

## CHAPTER 11—WALLS

### CODE

### COMMENTARY

#### **11.1—Scope**

**11.1.1** This chapter shall apply to the design of nonprestressed and prestressed walls including (a) through (c):

- (a) Cast-in-place
- (b) Precast in-plant
- (c) Precast on-site including tilt-up

**11.1.2** Design of special structural walls shall be in accordance with [Chapter 18](#).

**11.1.3** Design of plain concrete walls shall be in accordance with [Chapter 14](#).

**11.1.4** Design of cantilever retaining walls shall be in accordance with [Chapter 13](#).

**11.1.5** Design of walls as grade beams shall be in accordance with [13.3.5](#).

**11.1.6** Cast-in-place walls with insulating forms shall be permitted by this Code.

#### **11.2—General**

##### **11.2.1 Materials**

**11.2.1.1** Design properties for concrete shall be selected to be in accordance with [Chapter 19](#).

**11.2.1.2** Design properties for steel reinforcement shall be selected to be in accordance with [Chapter 20](#).

**11.2.1.3** Materials, design, and detailing requirements for embedments in concrete shall be in accordance with [20.6](#).

##### **11.2.2 Connection to other members**

**11.2.2.1** For precast walls, connections shall be designed in accordance with [16.2](#).

**11.2.2.2** Connections of walls to foundations shall satisfy [16.3](#).



**CODE****COMMENTARY****11.2.3 Load distribution**

**11.2.3.1** Unless otherwise demonstrated by an analysis, the horizontal length of wall considered as effective for resisting each concentrated load shall not exceed the lesser of the center-to-center distance between loads, and the bearing width plus four times the wall thickness. Effective horizontal length for bearing shall not extend beyond vertical wall joints unless design provides for transfer of forces across the joints.

**11.2.4 Intersecting elements**

**11.2.4.1** Walls shall be anchored to intersecting elements, such as floors and roofs; columns, pilasters, buttresses, or intersecting walls; and to footings.

**11.2.4.2** For cast-in-place walls having  $P_u > 0.2f'_c A_g$ , the portion of the wall within the thickness of the floor system shall have specified compressive strength at least  $0.8f'_c$  of the wall.

**11.3—Design limits****11.3.1 Minimum solid wall thickness**

**11.3.1.1** Minimum solid wall thicknesses shall be in accordance with Table 11.3.1.1. Thinner walls are permitted if adequate strength and stability can be demonstrated by structural analysis.

**Table 11.3.1.1—Minimum solid wall thickness  $h$** 

Wall type	Minimum thickness $h$		
Bearing <sup>[1]</sup>	Greater of:	4 in.	(a)
		1/25 the lesser of unsupported length and unsupported height	(b)
Nonbearing	Greater of:	4 in.	(c)
		1/30 the lesser of unsupported length and unsupported height	(d)
Exterior basement and foundation <sup>[1]</sup>		7.5 in.	(e)

<sup>[1]</sup>Only applies to walls designed in accordance with the simplified design method of 11.5.3.

**11.4—Required strength****11.4.1 General**

**11.4.1.1** Required strength shall be calculated in accordance with the factored load combinations in [Chapter 5](#).

**R11.2.4 Intersecting elements**

**R11.2.4.1** Walls that do not depend on intersecting elements for support, do not have to be connected to those elements. It is not uncommon to separate massive retaining walls from intersecting walls to accommodate differences in deformations.

**R11.2.4.2** The 0.8 factor reflects reduced confinement in floor-wall joints compared with floor-column joints under gravity loads. 

**R11.4—Required strength****R11.4.1 General**

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**11.4.1.2** Required strength shall be calculated in accordance with the analysis procedures in [Chapter 6](#).

**11.4.1.3** Slenderness effects shall be calculated in accordance with [6.6.4](#), [6.7](#), or [6.8](#). Alternatively, out-of-plane slenderness analysis shall be permitted using 11.8 for walls meeting the requirements of that section.

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**R11.4.1.3** The forces typically acting on a wall are illustrated in Fig. R11.4.1.3.

