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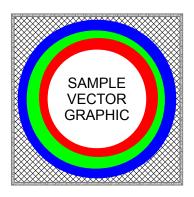
In Partial Fulfillment of the Requirements

for the Degree of

Doctor of Philosophy

in

Electrical Engineering and Computer Science



University Institute of College Springfield, New York, USA

2016

(Defended November 25, 2016)

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Acknowledgments

Insert thesis acknowledgments here. Thesis acknowledgments typically include research advisers and mentors, thesis committee members, collaborators, and funding sources.

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Abstract

Insert thesis abstract here. The thesis abstract provides a concise description of the main contributions in the thesis. Abstracting and indexing services usually include the thesis abstract in the catalog presented to users. A well-written abstract could improve the chances of your work being discovered and cited by others in the research community. The abstract should be self-contained (avoid citations and cross references) and should contain only plain text (avoid complicated mathematical expressions).

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Contents

A	Acknowledgments		
Al	bstract	V	
I	Background	1	
1	Stern-Gerlach Experiments	2	
	1.1 Stern-Gerlach Backgorund	2	
	1.2 Stern-Gerlach Measurement	2	
	1.3 Complementarity	3	
2	Insert Chapter Title Here	6	
	2.1 Introduction	6	
	2.2 Some Examples	7	
	2.2.1 Examples of Figures and Tables	8	
	2.2.2 Examples of Enumerated and Itemized Lists	11	
	2.3 Some More Examples	11	
	2.3.1 Examples of Mathematical Expressions, Definitions, and		
	Theorems	12	
	2.4 Conclusion and Future Work	13	
	2.5 Proofs of Theorems	14	
	2.6 Acknowledgment	16	
3	Summary and Future Work	17	
	3.1 Summary	17	
	3.2 Future Work	18	
Bi	ibliography	20	

List of Figures

1.1	Insert an abbreviated caption here to show in the List of Figures .	3
1.2	Insert an abbreviated caption here to show in the List of Figures .	4
1.3	Insert an abbreviated caption here to show in the List of Figures .	5
1.4	Insert an abbreviated caption here to show in the List of Figures .	5
1.5	Insert an abbreviated caption here to show in the List of Figures .	5
2.1	Insert an abbreviated caption here to show in the List of Figures .	8
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List of Tables

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2.2	Insert an abbreviated	caption here	to show	in the List of	Tables	10

PART I

Background

1 Stern-Gerlach Experiments

1.1 Stern-Gerlach Backgorund

TODO

1.2 Stern-Gerlach Measurement

We begin by comparing standard and consistent descriptions of measuring a quantum states' spin along one axis using a Stern-Gerlach apparatus. In standard quantum mechanics, the act of measurement plays a special role in assigning probabilities to the outcome and the evolution of the state through the probability and projection postulates.

The probability postulate assigns probabilities to each measurement by taking the inner product of the state $|n\rangle$ corresponding to a measurement result n and $|\psi\rangle$:

$$\mathcal{P}_n = |\langle n|\psi\rangle|^2 \tag{1.1}$$

The projection postulate describes an instantaneous evolution of the input state to an output state that corresponds to an allowed measurement value. If input $|\psi\rangle$ is measured to have spin n (up or down), then the new state is

$$|\psi\rangle' = \frac{P_n |\psi\rangle}{\sqrt{\langle\psi|P_n|\psi\rangle}} \tag{1.2}$$

where $P_n = |n\rangle \langle n|$ is the projection operator for state $|n\rangle$. This operation projects $|\psi\rangle$ onto $|n\rangle$, then divides by the magnitude of that projection. The end result is that $|\psi\rangle$ becomes the normalized state $|n\rangle$ corresponding to measuring spin n, which is shown by the states exiting the each apparatus.

