

0. MOTIVATION
1. PROBLEM SOLVING
2. INFORMATION
3. COUNTING
4. BITS
5. CODES
6. ALGORITHMS
7. COMPUTERS
8. ARITHMETIC
9. MEMORY
10. ANALOG VS. DIGITAL

The slides are meant as visual support for the lecture.  
They are not a documentation nor a script.

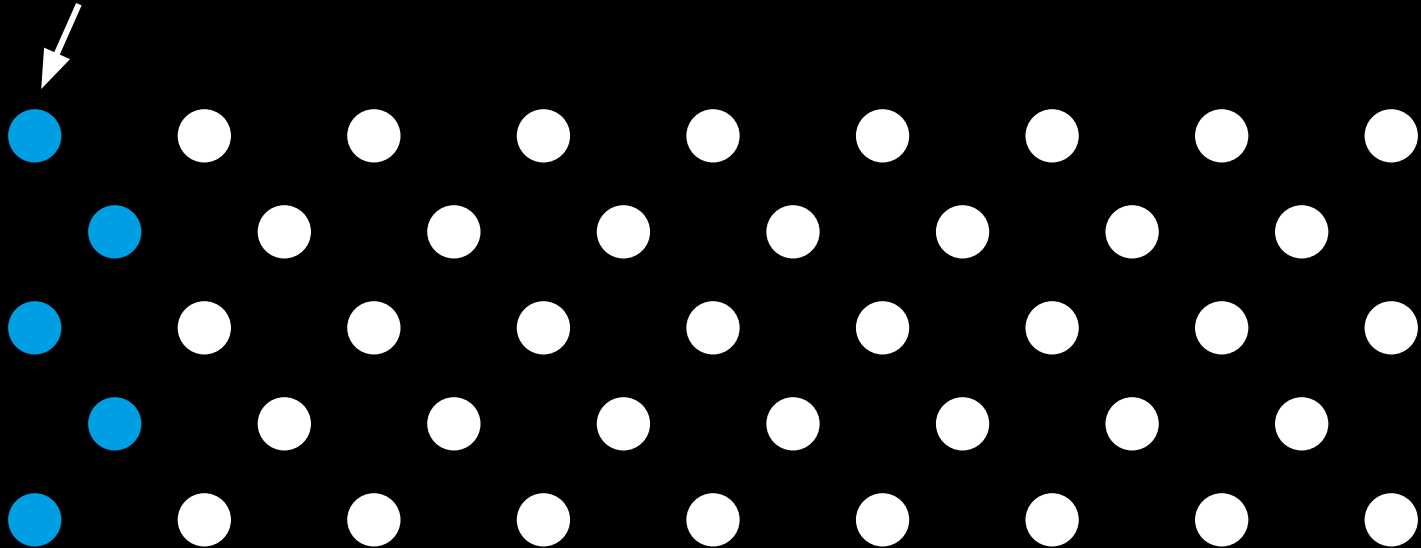
Please do not print the slides.

Comments and feedback at [n.meseth@hs-osnabrueck.de](mailto:n.meseth@hs-osnabrueck.de)

# MOTIVATION

a few  
experts

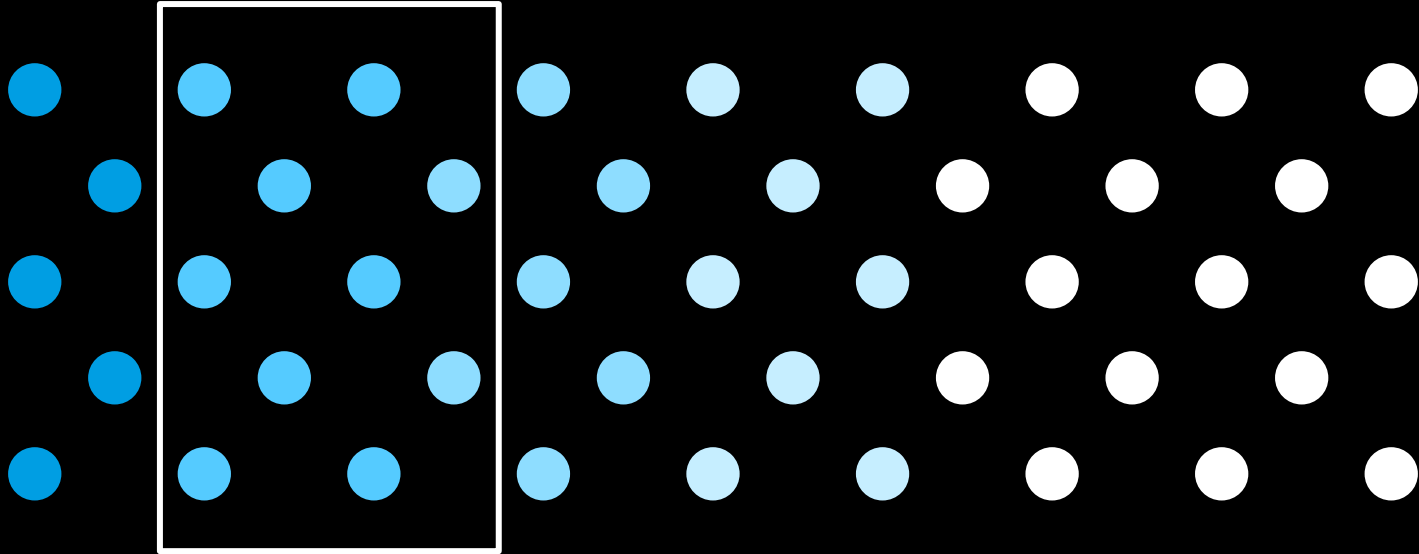
digitally uneducated  
society



digitally illiterate society with a few experts

# collective understanding

You?



society with a distributed and high degree of digital education

artificial  
Intelligence

data analysis

representation

processing

programming

artificial  
intelligence

data analysis

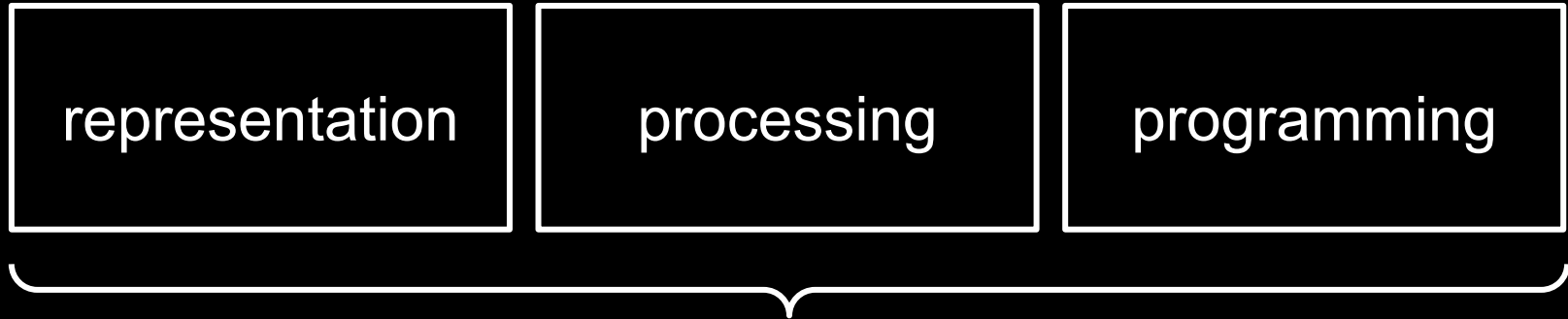
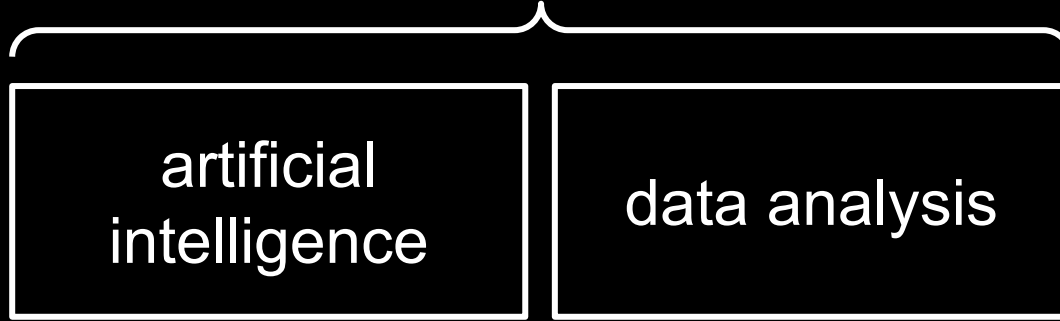
representation

processing

programming

digital fundamentals

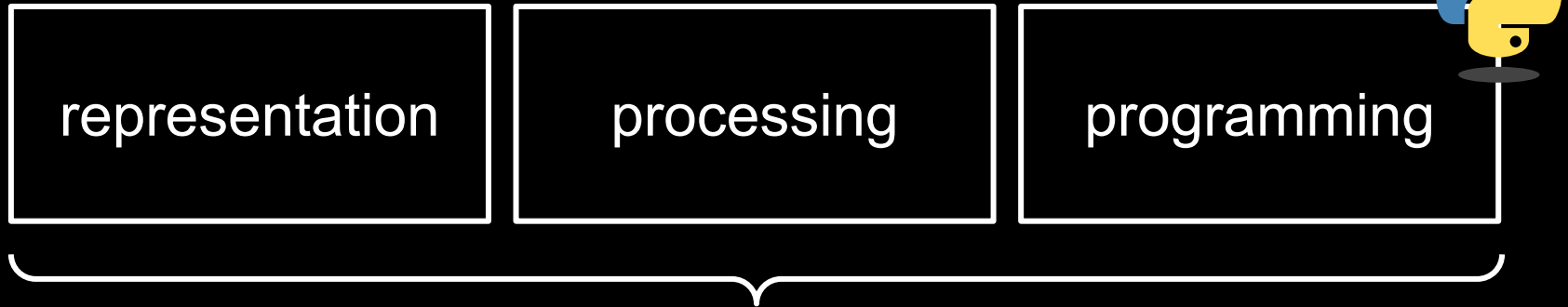
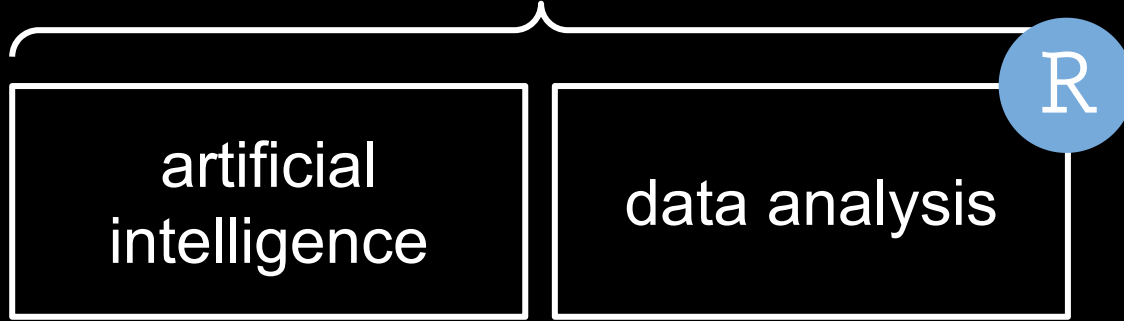
digital applications



digital fundamentals



digital applications



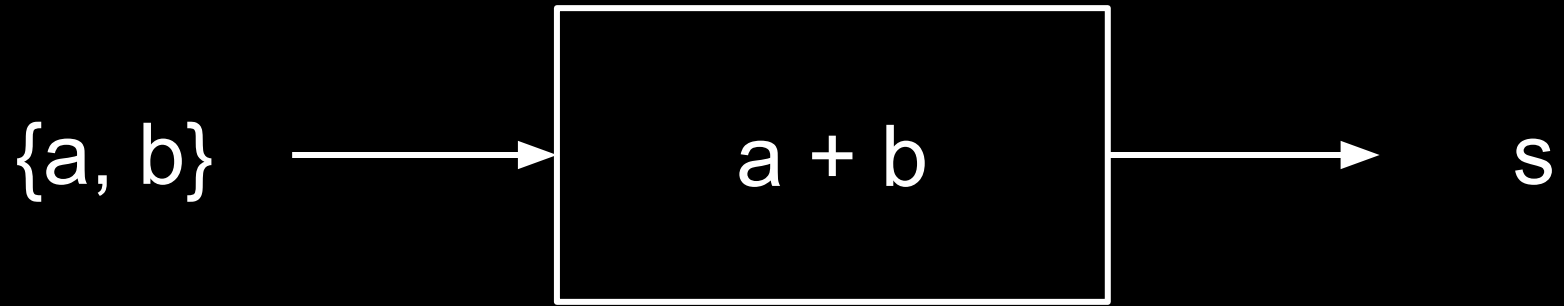
digital fundamentals

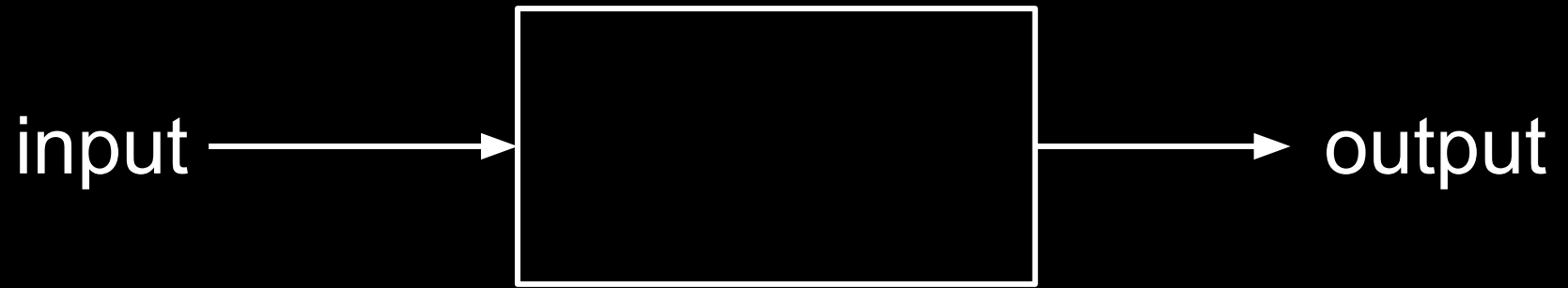
# PROBLEM SOLVING

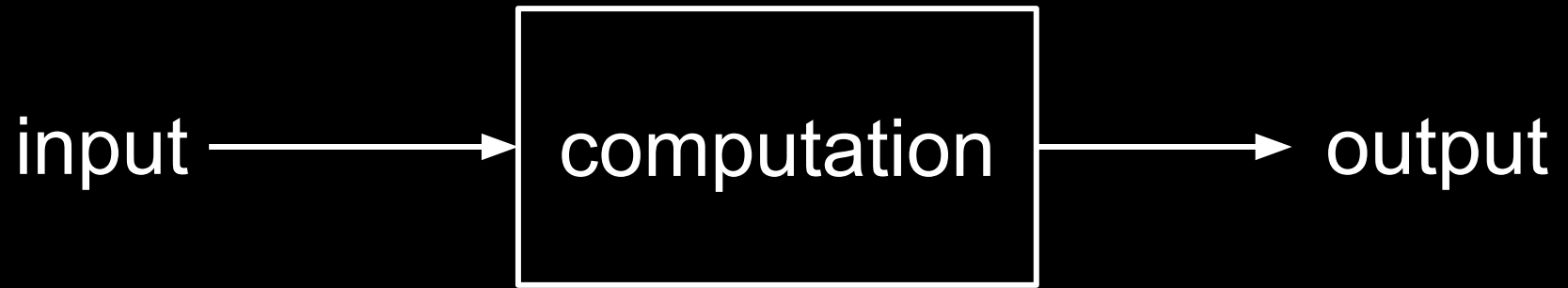
# a model for solving problems



# a model for solving problems







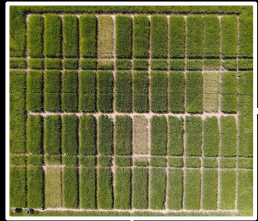




42



processing of  
information

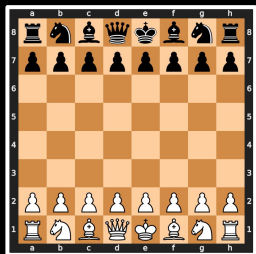


`count_plants()`

42

representation of  
information





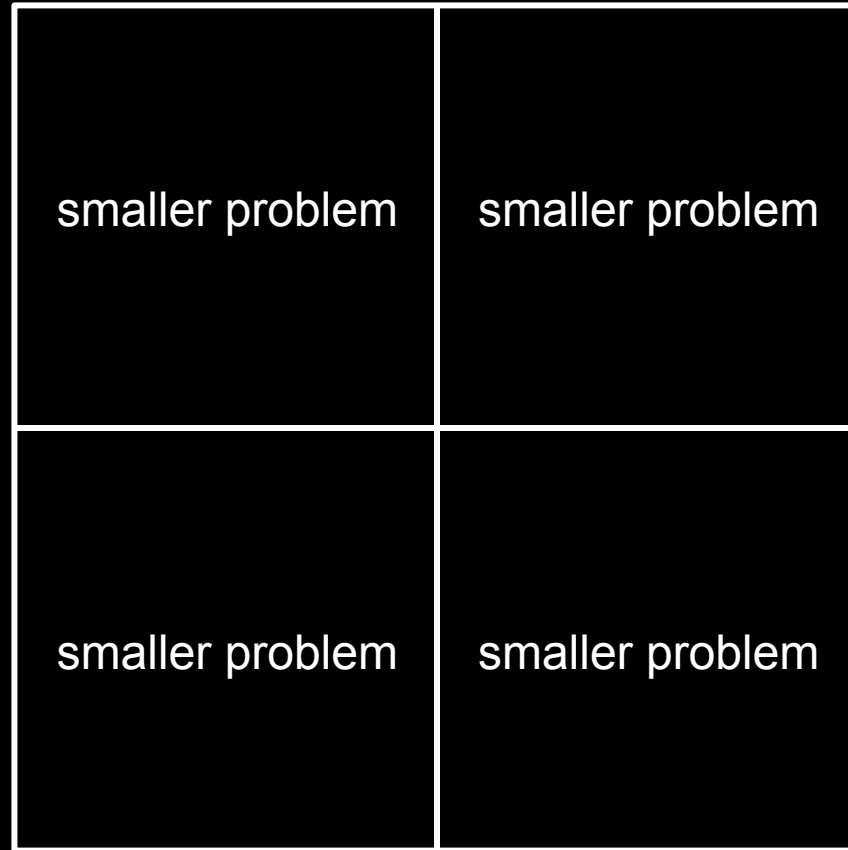
next\_move()

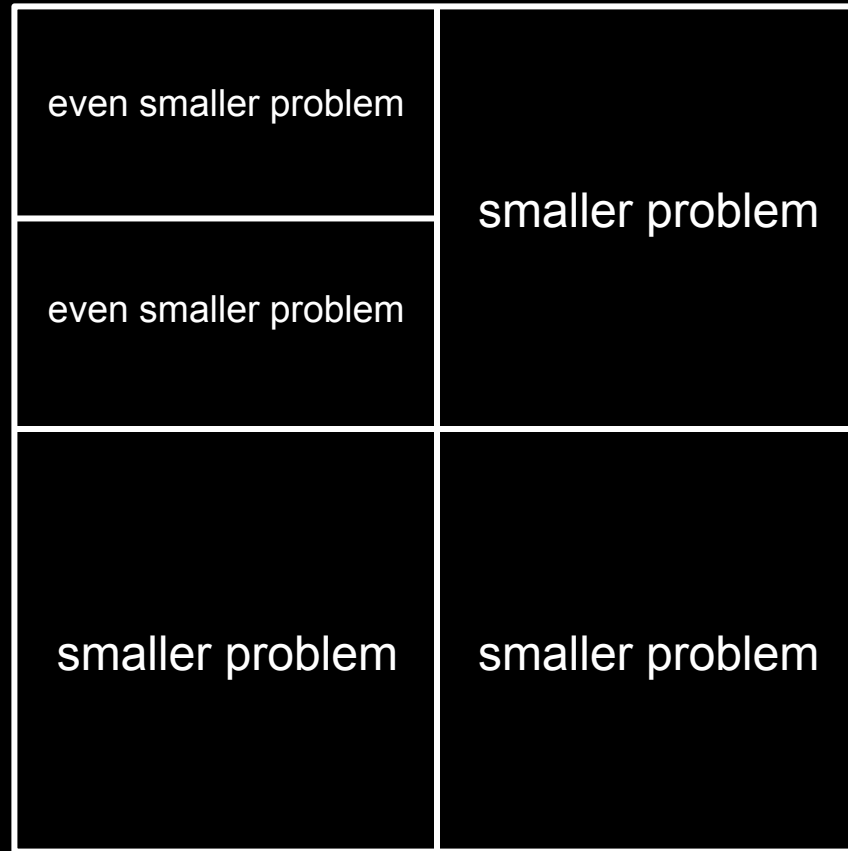
E2 → E4

problem solving strategies

divide and conquer

large and complex problem







sorted list +  
element



search()



yes / no

is 67 a prime number?

