Technical Report: Description-Similarity Rules

Yafeng Tang[1]
Harbin Institute of Technology
Harbin, China
yafengtang@hit.edu.cn

Zheng Liang[1]
Harbin Institute of Technology
Harbin, China
lz20@hit.edu.cn

Xiaoou Ding
Harbin Institute of Technology
Harbin, China
dingxiaoou_hit@hit.edu.cn

Hongzhi Wang
Harbin Institute of Technology
Harbin, China
wangzh@hit.edu.cn

Huan Hu
Huawei Cloud Computing
Technologies Co., Ltd
Hangzhou, China
huhuan18@huawei.com

Zhaoqiang Chen
Huawei Cloud Computing
Technologies Co., Ltd
Hangzhou, China
chenzhaoqiang1@huawei.com

ABSTRACT

1 DESIGN CHOICE OF DESCRIPTIONS

In this section, we conducted an analysis to examine the relationship between attribute description and similarities. We present four statistical measures for attribute descriptions, including: (1)average length: `length` (2)number of text segments `AWN`, (3)`entropy`, and (4) index of coincidence `IC`. These descriptions have covered all six mainstream similarity functions [1]. Based on similarity function libraries established on [7] and mentioned in AutoEM [2], we show all similarity functions used in our experiment, which are sampled from each category as follows. The input attribute pairs are presented as s_1 and s_2

Levenshtein Distance. Levenshtein Distance [8] tends to increase with the `length` of the strings. This is because longer strings offer more possibilities for editing operations, making it more challenging to find the best matching edit sequence between two strings. Levenshtein Distance can be defined as

$$D[i,j] = \begin{cases} 0 & \text{if } i = 0 \& j = 0 \\ i & \text{if } j = 0 \& i > 0 \\ j & \text{if } i = 0 \& j > 0 \\ \min \begin{cases} D[i-1,j]+1 \\ D[i,j-1]+1 \\ D[i-1,j-1]+\text{cost}(s_1[i],s_2[j]) \end{cases} & \text{else} \end{cases} \tag{1}$$

where the function $cost(s_1[i], s_2[j])$ represents the editing cost required to transform character s_1 into character s_2. If s_1 is equal to s_2, then the cost of transformation $cost(s_1[i], s_2[j])$ is 0; otherwise, it is 1.

Mmcwpa Similarity. Modified MinCost With Prefix and Approximate Similarity, which abbreviated as mmcwpa, is the regularized version of Levenshtein similarity. It is also associate with `length`

Affine. Affine [10] assigns scores to the following four operations between characters defined by Levenshtein: the match/mismatch, insert, and delete. By comparing these scores, affine selects the path that maximizes the score as the optimization target to calculate the final score. The Affine formula is shown below.

$$\text{Affine}(s_1,s_2) = \frac{Levenshtein(match, mismatch, insert, delete)}{max(length(s1), length(s2))} \tag{2}$$

Clearly, there is a strong correlation between length, as the denominator in equation (2) is the `length` of attribute pairs.

Needleman-Wensch As a sequence-based similarity, Needleman-Wensch [11] is related to sequence statistics `AWN` and has similar definition as Affine Similarity on the scoring for characters operation between two sequences. The goal of Needleman-Wensch is to maintain as many corresponding characters in the same position throughout the calculation process.

Needleman's potential optimization goal is to have the same length for both strings after multiple operations, which indicates that `length` is related to the calculation of Needleman-Wensch.

Smith-Waterman. Smith-Waterman and the Needleman-Wensch algorithms are both dynamic programming-based sequence alignment algorithms. However, Smith-Waterman algorithm [12] allows for faster backtracking without requiring reaching the end of either sequence. Despite this difference, both algorithms use the same fundamental calculation method for scoring sequence similarity, making them both related in terms of `length` and `AWN`.

Birnbaum Similarity. Birnbaum similarity [13] calculation is based on the co-occurrence matrix. Given a co-occurrence matrix A, where A_{ij} represents the frequency of character j co-occurring with attribute value i. It is worth noting that `IC` can be derived from matrix A. Birnbaum similarity can be defined as Equation 3.

$$\text{Birnbaum}(s_1,s_2) = \frac{\sum_i \min(A_i,B_i)}{\sum_i \max(A_i,B_i)} \tag{3}$$

where A and B present the co-occurrence matrix of s_1 and s_2.