TODO: show probability computations TODO: explain how measurement is not itself modeled as a physical process, and we are directed to use these postulates upon poorly defined "measurement"

In consistent quantum theory, measurement is modeled as a physical process. Each Stern-Gerlach apparatus has its own detector Hilbert space, containing orthonormal states representing each measurement result. Let the state space of the z apparatus be represented by $\mathcal{H}_{Dz} = \{|D_z\rangle_+, |D_z\rangle_-\}$ where

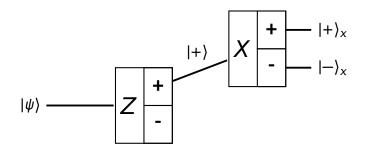


FIGURE 1.1 Demonstrating renormalizing upon measurment in standard quantum mechanics

 $_{+}\langle D_{z}|D_{z}\rangle_{+}=1$ and $_{+}\langle D_{z}|D_{z}\rangle_{-}=0$. \mathcal{H}_{Dx} is similarly defined. Each detector state is orthogonal to states in seperate detector spaces.

The act of measurement is described by correlating the detector states with the corresponding quantum states. The system then evolves by

$$V:$$

$$\mathcal{H}_{s} \mapsto \mathcal{H}_{s} \otimes \mathcal{H}_{D}$$

$$|\psi\rangle = \sum_{n} P_{n} |\psi\rangle \mapsto \sum_{n} P_{n} |\psi\rangle \otimes |D\rangle_{n}$$
(1.3)

Measurment is now described by an abstract physical process. In this model, it is now feasible for "state collapse" to occur independent of physicists conducting clever experiments.

To compute probabilities of each outcome, we sum the magnitudes of each branch wavefunction that includes the corresponding detector state. This is accomplished by finding the trace of the projection operator of that detector state acting on the projection operator or the overall evolved state.

$$\mathcal{P}_n = Tr(P_n^D \cdot V | \psi \rangle \langle \psi | V^{\dagger}) \tag{1.4}$$

In this simple Stern-Gerlach example, there is only one branch wavefunction correlated with each detector state. So, computing probabilities is done by finding the magnitude of each branch wavefunction.

TODO: compute probabilities, show it is equal to std QM

1.3 Complementarity

We now compare standard and consistent quantum mechanics' treatment of the principle of complementarity. Arguably the most fundamental feature of quantum mechanics, the principle of complementarity states that a quantum system has pairs of physical observables which cannot

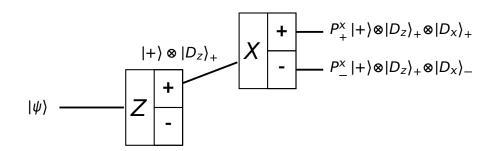


FIGURE 1.2 Demonstrating description of measurment as an abstract physical process in consistent quantum mechanics

be measured simultaneously. Components of spin on orthogonal axes are complemntary properties, so we examine measurements of succesive Stern-Gerlach experiments.

First, we compute the probabilities of each outcome using standard quantum mechanics. The first apparatus serves as a state preparation device with output $|+\rangle$. By the direction of the projection postulate, the state is renormalized upon each measruement. After measuring a property complementary to what is known (such as spin along x, knowing spin along z), any information known about the input state is lost; the input state instantaneously changes to the state corresponding to the observed quantity. Consequently, there is an equal probability of observing the final state as $|+\rangle$ or $|-\rangle$ at either final apparatus, even though the state was initially prepared as $|+\rangle$, since

$$\mathcal{P}_n = |\langle +|+\rangle_X|^2$$

$$= |\langle -|+\rangle_X|^2$$

$$= |\langle +|-\rangle_X|^2$$

$$= |\langle -|-\rangle_X|^2$$

$$= \frac{1}{4}$$

This contradiction with classical intuition is a direct result of the projection postulate. TODO: describe measurement problem.

