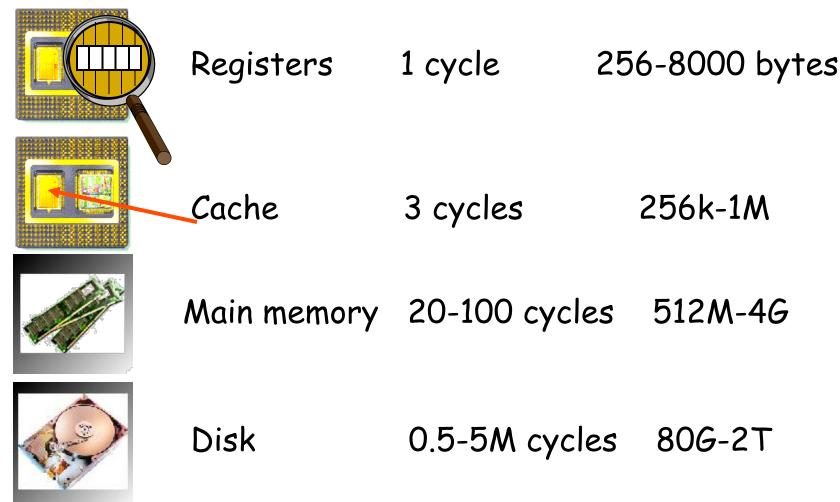
## Register Allocation

Lecture 16

#### Lecture Outline

- Memory Hierarchy Management
- Register Allocation
  - Register interference graph
  - Graph coloring heuristics
  - Spilling
- Cache Management

## The Memory Hierarchy



#### Managing the Memory Hierarchy

- Most programs are written as if there are only two kinds of memory: main memory and disk
  - Programmer is responsible for moving data from disk to memory (e.g., file I/O)
  - Hardware is responsible for moving data between memory and caches
  - Compiler is responsible for moving data between memory and registers

#### Current Trends

- · Power usage limits
  - Size and speed of registers/caches
  - Speed of processors
- But
  - The cost of a cache miss is very high
  - Typically requires 2-3 caches to bridge fast processor with large main memory
- It is very important to:
  - Manage registers properly
  - Manage caches properly
- Compilers are good at managing registers

#### The Register Allocation Problem

- Intermediate code uses unlimited temporaries
  - Simplifies code generation and optimization
  - Complicates final translation to assembly
- Typical intermediate code uses too many temporaries

#### The Register Allocation Problem (Cont.)

#### The problem:

Rewrite the intermediate code to use no more temporaries than there are machine registers

#### Method:

- Assign multiple temporaries to each register
- But without changing the program behavior

#### History

- Register allocation is as old as compilers
  - Register allocation was used in the original FORTRAN compiler in the '50s
  - Very crude algorithms
- A breakthrough came in 1980
  - Register allocation scheme based on graph coloring
  - Relatively simple, global and works well in practice

## An Example

Consider the program

$$a := c + d$$
  
 $e := a + b$   
 $f := e - 1$ 

 Can allocate a, e, and f all to one register (r<sub>1</sub>):

$$r_1 := r_2 + r_3$$
  
 $r_1 := r_1 + r_4$   
 $r_1 := r_1 - 1$ 

- Assume a and e dead after use
  - Temporary a can be "reused" after e := a + b
  - So can temporary e

- A dead temporary is not needed
  - A dead temporary can be reused

#### The Idea

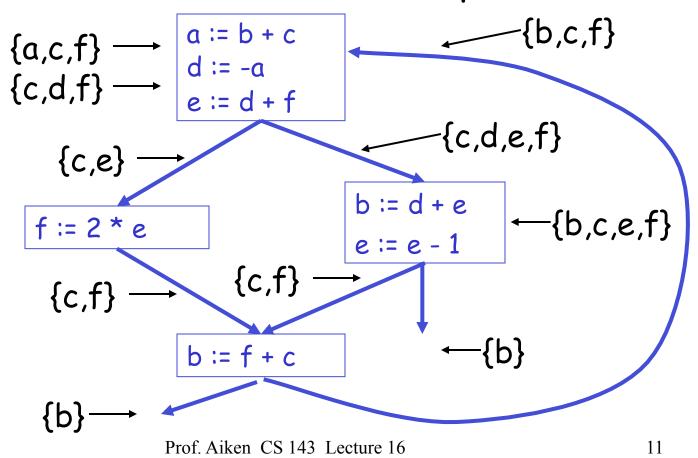
Temporaries  $t_1$  and  $t_2$  can share the same register if at any point in the program at most one of  $t_1$  or  $t_2$  is live.