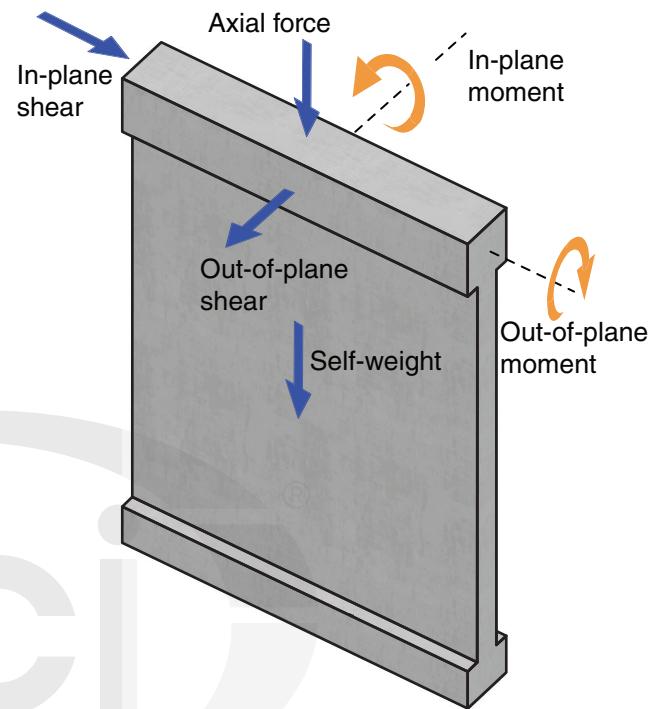


Fig. R11.4.1.3—In-plane and out-of-plane forces.

**11.4.1.4** Walls shall be designed for eccentric axial loads and any lateral or other loads to which they are subjected.

**11.4.1.5** Design of basement walls to resist out-of-plane lateral earth pressure shall be in accordance with [Section 13.3.7](#).

#### 11.4.2 Factored axial force and moment

**11.4.2.1** Walls shall be designed for the maximum factored moment  $M_u$  that can accompany the factored axial force for each applicable load combination. The factored axial force  $P_u$  at given eccentricity shall not exceed  $\phi P_{n,max}$ , where  $P_{n,max}$  shall be as given in [22.4.2.1](#) and strength reduction factor  $\phi$  shall be that for compression-controlled sections in [21.2.2](#). The maximum factored moment  $M_u$  shall be magnified for slenderness effects in accordance with [6.6.4](#), [6.7](#), or [6.8](#).

#### 11.4.3 Factored shear

**11.4.3.1** Walls shall be designed for the maximum in-plane  $V_u$  and out-of-plane  $V_u$ .

**CODE****COMMENTARY****11.5—Design strength****11.5.1 General**

**11.5.1.1** For each applicable factored load combination, design strength at all sections shall satisfy  $\phi S_n \geq U$ , including (a) through (c). Interaction between axial load and moment shall be considered.

- (a)  $\phi P_n \geq P_u$
- (b)  $\phi M_n \geq M_u$
- (c)  $\phi V_n \geq V_u$

**11.5.1.2**  $\phi$  shall be determined in accordance with 21.2.

**11.5.2 Axial load and in-plane or out-of-plane flexure**

**11.5.2.1** For bearing walls,  $P_n$  and  $M_n$  (in-plane or out-of-plane) shall be calculated in accordance with 22.4. Alternatively, axial load and out-of-plane flexure shall be permitted to be considered in accordance with 11.5.3.

**11.5.2.2** For nonbearing walls,  $M_n$  shall be calculated in accordance with 22.3.

**11.5.3 Axial load and out-of-plane flexure – simplified design method**

**11.5.3.1** If the resultant of all factored loads is located within the middle third of the thickness of a solid wall with a rectangular cross section,  $P_n$  shall be permitted to be calculated by:

$$P_n = 0.55 f'_c A_g \left[ 1 - \left( \frac{k \ell_c}{32 h} \right)^2 \right] \quad (11.5.3.1)$$

**R11.5—Design strength****COMMENTARY****R11.5.2 Axial load and in-plane or out-of-plane flexure**

**R11.5.2.2** Nonbearing walls, by definition, are not subject to any significant axial force; therefore, flexural strength is not a function of axial force.

**R11.5.3 Axial load and out-of-plane flexure – simplified design method**

**R11.5.3.1** The simplified design method applies only to solid rectangular cross sections; all other shapes should be designed in accordance with 11.5.2.

Eccentric axial loads and moments due to out-of-plane forces are used to determine the maximum total eccentricity of the factored axial force  $P_u$ . When the resultant axial force for all applicable load combinations falls within the middle third of the wall thickness (eccentricity not greater than  $h/6$ ) at all sections along the length of the undeformed wall, no tension is induced in the wall and the simplified design method may be used. The design is then carried out considering  $P_u$  as a concentric axial force.

