

Haskell Mini-Course: Functors, Applicatives, Readers, Traverses

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Table of Contents

1. Overview
2. The Code (verbatim)
3. Part A — Either
4. Part B — Reader
5. Part C — traverse / sequence
6. Part D — Mix & Match
7. Add-on 1 — Validation (accumulating)
8. Add-on 2 — ReaderT + Either
9. Add-on 3 — Functor law sanity checks
10. Add-on 4 — Reader ask/asks/local
11. Add-on 5 — traverse_ variants
12. Exercises
13. Glossary
- 1) Overview

Overview

This tutorial explains how the single module above demonstrates core FP patterns in Haskell:

- Either for safe parsing and validation (fail-fast)
- Reader (as plain functions and as Reader/ReaderT) for environment-dependent code
- Functor/Applicative/Monad patterns and when to use each
- traverse/sequence to collect effects across lists
- A custom Validation applicative that accumulates multiple errors

Each section below summarizes the intent, then the Exercises section helps you practice.

2) The Code (verbatim – do not modify)

```
{-# OPTIONS_GHC -Wall #-}
module Main where

import Control.Applicative (liftA2, (*>))
import Data.List.NonEmpty (NonEmpty(..))
import Text.Read (readMaybe)

-- Reader (plain) utilities
import Control.Monad.Reader (Reader, asks, local, runReader)
-- ReaderT transformer (qualified to avoid name clashes)
import qualified Control.Monad.Trans.Reader as RT
import Control.Monad.Trans.Class (lift)
import Data.Foldable (foldMap)

-----

-- Part A – Either
-----

-- (3) readPositive
readPositive :: String -> Either String Int
readPositive s =
  case readMaybe s of
```

```

    Nothing -> Left ("not an Int: " ++ s)
    Just n  -> if n > 0 then Right n else Left ("non-positive: " ++ s)

-- (4) mkRange
mkRange :: String -> String -> Either String (Int,Int)
mkRange loS hiS =
    liftA2 (,) (readPositive loS) (readPositive hiS) >= \ (lo,hi) ->
        if lo < hi then Right (lo,hi) else Left "invalid range: lo>=hi"

-- (5) parseAll
parseAll :: [String] -> Either String [Int]
parseAll = traverse readPositive

-----
-- Part B – Reader (as (-> r))
-----

-- (6) incEnv
incEnv :: Int -> Int
incEnv = fmap (+1) id

-- (7) Applicative combine: Env greeting (curried greet)
data Env = Env { firstName :: String, lastName :: String } deriving Show

greet :: String -> String -> String
greet first last = "Hi " ++ first ++ " " ++ last

fullGreeting :: Env -> String
fullGreeting = greet <$> firstName <*> lastName

-- (8) Reader monad composition
data Cfg = Cfg { base :: Int, factor :: Int } deriving Show

step1 :: Cfg -> Int
step1 = base

step2 :: Int -> Cfg -> Int
step2 x cfg = x * factor cfg

step3 :: Int -> Cfg -> String
step3 x _ = "result=" ++ show x

pipeline :: Cfg -> String
pipeline = step1 >= step2 >= step3    -- (-> Cfg) monad

-- (9) local environment tweak (pure functions)
priceWithTax :: Double -> (Double -> Double)
priceWithTax taxRate = \basePrice -> basePrice * (1 + taxRate)

total :: Double -> Double -> Double
total tax basePrice = priceWithTax tax basePrice

totalDiscounted :: Double -> Double -> Double