Or

If  $t_1$  and  $t_2$  are live at the same time, they cannot share a register

#### Algorithm: Part I

· Compute live variables for each point:

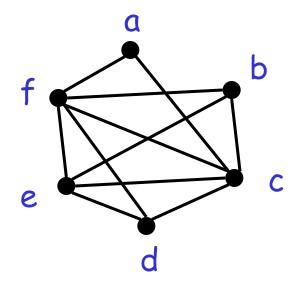


## The Register Interference Graph

- Construct an undirected graph
  - A node for each temporary
  - An edge between  $t_1$  and  $t_2$  if they are live simultaneously at some point in the program
- This is the register interference graph (RIG)
  - Two temporaries can be allocated to the same register if there is no edge connecting them

#### Example

For our example:



- E.g., b and c cannot be in the same register
- E.g., b and d could be in the same register

## Notes on Register Interference Graphs

- Extracts exactly the information needed to characterize legal register assignments
- Gives a global (i.e., over the entire flow graph)
  picture of the register requirements
- After RIG construction the register allocation algorithm is architecture independent

#### Definitions

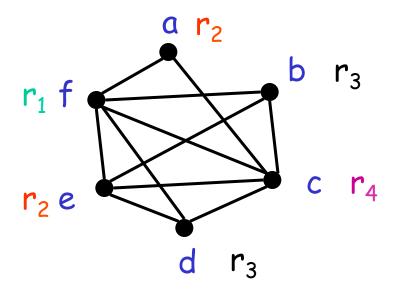
- A coloring of a graph is an assignment of colors to nodes, such that nodes connected by an edge have different colors
- A graph is k-colorable if it has a coloring with k colors

## Register Allocation Through Graph Coloring

- In our problem, colors = registers
  - We need to assign colors (registers) to graph nodes (temporaries)
- Let k = number of machine registers
- If the RIG is k-colorable then there is a register assignment that uses no more than k registers

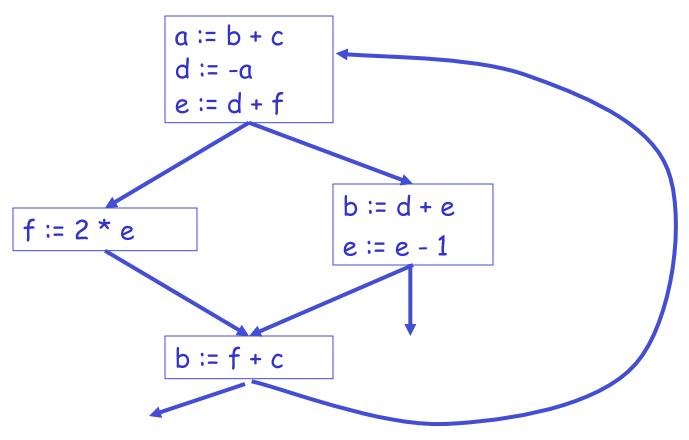
## Graph Coloring Example

Consider the example RIG



- There is no coloring with less than 4 colors
- There are 4-colorings of this graph

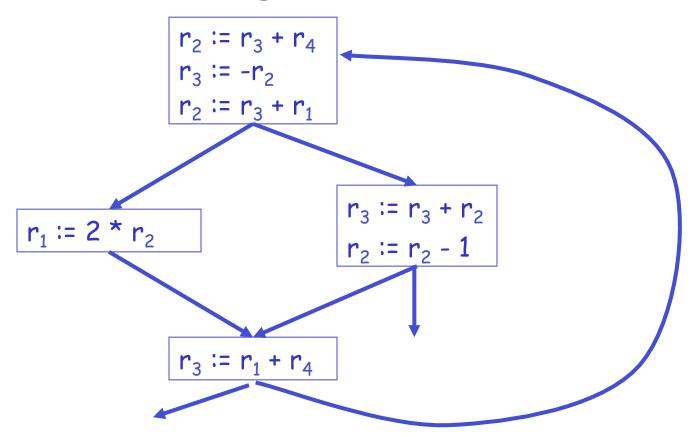
# Example Review



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#### Example After Register Allocation

Under this coloring the code becomes:



#### Computing Graph Colorings

- How do we compute graph colorings?
- It isn't easy:
  - 1. This problem is very hard (NP-hard). No efficient algorithms are known.
    - Solution: use heuristics
  - 2. A coloring might not exist for a given number of registers
    - Solution: later

## Graph Coloring Heuristic

#### Observation:

- Pick a node t with fewer than k neighbors in RIG
- Eliminate t and its edges from RIG
- If resulting graph is k-colorable, then so is the original graph

#### · Why?

- Let  $c_1,...,c_n$  be the colors assigned to the neighbors of t in the reduced graph
- Since n < k we can pick some color for t that is different from those of its neighbors

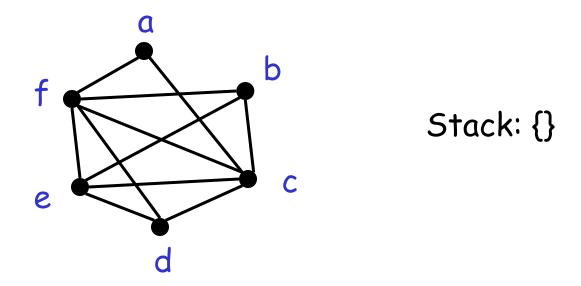
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## Graph Coloring Heuristic

- The following works well in practice:
  - Pick a node t with fewer than k neighbors
  - Put t on a stack and remove it from the RIG
  - Repeat until the graph has one node
- Assign colors to nodes on the stack
  - Start with the last node added
  - At each step pick a color different from those assigned to already colored neighbors

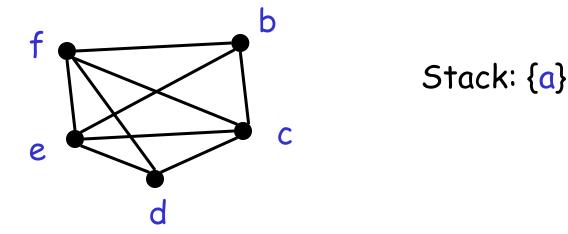
## Graph Coloring Example (1)

Start with the RIG and with k = 4:



Remove a

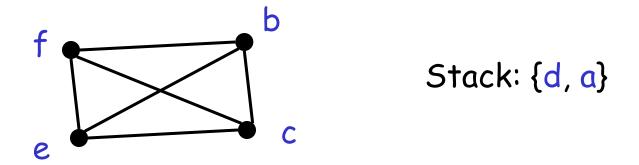
## Graph Coloring Example (2)



Remove d

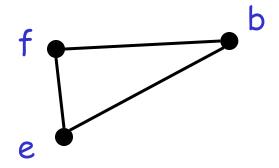
## Graph Coloring Example (3)

Note: all nodes now have fewer than 4 neighbors



Remove c

# Graph Coloring Example (4)



Stack: {c, d, a}

Remove b

## Graph Coloring Example (5)



Stack: {b, c, d, a}

· Remove e

# Graph Coloring Example (6)

f

Stack: {e, b, c, d, a}

Remove f

## Graph Coloring Example (7)

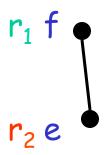
 Now start assigning colors to nodes, starting with the top of the stack

Stack: {f, e, b, c, d, a}

## Graph Coloring Example (8)

$$r_1 f \bullet$$

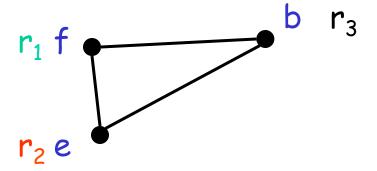
# Graph Coloring Example (9)



Stack: {b, c, d, a}

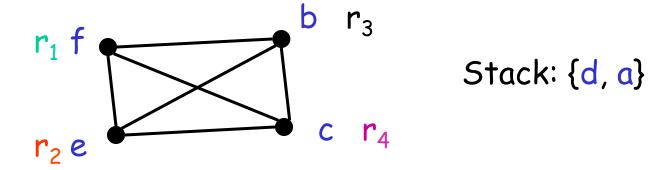
e must be in a different register from f