BulkDelete Similarity. BulkDelete similarity [14] is based on LCS distance [3] and the `length` of attribute pairs, which is defined as follows.

$$\text{BulkDelete}(s_1,s_2) = \frac{LCS(s_1,s_2)}{min(length(s_1), length(s_2))} \tag{4}$$

BulkDelete similarity is widely used especially when two strings have a significant amount of similar content but are not entirely identical.

Euclidean Distance. Euclidean Distance is a vector-based similarity, which calculate the distance between two points in the

Yafeng Tang and Zheng Liang contributed equally to this work and should be considered co-first authors.

given space. As we can see, given the attribute A_1, A_2 and its corresponding vocabulary, `entropy` can describe them in vector form. Euclidean Distance is defined as follows.

$$\text{Euclidean distance} = \sqrt{\sum_{i=1}^{n}(v_{2,i} - v_{1,i})^2} \tag{5}$$

where v_1, v_2 are the `entropy` vector of attribute pairs.

Exact Match. Exact Match is used to determine whether two strings are completely identical, returning a boolean variable. During the calculation process, it first checks if the length of the input strings are equal, hence it can be considered as being related to `length`.

Jaccard. Jaccard similarity [15] is individual-based similarity, which is defined as the size of the intersection of two sets divided by the size of their union, indicating the degree of overlap between the sets. Given attribute pairs (s_1, s_2), their Jaccard similarity can be calculated using Equation 6

$$\text{Jaccard}(s_1, s_2) = \frac{|s_1 \cap s_2|}{|s_1 \cup s_2|} \tag{6}$$

It is worth noting that by using different tokenizers, the inputs of the Jaccard Similarity also differ. For example, without any segmentation processing, sets A and B are simply vocabulary sets that appear in strings s_1 and s_2 respectively, making Jaccard related to description `length`. However, if space/3-gram segmentation is applied, `AWN` becomes more relevant than `length`. In our experiment, we provide five different tokenizer including:space, 3-gram and index-split, nlp-split, base-split, which are recommended in HANLP [19].

Dice. Similar to Jaccard, Dice similarity coefficient [16] performs better when dealing with binary data or when focusing on the presence or absence of elements in sets. Given attribute pairs (s_1, s_2), Dice is calculated using Equation 7:

$$\text{Dice}(s_1, s_2) = \frac{2 \times |s_1 \cap s_2|}{length(s_1) + length(s_2)} \tag{7}$$

As we can see, the denominator in Equation 7 calculates the size of the set. Similar to the above conclusion, there is a potential correlation between Dice and `length` or `AWN`.

Simpson. As an extension of Jaccard similarity, Simpson similarity [17] is calculated based on the ratio of the number of members that are common to both sets to the number of members in the smaller set. Simpson similarity can be defined as Equation 8

$$\text{Simpson Similarity}(s_1, s_2) = \frac{|s_1 \cap s_2|}{min(length(s_1), length(s_2))} \tag{8}$$

As we can see, the denominator of Simpson calculates the minimum value of (s_1, s_2) length, hence it is related to the description `length`.

Overlap-Coefficient. By applying tokenizer on Simpson similarity, we have Overlap-coefficient [4]„ a set-based and sequences-based similarity, where `AWN` is used to calculate the minimal set size as follows.

$$overlap - coefficient = \frac{bag1 \cap bag2}{\min(d_2(bag1), d_2(bag2))}$$

where $bag1$ and $bag2$ denotes the wordBag for $s1$ and $s2$ after tokenization, respectively.

Jaro As an individual-based similarity, Jaro [5] defines a tolerance range R as the half of $\max(len(s1), len(s2))$. Then, the Jaro similarity can be defined as Equation 9.

$$Jaro(s_1, s_2) = \frac{1}{3}\left(\frac{m}{d_1(s1)} + \frac{m}{d_1(s2)} + \frac{m-n}{m}\right) \tag{9}$$

where m denotes the number of matched characters inside R, and n denotes that of identical characters at the different positions. Obviously, `length` has an impact on the Jaro similarity.

Jaro Winkler. As an extension of the Jaro similarity metric, Jaro-Winkler similarity [18] metric considers `length` and the position of matching characters, making it suitable for comparing strings of different lengths and identifying similarities even in the presence of minor discrepancies or variations. The Jaro-Winkler similarity is calculated using Equation 10:

$$JaroWinkler(s_1, s_2) = J(s_1, s_2) + \frac{lp(1 - J(s_1, s_2))}{3} \tag{10}$$

where $J(s_1, s_2)$ represents the Jaro similarity between the strings (s_1, s_2) and lp is the prefix scaling factor, which increases the similarity score for strings with a common prefix. Typically, lp is set to 0.1.