Equation (11.5.3.1) results in strengths comparable to those determined in accordance with 11.5.2 for members loaded at the middle third of the thickness with different braced and restrained end conditions. Refer to Fig. R11.5.3.1.

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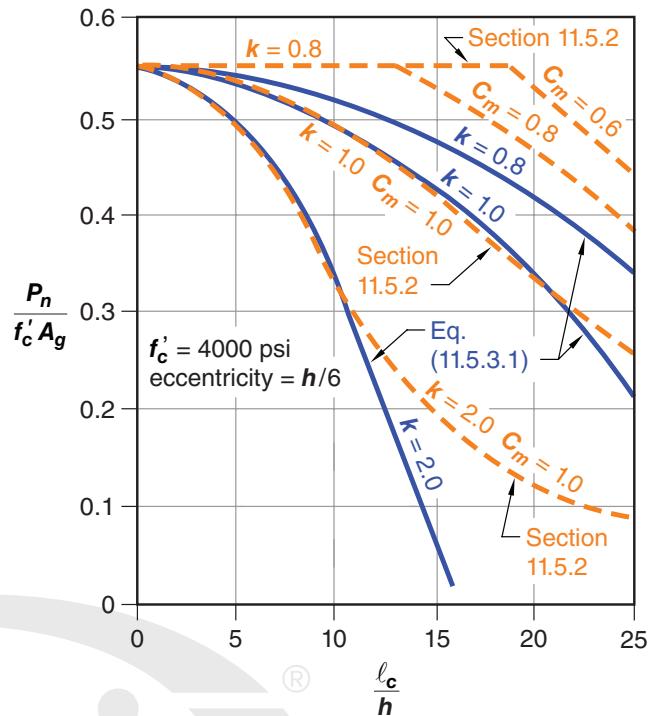


Fig. R11.5.3.1—Simplified design of walls, Eq. (11.5.3.1) versus 11.5.2.

**11.5.3.2** Effective length factor  $k$  for use with Eq. (11.5.3.1) shall be in accordance with Table 11.5.3.2.

**Table 11.5.3.2—Effective length factor  $k$  for walls**

Boundary conditions	$k$
Walls braced top and bottom against lateral translation and:	
(a) Restrained against rotation at one or both ends (top, bottom, or both)	0.8
(b) Unrestrained against rotation at both ends	1.0
Walls not braced against lateral translation	2.0

**11.5.3.3**  $P_n$  from Eq. (11.5.3.1) shall be reduced by  $\phi$  for compression-controlled sections in 21.2.2.

**11.5.3.4** Wall reinforcement shall be at least that required by 11.6.

#### 11.5.4 In-plane shear

**11.5.4.1**  $V_n$  shall be calculated in accordance with 11.5.4.2 through 11.5.4.4. Alternatively, for walls with  $h_w/l_w < 2$ , it shall be permitted to design for in-plane shear in accordance with the strut-and-tie method of Chapter 23. In all cases, reinforcement shall satisfy the limits of 11.6, 11.7.2, and 11.7.3.

#### R11.5.4 In-plane shear

**R11.5.4.1** In-plane shear is primarily of importance for structural walls with a small height-to-length ratio ( $h_w/l_w < 2$ ). The design of taller walls, particularly walls with uniformly distributed reinforcement, will likely be controlled by flexural considerations. Possible exceptions may occur in tall structural walls subject to strong earthquake excitation.

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**11.5.4.2**  $V_n$  at any horizontal section shall not exceed 8  $\sqrt{f'_c} A_{cv}$ .

**11.5.4.3**  $V_n$  shall be calculated by:

$$V_n = (\alpha_c \lambda \sqrt{f'_c} + \rho_t f_{yt}) A_{cv} \quad (11.5.4.3)$$

where:

$\alpha_c = 3$  for  $h_w/\ell_w \leq 1.5$

$\alpha_c = 2$  for  $h_w/\ell_w \geq 2.0$

$\alpha_c$  varies linearly between 3 and 2 for  $1.5 < h_w/\ell_w < 2.0$

**11.5.4.4** For walls subject to a net axial tension,  $\alpha_c$  in Eq. (11.5.4.3) shall be taken as:

$$\alpha_c = 2 \left( 1 + \frac{N_u}{500A_g} \right) \geq 0.0 \quad (11.5.4.4)$$

where  $N_u$  is negative for tension.