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

## linear search



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

## linear search



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

## linear search



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

## linear search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
~~43~~, 47, ~~53~~, 59, ~~61~~, 67, 71, 73, 79, 83, 89, 97  
↑

19 steps... can't we do better?

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97  
↑

binary search

67 != 41



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, ~~41~~,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97



binary search

67 > 41



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, ~~41~~,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

binary search

67 > 41



2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

## binary search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97



67 != 71

## binary search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97



67 != 71

## binary search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97



$67 < 71$

## binary search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97



67 != 59

## binary search

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,  
~~43~~, 47, ~~53~~, 59, 61, 67, ~~71~~, ~~73~~, 79, ~~83~~, ~~89~~, 97



67 > 59

## binary search

2, 3, 5, 7, 11, ~~13~~, 17, 19, ~~23~~, ~~29~~, 31, 37, 41,  
~~43~~, 47, ~~53~~, ~~59~~, 61, 67, ~~71~~, ~~73~~, ~~79~~, ~~83~~, ~~89~~, 97



67 = 67



## binary search

2, 3, 5, 7, 11, ~~13~~, 17, 19, ~~23~~, ~~29~~, 31, 37, 41,  
~~43~~, 47, ~~53~~, 59, ~~61~~, 67, ~~71~~, ~~73~~, 79, ~~83~~, ~~89~~, 97



67 = 67

3 splits → much better

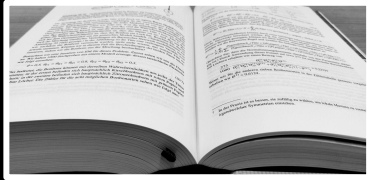
2, 3, 5, 7, 11, ~~13~~, 17, 19, ~~23~~, 29, 31, 37, 41,  
~~43~~, 47, ~~53~~, 59, ~~61~~, 67, ~~71~~, ~~73~~, 79, ~~83~~, ~~89~~, 97



67 = 67



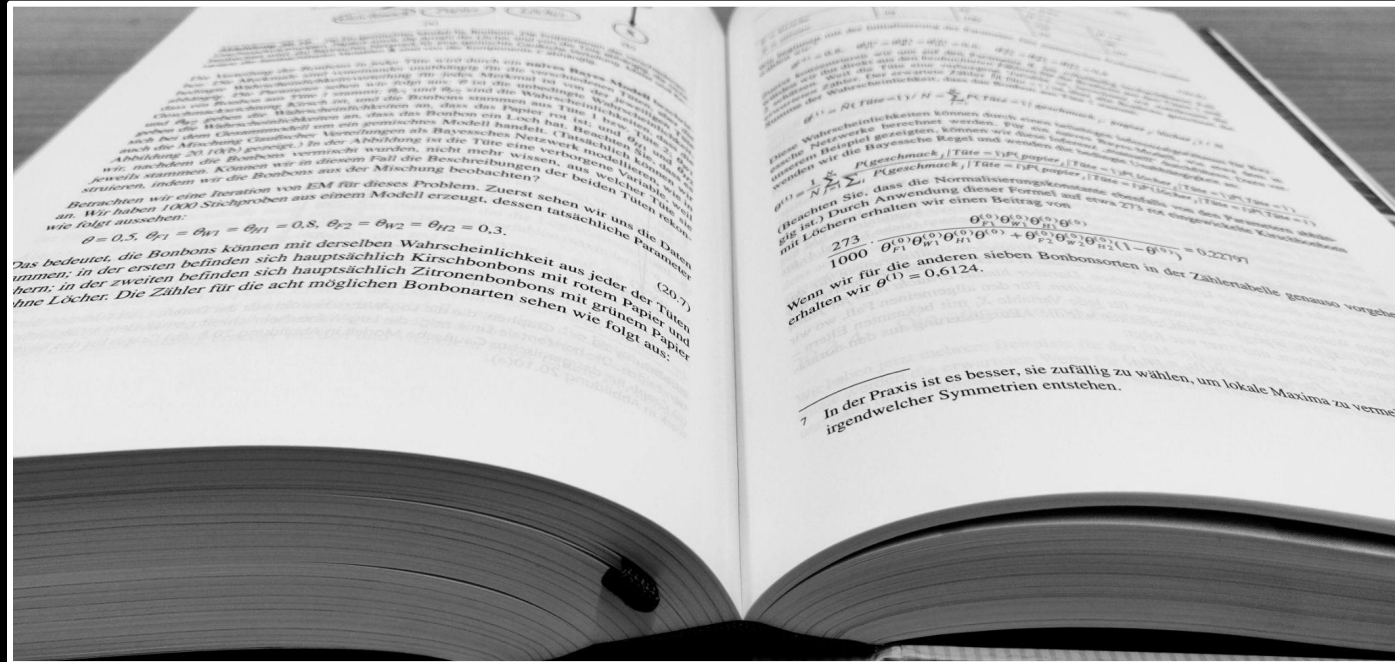
how efficient are linear and  
binary search in general?



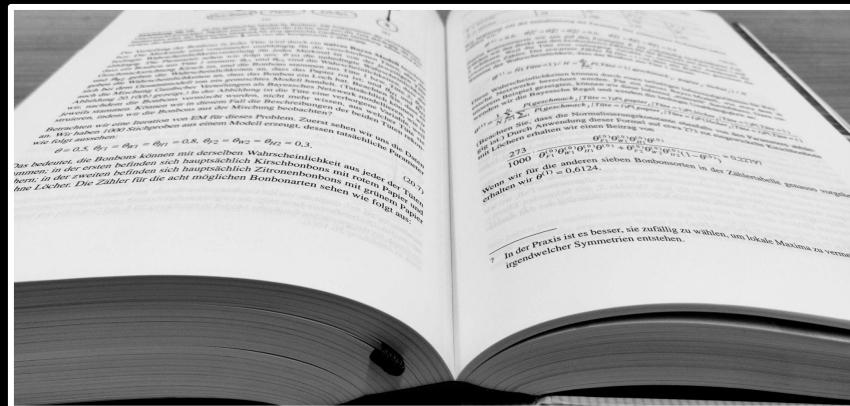
`count_words()`

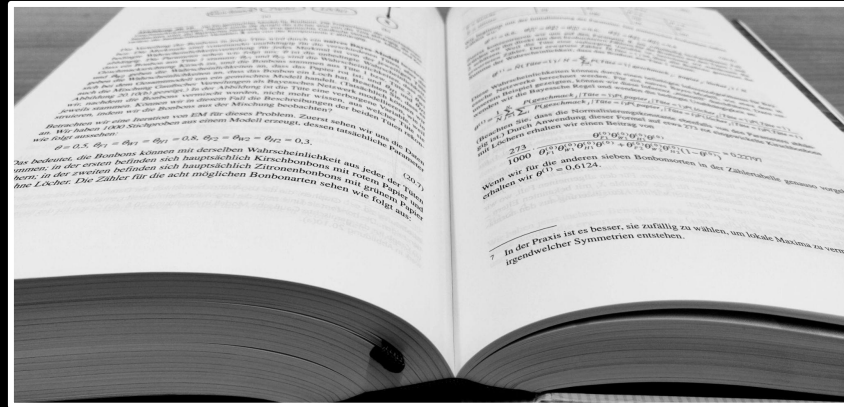
word count

# how many words are in the book?



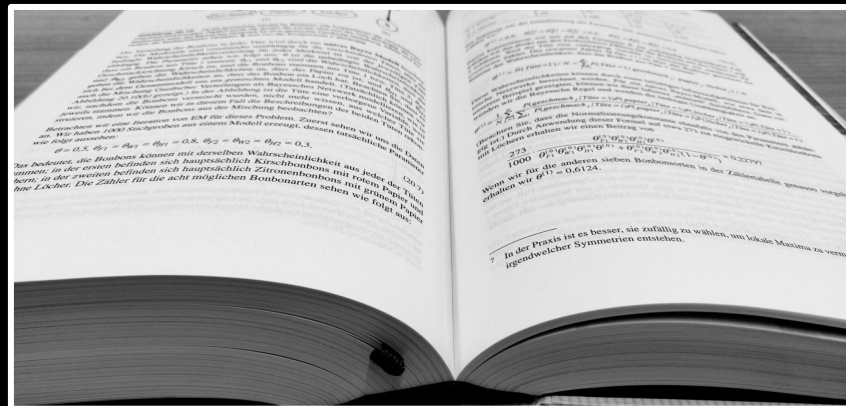
strategies, anyone?





page 1

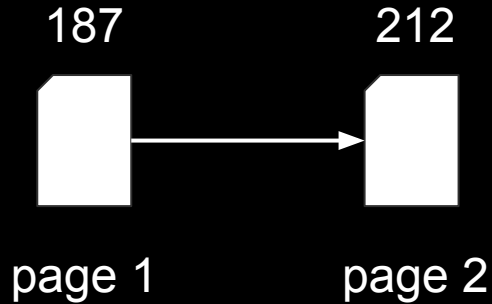
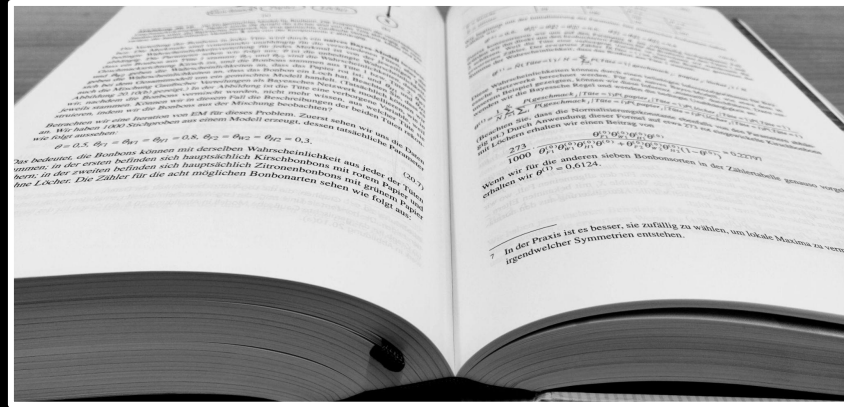


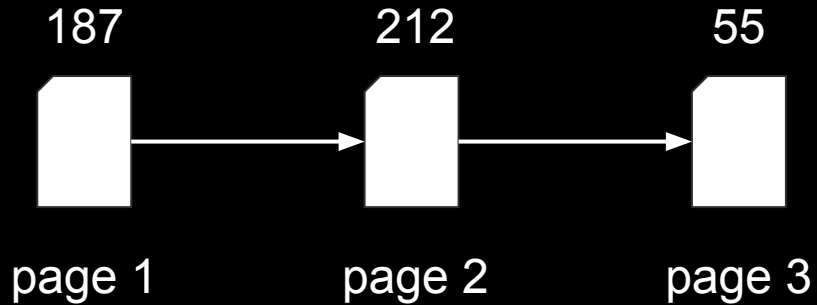
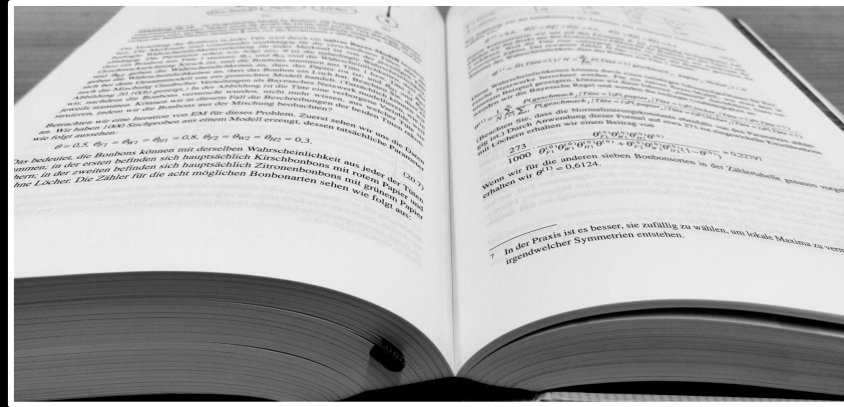


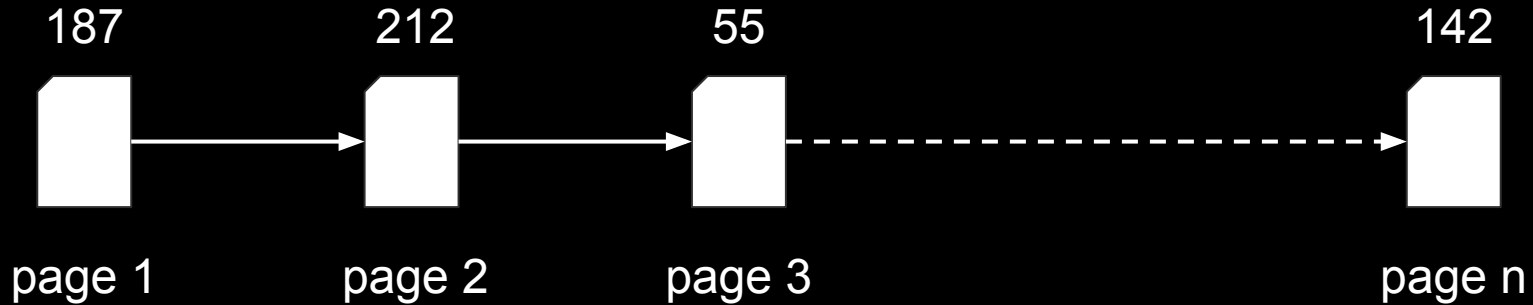
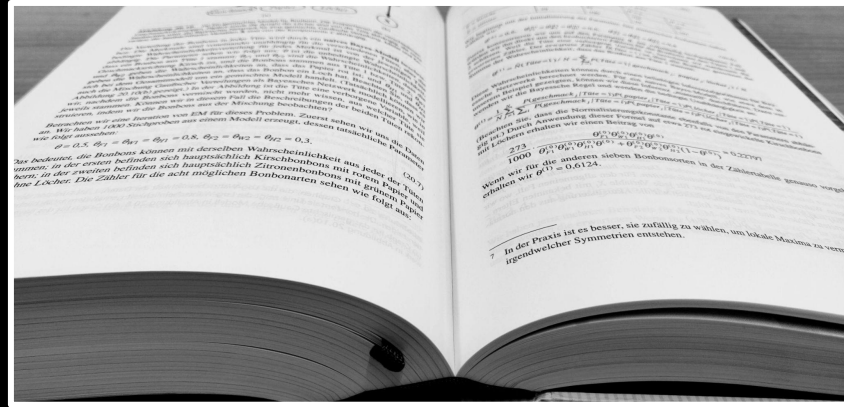
187

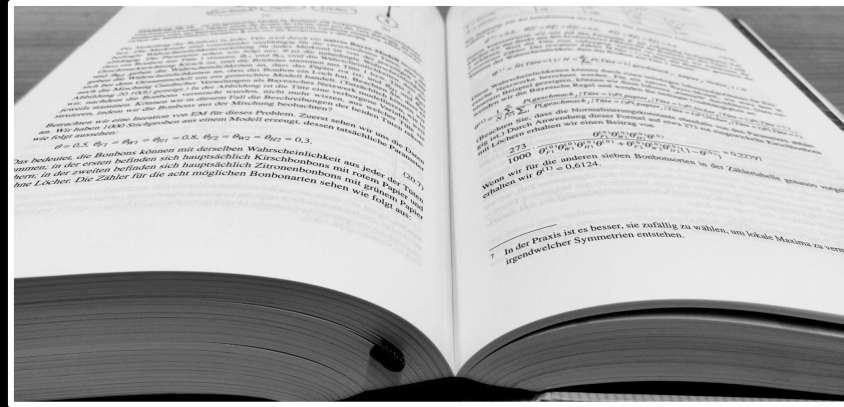


page 1









$n = 1327$  pages

$\varnothing$  2:23 minutes per page

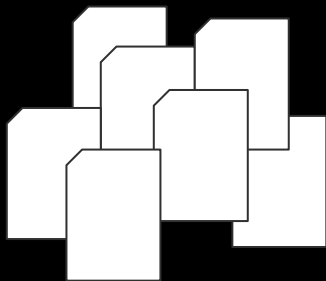
$\sim 52.34$  hours

divide and conquer

+

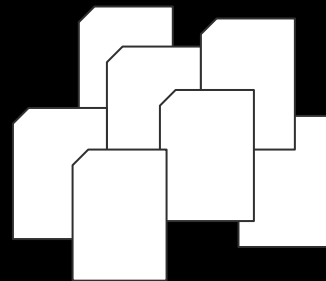
?

pages 1 - 700



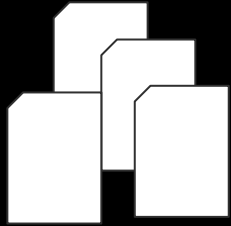
student 1

pages 701 - 1327



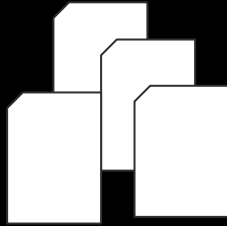
student 2

pages 1 - 350



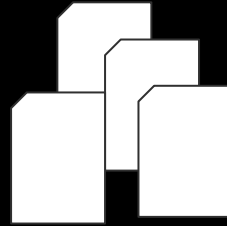
student 1

pages 351 - 700



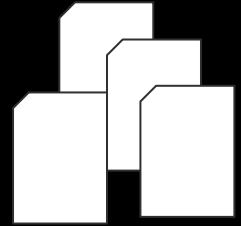
student 2

pages 701 - 1050



student 3

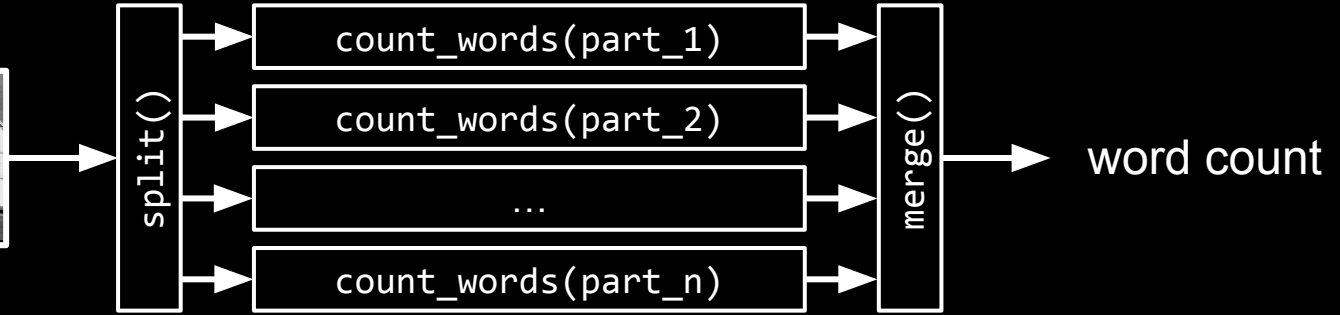
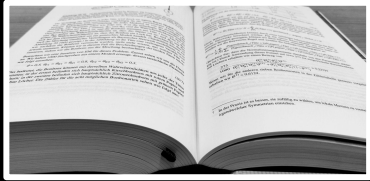
pages 1051- 1327



student 4



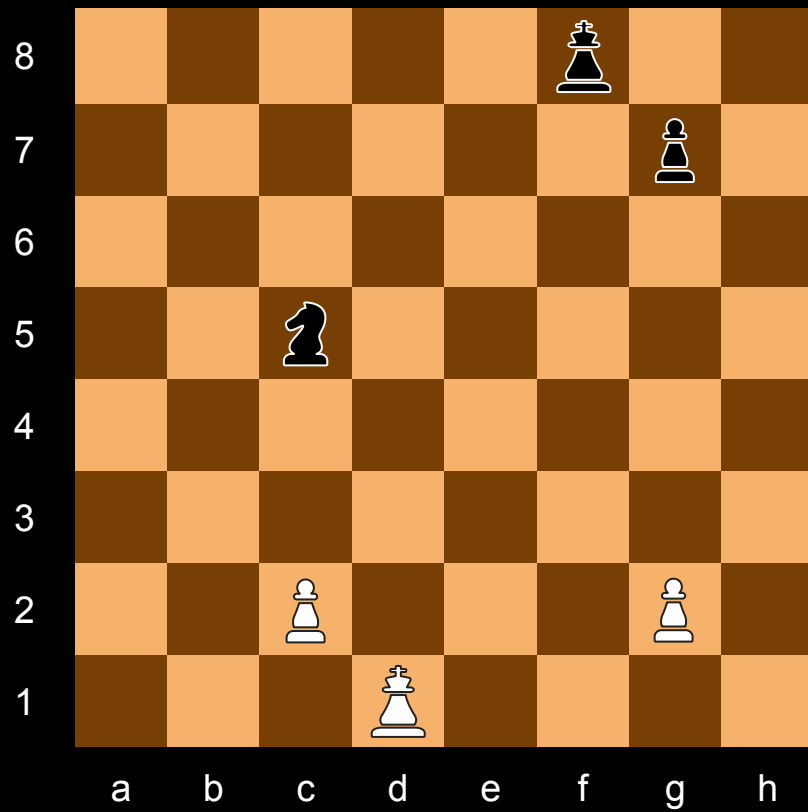
divide and conquer  
+  
distribution and parallelization

