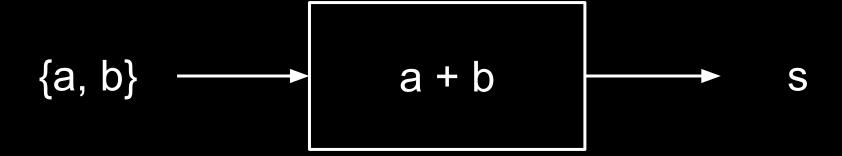
# PROBLEM SOLVING

# a model for solving problems

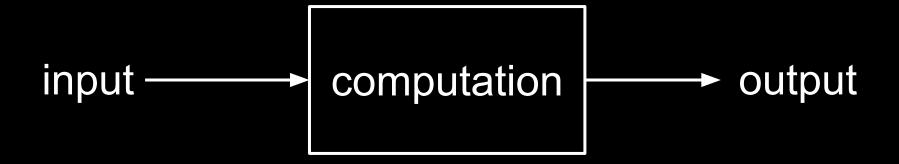


# a model for solving problems

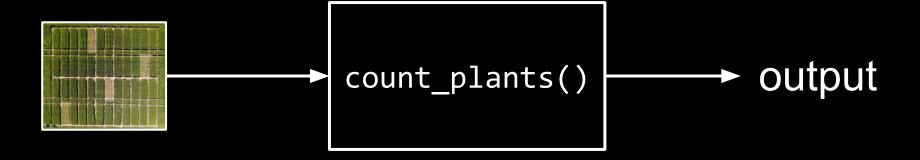


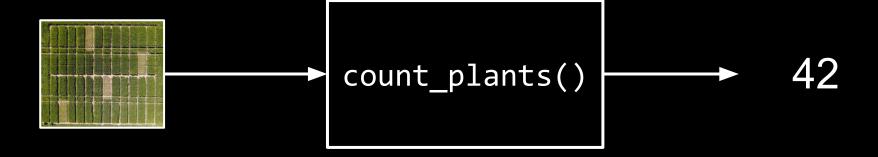


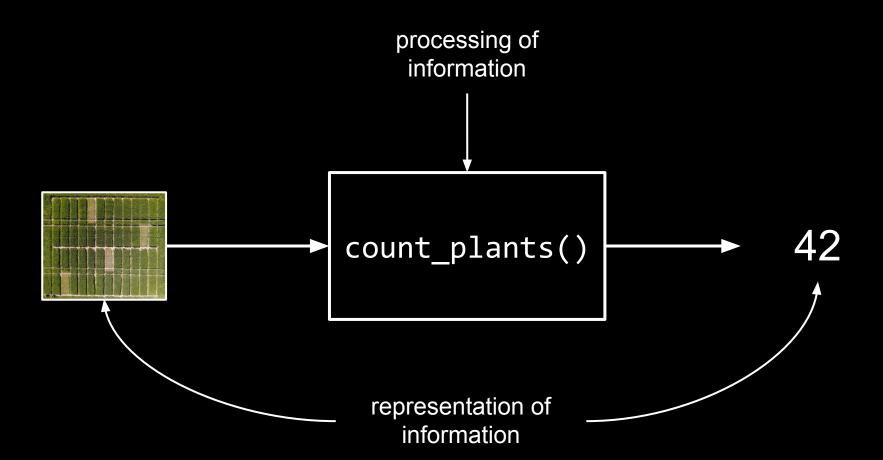
## a model for solving problems









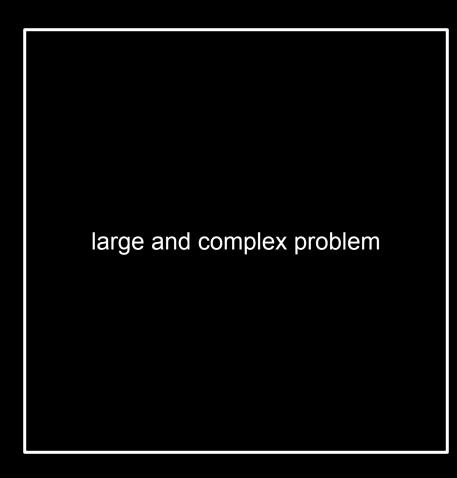






# problem solving strategies

# divide and conquer



smaller problem	smaller problem
smaller problem	smaller problem

even smaller problem	smaller problem
even smaller problem	
smaller problem	smaller problem