```

```
totalDiscounted tax basePrice = priceWithTax (tax * 0.9) basePrice
```

```
-----  
-- Part C – traverse / sequence  
-----
```

```
safeDiv :: Int -> Int -> Maybe Int  
safeDiv _ 0 = Nothing  
safeDiv x y = Just (x `div` y)
```

```
-----  
-- Part D – Mix & Match  
-----
```

```
lookupKey :: String -> [(String, Int)] -> Either String Int  
lookupKey k env =  
  case lookup k env of  
    Nothing -> Left ("missing: " ++ k)  
    Just v   -> Right v
```

```
type Assoc = [(String, Int)]
```

```
need :: [String] -> (Assoc -> Either String [Int])  
need ks env = traverse (\k -> lookupKey k env) ks
```

```
data C = C { low :: Int, high :: Int } deriving Show
```

```
mkC :: Int -> Int -> Either String C  
mkC l h | l < h      = Right (C l h)  
        | otherwise = Left "low>=high"
```

```
render :: C -> String  
render c = "range: [" ++ show (low c) ++ ", " ++ show (high c) ++ "]"
```

```
build :: (Int, Int) -> (C -> String)  
build (l,h) =  
  case mkC l h of  
    Left e   -> const ("error: " ++ e)  
    Right c  -> const (render c)
```

```
-- (20) traverse_ (custom)  
traverse_ :: Applicative f => (a -> f b) -> [a] -> f ()  
traverse_ _ []      = pure ()  
traverse_ g (x:xs) = g x *> traverse_ g xs
```

```
-----  
-- Add-on 1: Validation style Applicative that accumulates errors  
-----
```

```
data V e a = Failure e | Success a  
  deriving (Show, Eq)
```

```
instance Functor (V e) where
```

```

fmap f (Success a) = Success (f a)
fmap _ (Failure e) = Failure e

instance Semigroup e => Applicative (V e) where
  pure = Success
  Success f <*> Success a = Success (f a)
  Failure e1 <*> Failure e2 = Failure (e1 <> e2)
  Failure e <*> _ = Failure e
  _ <*> Failure e = Failure e

-- A helper to lift String messages into NonEmpty
one :: a -> NonEmpty a
one x = x :| []

readPositiveV :: String -> V (NonEmpty String) Int
readPositiveV s =
  case readMaybe s of
    Nothing -> Failure (one ("not an Int: " ++ s))
    Just n -> if n > 0 then Success n else Failure (one ("non-positive: " ++ s))

-- Combine two validated fields, then check a cross-field invariant
mkRangeV :: String -> String -> V (NonEmpty String) (Int, Int)
mkRangeV loS hiS =
  case liftA2 (,) (readPositiveV loS) (readPositiveV hiS) of
    Failure es -> Failure es
    Success (lo,hi) -> if lo < hi
                        then Success (lo,hi)
                        else Failure (one "invalid range: lo>=hi")

-----
-- Add-on 2: ReaderT + Either composition
-----

type App e r a = RT.ReaderT r (Either e) a

askAssoc :: App String Assoc Assoc
askAssoc = RT.ask

needKeyT :: String -> App String Assoc Int
needKeyT k = do
  env <- RT.ask
  case lookup k env of
    Nothing -> lift (Left ("missing: " ++ k))
    Just v -> pure v

needAllT :: [String] -> App String Assoc [Int]
needAllT = traverse needKeyT

-----
-- Add-on 3: QuickCheck-style notes (kept simple & runnable without QuickCheck)
-----

-- We show the Functor laws on a few concrete examples

```

```

functorIdTests :: IO ()
functorIdTests = do
  putStrLn "Functor identity law (Maybe):"
  print (fmap id (Just 5) == (Just 5))
  print (fmap id (Nothing :: Maybe Int) == Nothing)

functorCompTests :: IO ()
functorCompTests = do
  putStrLn "Functor composition law (Maybe):"
  let f = (+1); g = (*2)
  print (fmap (f . g) (Just 10) == (fmap f . fmap g) (Just 10))
  print (fmap (f . g) (Nothing :: Maybe Int) == (fmap f . fmap g) (Nothing :: Maybe Int))

{-
-- If you want real QuickCheck, uncomment and add quickcheck to your build:
import Test.QuickCheck
prop_Functor_Id :: Maybe Int -> Bool
prop_Functor_Id x = fmap id x == x

prop_Functor_Comp :: Fun Int Int -> Fun Int Int -> Maybe Int -> Bool
prop_Functor_Comp (Fun _ f) (Fun _ g) x =
  fmap (f . g) x == (fmap f . fmap g) x
-}

-----
-- Add-on 4: Reader newtype demo with ask/asks/local
-----

fullGreetingR :: Reader Env String
fullGreetingR = do
  f <- asks firstName
  l <- asks lastName
  pure (greet f l)

promoGreeting :: Reader Env String
promoGreeting =
  local (\e -> e { lastName = lastName e ++ " (VIP)" }) fullGreetingR

-----
-- Add-on 5: traverse_ via foldMap (alternative implementation)
-----

traverse_foldMap_ :: (Applicative f, Monoid (f ())) => (a -> f b) -> [a] -> f ()
traverse_foldMap_ g = foldMap (\x -> g x *> pure ())

-----
-- Alternate styles (point-free / do-notation where it helps)
-----

-- A3-alt) readPositive (point-free-ish helper)
readPositivePF :: String -> Either String Int
readPositivePF = maybeErr . readMaybe
  where