KendallTau Similarity. KendallTau similarity [20] is a sequence-based and vector-based similarity. It maintains a vocabulary that includes all characters appearing in s1 and s2. KendallTau assigns a vector to each input string, where each dimension corresponds to a character in the vocabulary. The function then counts the occurrences of each character in the two input strings separately, resulting in Kendall vectors v_1 and v_2. KendallTau can be defined as Equation 11.

$$\text{KendallTau}(s_1, s_2) = \frac{2}{n(n-1)} \sum_{n}^{i<j} sgn(v_{1i} - v_{1j}) sgn(v_{2i} - v_{2j}) \tag{11}$$

where sgn is defined as

$$sgn(x) = \begin{cases} 1 & \text{if } x > 0 \\ 0 & \text{if } x = 0 \\ -1 & \text{if } x < 0 \end{cases} \tag{12}$$

The way KendallTau generates vectors is similar to the `entropy` vector used in our attribute description. Kendall Tau correlation coefficient can be used to measure the similarity of permutation order between time series. Therefore, when analyzing permutation entropy, there may exist a certain correlation with Kendall Tau similarity.

SimHash. SimHash [22] is a locality-sensitive hashing algorithm. It utilizes existing hash functions to represent strings as hash values, and then applies the Hamming distance [21] to calculate their similarity. SimHash similarity can be formulated as follows:

$$\text{Simhash}(s_1, s_2) = 1 - \frac{Hamming(hf(s_1), hf(s_2))}{n} \tag{13}$$

where hf is the customizable hash function, n represents the length of the SimHash value (usually 64 or 128 bits, in our experiment,

n=64). In certain cases, shorter strings may increase the likelihood of SimHash collisions, thereby reducing the reliability of SimHash. Therefore, we usually recommend using Simhash to calculate similarities between long-text attributes.

cosine-Doc. • `entropy`: `entropy` is related to vector-based and taxonomies-based similarities [6]. Cosine is considered to be a commonly used similarity function for calculating numerical attributes [9]. However, we can invert attribute pairs into `entropy` vectors, and calculate cosine-Doc similarity as follows.

$$cosine - Doc = cosineSimilarity(d_3(s1), d_3(s2)) \tag{14}$$

where d_3 is the `entropy` vector for the given attribute. For more details, please refer our Equation (3) in the origin paper.

2 FULL PROOF OF PROPOSITION

Proof for Theorem 1 Consider the event ξ defined by

$$\xi = \{j \in \{1, ..., K\}, |\frac{1}{n_k}\sum_{s=1}^{n_k} X_s - f_j| \leq \frac{1}{2}\Delta_{K+1-k}\} \tag{15}$$

By Hoeffding's Inequality and an union bound, the probability of the complementary event $\overline{\xi}$ can be bounded as follows

$$\begin{aligned} P(\overline{\xi}) &\leq \sum_{j=1}^{K}\sum_{k=1}^{K-1} P(|\frac{1}{n_k}\sum_{s=1}^{n_k} X_s - f_j| \leq \frac{1}{2}\Delta_{K+1-k}) \\ &\leq \sum_{j=1}^{K}\sum_{k=1}^{K-1} 2exp(2n_k(\Delta_{K+1-k})/2)^2) \\ &\leq 2K^2 exp(-\frac{n-K}{2\overline{log}K * H}) \end{aligned} \tag{16}$$

where the last inequality comes from the fact that

$$\begin{aligned} &\geq \frac{n_k(\Delta_{K+1-k})^2}{\overline{log}(K)(K+1-H)(\Delta_{K+1-k})^{-2}} \\ &\geq \frac{n-K}{\overline{log}(K) * H} \end{aligned} \tag{17}$$

Thus, it suffices to show that on the event ξ, the algorithm does not make any error. We prove this by induction on k. Let $k \geq 1$. Assume the algorithm makes no error in all previous $k-1$ stages, that is no bad arm $\mu_i < \theta$ has been accepted and no good arm $\mu_i \geq \theta$ has been rejected. Note that event ξ implies that at the end of stage k, all empirical means are within $\frac{1}{2}(\Delta_{K+1-k})^{-2}$ of the respective true means.