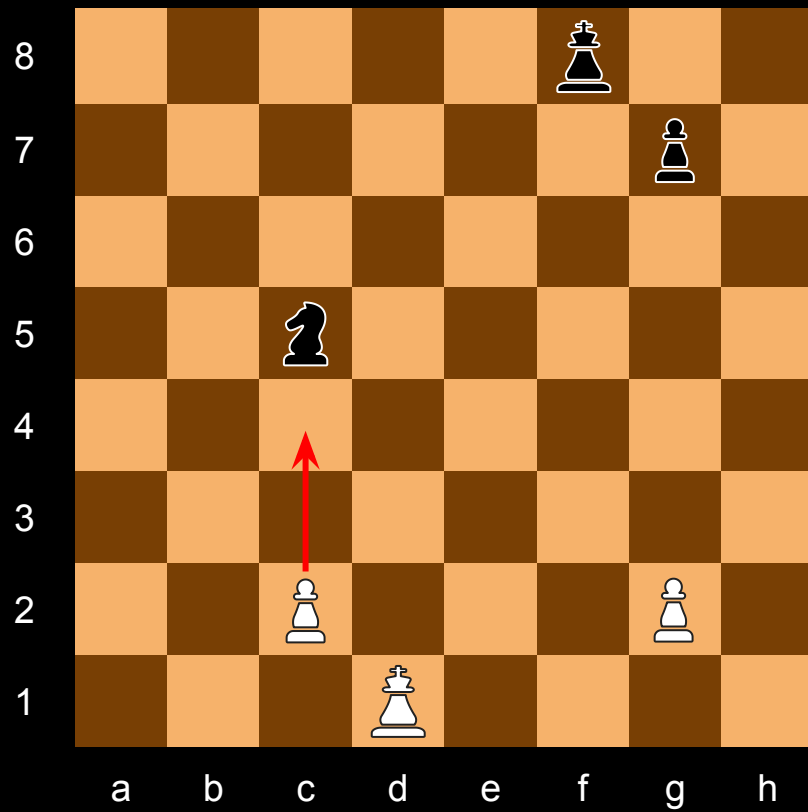


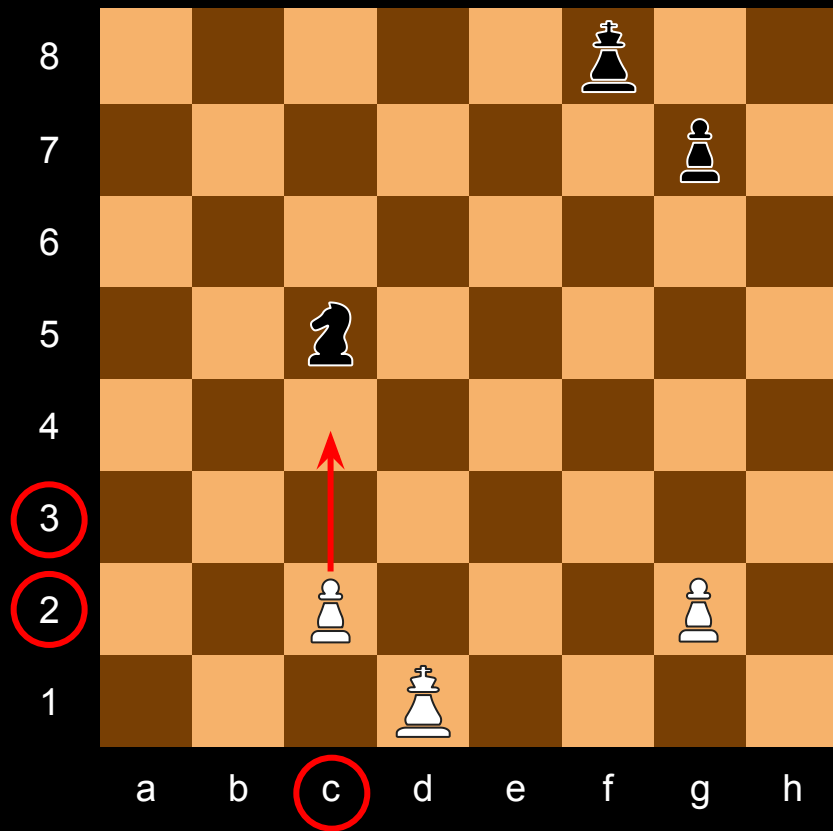
# INFORMATION



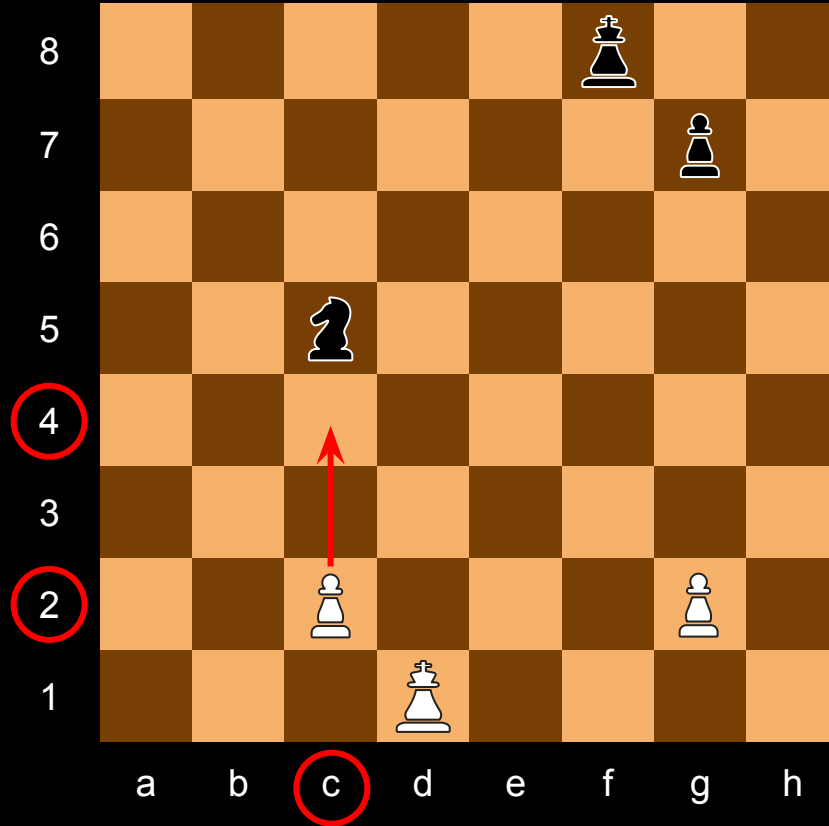
Image created with DALLE-3





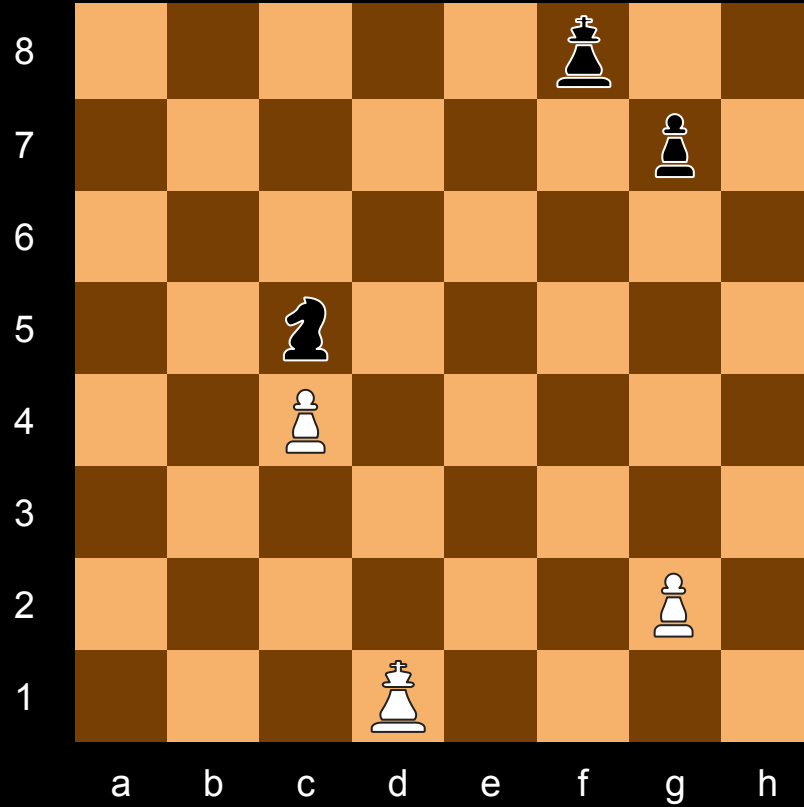


c2 → c4

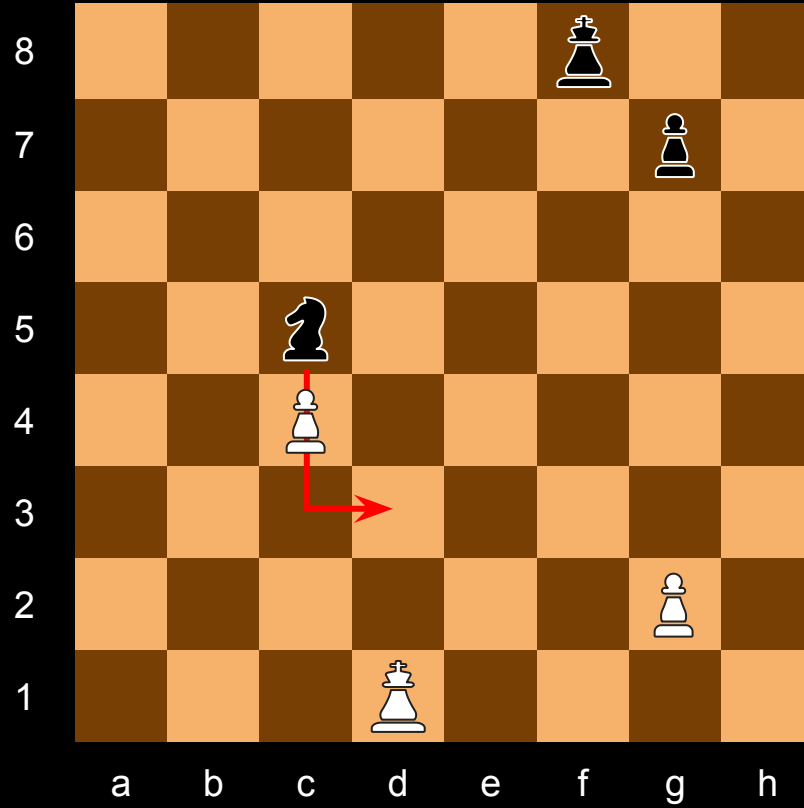




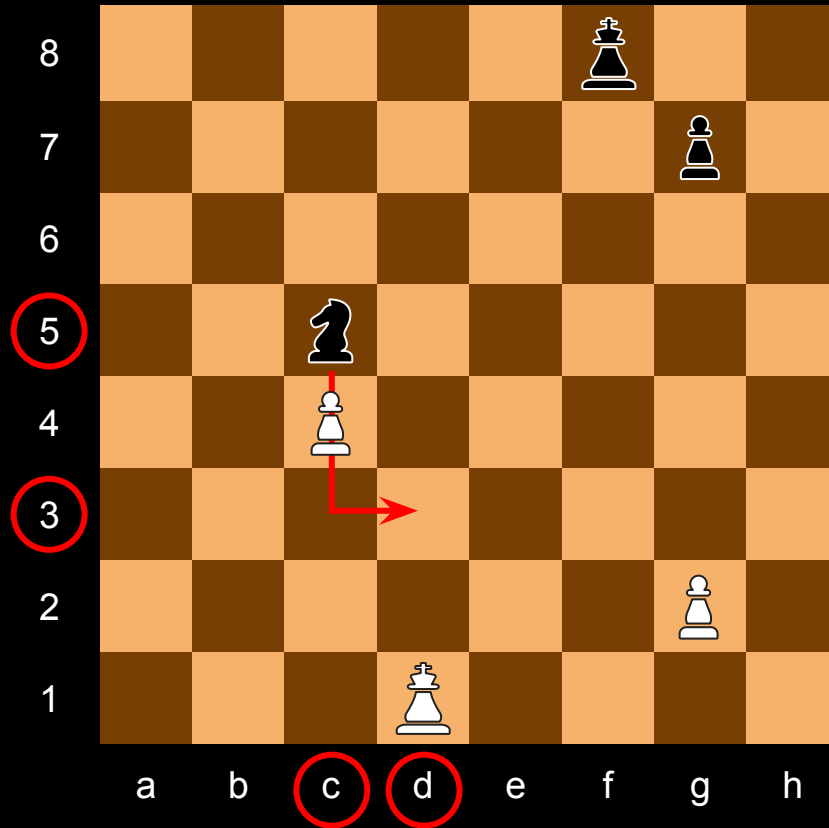
c2 → c4



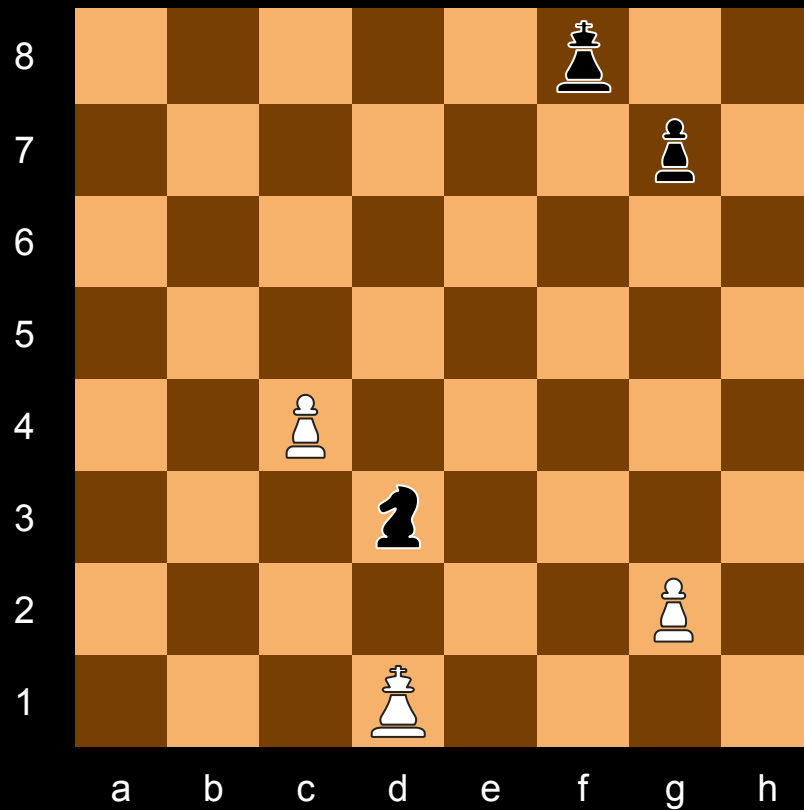
c2 → c4



c2 → c4  
c5 → d3



c2 → c4  
c5 → d3  
...



$\{A\}$

— —

$\{A\}$

A A

$\{A, B\}$

— —

$\{A, B\}$

A A



$\{A, B\}$

A B

$\{A, B\}$

B A

$\{A, B\}$

B B

$\{A, B\}$

AA, AB, BA, BB

$\{A, B, C\}$

— —

$\{A, B, C\}$

AA, AB, BA, BB,  
AC, BC, CA, CB, CC

{A, B, C, D}

— —

$\{A, B, C, D\}$

AA, AB, BA, BB, AC, BC, CA, CB,  
CC, AD, DA, BD, DB, CD, DC, DD



{A, B, C, D, E}

— —

$\{A, B, C, D, E\}$

AA, AB, BA, BB, AC, BC, CA, CB, CC,  
AD, DA, BD, DB, CD, DC, DD, AE, EA,  
BE, EB, CE, EC, DE, ED, EE

with length  $n = 2$

# symbols

# messages

1

1

2

4

3

9

4

16

5

25

with length  $n = 2$

# symbols

# messages

1

1

2

4

3

9

4

16

5

25

$f(x)$



$\{A, B\}$

— — —

# COUNTING

1

2

3

1

2

3

---

$10^2$

$10^1$

$10^0$



1 2 3

---

$10^2$

$10^1$

$10^0$

$$= 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$

$$= 1 \times 100 + 2 \times 10 + 3 \times 1$$

$$= 123$$

4

1

2

3

---

?

$10^2$

$10^1$

$10^0$

4 1 2 3

---

?

$10^2$

$10^1$

$10^0$

$$= 4 \times 10^3 + 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$

4 1 2 3

---

?

$10^2$

$10^1$

$10^0$

$$= 4 \times 10^3 + 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$

$$= 4 \times 1000 + 1 \times 100 + 2 \times 10 + 3 \times 1$$

4 1 2 3

---

?

$10^2$

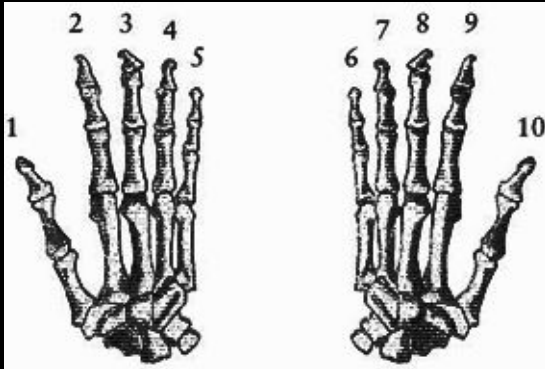
$10^1$

$10^0$

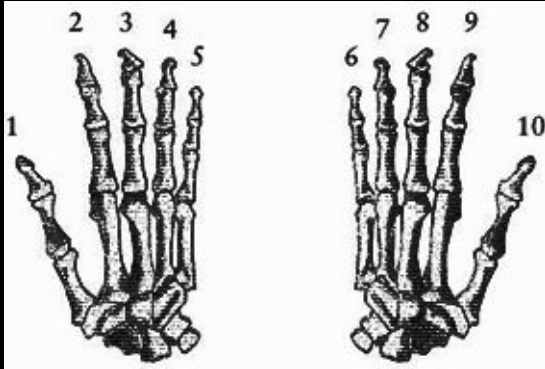
$$= 4 \times 10^3 + 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$

$$= 4 \times 1000 + 1 \times 100 + 2 \times 10 + 3 \times 1$$

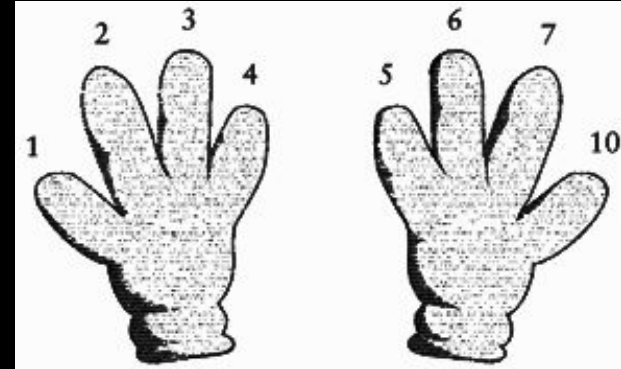
$$= 4123$$



Human Hand



Human Hand



Cartoon Character's Hand

1

2

3

(octal)



1

2

3

(octal)

---

$8^2$

$8^1$

$8^0$

1

2

3

(octal)

---

$8^2$

$8^1$

$8^0$

$$= 1 \times 8^2 + 2 \times 8^1 + 3 \times 8^0$$

1

2

3

(octal)

---

$8^2$

$8^1$

$8^0$

$$= 1 \times 8^2 + 2 \times 8^1 + 3 \times 8^0$$

$$= 1 \times 64 + 2 \times 8 + 3 \times 1$$

1

2

3

(octal)

---

$8^2$

$8^1$

$8^0$

$$= 1 \times 8^2 + 2 \times 8^1 + 3 \times 8^0$$

$$= 1 \times 64 + 2 \times 8 + 3 \times 1$$

$$= 83 \text{ (decimal)}$$

decimal

octal

8



?

decimal

octal

?



7

decimal

octal

16



?

decimal

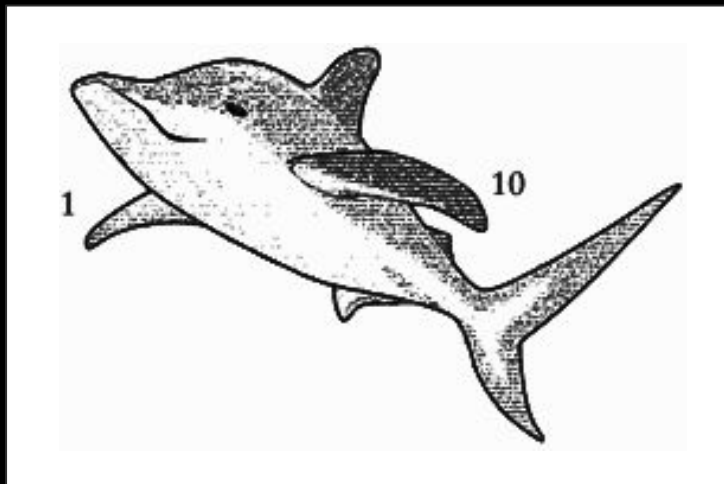
octal

?



100





What now?

0, 1, ...

0, 1, 10, ...

0, 1, 10, 11, ...

0, 1, 10, 11, 100, ...

0, 1, 10, 11, 100, 101, ...