```

```

    maybeErr Nothing = Left "not an Int"
    maybeErr (Just n) = if n > 0 then Right n else Left "non-positive"

-- A4-alt) mkRange using do-notation
mkRangeDo :: String -> String -> Either String (Int,Int)
mkRangeDo loS hiS = do
    lo <- readPositive loS
    hi <- readPositive hiS
    if lo < hi then pure (lo,hi) else Left "invalid range: lo>=hi"

-- B7-alt) fullGreeting point-free (same shape as fullGreeting)
fullGreetingPF :: Env -> String
fullGreetingPF = greet <$> firstName <*> lastName

-- B8-alt) pipeline with explicit composition
pipelinePF :: Cfg -> String
pipelinePF cfg = step3 (step2 (step1 cfg) cfg) cfg

-- C12-alt) traverse with safeDiv (same but explicit)
safeDivs :: [Int] -> Maybe [Int]
safeDivs = traverse (safeDiv 100)

-- D15-alt) lookupKey using maybe
lookupKeyPF :: String -> (Assoc -> Either String Int)
lookupKeyPF k env = maybe (Left ("missing: " ++ k)) Right (lookup k env)

-- D16-alt) need (more point-free)
needPF :: [String] -> (Assoc -> Either String [Int])
needPF ks env = traverse (`lookupKey` env) ks

-- D20-alt) traverse_ using foldr
traverse_foldr :: Applicative f => (a -> f b) -> [a] -> f ()
traverse_foldr g = foldr (\x acc -> g x *> acc) (pure ())

-----
-- Demo helpers
-----

sep :: String -> IO ()
sep title = putStrLn ("\n--- " ++ title ++ " ---")

showEitherList :: Show a => Either String [a] -> String
showEitherList (Left e) = "Left " ++ show e
showEitherList (Right x) = "Right " ++ show x

main :: IO ()
main = do
    sep "Part A – Either"
    print (fmap (+1) (Right 4 :: Either String Int))
    print (fmap (+1) (Left "err" :: Either String Int))
    print (Right 3 >>= (\x -> Right (x*10) :: Either String Int))
    print (Left "bad" >>= (\x -> Right (x*10) :: Either String Int))
    print (liftA2 (+) (Left "A") (Left "B") :: Either String Int)

```

```

print (readPositive "10")
print (readPositive "0")
print (readPositive "abc")
print (mkRange "2" "5")
print (mkRange "5" "2")
putStrLn (showEitherList (parseAll ["3","2","x","5"]))
putStrLn (showEitherList (parseAll ["3","2","5"]))

sep "Part B – Reader"
print (incEnv 41) -- 42
print (fullGreeting (Env "Ada" "Lovelace"))
putStrLn (pipeline (Cfg 3 7))
print (total 0.15 100)
print (totalDiscounted 0.15 100)

sep "Part C – traverse / sequence"
print (sequence [Just 1, Just 2, Just 3])
print (sequence [Just 1, Nothing, Just 3])
print (traverse (safeDiv 100) [5,4,0,2])

sep "Part D – Mix & Match"
let env = [("a",10),("b",20)] :: Assoc
print (lookupKey "a" env)
print (lookupKey "c" env)
print (need ["a","b"] env)
print (need ["a","z"] env)
putStrLn (render (C 1 4))
putStrLn (build (1,4) (C 100 200))
putStrLn (build (4,1) (C 100 200))

sep "Add-on 1 – Validation (accumulating)"
print (readPositiveV "10")
print (readPositiveV "0")
print (mkRangeV "2" "5")
print (mkRangeV "0" "x") -- two errors accumulated

sep "Add-on 2 – ReaderT + Either"
let assoc = [("a",1),("b",2)] :: Assoc
print (RT.runReaderT (needAllT ["a","b"]) assoc)
print (RT.runReaderT (needAllT ["a","z"]) assoc)

sep "Add-on 3 – QuickCheck-style sanity checks"
functorIdTests
functorCompTests

sep "Add-on 4 – Reader ask/asks/local"
print (runReader fullGreetingR (Env "Grace" "Hopper"))
print (runReader promoGreeting (Env "Grace" "Hopper"))

sep "Add-on 5 – traverse_ variants"
print (traverse_ (\n -> if n>0 then Just () else Nothing) [1,2,3])
print (traverse_ (\n -> if n>0 then Just () else Nothing) [1,0,3])

```

```
print (traverse_foldMap_ (\n -> if n>0 then Just () else Nothing) [1,2,3])
print (traverse_foldr (\n -> if n>0 then Just () else Nothing) [1,2,3])
```

```
putStrLn "Done."
```

3) Part A — Either

Use Either for parsing/validation. Applicative (liftA2) parses independent fields; Monad (>>=) checks cross-field constraints like `lo < hi`. `traverse readPositive` turns `[String]` into `Either String [Int]`.