Let $A_k = \{a_1, ..., a_{K+1-k}\}$ be the set of active arms during phase k. We order the a_i's such that $\mu_{a_1} > \mu_{a_2} > ... > \mu_{a_{K+1-k}}$. Denote $m' = m(k)$ for the number of arms that are left to find in phase k. The assumption that no error occurs in the first $k-1$ stages implies that

$$a_1, a_2, ..., a_{m'} \in \{1, ..., m\} \tag{18}$$

and

$$a_{m'+1}, ..., a_{K+1-k} \in \{m+1, ..., K\} \tag{19}$$

If an error is made at stage k, it can be one of the following two types:

1. The algorithm accepts a_j at stage k for some $k \geq m' + 1$
2. The algorithm rejects a_j at stage k for some $j \leq m'$

Denote $\sigma = \sigma_k$ for the bijection (from $\{1, ..., K+1-k\}$ to A_k) such that $\overline{\mu}_{\sigma(1),n_k} \geq \overline{\mu}_{\sigma(2),n_k} \geq ... \geq \overline{\mu}_{\sigma(K+1-k),n_k}$. Suppose Type 1 error occurs. Then $a_j = \sigma(1)$ since if algorithm accepts, it must accept the empirical best arm. Furthermore we also have

$$\overline{\mu}_{a_j,n_k} - \theta \geq \theta - \overline{\mu}_{\sigma(K+1-k),n_k} \tag{20}$$

since otherwise the algorithm would rather reject arm $\sigma(K+1-k)$. The condition $a_j = \sigma(1)$ and the event ξ implies that

$$\begin{aligned} \overline{\mu}_{a_j,n_k} &\geq \overline{\mu}_{a_j,n_k}, \\ \mu_{a_j} + \frac{1}{2}(\Delta_{K+1-k}) &\geq \mu_{a_1} - \frac{1}{2}(\Delta_{K+1-k}), \\ (\Delta_{K+1-k}) &\geq \mu_{a_1} - \mu_{a_j} \geq \mu_{a_1} - \theta \end{aligned} \tag{21}$$

We then look at the condition (16). In the event of ξ, for all $i \leq m'$ we have

$$\begin{aligned} \overline{\mu}_{a_j,n_k} &\geq \mu_{a_j} - \frac{1}{2}\Delta_{(K+1-k)} \\ &\geq \mu_{a_{m'}} - \frac{1}{2}\Delta_{(K+1-k)} \\ &\geq \theta - \frac{1}{2}\Delta_{(K+1-k)} \end{aligned} \tag{22}$$

On the other hand, $\overline{\mu}_{\sigma(K+1-k),n_k} \leq \overline{\mu}_{a_{K+1-k},n_k} \leq \overline{\mu}_{a_{K+1-k},n_k} + \frac{1}{2}\Delta_{(K+1-k)}$. Therefore, using those two observations and (16) we deduce

$$\begin{aligned} (\mu_{a_j} + \frac{1}{2}\Delta_{(K+1-k)}) - \theta &\geq \theta - (\mu_{a_{K+1-k}} + \frac{1}{2}\Delta_{(K+1-k)}), \\ \Delta_{(K+1-k)} \geq 2\theta - \mu_{a_j} - \mu_{a_{K+1-k}} &> \theta - \mu_{a_{K+1-k}} \end{aligned} \tag{23}$$

Thus so far we proved that if there is a Type 1 error, then

$$\Delta_{(K+1-k)} > max(\mu_{a_1} - \theta, \theta - \mu_{a_{K+1-k}}) \tag{24}$$

But at stage k, only k-1 arms have been accepted or rejected, thus $\Delta_{(K+1-k)} \leq max(\mu_{a_1} - \theta, \theta - \mu_{a_{K+1-k}})$. By contradiction, we conclude that Type 1 error does not occur.

Suppose Type 2 error occurs. The reasoning is symmetric to Type 1. This completes the induction and consequently the proof of the theorem. □

Proof for Theorem 2 Consider the events ξ_d for each pre-trained MAB defined by

$$\xi_{d_1} = \{j \in \{1, ..., K\}, |\frac{1}{n_k}\sum_{s=1}^{n_k} X_{s,d_1} - f_{j,d_1}| \leq \frac{1}{2}\Delta_{K+1-k}\}$$
$$\xi_{d_2} = \{j \in \{1, ..., K\}, |\frac{1}{n_k}\sum_{s=1}^{n_k} X_{s,d_2} - f_{j,d_2}| \leq \frac{1}{2}\Delta_{K+1-k}\} \quad (25)$$
$$...$$
$$\xi_{d_{|D|}} = \{j \in \{1, ..., K\}, |\frac{1}{n_k}\sum_{s=1}^{n_k} X_{s,d_{|D|}} - f_{j,d_{|D|}}| \leq \frac{1}{2}\Delta_{K+1-k}\}$$