0, 1, 10, 11, 100, 101, 110

1

1

0

(binary)



1

1

0

(binary)

---

$2^2$

$2^1$

$2^0$

1

1

0

(binary)

---

$2^2$

$2^1$

$2^0$

$$= 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

1 1 0

---

(binary)

$2^2$

$2^1$

$2^0$

$$= 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$= 1 \times 4 + 1 \times 2 + 0 \times 1$$

1 1 0

---

(binary)

$2^2$

$2^1$

$2^0$

$$= 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$= 1 \times 4 + 1 \times 2 + 0 \times 1$$

$$= 6 \text{ (decimal)}$$

2 3 4 5 6

0, 1, 10, 11, 100, 101, 110

# Place Value Systems

$$N = d_n * R^{n-1} + \dots + d_1 * R^1 + d_0 * R^0$$

$$d \in \{ 0, 1, \dots R-1 \}$$

$n$  = Number of digits

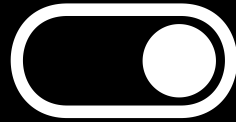
# Place Value Systems

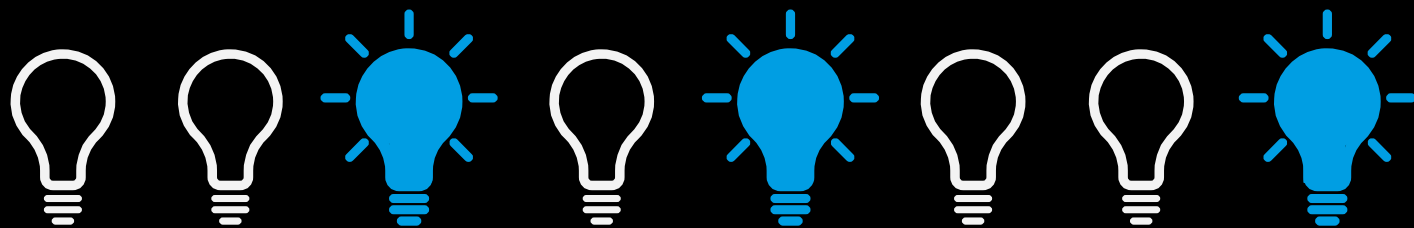
$$R \geq 2$$

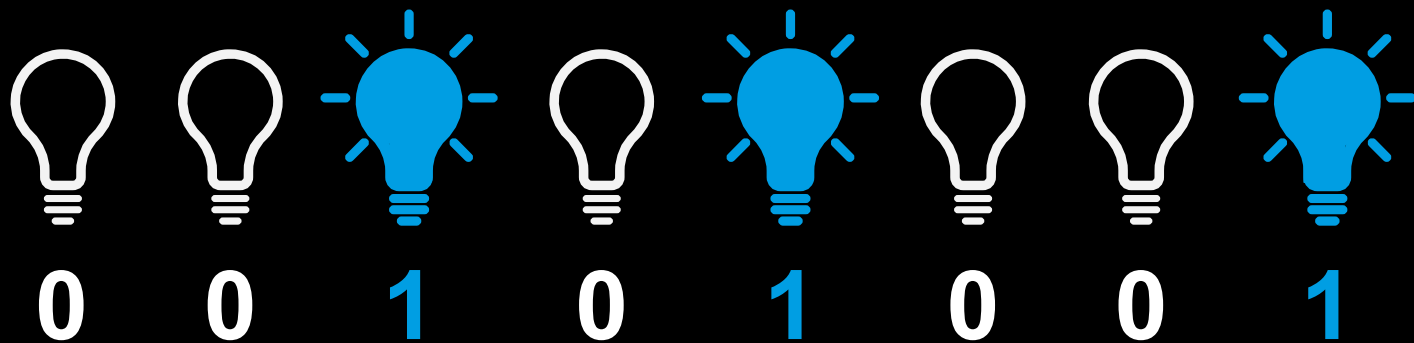
# BITS

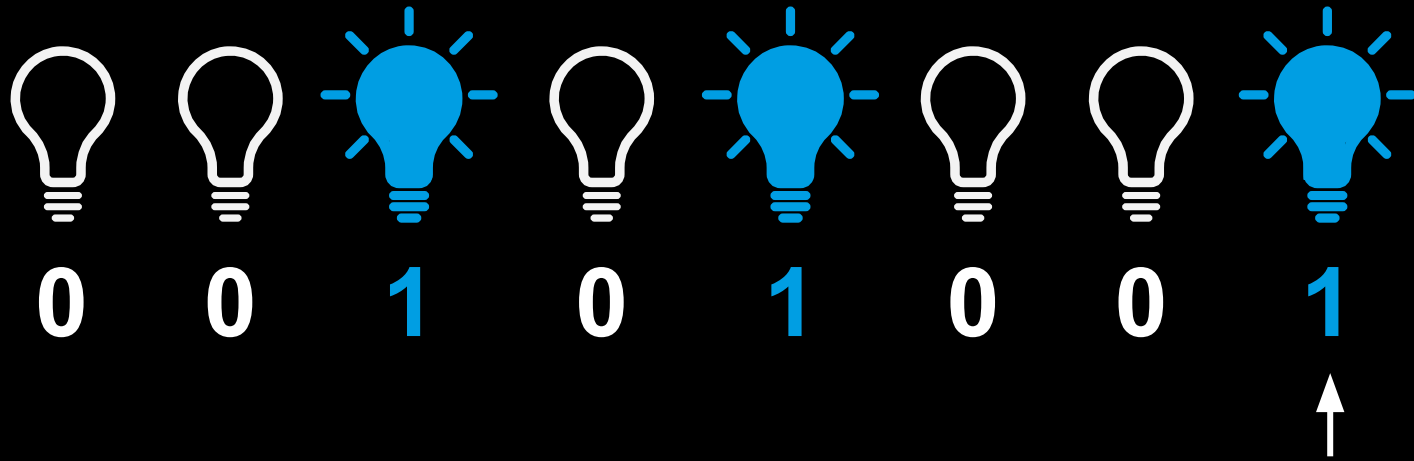


Why do computers think **binary**?

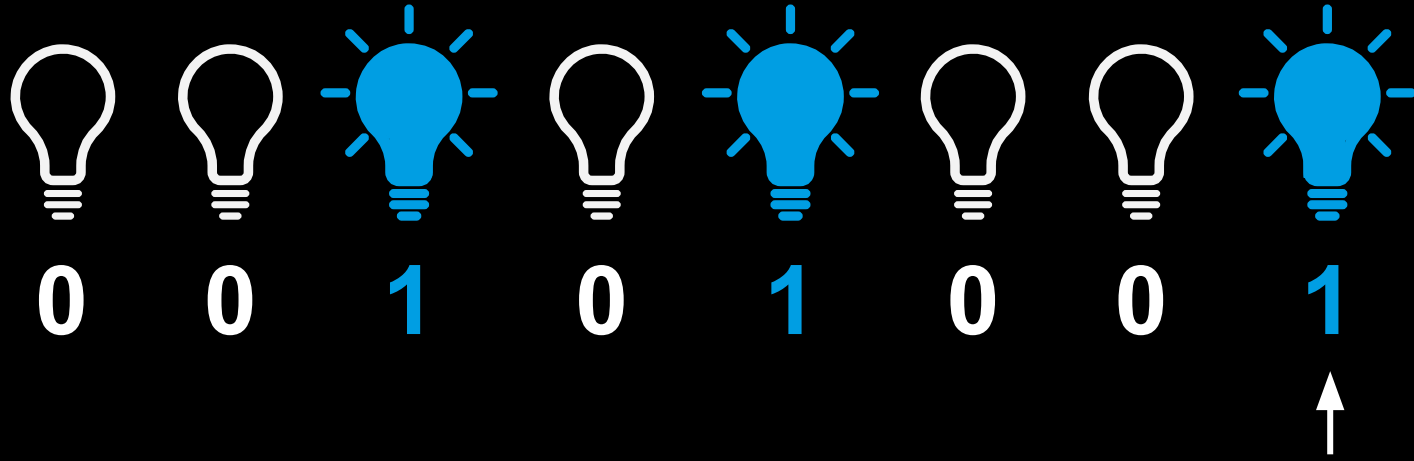






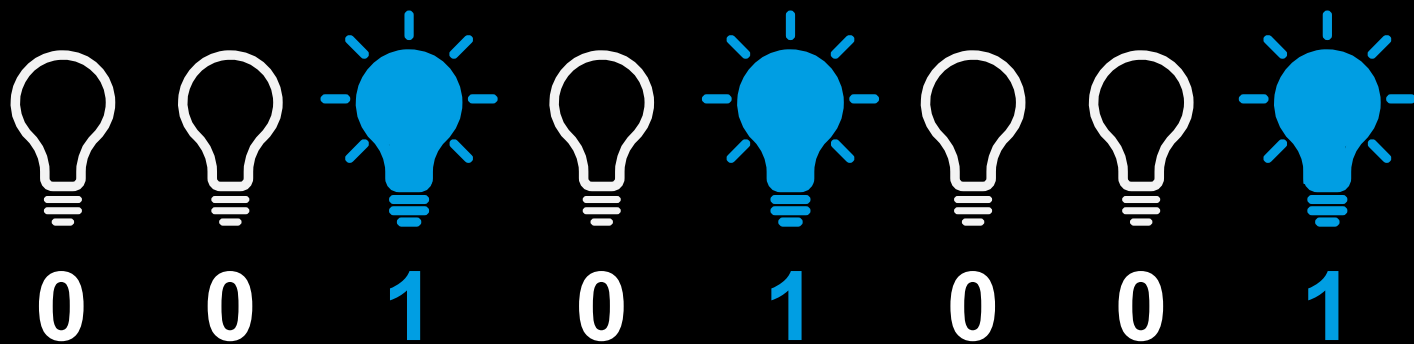


A **Bit** (binary digit)



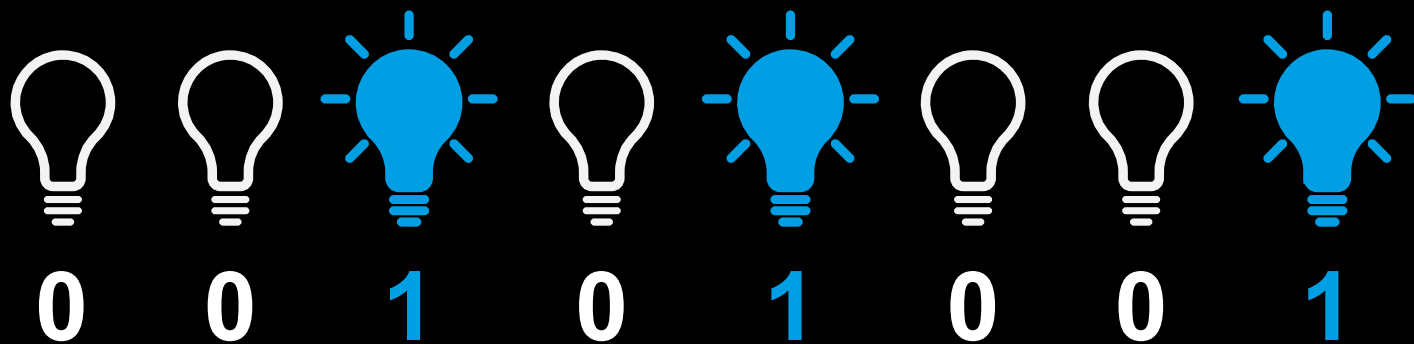
A **Bit** (binary digit)

A **byte** (8 bits)



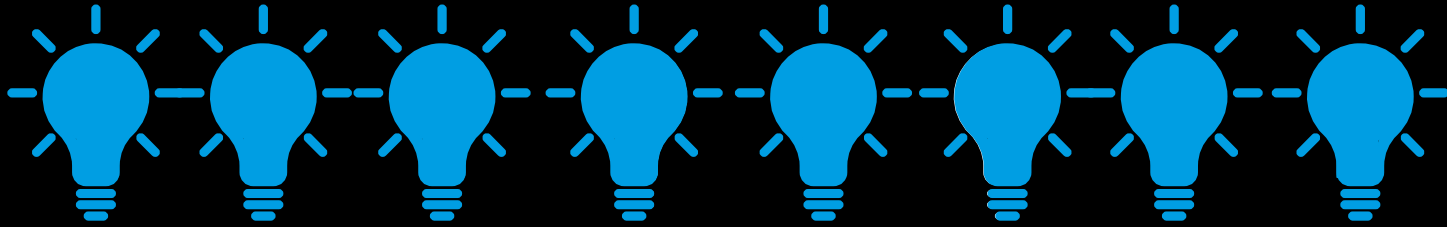
---

$2^7$   $2^6$   $2^5$   $2^4$   $2^3$   $2^2$   $2^1$   $2^0$



---

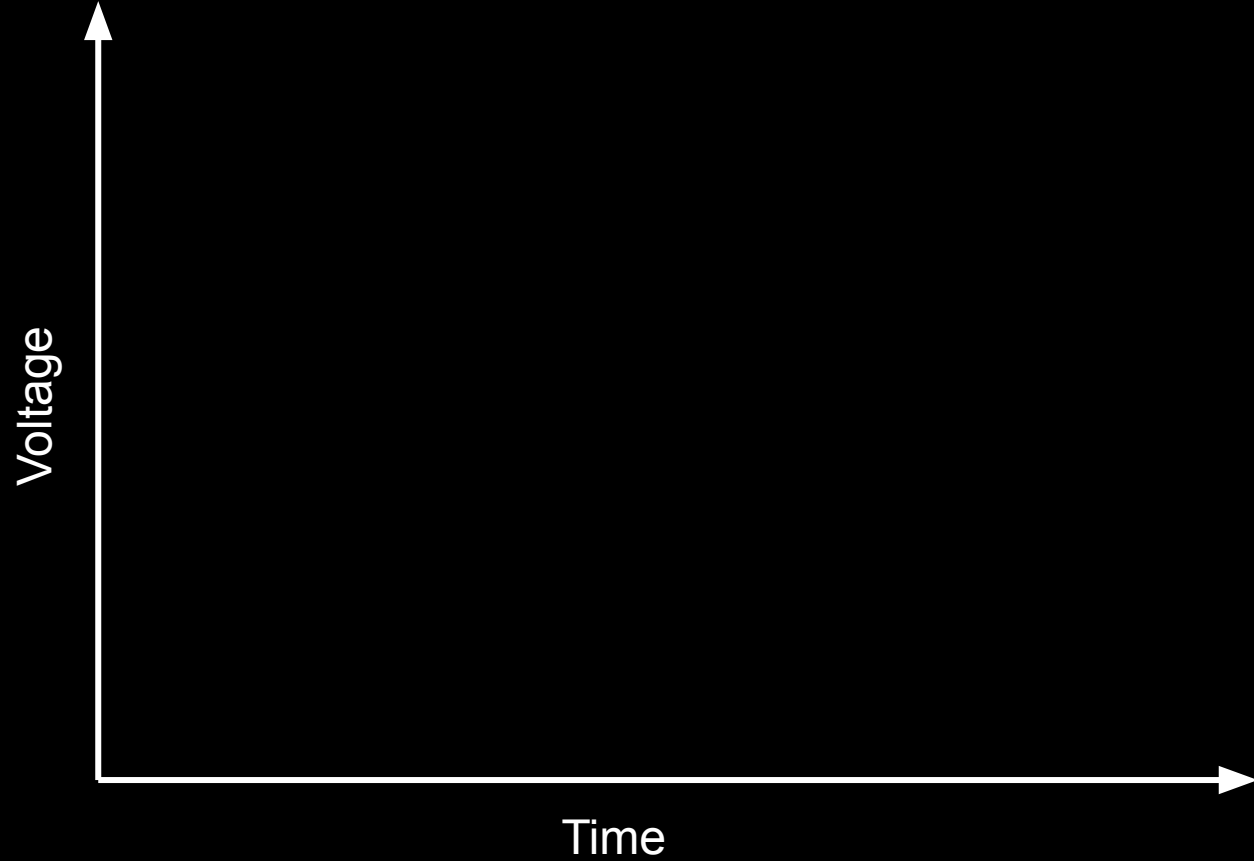
|       |       |       |       |       |       |       |       |
|-------|-------|-------|-------|-------|-------|-------|-------|
| $2^7$ | $2^6$ | $2^5$ | $2^4$ | $2^3$ | $2^2$ | $2^1$ | $2^0$ |
| 128   | 64    | 32    | 16    | 8     | 4     | 2     | 1     |

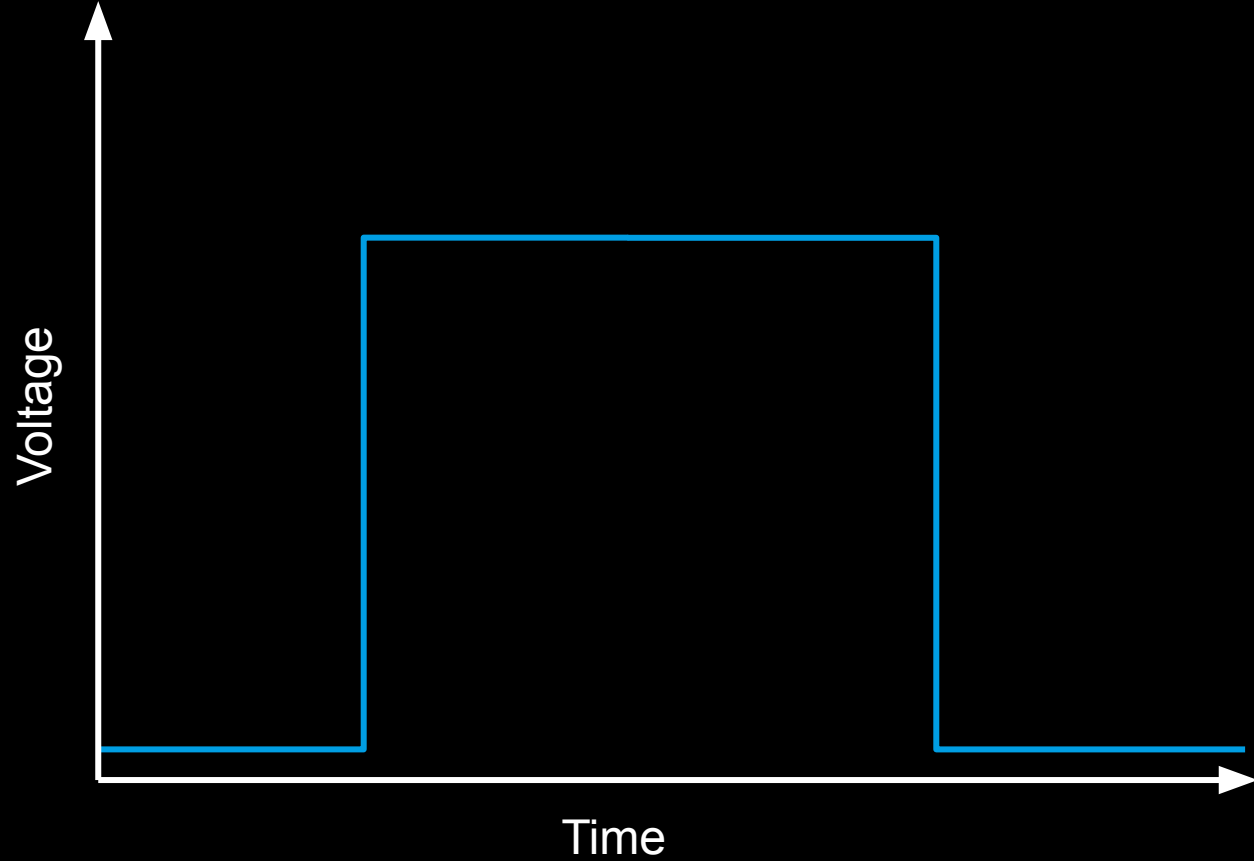


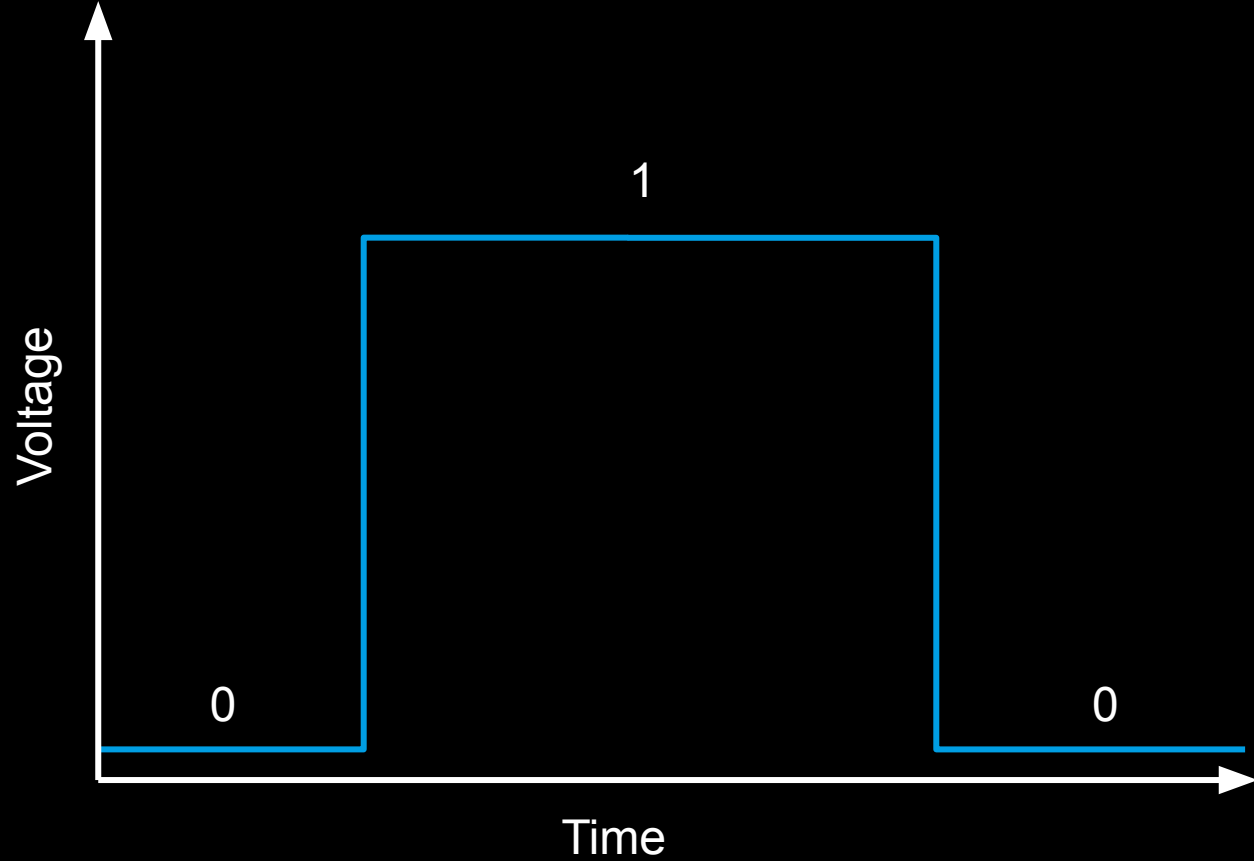
What can we store in one byte?

