{d+1}} \end{split}$$

Which gives us the Jacobian:

$$J = \begin{bmatrix} \frac{\partial x_1}{\partial u_1} & \cdots & \frac{\partial x_1}{\partial u_d} \\ \vdots & \ddots & \vdots \\ \frac{\partial x_d}{\partial u_1} & \cdots & \frac{\partial x_n}{\partial u_d} \end{bmatrix} = \begin{bmatrix} \frac{1}{u_1} + \frac{1}{u_{d+1}} & & \frac{1}{u_{d+1}} \\ & & \ddots & \\ \frac{1}{u_{d+1}} & & \frac{1}{u_d} + \frac{1}{u_{d+1}} \end{bmatrix}$$

$$= \begin{bmatrix} \frac{1}{u_1} \\ \vdots \\ \frac{1}{u_d} \end{bmatrix} I_d + \begin{bmatrix} \vdots \\ \frac{1}{u_{d+1}} \\ \vdots \end{bmatrix}$$

Letting 
$$X = \begin{bmatrix} \frac{1}{u_1} \\ \vdots \\ \frac{1}{u_d} \end{bmatrix}$$
 and  $C = \begin{bmatrix} \vdots \\ \frac{1}{u_{d+1}} \\ \vdots \end{bmatrix}$ ,

Sylvester's formula gives us that:

$$\det(J) = \det(X) \cdot (1 + CX^{-1}C^T)$$