Also, consider the event ξ defined by

$$\xi = \{j \in \{1, ..., K\}, |\frac{1}{n_k}\sum_{s=1}^{n_k} X_s - f_j| \leq \frac{1}{2}\Delta_{K+1-k}\} \quad (26)$$

where f_j is defined as:

$$\begin{aligned} f_j &= \frac{\sum_{sim_j \in t, A' \in D} cos < \vec{D}, \vec{D'} > *p(t, A')}{\sum_{sim_j \in t, A' \in D} cos < \vec{D}, \vec{D'} >} \\ &= \frac{\sum_d cos < \vec{D}, \vec{d} > *p(t, d)}{\sum_d cos < \vec{D}, \vec{d} >} \\ &= \frac{\sum_d cos < \vec{D}, \vec{d} > *f_{j,d}}{\sum_d cos < \vec{D}, \vec{d} >} \end{aligned} \quad (27)$$

Setting $w_d = cos < \vec{D}, \vec{d} >$, we can rewrite (26) as:

$$\begin{aligned} \xi &= \{1 \leq j \leq K, |\frac{1}{n_k}\sum_{s=1}^{n_k} \frac{\sum_d w_d * X_{s,d}}{\sum_{d \in D} w_d} - \frac{\sum_d w_d * f_{j,d}}{\sum_{d \in D} w_d}| \leq \frac{1}{2}\Delta_{K+1-k}\} \\ &= \{1 \leq j \leq K, |\frac{1}{n_k}\sum_{s=1}^{n_k}\sum_d w_d * X_{s,d} - \sum_d w_d * f_{j,d}| \leq \frac{1}{2}\sum_{d \in D} w_d \Delta_{K+1-k}\} \end{aligned} \quad (28)$$

Suppose (25) is true. Using the absolute value inequality, for any $1 \leq j \leq K$, we have:

$$\begin{aligned} &|\frac{1}{n_k}\sum_{s=1}^{n_k}\sum_d w_d * X_{s,d} - \sum_d w_d * f_{j,d}| \\ &= |\sum_d (\frac{1}{n_k}\sum_{s=1}^{n_k} w_d * X_{s,d} - w_d * f_{j,d})| \\ &\leq \sum_d w_d * |\frac{1}{n_k}\sum_{s=1}^{n_k} X_{s,d} - f_{j,d}| \\ &\leq \frac{1}{2}\sum_{d \in D} w_d \Delta_{K+1-k} \end{aligned} \quad (29)$$

This means when $\xi_{d_1} \cap ... \cap \xi_{d_{|D|}}$ is true, ξ has to hold true regardless of w_d. Its contrapositive implies that when $\bar{\xi}$ is true, $\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}$ has to hold true regardless of w_d. By full probability law, we have

$$\begin{aligned} P(\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}) &= P(\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}|\xi) * P(\xi) + \\ &\quad P(\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}|\bar{\xi}) * P(\bar{\xi}) \\ &\geq P(\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}|\bar{\xi}) * P(\bar{\xi}) = P(\bar{\xi}) \end{aligned} \quad (30)$$

In algorithm 2, for each $MAB_i \in \{MAB_1, ..., MAB_n\}$ we have

$$P(\overline{\xi_d}) \leq 2K^2 exp(-\frac{\frac{n}{a} - K}{2\overline{log}K * H(i)}) \quad (31)$$

By union bound, we come to the conclusion that

$$\begin{aligned} P(\bar{\xi}) \leq P(\overline{\xi_{d_1}} \cup ... \cup \overline{\xi_{d_{|D|}}}) &\leq \sum_{i=1}^{a} 2K^2 exp(-\frac{\frac{n}{a} - K}{2\overline{log}K * H(i)}) \\ &\leq 2aK^2 exp(-\frac{\frac{n}{a} - K}{2\overline{log}K * H(a)}) \end{aligned} \quad (32)$$

Thus, it suffices to show that, by probability of $2aK^2 exp(-\frac{\frac{n}{a}-K}{2\overline{log}K*H(a)})$, the algorithm does not make any error. □