## Graph Coloring Example (10)

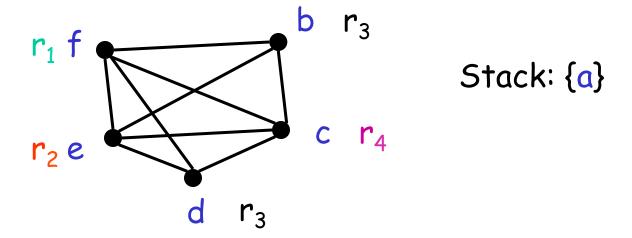


Stack: {c, d, a}

## Graph Coloring Example (11)

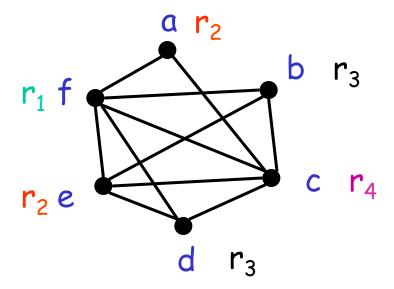


## Graph Coloring Example (12)



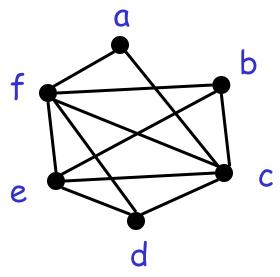
d can be in the same register as b

## Graph Coloring Example (13)



#### What if the Heuristic Fails?

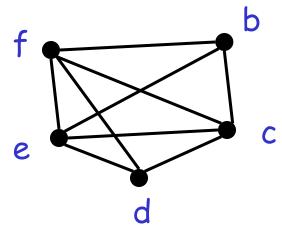
- What if all nodes have k or more neighbors?
- Example: Try to find a 3-coloring of the RIG:



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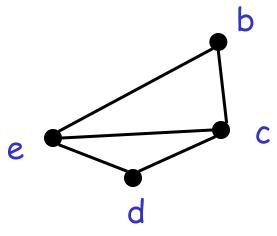
### What if the Heuristic Fails?

- Remove a and get stuck (as shown below)
- · Pick a node as a candidate for spilling
  - A spilled temporary "lives" in memory
  - Assume that f is picked as a candidate



### What if the Heuristic Fails?

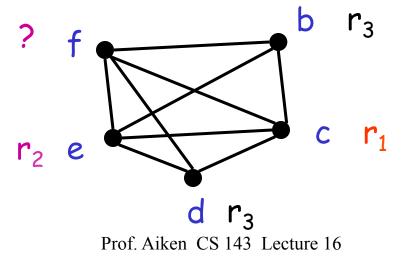
- Remove f and continue the simplification
  - Simplification now succeeds: b, d, e, c



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### What if the Heuristic Fails?

- · Eventually we must assign a color to f
- We hope that among the 4 neighbors of f we use less than 3 colors  $\Rightarrow$  optimistic coloring



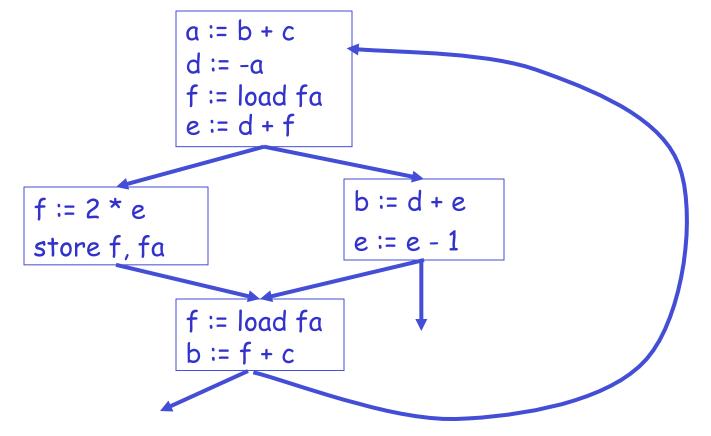
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# Spilling

- If optimistic coloring fails, we spill f
  - Allocate a memory location for f
    - Typically in the current stack frame
    - Call this address fa
- Before each operation that reads f, insert
   f := load fa
- After each operation that writes f, insert store f, fa