**11.5.5 Out-of-plane shear**

**11.5.5.1**  $V_n$  shall be calculated in accordance with 22.5.

**11.6—Reinforcement limits**

**11.6.1** If in-plane  $V_u \leq 0.5\phi\alpha_c\lambda\sqrt{f'_c} A_{cv}$ , minimum  $\rho_\ell$  and minimum  $\rho_t$  shall be in accordance with Table 11.6.1. These limits need not be satisfied if adequate strength and stability can be demonstrated by structural analysis.

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**R11.5.4.2** This limit is imposed to guard against diagonal compression failure in structural walls.

**R11.5.4.4** For structural walls where a net axial tension force is calculated for the entire wall section, the shear strength contribution attributed to the concrete is reduced and may be negligible. For these members, wall transverse reinforcement must be designed to resist most, if not all, of the factored shear force.

**R11.6—Reinforcement limits**

**R11.6.1** Both horizontal and vertical shear reinforcement are required for all walls. The distributed reinforcement is identified as being oriented parallel to either the longitudinal or transverse axis of the wall. Therefore, for vertical wall segments, the notation used to describe the horizontal distributed reinforcement ratio is  $\rho_t$ , and the notation used to describe the vertical distributed reinforcement ratio is  $\rho_\ell$ .

The reduced minimum reinforcement for precast walls recognizes that precast members have less restraint to shrinkage during curing and are usually not as rigidly connected as monolithic concrete, resulting in reduced restraint stresses due to both shrinkage and temperature change (PCI Committee on Precast Concrete Bearing Wall Buildings 1976; Portland Cement Association 1980). Reduced minimum reinforcement and greater spacings in 11.7.2.2 are allowed because precast wall panels have very little restraint at their edges during early stages of curing and develop less shrinkage stress than comparable cast-in-place walls.

Transverse reinforcement is not required in precast, prestressed walls equal to or less than 12 ft wide because this width is less than that in which shrinkage and temperature stresses can build up to a magnitude requiring transverse reinforcement. In addition, much of the shrinkage occurs before the members are connected into the structure. Once in the final structure, the members are usually not as rigidly connected transversely as monolithic concrete; thus, the transverse restraint stresses due to both shrinkage and temperature change are significantly reduced.

**CODE****COMMENTARY****Table 11.6.1—Minimum reinforcement for walls with in-plane  $V_u \leq 0.5\phi\alpha_c\lambda\sqrt{f'_c}A_{cv}$** 

Wall type	Type of non prestressed reinforcement	Bar/wire size	$f_y$ , psi	Minimum longitudinal <sup>[1]</sup> , $\rho_\ell$	Minimum transverse, $\rho_t$
Cast-in-place	Deformed bars	≤ No. 5	≥ 60,000	0.0012	0.0020
			< 60,000	0.0015	0.0025
	Welded-wire reinforcement	> No. 5 ≤ W31 or D31	Any	0.0015	0.0025
Precast <sup>[2]</sup>	Deformed bars or welded-wire reinforcement	Any	Any	0.0012	0.0020

<sup>[1]</sup>Walls with an average compressive stress, due to effective prestress force only, of at least 225 psi need not meet the requirement for minimum longitudinal reinforcement  $\rho_\ell$ .

<sup>[2]</sup>In one-way precast, prestressed walls not wider than 12 ft and not mechanically connected to cause restraint in the transverse direction, the minimum reinforcement requirement in the direction normal to the flexural reinforcement need not be satisfied.

**11.6.2** If in-plane  $V_u > 0.5\phi\alpha_c\lambda\sqrt{f'_c}A_{cv}$ , (a) and (b) shall be satisfied:

(a)  $\rho_\ell$  shall be at least the greater of the value calculated by Eq. (11.6.2) and 0.0025, but need not exceed  $\rho_t$  required for strength by 11.5.4.3.

$$\rho_\ell \geq 0.0025 + 0.5(2.5 - h_w/\ell_w)(\rho_t - 0.0025) \quad (11.6.2)$$

(b)  $\rho_t$  shall be at least 0.0025.

**R11.6.2** For monotonically loaded walls with low height-to-length ratios, test data (Barda et al. 1977) indicate that horizontal shear reinforcement becomes less effective for shear resistance than vertical reinforcement. This change in effectiveness of the horizontal versus vertical reinforcement is recognized in Eq. (11.6.2); if  $h_w/\ell_w$  is less than 0.5, the amount of vertical reinforcement is equal to the amount of horizontal reinforcement. If  $h_w/\ell_w$  is greater than 2.5, only a minimum amount of vertical reinforcement is required (0.0025sh).