REFERENCES

[1] Santiago Ontañón: An Overview of Distance and Similarity Functions for Structured Data. CoRR abs/2002.07420 (2020)
[2] Pei Wang, Weiling Zheng, Jiannan Wang, Jian Pei: Automating Entity Matching Model Development. ICDE 2021: 1296-1307
[3] V. Chvátal and D. Sankoff, "Longest common subsequences of two random sequences," Journal of Applied Probability, vol. 12, no. 2, pp. 306–315, 1975. doi:10.2307/3212444
[4] Vijaymeena M K , Kavitha K , .A Survey on Similarity Measures in Text Mining[J].Machine Learning & Applications An International Journal, 2016, 3(1):19-28.DOI:10.5121/mlaij.2016.3103.
[5] Matthew A. Jaro (1989) Advances in Record-Linkage Methodology as Applied to Matching the 1985 Census of Tampa, Florida, Journal of the American Statistical Association, 84:406, 414-420, DOI: 10.1080/01621459.1989.10478785
[6] Dan Tian, Mingchao Li, Yang Shen, Shuai Han: Intelligent mining of safety hazard information from construction documents using semantic similarity and information entropy. Eng. Appl. Artif. Intell. 119: 105742 (2023)
[7] https://github.com/anhaidgroup/deepmatcher/blob/master/Datasets.md
[8] Schulz, Klaus U. and Stoyan Mihov. "Fast string correction with Levenshtein automata." International Journal on Document Analysis and Recognition 5 (2002): 67-85.
[9] Topsoe, F.: Some inequalities for information divergence and related measures of discrimination. IEEE Trans. Inf. Theor. 46(4), 1602–1609 (2000)
[10] Snapper, Ernst . "Metric affine geometry. " Metric Affine Geometry 430.11(1971):1-111.
[11] Saul B. Needleman, Christian D. Wunsch, A general method applicable to the search for similarities in the amino acid sequence of two proteins, Journal of Molecular Biology,Volume 48, Issue 3,1970,Pages 443-453
[12] Shiwei Wei, Yuping Wang, Yiu-ming Cheung, A Branch Elimination-based Efficient Algorithm for Large-scale Multiple Longest Common Subsequence Problem, IEEE Transactions on Knowledge and Data Engineering, (1-1), (2021).
[13] Amores A, Force A, Yan YL, Joly L, Amemiya C, Fritz A, Ho R, Langeland J, Prince V, Wang YL, Westerfield M, Ekker M, Postlethwait JM. 1998. Zebrafish hox clusters and vertebrate genome evolution. Science 282: 1711–1714.
[14] Ballantine, J. P., Jerbert, A. R. (1952). Distance from a Line, or Plane, to a Poin. The American Mathematical Monthly, 59(4), 242–243. https://doi.org/10.2307/2306514
[15] LEVANDOWSKY, M., WINTER, D. Distance between Sets. Nature 234, 34–35 (1971). https://doi.org/10.1038/234034a0
[16] Reuben R Shamir, Yuval Duchin, Jinyoung Kim, Guillermo Sapiro, Noam Harel bioRxiv 306977; doi: https://doi.org/10.1101/306977
[17] Vijaymeena, M. K.; Kavitha, K. (March 2016). "A Survey on Similarity Measures in Text Mining" (PDF). Machine Learning and Applications. 3 (1): 19–28. doi:10.5121/mlaij.2016.3103.
[18] William W. Cohen, Pradeep Ravikumar, and Stephen E. Fienberg. 2003. A comparison of string distance metrics for name-matching tasks. In Proceedings of the 2003 International Conference on Information Integration on the Web (IIWEB'03). AAAI Press, 73–78.
[19] https://www.hanlp.com/semantics/dashboard/index

[20] Fagin, R.; Kumar, R.; Sivakumar, D. (2003). Comparing top k lists. SIAM Journal on Discrete Mathematics. 17 (1): 134–160

[21] R. W. Hamming, "Error detecting and error correcting codes," in The Bell System Technical Journal, vol. 29, no. 2, pp. 147-160, April 1950, doi: 10.1002/j.1538-7305.1950.tb00463.x.

[22] Moses S. Charikar. 2002. Similarity estimation techniques from rounding algorithms. In Proceedings of the thiry-fourth annual ACM symposium on Theory of computing (STOC '02). Association for Computing Machinery, New York, NY, USA, 380–388. https://doi.org/10.1145/509907.509965