4) Part B — Reader

Functions `(r -> a)` form Functor/Applicative/Monad. `<$>` and `<*>` feed the same `Env` to multiple getters; `>>=` threads the same `Cfg` through steps.

5) Part C — traverse / sequence

Flip structure and effect: `traverse :: (a -> f b) -> t a -> f (t b)`. With `Maybe/Either`, failures short-circuit; successes collect.

6) Part D — Mix & Match

Combine Reader and Either: lookups read from an environment and may fail. Build separates validation (`mkC`) from rendering (pure function).

7) Add-on 1 — Validation

Applicative that accumulates errors via Semigroup/NonEmpty, allowing multiple validation messages.

8) Add-on 2 — ReaderT + Either

A tiny app stack: configuration + fail-with-message. `Traverse` batches dependent reads.

9) Add-on 3 — Functor law checks

Executable checks for identity and composition laws on `Maybe`.

10) Add-on 4 — Reader utilities

`asks` extracts fields; `local` runs a computation under a tweaked environment.

11) Add-on 5 — traverse_ variants

Three ways to sequence effects while discarding results; `foldMap` variant needs `Monoid (f ())`.

12) Exercises (keyed to sections)

Part A — Either (Parsing & Validation)

- 1) Evaluate: `fmap (+1) (Right 4)`; `fmap (+1) (Left "err" :: Either String Int)`.
- 2) Write inputs that make `readPositive` return `Left` for (a) non-number, (b) non-positive.
- 3) Predict `mkRange "2" "5"` and `mkRange "5" "2"` results; explain why.
- 4) Using `parseAll`, find the first failing element in `["3","2","x","5"]`.
- 5) Modify the idea: enforce `lo < hi` after parsing both ends (explain Applicative vs Monad use).

Part B — Reader (Functions as Environments)

- 6) Explain `incEnv = fmap (+1) id` in terms of composing functions.
- 7) For `Env {firstName, lastName}`, explain `fullGreeting = greet <$> firstName <*> lastName`.
- 8) For `Cfg {base,factor}`, trace pipeline (`Cfg 3 7`).
- 9) Compare `total` vs `totalDiscounted` on (`tax=0.15`, `base=100`).

Part C — traverse / sequence

- 10) Evaluate: sequence [Just 1, Just 2, Just 3] and sequence [Just 1, Nothing, Just 3].
- 11) Evaluate: traverse (safeDiv 100) [5,4,0,2] — where does it stop and why?
- 12) Replace Maybe with Either String in safeDiv to return division-by-zero messages.

Part D — Mix & Match

- 13) Using need ["a","b"] with env = [("a",10),("b",20)], compute the result.
- 14) Using need ["a","z"] with same env, what happens and why?
- 15) Explain how build makes a total renderer from possibly failing mkC.

Add-on 1 — Validation (Accumulating Errors)

- 16) Give inputs that produce two errors in mkRangeV (e.g., both ends invalid).
- 17) Why does V require Semigroup for its error type? Give a concrete error combination.

Add-on 2 — ReaderT + Either

- 18) Show RT.runReaderT (needAllT ["a","b"]) [("a",1),("b",2)].
- 19) Show RT.runReaderT (needAllT ["a","z"]) [("a",1),("b",2)]. Explain the Left.

Add-on 3/4/5 — Laws & Utilities

- 20) Run functorIdTests and functorCompTests. Explain why they print True.
- 21) Show how local changes an Env in promoGreeting compared to fullGreetingR.
- 22) Compare traverse_, traverse_foldr, traverse_foldMap_ in terms of constraints.

13) Glossary

Functor: Type constructor supporting fmap to map $a \rightarrow b$ over $f\ a$.

Applicative: Extends Functor; apply effectful functions to effectful args with $\langle * \rangle$; liftA2 for binary functions.

Monad: Extends Applicative; bind ($\gg=$) allows dependent sequencing.

Reader: Environment-passing pattern; plain functions $r \rightarrow a$ behave as a Reader.

ReaderT: Adds a read-only environment on top of another effect.

Either: Error-aware computation: Left e for error, Right a for success.

Maybe: Partial computation: Nothing = failure, Just a = success.

traverse: Map with effects and flip: $t\ a \rightarrow f\ (t\ b)$.

sequence: Flip $t\ (f\ a)$ to $f\ (t\ a)$.

NonEmpty: List with at least one element; useful for aggregating one-or-more errors.

Semigroup: Types with an associative ($\langle \rangle$) operation.

Monoid: Semigroup with identity mempty; required by foldMap aggregation.