**11.7—Reinforcement detailing****11.7.1 General**

**11.7.1.1** Concrete cover for reinforcement shall be in accordance with 20.5.1.

**11.7.1.2** Development lengths of deformed and prestressed reinforcement shall be in accordance with 25.4.

**11.7.1.3** Splice lengths of deformed reinforcement shall be in accordance with 25.5.

**11.7.2 Spacing of longitudinal reinforcement**

**11.7.2.1** Spacing  $s$  of longitudinal bars in cast-in-place walls shall not exceed the lesser of  $3h$  and 18 in. If shear reinforcement is required for in-plane strength, spacing of longitudinal reinforcement shall not exceed  $\ell_w/3$ .

**11.7.2.2** Spacing  $s$  of longitudinal bars in precast walls shall not exceed the lesser of (a) and (b):

- (a)  $5h$
- (b) 18 in. for exterior walls or 30 in. for interior walls

If shear reinforcement is required for in-plane strength,  $s$  shall not exceed the smallest of  $3h$ , 18 in., and  $\ell_w/3$ .

**11.7.2.3** For walls with thickness greater than 10 in., except single story basement walls and cantilever retaining

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walls, distributed reinforcement in each direction shall be placed in at least two curtains, one near each face.

**11.7.2.4** Flexural tension reinforcement shall be well distributed and placed as close as practicable to the tension face.

**11.7.3 Spacing of transverse reinforcement**

**11.7.3.1** Spacing  $s$  of transverse reinforcement in cast-in-place walls shall not exceed the lesser of  $3h$  and 18 in. If shear reinforcement is required for in-plane strength,  $s$  shall not exceed  $\ell_w/5$ .

**11.7.3.2** Spacing  $s$  of transverse bars in precast walls shall not exceed the lesser of (a) and (b):

- (a)  $5h$
- (b) 18 in. for exterior walls or 30 in. for interior walls

If shear reinforcement is required for in-plane strength,  $s$  shall not exceed the least of  $3h$ , 18 in., and  $\ell_w/5$ .

**11.7.4 Through-thickness shear reinforcement**

**11.7.4.1** Shear reinforcement required for out-of-plane strength shall extend as close to the extreme compression and tension surfaces of the wall as practicable, and satisfy the requirements of **25.7.1.3** or **25.7.1.8**.

**11.7.5 Lateral support of longitudinal reinforcement**

**11.7.5.1** If longitudinal reinforcement is required for compression and if  $A_{st}$  exceeds  $0.01A_g$ , longitudinal reinforcement shall be laterally supported by transverse ties.

**11.7.6 Reinforcement around openings**

**11.7.6.1** In addition to the minimum reinforcement required by 11.6, at least two No. 5 bars in walls having two layers of reinforcement in both directions and one No. 5 bar in walls having a single layer of reinforcement in both directions shall be provided around window, door, and similarly sized openings. Such bars shall develop  $f_y$  in tension at the corners of the openings.

**11.8—Alternative method for out-of-plane slender wall analysis****11.8.1 General**

**11.8.1.1** It shall be permitted to analyze out-of-plane slenderness effects in accordance with this section for walls satisfying (a) through (e):

- (a) Cross section is constant over the height of the wall

**COMMENTARY****R11.8—Alternative method for out-of-plane slender wall analysis****R11.8.1 General**

**R11.8.1.1** This procedure is presented as an alternative to the requirements of 11.5.2.1 for the out-of-plane design of slender wall panels, where the panels are restrained against overturning at the top.

Panels that have windows or other large openings are not considered to have constant cross section over the height of

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- (b) Wall is tension-controlled for out-of-plane moment effect
- (c)  $\phi M_n$  is at least  $M_{cr}$ , where  $M_{cr}$  is calculated using  $f_r$  as provided in 19.2.3
- (d)  $P_u$  at the midheight section does not exceed  $0.06f_c' A_g$
- (e) Calculated out-of-plane deflection due to service loads,  $\Delta_s$ , including  $P\Delta$  effects, does not exceed  $\ell_c/150$

### 11.8.2 Modeling

**11.8.2.1** The wall shall be analyzed as a simply supported, axially loaded member subject to an out-of-plane uniformly distributed lateral load, with maximum moments and deflections occurring at midheight.