TODO: Demonstrate complementarity and single framework rule

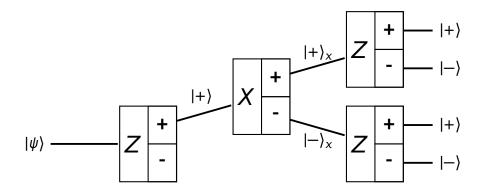


FIGURE 1.3 Demonstrating complementary measurments in standard quantum mechanics

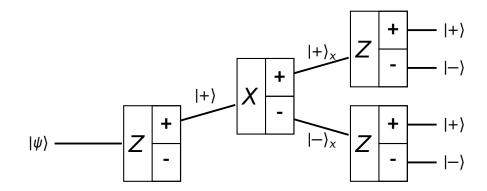


FIGURE 1.4 Demonstrating complementary measurments in consistent quantum mechanics

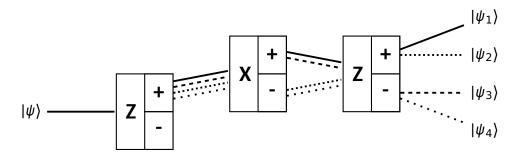


FIGURE 1.5 TODO: create section to discuss this example, and how it creates an inconsistent set of histories. Describe how the set can be made to be consistent

2 Insert Chapter Title Here

2.1 Introduction

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Proofs of theorems are deferred to Section 2.5.

2.2 Some Examples

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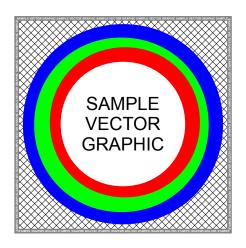


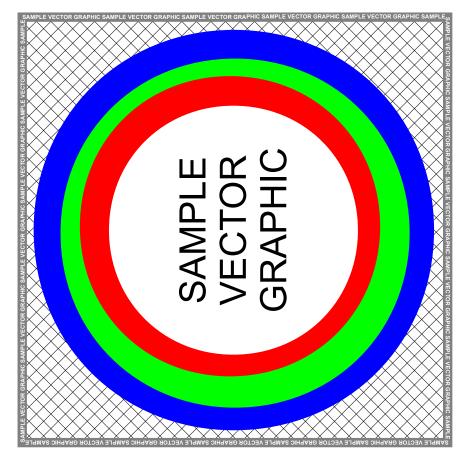
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2.2.1 Examples of Figures and Tables

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We summarize our notation in Table 2.1. Suspendisse vitae elit. Aliquam arcu neque, ornare in, ullamcorper quis, commodo eu, libero. Fusce sagittis erat at erat tristique mollis. Maecenas sapien libero, molestie et, lobortis in,



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TABLE 2.1 Insert the full caption here for this floating table.

Symbol	Definition
α	insert definition of α here, $\alpha \ge 1$
β	insert definition of β here, $\beta \geq 2$
γ	insert definition of γ here, $\gamma \geq 3$
δ	insert definition of δ here, $\delta \geq 4$

TABLE 2.2 Insert the full caption here for this floating table. The caption should provide sufficient context to interpret the table. Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris.

Variable	Initial Value	Value at $t = 100$
С	0.012	3.456
δ	0.312	1.416
γ	0.042	3.252
h	0.012	3.353
С	0.012	4.446
δ	0.015	3.556
γ	0.612	6.656
h	0.072	7.456
С	0.018	8.756
δ	0.912	9.456
γ	0.092	5.956
h	0.012	2.326

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Table 2.2 summarizes our simulation results. Sed feugiat. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Ut pellentesque augue sed urna. Vestibulum diam eros, fringilla et, consectetuer eu, nonummy id, sapien. Nullam at lectus. In sagittis ultrices mauris. Curabitur malesuada erat sit amet massa. Fusce blandit. Aliquam erat volutpat. Aliquam euismod. Aenean vel lectus. Nunc imperdiet justo nec dolor.

2.2.2 Examples of Enumerated and Itemized Lists

Here are some citations [5–10]. The following is an enumerated list, or numbered list, with multiple levels:

- 1) First level item
- 2) First level item
 - a) Second level item
 - b) Second level item
 - i) Third level item
 - A) Fourth level item
 - B) Fourth level item
 - ii) Third level item
 - c) Second level item
- 3) First level item

We draw your attention to items 1 and 3 in particular because they are very important in our study. The following is an itemized list, or unnumbered list, with multiple levels:

- First level item
- First level item
 - Second level item
 - Second level item
 - * Third level item
 - · Fourth level item
 - · Fourth level item
 - * Third level item
 - Second level item
- First level item

2.3 Some More Examples

According to [11], this behavior can be explained this way. Etiam euismod. Fusce facilisis lacinia dui. Suspendisse potenti. In mi erat, cursus id, nonummy sed, ullamcorper eget, sapien. Praesent pretium, magna in eleifend egestas, pede pede pretium lorem, quis consectetuer tortor sapien facilisis magna. Mauris quis magna varius nulla scelerisque imperdiet. Aliquam non quam.