# Spilling Example

This is the new code after spilling f

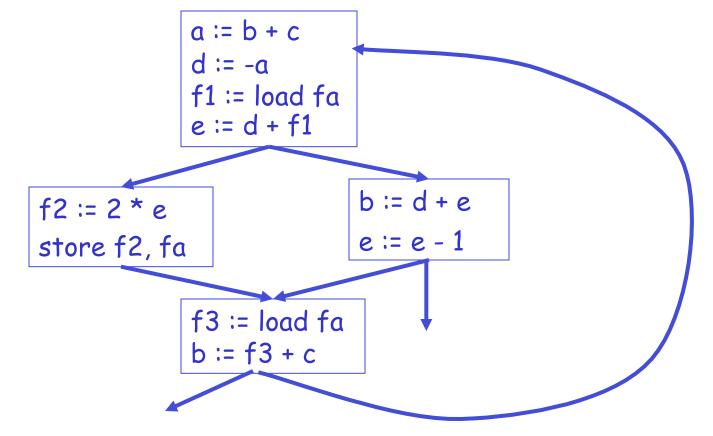


#### A Problem

- This code reuses the register name f
- · Correct, but suboptimal
  - Should use distinct register names whenever possible
  - Allows different uses to have different colors

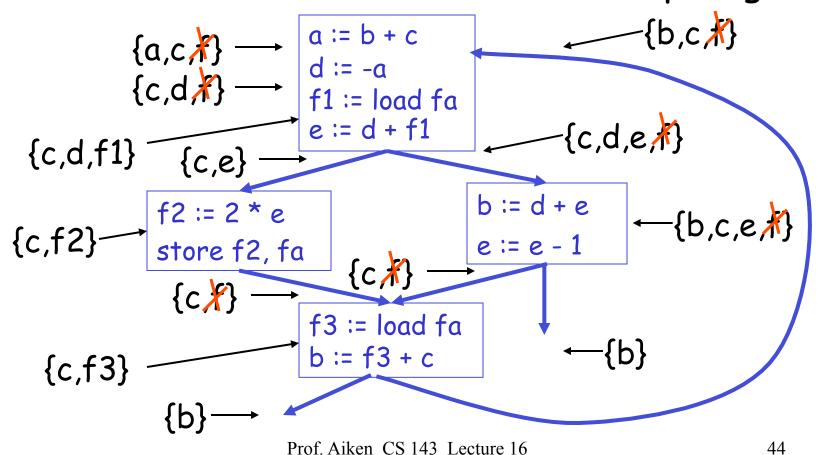
# Spilling Example

This is the new code after spilling f



## Recomputing Liveness Information

The new liveness information after spilling:

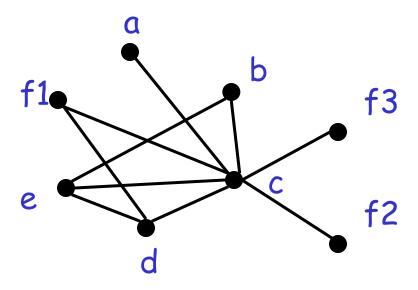


### Recomputing Liveness Information

- New liveness information is almost as before
  - Note f has been split into three temporaries
- fi is live only
  - Between a fi := load fa and the next instruction
  - Between a store fi, fa and the preceding instr.
- Spilling reduces the live range of f
  - And thus reduces its interferences
  - Which results in fewer RIG neighbors

## Recompute RIG After Spilling

- Some edges of the spilled node are removed
- In our case f still interferes only with c and d
- And the resulting RIG is 3-colorable



# Spilling Notes

- Additional spills might be required before a coloring is found
- The tricky part is deciding what to spill
  - But any choice is correct
- Possible heuristics:
  - Spill temporaries with most conflicts
  - Spill temporaries with few definitions and uses
  - Avoid spilling in inner loops

#### Caches

- · Compilers are very good at managing registers
  - Much better than a programmer could be
- Compilers are not good at managing caches
  - This problem is still left to programmers
  - It is still an open question how much a compiler can do to improve cache performance
- Compilers can, and a few do, perform some cache optimizations

## Cache Optimization

· Consider the loop

```
for(j := 1; j < 10; j++)
for(i=1; i<1000; i++)
a[i] *= b[i]
```

- This program has terrible cache performance
  - · Why?

## Cache Optimization (Cont.)

Consider the program:

```
for(i=1; i<1000; i++)
for(j := 1; j < 10; j++)
a[i] *= b[i]
```

- Computes the same thing
- But with much better cache behavior
- Might actually be more than 10x faster
- · A compiler can perform this optimization
  - called loop interchange

#### Conclusions

- Register allocation is a "must have" in compilers:
  - Because intermediate code uses too many temporaries
  - Because it makes a big difference in performance
- Register allocation is more complicated for CISC machines