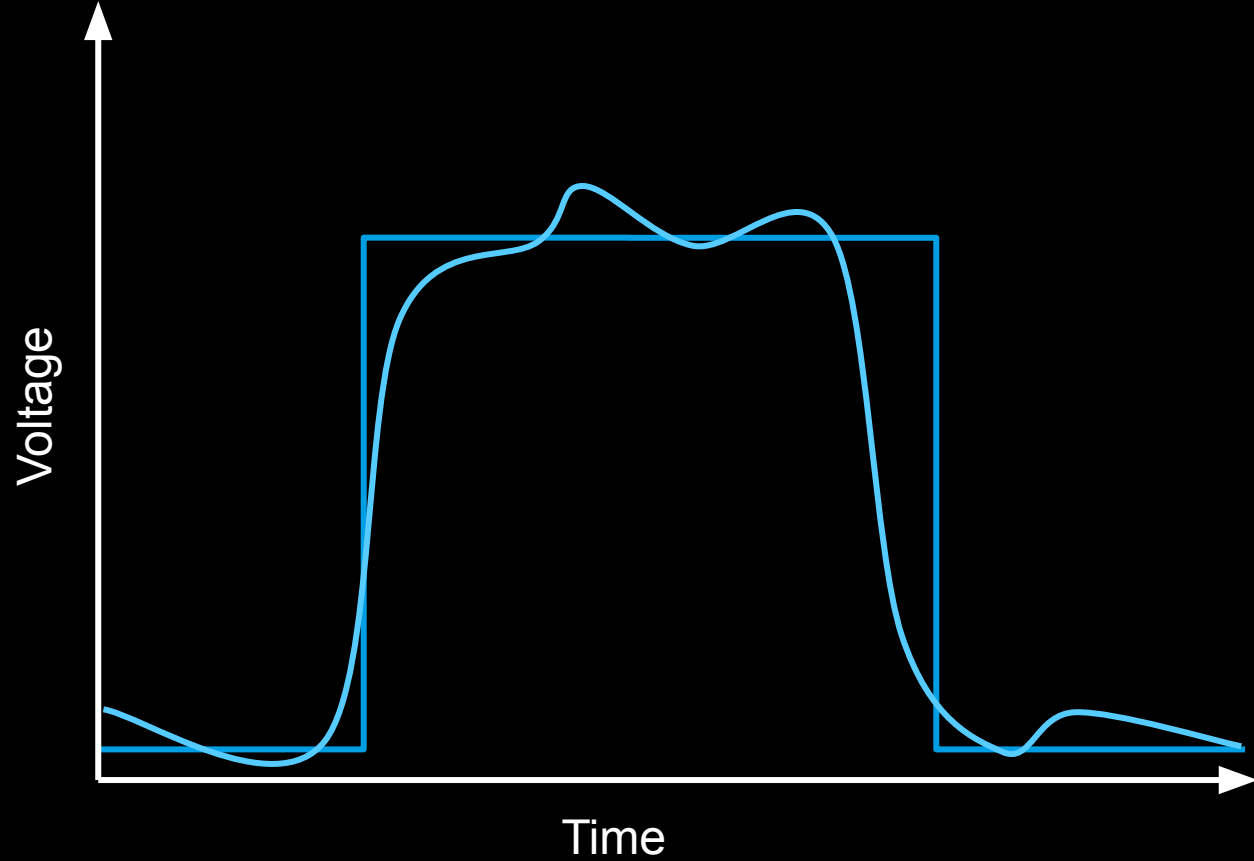


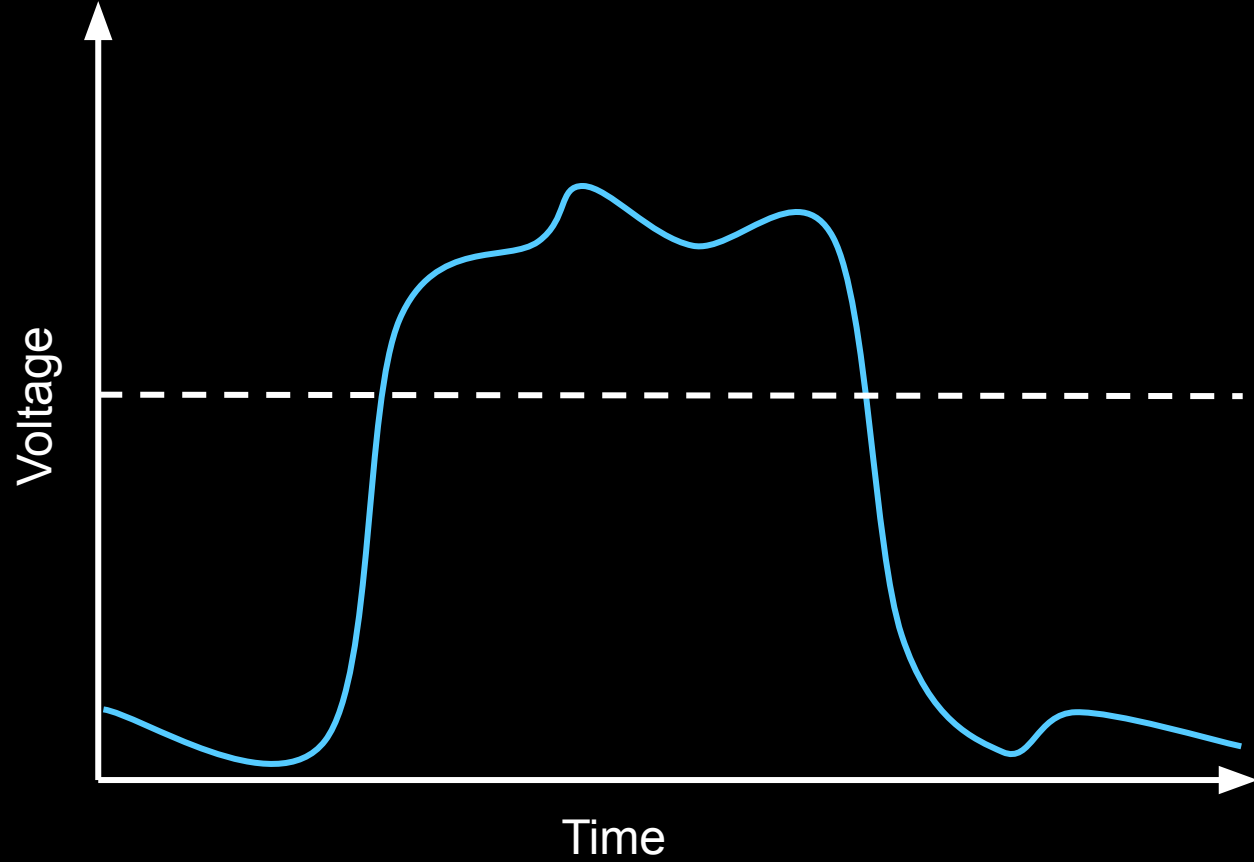
Are we stuck with binary?