**11.8.2.2** Concentrated gravity loads applied to the wall above any section shall be assumed to be distributed over a width equal to the bearing width, plus a width on each side that increases at a slope of 2 vertical to 1 horizontal, but not extending beyond (a) or (b):

- (a) The spacing of the concentrated loads
- (b) The edges of the wall panel

### 11.8.3 Factored moment

**11.8.3.1**  $M_u$  at midheight of wall due to combined flexure and axial loads shall include the effects of wall deflection in accordance with (a) or (b):

(a) By iterative calculation using

$$M_u = M_{ua} + P_u \Delta_u \quad (11.8.3.1a)$$

where  $M_{ua}$  is the maximum factored moment at midheight of wall due to lateral and eccentric vertical loads, not including  $P\Delta$  effects.  $\Delta_u$  shall be calculated by:

$$\Delta_u = \frac{5M_u \ell_c^2}{(0.75)48E_c I_{cr}} \quad (11.8.3.1b)$$

where  $I_{cr}$  shall be calculated by:

$$I_{cr} = \frac{E_s}{E_c} \left( A_s + \frac{P_u h}{f_y 2d} \right) (d - c)^2 + \frac{\ell_w c^3}{3} \quad (11.8.3.1c)$$

and the value of  $E_s/E_c$  shall be at least 6.

(b) By direct calculation using:

$$M_u = \frac{M_{ua}}{\left( 1 - \frac{5P_u \ell_c^2}{(0.75)48E_c I_{cr}} \right)} \quad (11.8.3.1d)$$

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the panel. Such walls are to be designed taking into account the effects of openings.

Many aspects of the design of tilt-up walls and buildings are discussed in ACI PRC-551.2, ACI PRC-551.3, and Carter et al. (1993).

**CODE****11.8.4 Out-of-plane deflection – service loads**

**11.8.4.1** Out-of-plane deflection due to service loads,  $\Delta_s$ , shall be calculated in accordance with Table 11.8.4.1, where  $M_a$  is calculated by 11.8.4.2.

**Table 11.8.4.1—Calculation of  $\Delta_s$** 

$M_a$	$\Delta_s$	
$\leq(2/3)M_{cr}$	$\Delta_s = \left(\frac{M_a}{M_{cr}}\right)\Delta_{cr}$	(a)
$>(2/3)M_{cr}$	$\Delta_s = \frac{2}{3}\Delta_{cr} + \frac{\left(M_a - \frac{2}{3}M_{cr}\right)}{\left(M_a - \frac{2}{3}M_{cr}\right)}\left(\Delta_n - \frac{2}{3}\Delta_{cr}\right)$	(b)

**COMMENTARY****R11.8.4 Out-of-plane deflection – service loads**

**R11.8.4.1** Test data (Athey 1982) demonstrate that out-of-plane deflections increase rapidly when the service-level moment exceeds  $2/3M_{cr}$ . A linear interpolation between  $\Delta_u$  and  $\Delta_s$  is used to determine  $\Delta_s$  to simplify the design of slender walls if  $M_a > 2/3M_{cr}$ .

Service-level load combinations are not defined in Chapter 5 of the Code but are discussed in Appendix C of ASCE/SEI 7. Appendices to ASCE/SEI 7 are not considered mandatory parts of that standard. For calculating service-level lateral deflections of structures, Appendix C of ASCE/SEI 7 recommends using the following load combination:

$$D + 0.5L + W_a$$

in which  $W_a$  is wind load based on serviceability wind speeds provided in the commentary to Appendix C of ASCE/SEI 7. If the slender wall is designed to resist earthquake effects  $E$ , and  $E$  is based on strength-level earthquake effects, the following load combination is considered to be appropriate for evaluating service-level lateral deflections

$$D + 0.5L + 0.7E$$

**11.8.4.2** The maximum moment  $M_a$  at midheight of wall due to service lateral and eccentric vertical loads, including  $P_s\Delta_s$  effects, shall be calculated by Eq. (11.8.4.2) with iteration of deflections.

$$M_a = M_{sa} + P_s\Delta_s \quad (11.8.4.2)$$

**11.8.4.3**  $\Delta_{cr}$  and  $\Delta_n$  shall be calculated by (a) and (b):

$$(a) \Delta_{cr} = \frac{5M_{cr}\ell_c^2}{48E_c I_g} \quad (11.8.4.3a)$$

$$(b) \Delta_n = \frac{5M_n\ell_c^2}{48E_c I_{gr}} \quad (11.8.4.3b)$$

**11.8.4.4**  $I_{cr}$  shall be calculated by Eq. (11.8.3.1c).