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2.3.1 Examples of Mathematical Expressions, Definitions, and Theorems

We have the following unnumbered mathematical equation:

$$E = mc^2$$
.

On the other hand, the following is a numbered mathematical inequality:

$$x \le \frac{\sum_{i=1}^{n} y^{2} \cdot \mathbb{1} [y > 1]}{\int_{-\infty}^{\infty} x^{3} dz \cdot \begin{pmatrix} \alpha \\ \beta \end{pmatrix} \frac{\lfloor \frac{\alpha}{b} \rfloor}{\lceil \frac{c}{d} \rceil}}.$$
 (2.1)

Inequality (2.1) will be applied multiple times to prove our theorems, in a manner similar to [12,13]. We now introduce the following definition:

DEFINITION 2.1 (Name of Term Being Defined) This is the definition of the term, along with relevant conditions, trivial cases, exceptions, etc.

We can rewrite the result of [13, Theorem 2.5] in the following convenient form for our problem:

PROPOSITION 2.2 For all $\alpha, b, c \in \mathbb{Z}^+$, we have

$$\alpha^2+b^3\leq c^4.$$

Based on our numerical observations, we make the following conjecture about the upper bound:

CONJECTURE 2.3 If $x \ge 3$ and $0 < y < x^2$, then for all $n \in \mathbb{Z}^+$,

$$\sum_{i=1}^{n} x_i = x_1 + x_2 + \dots + x_n \le T_{\text{all}}.$$

Here is a lemma that will be quite useful in deriving our results:

LEMMA 2.4 (Name of Lemma if any) If $x, y, z \in \mathbb{Z}_0^+$, then f(x + y + z) = 1.

Applying Lemma 2.4 to [11, Theorem 4.2] produces the following theorem:

THEOREM 2.5 (Name of Theorem if any) If $x + y \ge z$, then

$$\sum_{i=x}^{y} f(i) \le z.$$

As a special case of Theorem 2.5, we have the following corollary: ∇^{V}

COROLLARY 2.6 If x = 4 and y = z, then $\sum_{i=x}^{y} f(i) = 5$.

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2.4 Conclusion and Future Work

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2.5 Proofs of Theorems

Remember to manually disable (and re-enable) updates to the table of contents (TOC), using

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2.5.1 Proof of Lemma 2.4

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2.5.2 Proof of Theorem 2.5

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nisl eu sapien cursus rutrum.

The following lemma will be quite useful in deriving the theorem:

LEMMA 2.7 If $a, b, c \in \mathbb{Z}$, then $g(a \cdot b \cdot c) \leq -1$.

Proof of Lemma 2.7: Nulla non mauris vitae wisi posuere convallis. Sed eu nulla nec eros scelerisque pharetra. Nullam varius. Etiam dignissim elementum metus. Vestibulum faucibus, metus sit amet mattis rhoncus, sapien dui laoreet odio, nec ultricies nibh augue a enim. Fusce in ligula. Quisque at magna et nulla commodo consequat. Proin accumsan imperdiet sem. Nunc porta. Donec feugiat mi at justo. Phasellus facilisis ipsum quis ante. In ac elit eget ipsum pharetra faucibus. Maecenas viverra nulla in massa.

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Applying Lemma 2.7 yields the following:

$$A + B + C + D + E + F + \alpha + \beta + \gamma + \delta + \Gamma$$

$$\leq \Omega + \Sigma + \omega + \sigma + \Theta + \theta + \epsilon + S + T + U + V + W + X + Y + Z. \quad (2.2)$$

Finally, the desired result is obtained by substituting A = b into (2.2).

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2.6 Acknowledgment

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3 Summary and Future Work

3.1 Summary

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3.2 Future Work

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