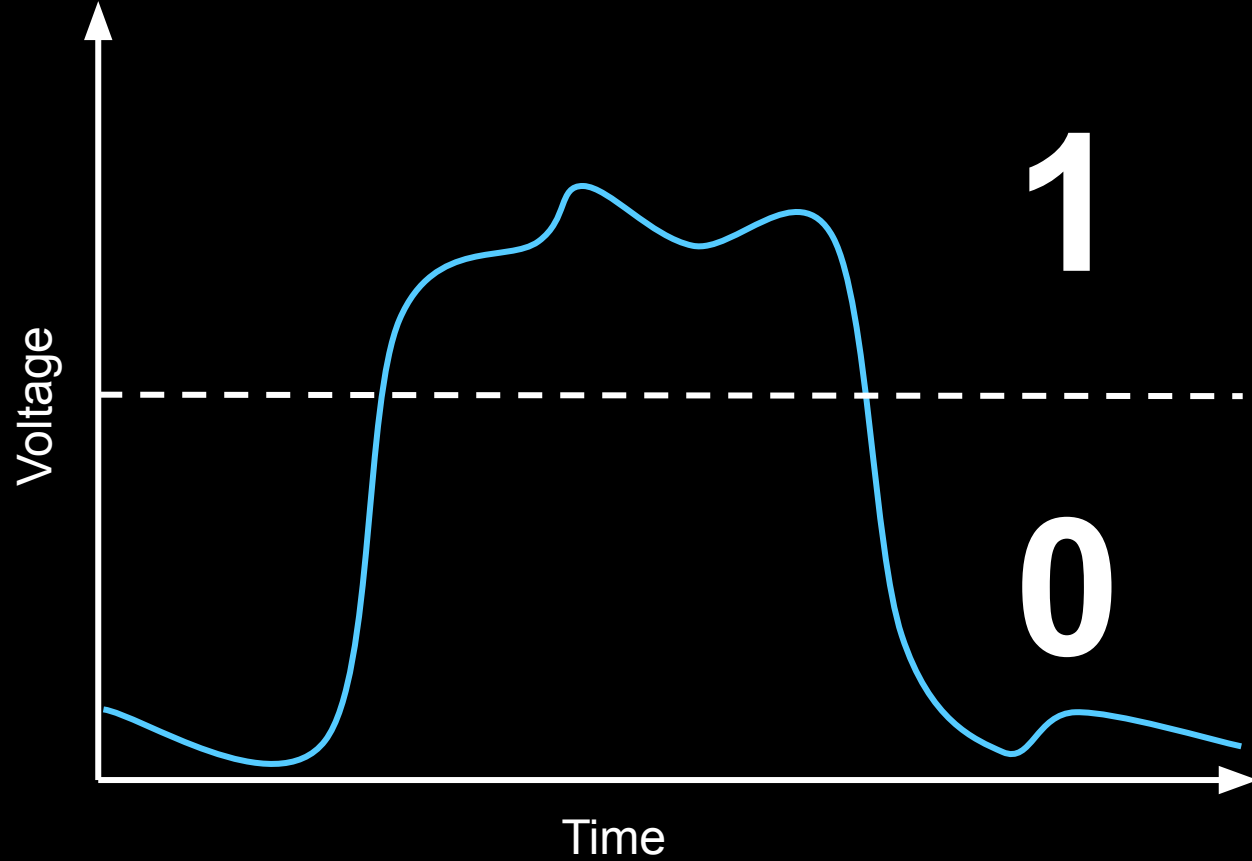


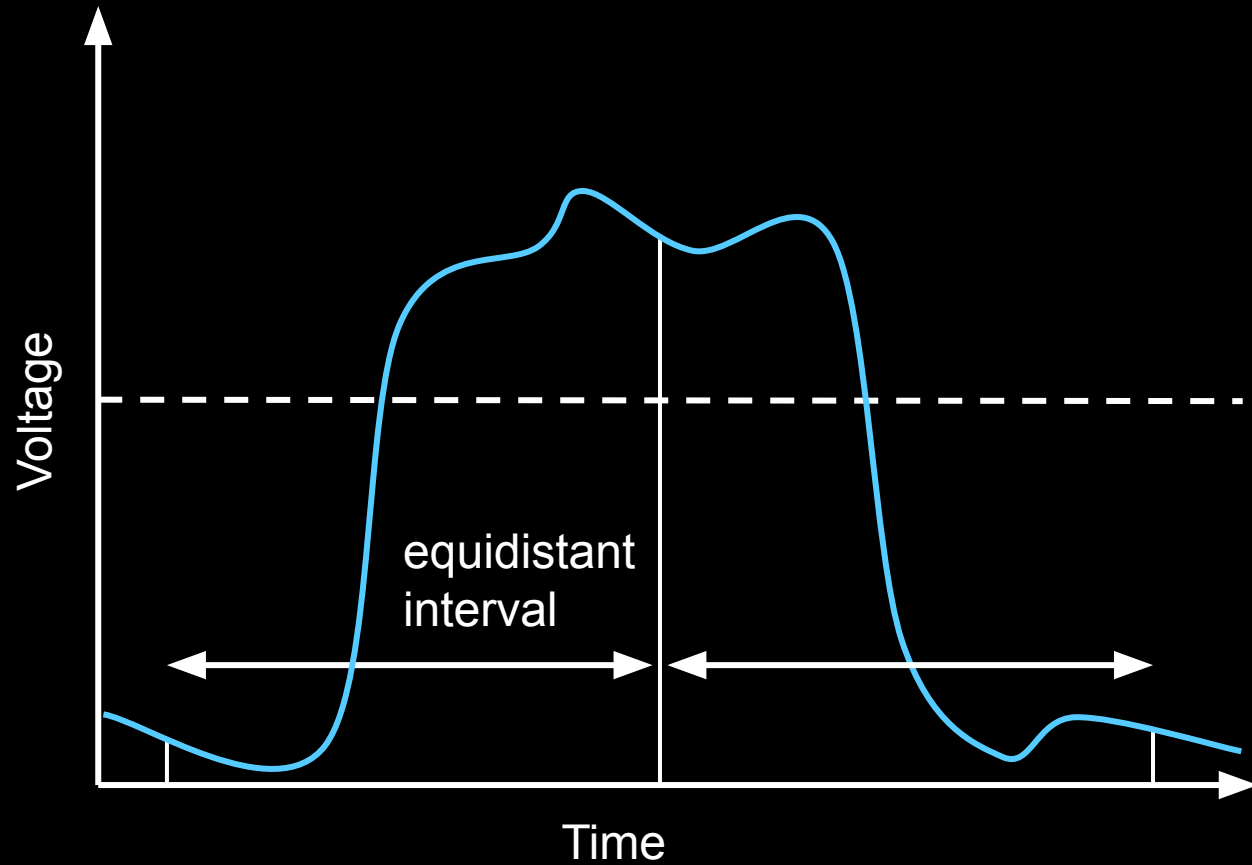




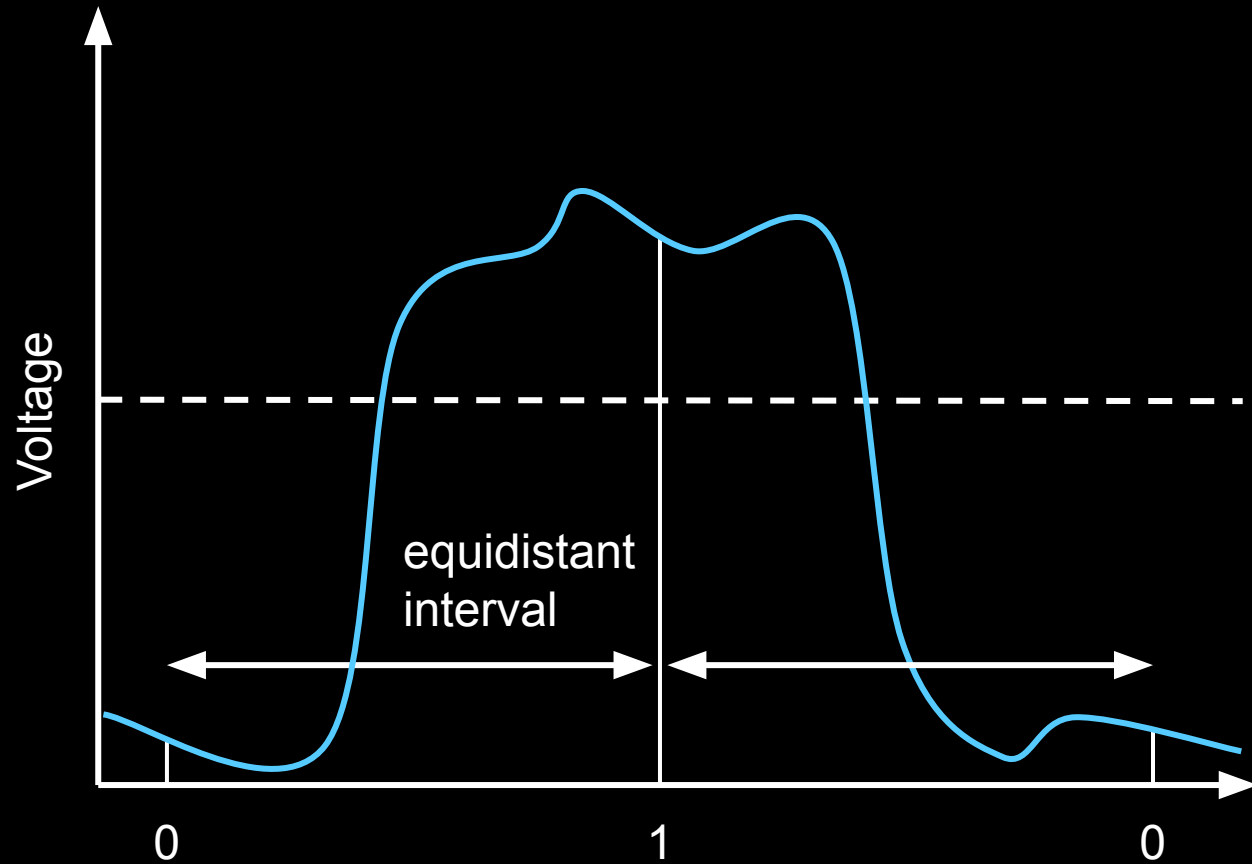


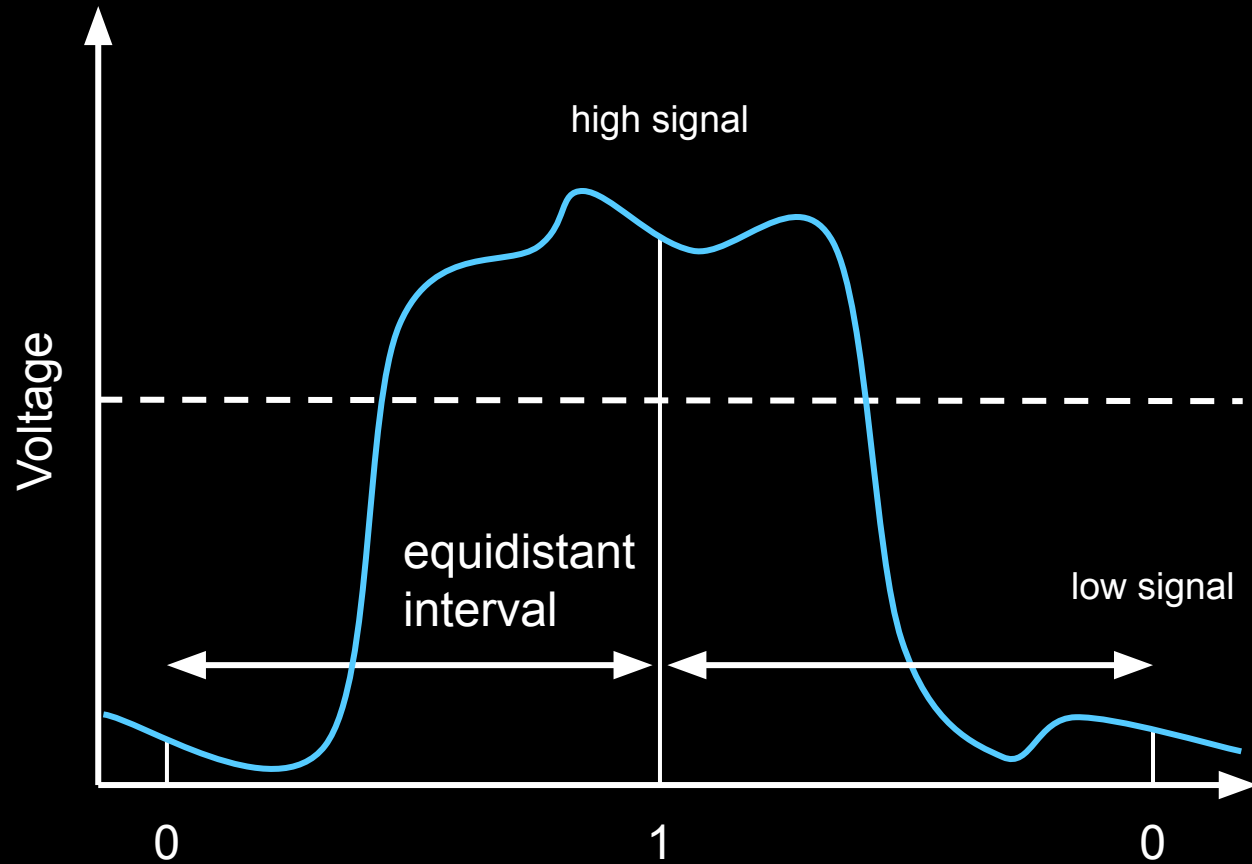




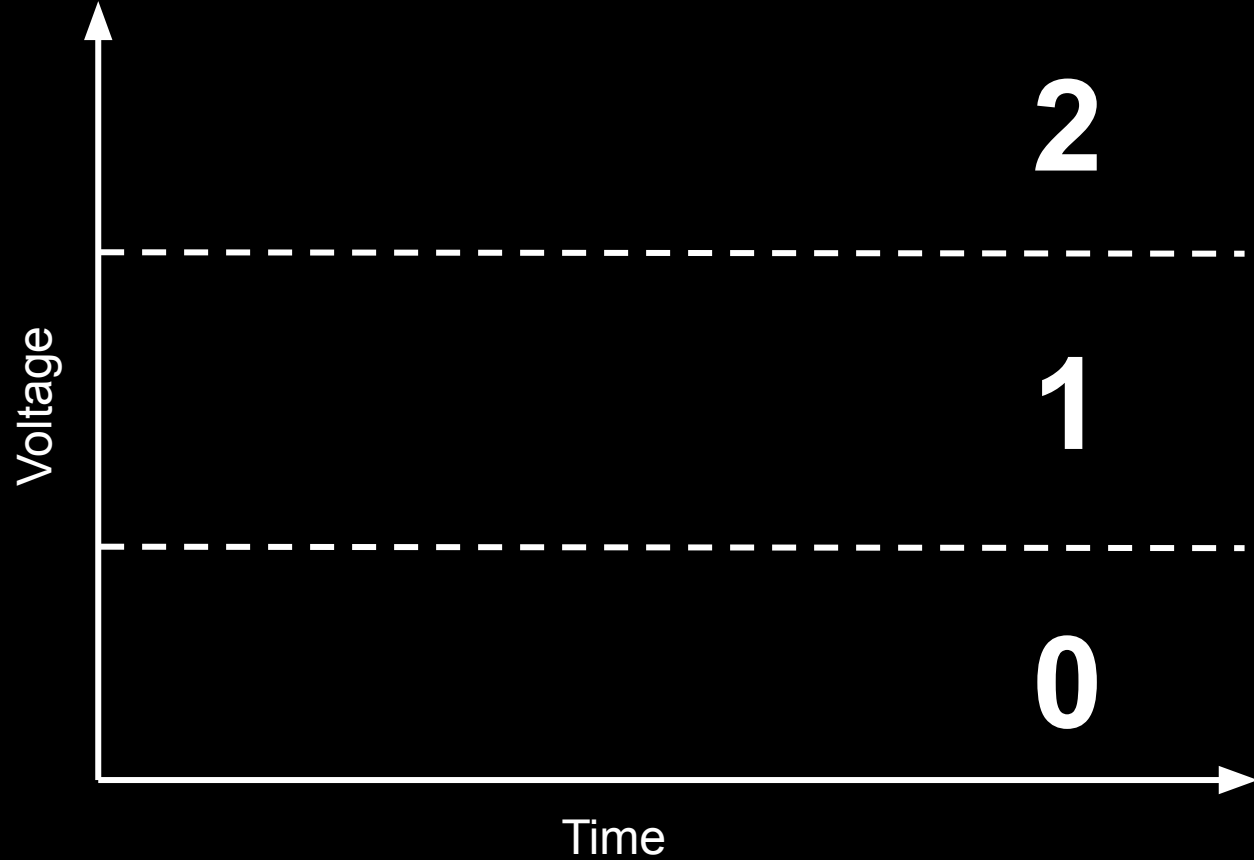


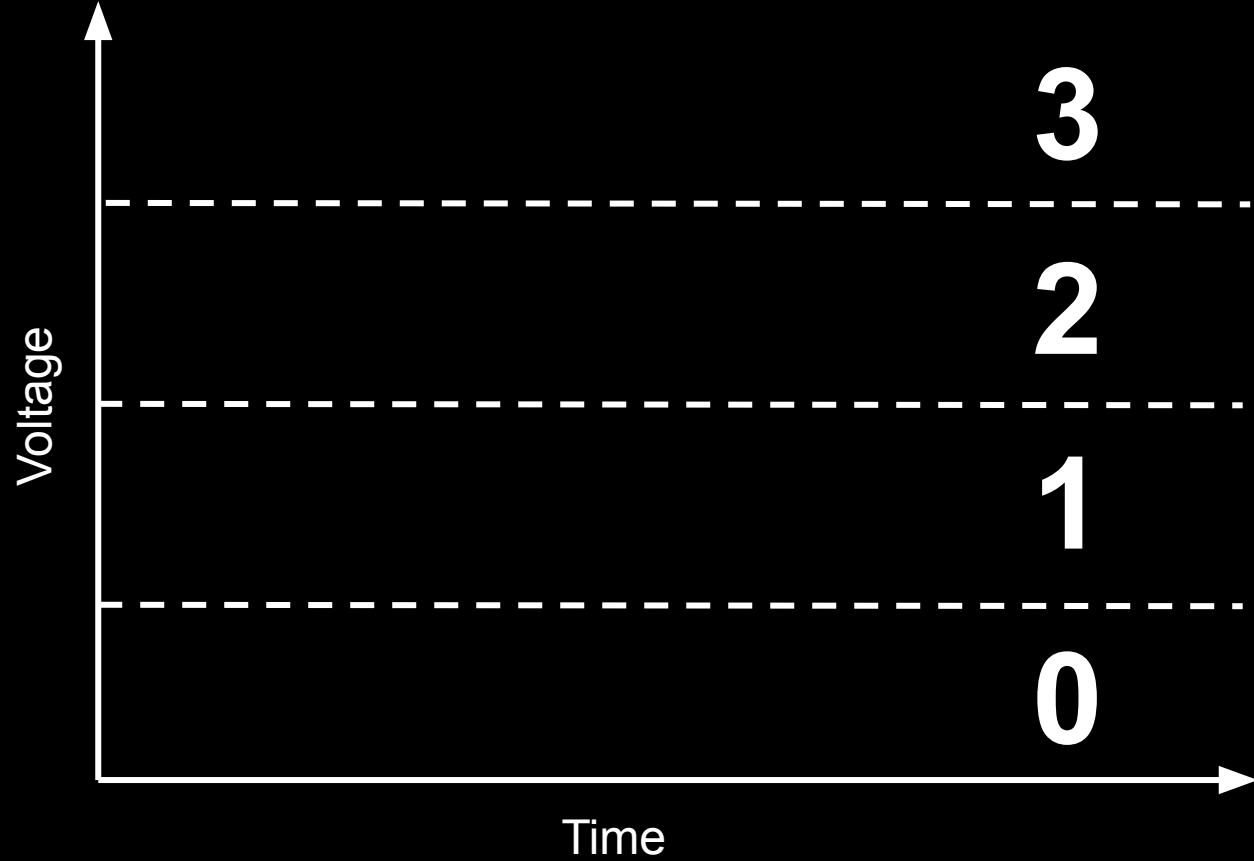


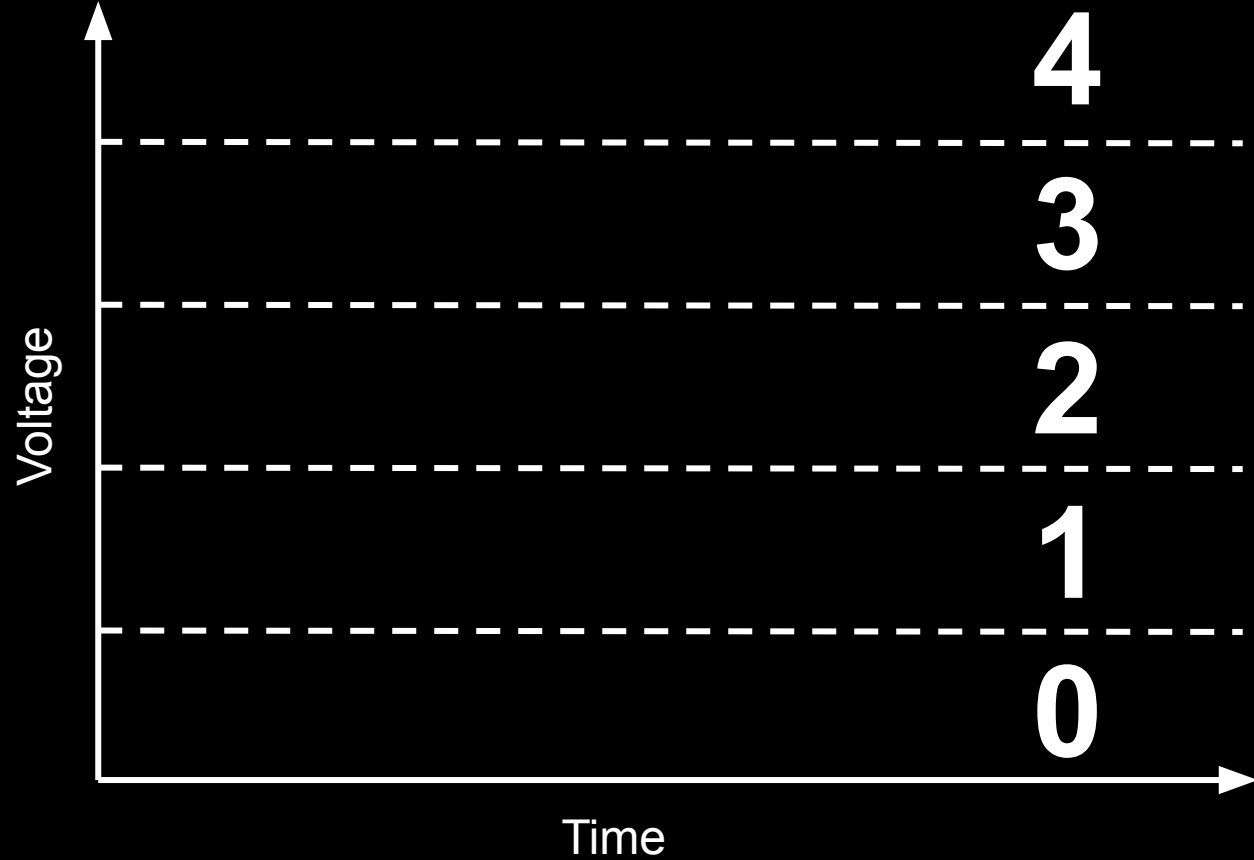


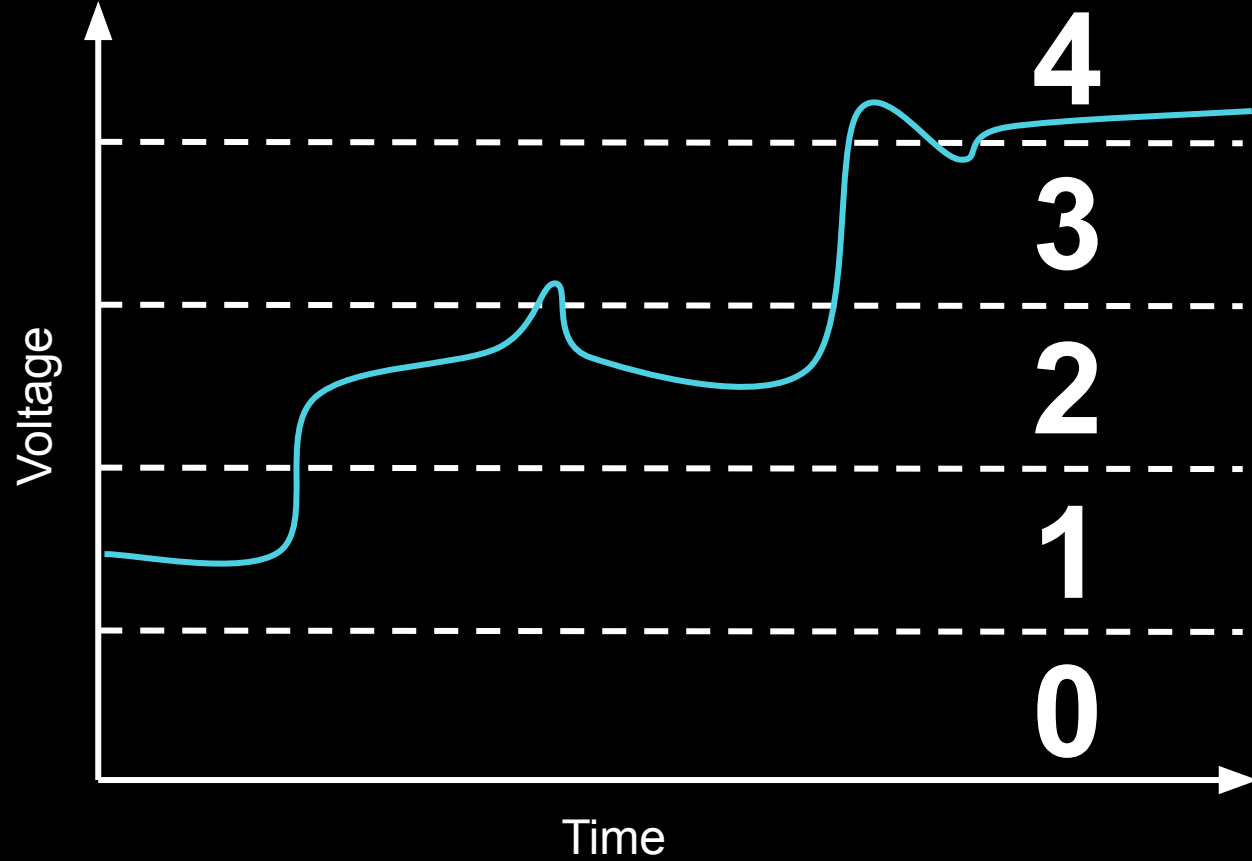


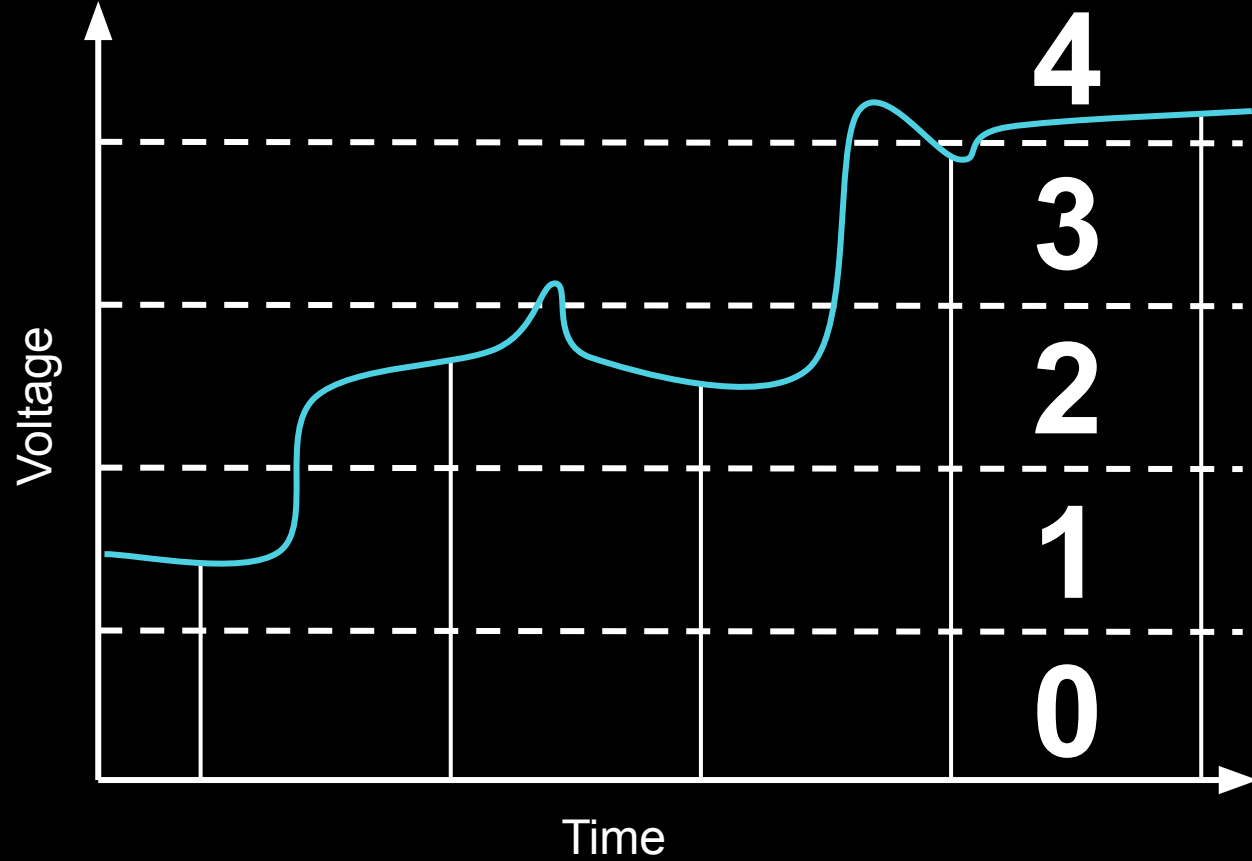
What about ternary?



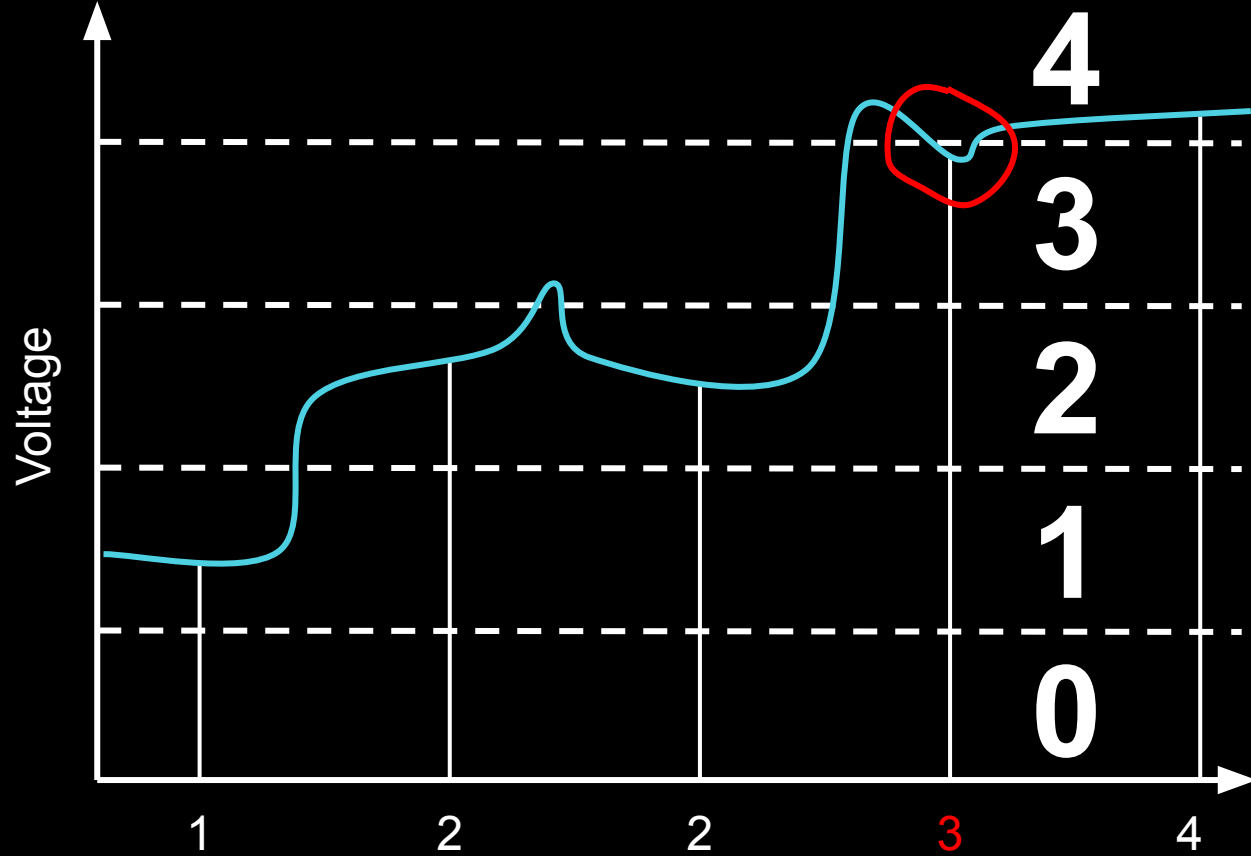






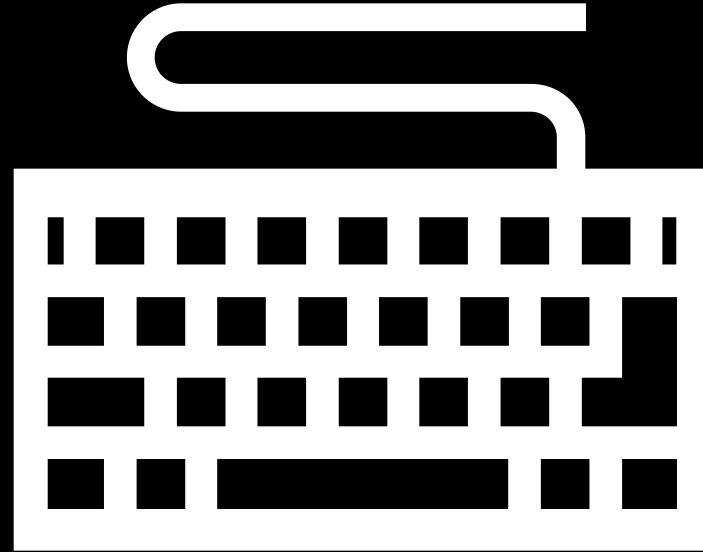






# CODES





|    |    |    |    |     |    |    |    |     |
|----|----|----|----|-----|----|----|----|-----|
| A  | B  | C  | D  | ... | a  | b  | c  | d   |
| 65 | 66 | 67 | 68 |     | 97 | 98 | 99 | 100 |

# ASCII Code

|    |    |    |    |     |    |    |    |     |
|----|----|----|----|-----|----|----|----|-----|
| A  | B  | C  | D  | ... | a  | b  | c  | d   |
| 65 | 66 | 67 | 68 |     | 97 | 98 | 99 | 100 |



1F600



1F601



1F602



1F603

...