### is 67 a prime number?

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

### 19 steps... can't we do better?

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

# large and complex problem

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

# large and complex problem

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

#### smaller problem

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41

#### smaller problem

43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

```
binary search 67!= 41

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,

43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

67 > 41



```
binary search 67 > 41

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41,

43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

67!=59
```

```
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

1
67 > 59
```

$$\frac{2}{5}$$
,  $\frac{5}{5}$ ,  $\frac{7}{7}$ ,  $\frac{11}{13}$ ,  $\frac{17}{17}$ ,  $\frac{19}{19}$ ,  $\frac{23}{29}$ ,  $\frac{29}{31}$ ,  $\frac{37}{37}$ ,  $\frac{41}{43}$ ,  $\frac{47}{53}$ ,  $\frac{59}{59}$ ,  $61$ ,  $67$ ,  $\frac{71}{73}$ ,  $\frac{79}{79}$ ,  $\frac{83}{89}$ ,  $\frac{89}{97}$ .

### binary search

$$\frac{2}{5}$$
,  $\frac{5}{5}$ ,  $\frac{7}{7}$ ,  $\frac{11}{13}$ ,  $\frac{17}{17}$ ,  $\frac{19}{19}$ ,  $\frac{23}{29}$ ,  $\frac{29}{31}$ ,  $\frac{37}{37}$ ,  $\frac{41}{43}$ ,  $\frac{47}{53}$ ,  $\frac{59}{59}$ ,  $\frac{61}{67}$ ,  $\frac{67}{71}$ ,  $\frac{73}{79}$ ,  $\frac{83}{89}$ ,  $\frac{89}{97}$ .