1F648



1F649



1F64A



1F64B

# Unicode



1F600



1F601



1F602



1F603

...



1F648



1F649

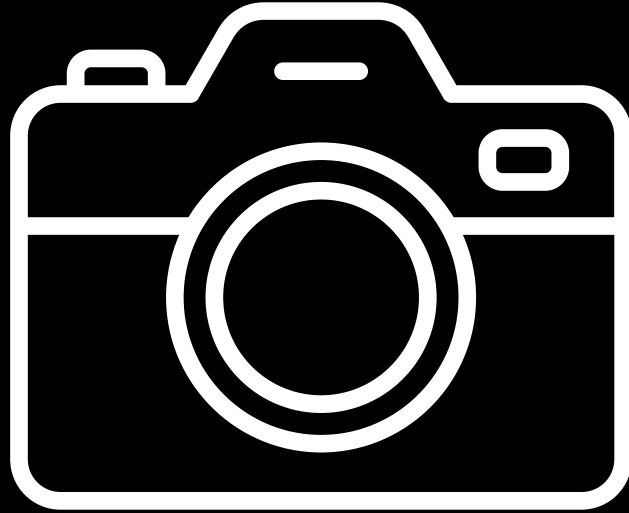


1F64A



1F64B



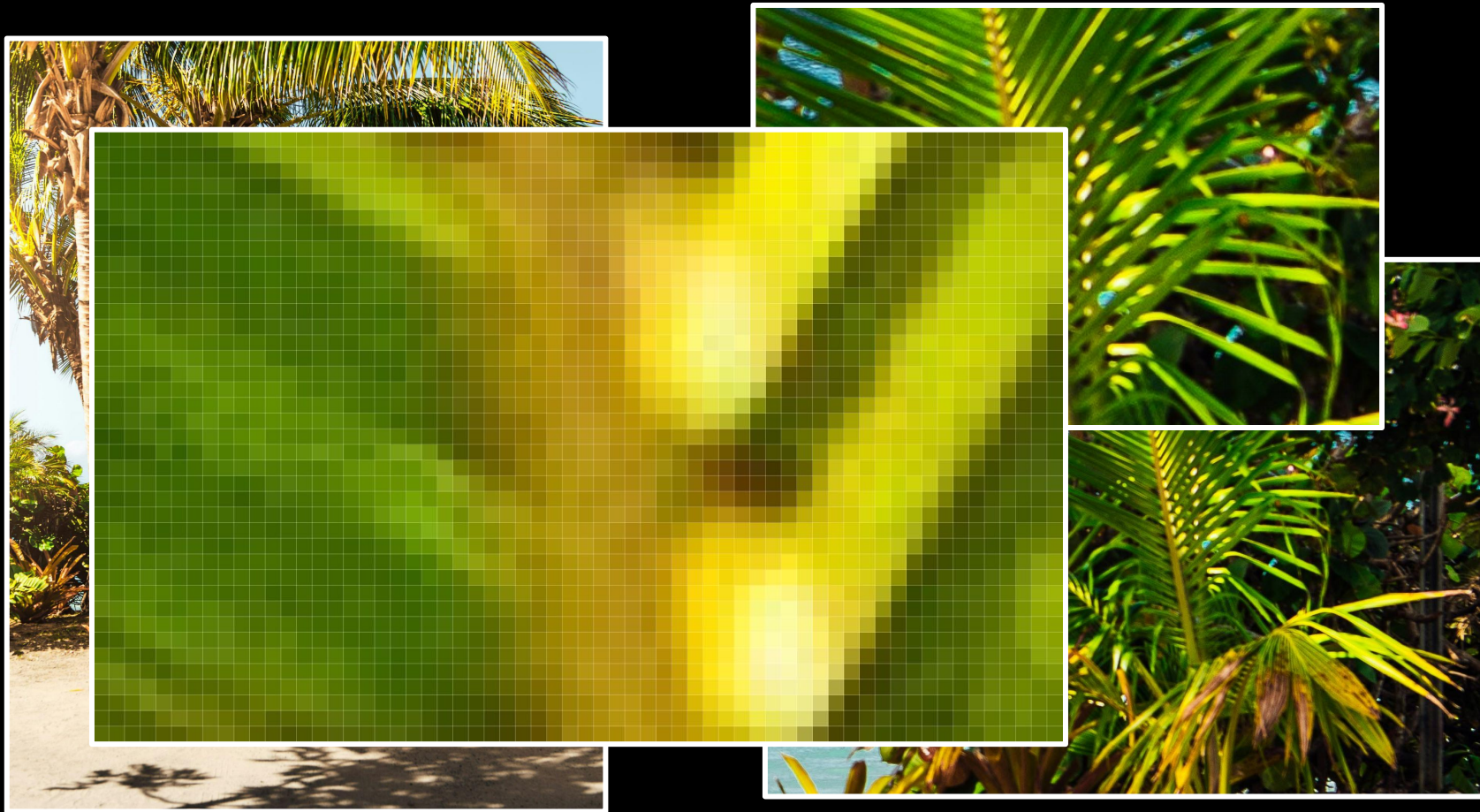




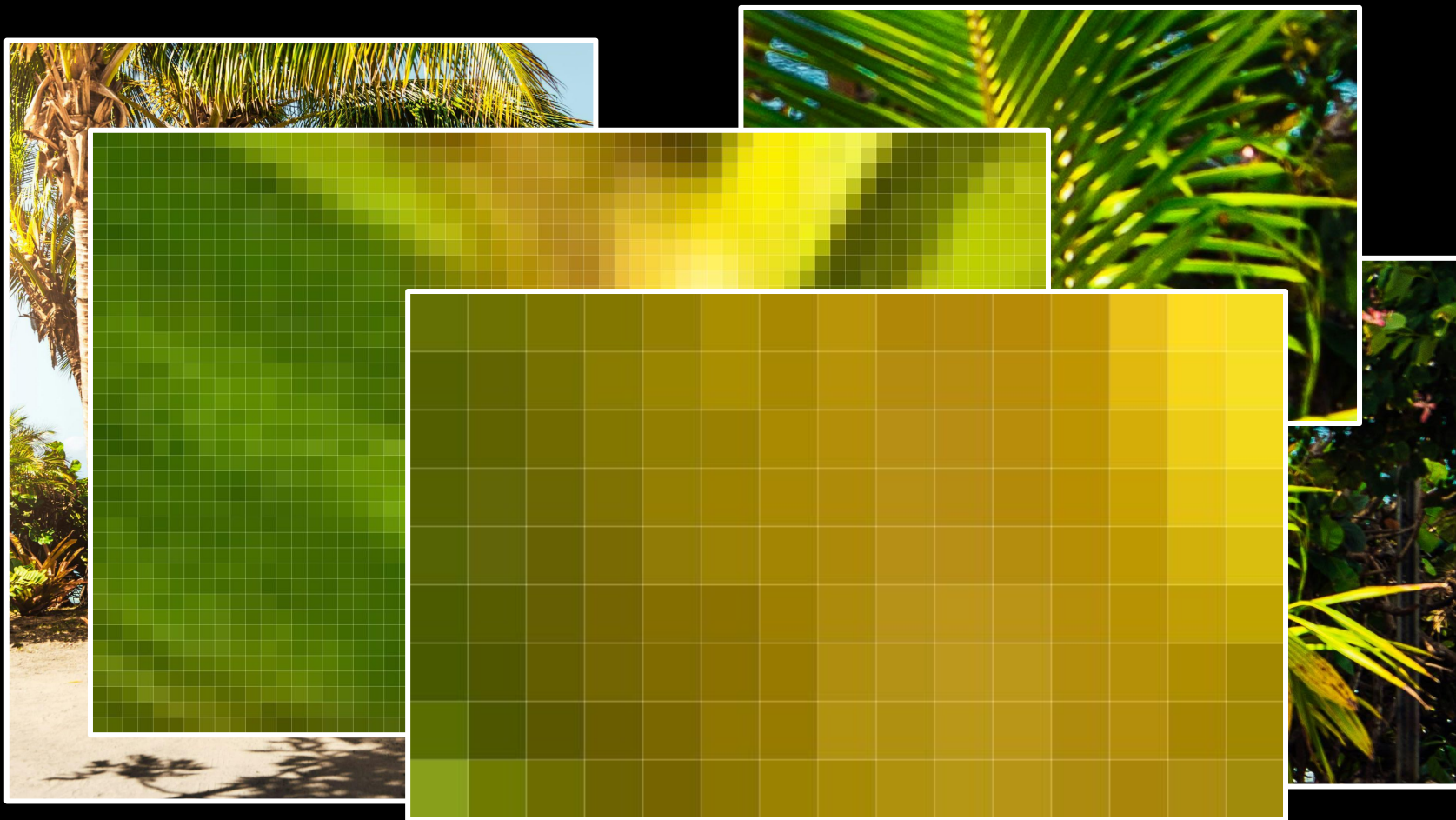


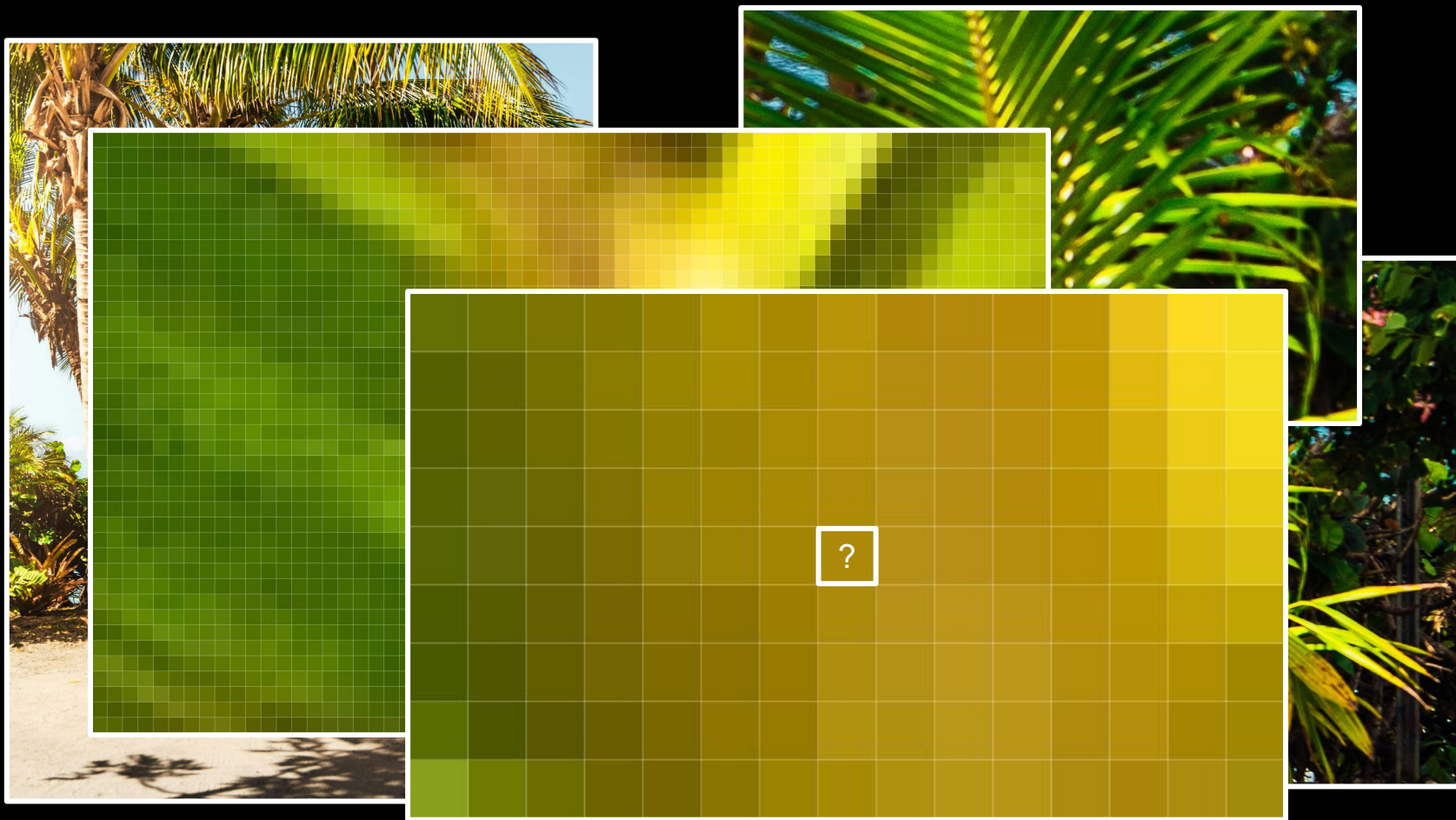


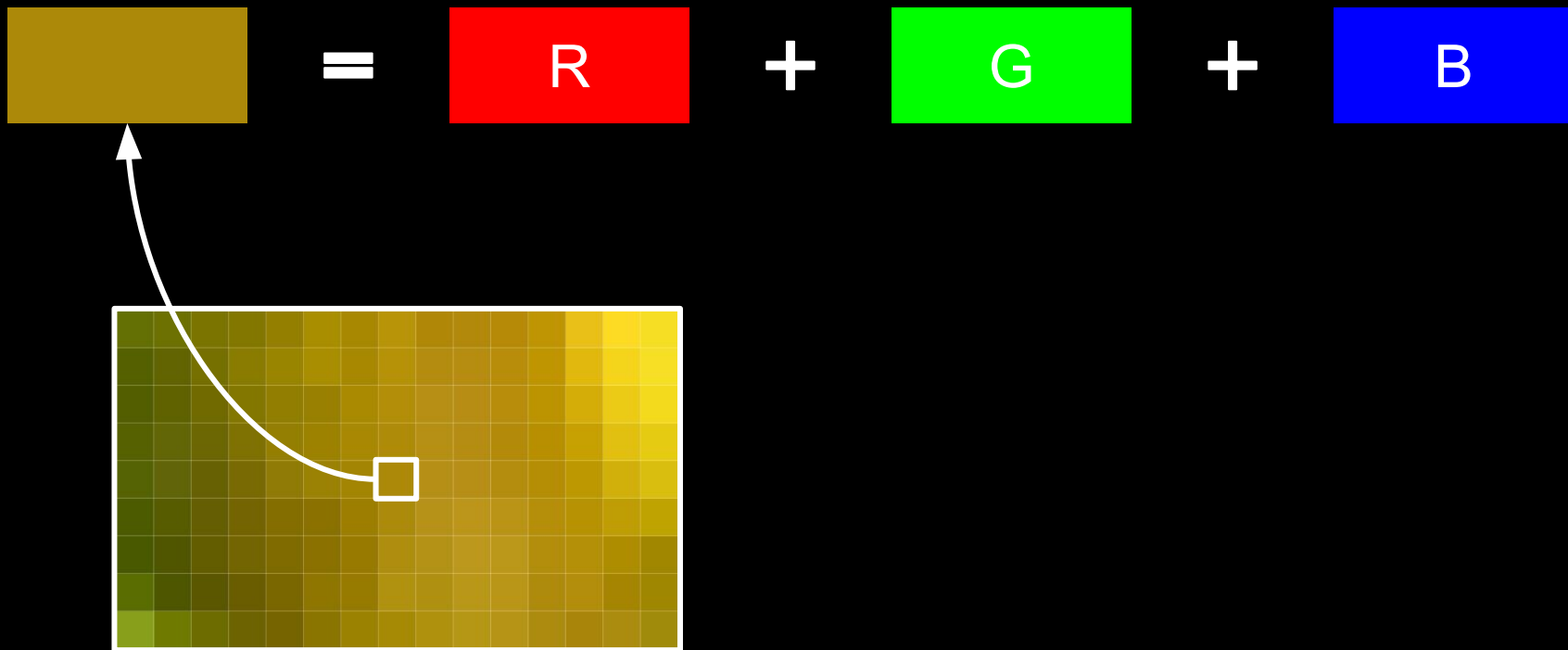




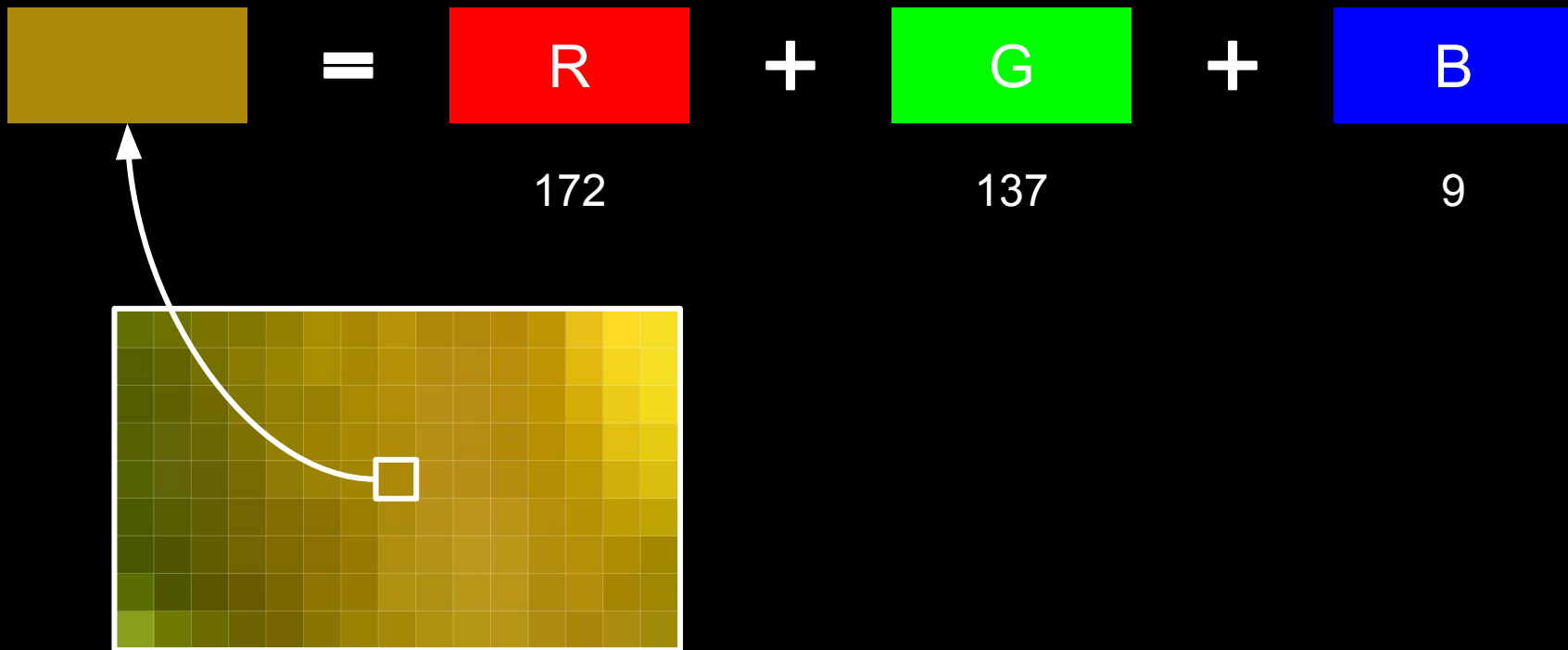


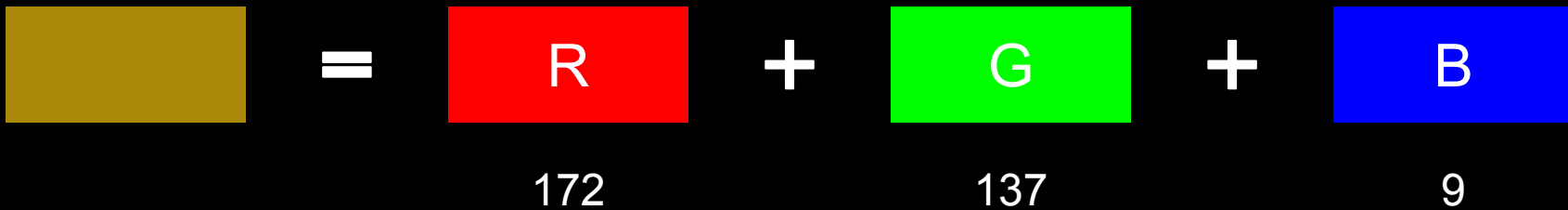








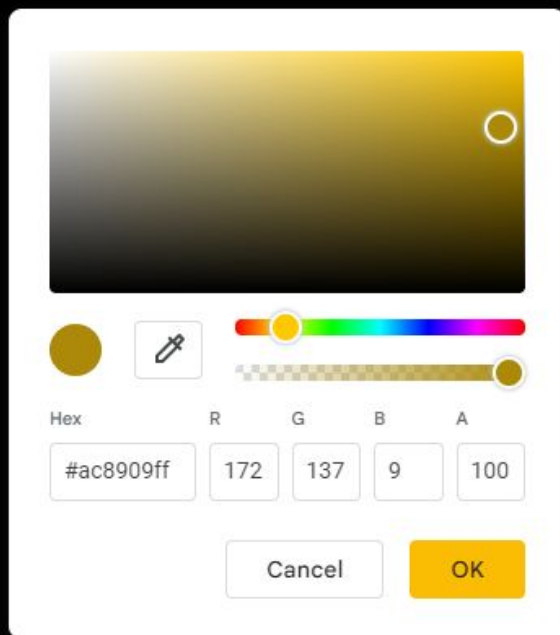





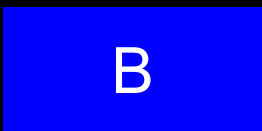


A diagram illustrating the RGB color model. On the left is a gold-colored rectangle. To its right is an equals sign. Further right are three colored rectangles: red, green, and blue. Above the red rectangle is a white 'R', and below it is the number '172'. Above the green rectangle is a white 'G', and below it is the number '137'. Above the blue rectangle is a white 'B', and below it is the number '9'. Plus signs are placed between the red and green rectangles, and between the green and blue rectangles.

$$\text{Gold} = R(172) + G(137) + B(9)$$

#AC8909



 =  R +  G +  B

172 137 9

AC 89 09

#AC8909



# possible colors?

R

$2^7$   $2^6$   $2^5$   $2^4$   $2^3$   $2^2$   $2^1$   $2^0$

A solid red square.

R

A solid green square.

G

A solid blue square.

B

$2^{23}$   $2^{22}$   $2^{21}$   $2^{20}$   $2^{19}$   $2^{18}$   $2^{17}$   $2^{16}$

$2^{15}$   $2^{14}$   $2^{13}$   $2^{12}$   $2^{11}$   $2^{10}$   $2^9$   $2^8$

$2^7$   $2^6$   $2^5$   $2^4$   $2^3$   $2^2$   $2^1$   $2^0$



RGB $2^{23} 2^{22} 2^{21} 2^{20} 2^{19} 2^{18} 2^{17} 2^{16}$  $2^{15} 2^{14} 2^{13} 2^{12} 2^{11} 2^{10} 2^9 2^8$  $2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0$ 8.388.608

+

8.388.607

=

16.777.215

R

G

B

$2^{23} 2^{22} 2^{21} 2^{20} 2^{19} 2^{18} 2^{17} 2^{16}$

$2^{15} 2^{14} 2^{13} 2^{12} 2^{11} 2^{10} 2^9 2^8$

$2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0$

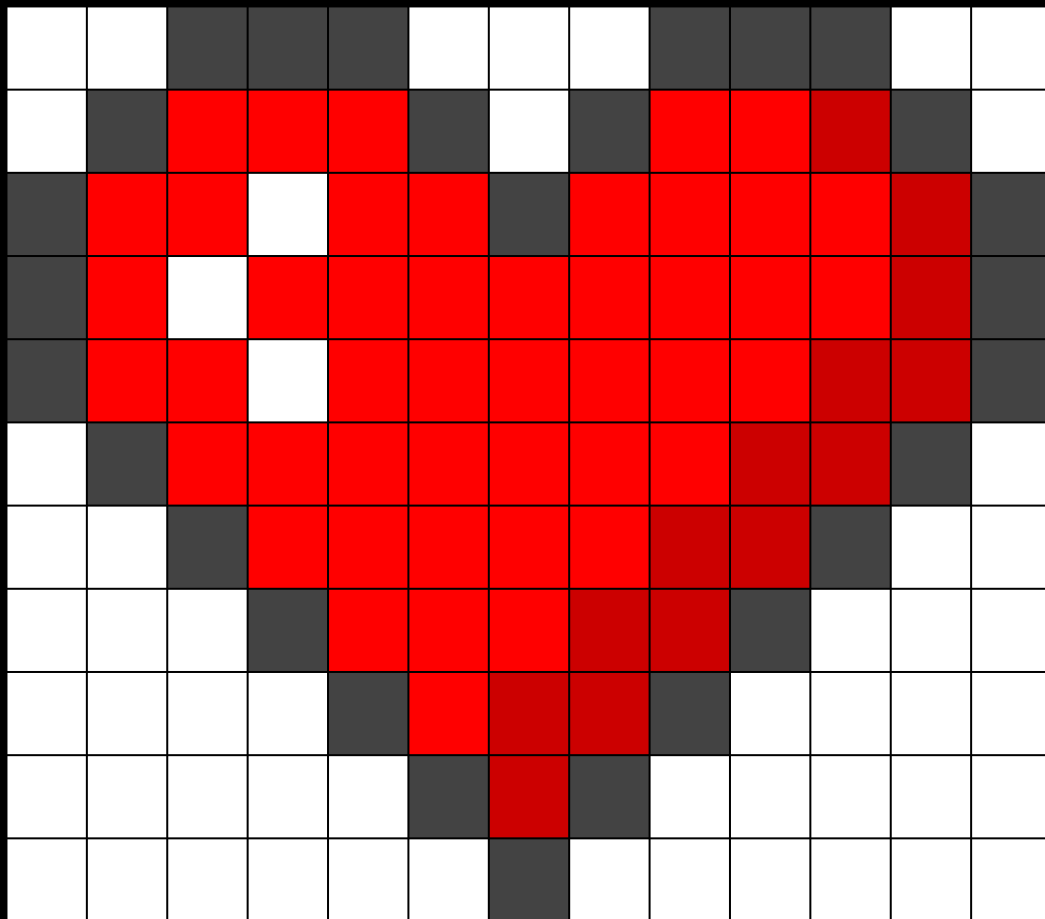
256

×

256

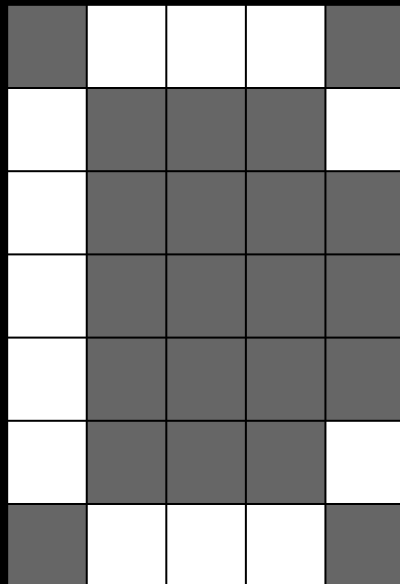
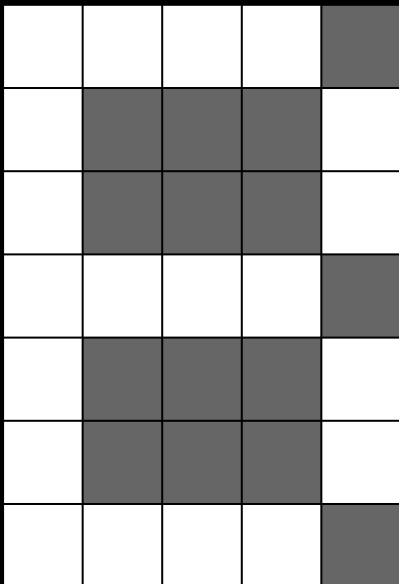
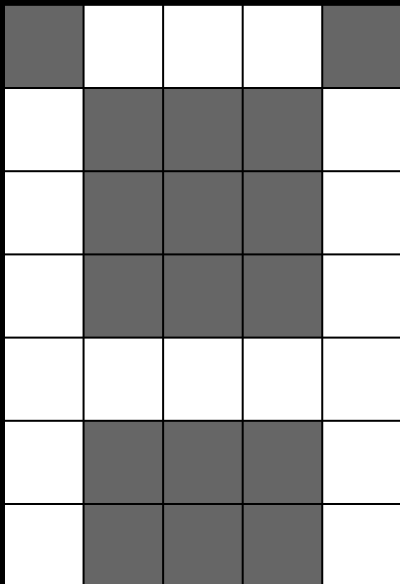
×

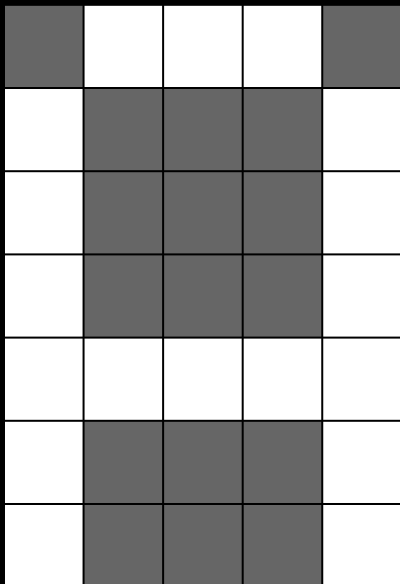
256





compression?





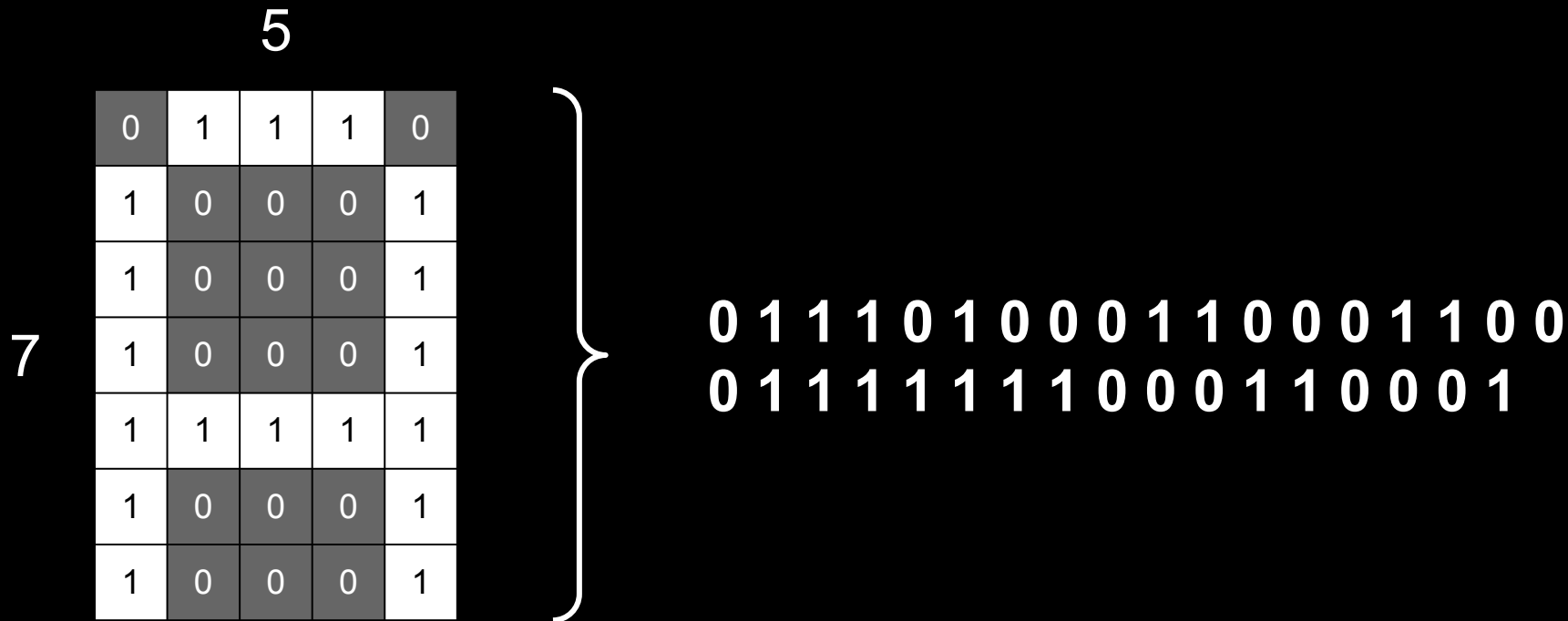
|   |   |   |   |   |
|---|---|---|---|---|
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |

|   |   |   |   |   |
|---|---|---|---|---|
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |



0 1 1 1 0 1 0 0 0 1 1 0 0 0 1 1 0 0  
0 1 1 1 1 1 1 1 0 0 0 1 1 0 0 0 1

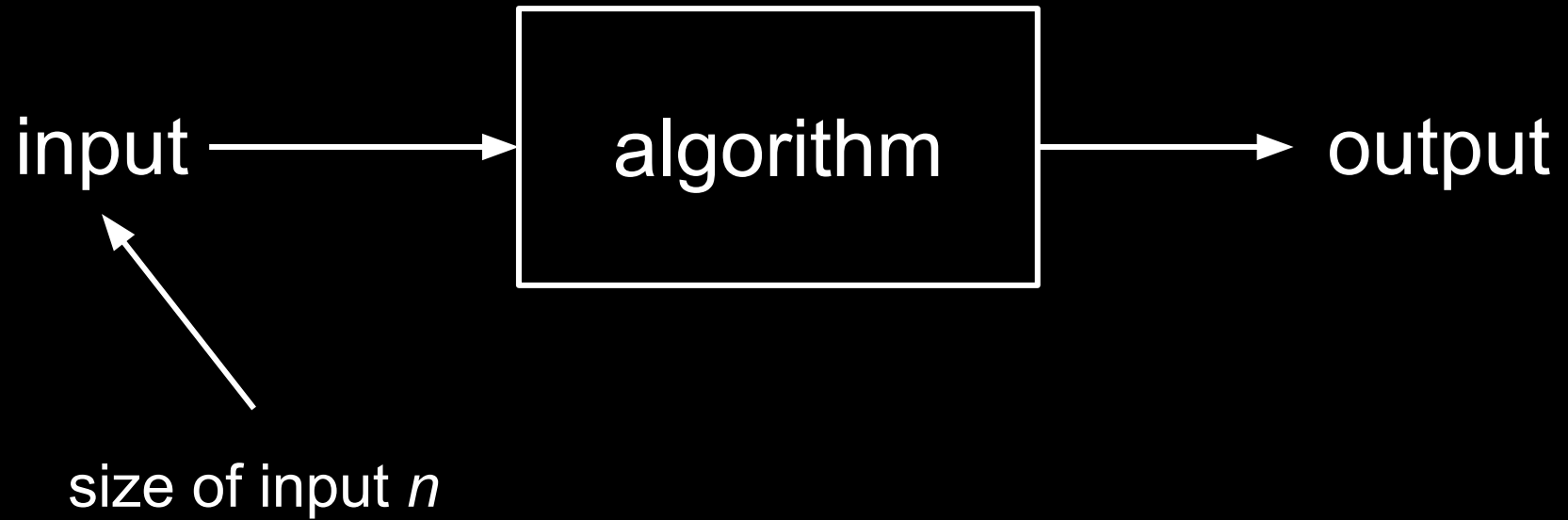


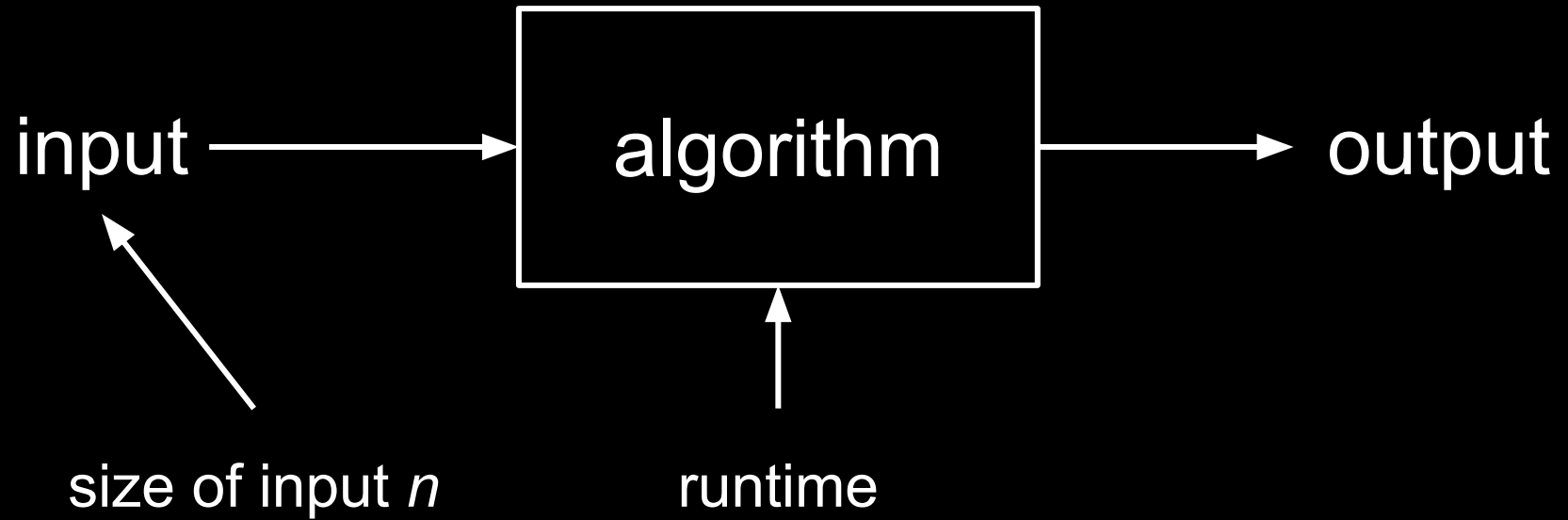


# ALGORITHMS

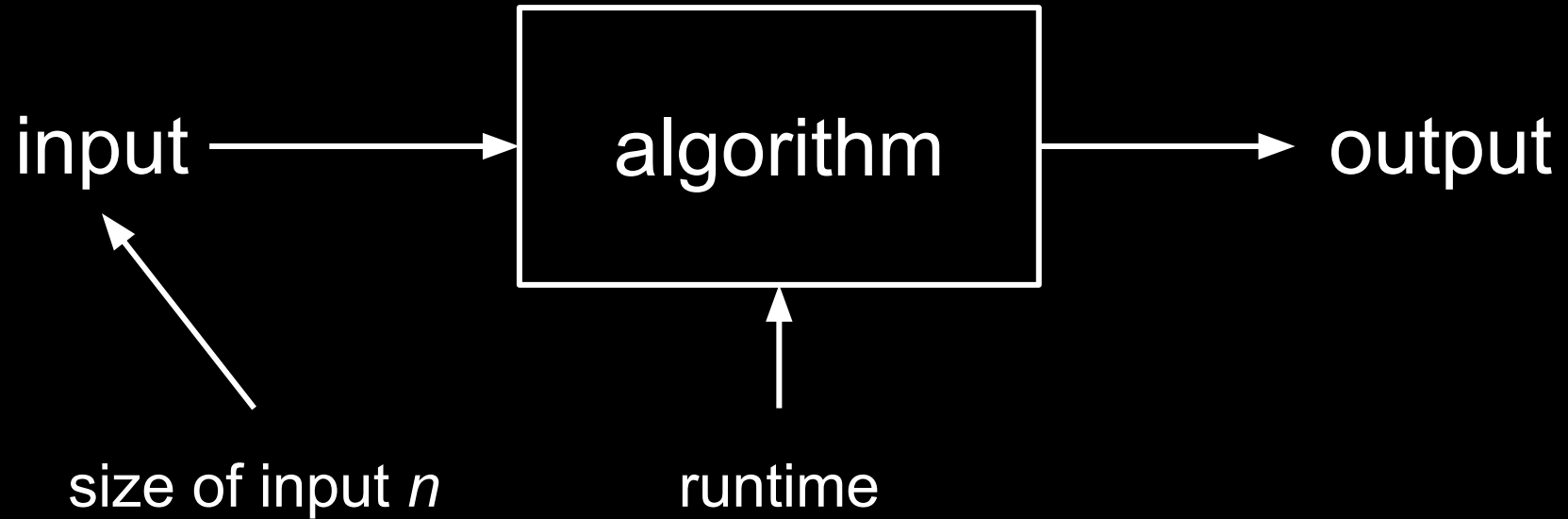
complexity







$O(n)$



# COMPUTERS



# ARITHMETIC

# MEMORY

# ANALOG VS. DIGITAL