### 3 splits → much better

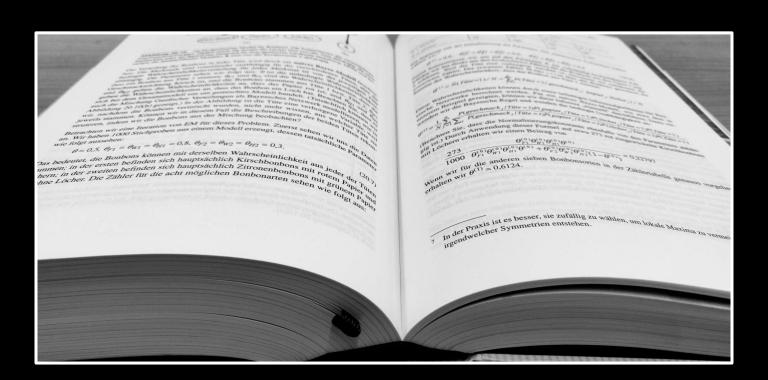
$$\frac{2}{5}$$
,  $\frac{5}{5}$ ,  $\frac{7}{7}$ ,  $\frac{11}{13}$ ,  $\frac{17}{17}$ ,  $\frac{19}{19}$ ,  $\frac{23}{29}$ ,  $\frac{29}{31}$ ,  $\frac{37}{37}$ ,  $\frac{41}{43}$ ,  $\frac{47}{53}$ ,  $\frac{59}{59}$ ,  $\frac{61}{67}$ ,  $\frac{67}{71}$ ,  $\frac{73}{79}$ ,  $\frac{83}{89}$ ,  $\frac{89}{97}$ .



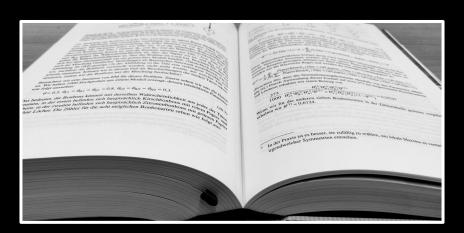
# how efficient are linear and binary search in general?

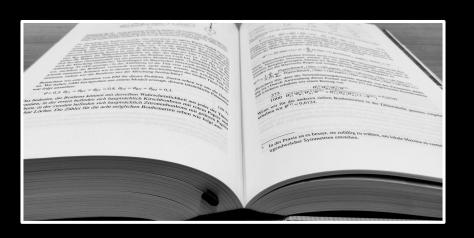


### how many words are in the book?

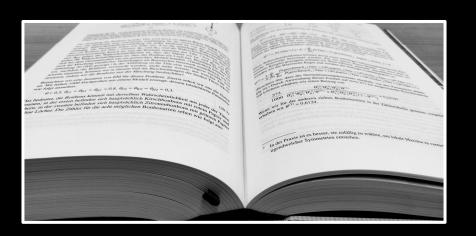


strategies, anyone?

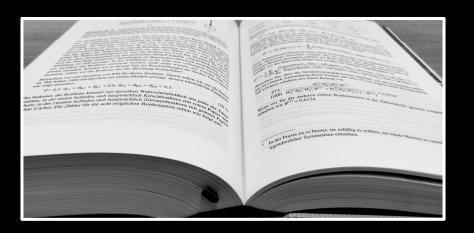


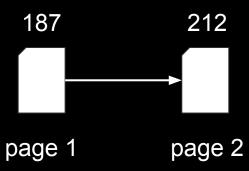


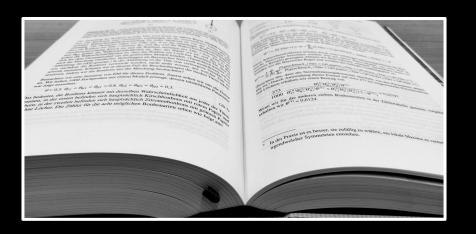
page 1

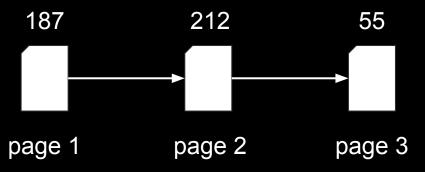


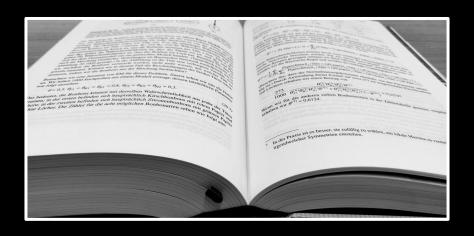


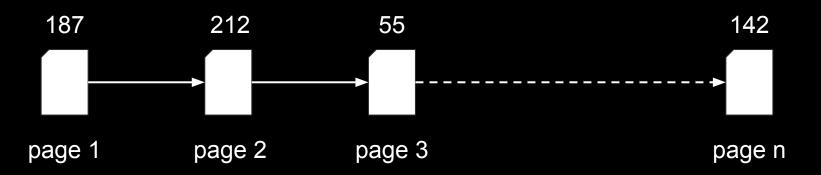


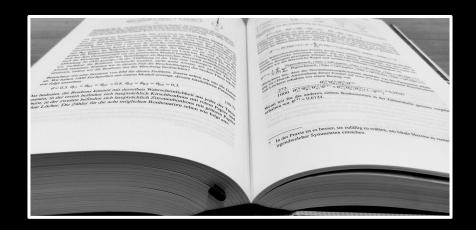














n = 1327 pages

Ø 2:23 minutes per page

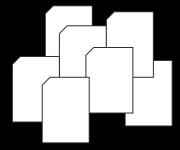
~ 52.34 hours

## divide and conquer

+

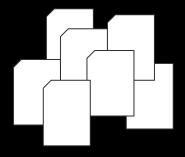
?

pages 1 - 700

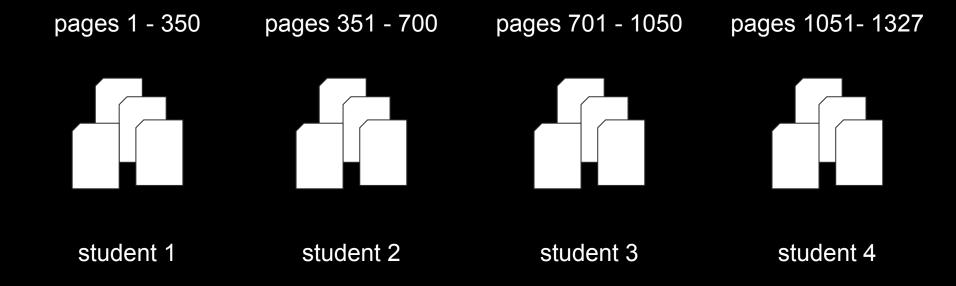


student 1

pages 701 - 1327



student 2



divide and conquer

 $\pm$ 

distribution and parallelization

