

AI Assignment 3:

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Question 1:

Question (a) $P(b|a) = 0.09091$ $P(-b|a) = 0.90909$

Question (b) $P(c|a) = 0.09091$ $P(-c|a) = 0.90909$

Question (c) $P(c|a,-e) = 0.11765$ $P(-c|a,-e) = 0.88235$

Question (d) $P(c|a,-f) = 0.09091$ $P(-c|a,-f) = 0.90909$

Question 2:

(1) Conditional Independence: knowing the state of Starter System makes the state of Starter Motor irrelevant to the probability of Car cranks.

$P(\text{Car cranks} = \text{true} | \text{Starter System} = \text{okay}, \text{Starter Motor} = \text{okay}) = P(\text{Car cranks} = \text{true} | \text{Starter System} = \text{okay}, \text{Starter Motor} = \text{faulty}) = 80.0$

$P(\text{Car cranks} = \text{false} | \text{Starter System} = \text{okay}, \text{Starter Motor} = \text{okay}) = P(\text{Car cranks} = \text{false} | \text{Starter System} = \text{okay}, \text{Starter Motor} = \text{faulty}) = 20.0$

$P(\text{Car cranks} = \text{true} | \text{Starter System} = \text{faulty}, \text{Starter Motor} = \text{okay}) = P(\text{Car cranks} = \text{true} | \text{Starter System} = \text{faulty}, \text{Starter Motor} = \text{faulty}) = 5.0$

$P(\text{Car cranks} = \text{false} | \text{Starter System} = \text{faulty}, \text{Starter Motor} = \text{okay}) = P(\text{Car cranks} = \text{false} | \text{Starter System} = \text{faulty}, \text{Starter Motor} = \text{faulty}) = 95.0$

(2) Knowing Starter System = okay increases the probability that Battery voltage = strong, Starter Motor = okay, and Main fuse = okay

$P(\text{Battery voltage} = \text{strong}) = 41.1$

$P(\text{Battery voltage} = \text{strong} | \text{Starter System} = \text{okay}) = 66.7$

$P(\text{Starter Motor} = \text{okay}) = 99.5$

$P(\text{Starter Motor} = \text{okay} | \text{Starter System} = \text{okay}) = 100.0$

$P(\text{Main fuse} = \text{okay}) = 99.0$

$P(\text{Main fuse} = \text{okay} | \text{Starter System} = \text{okay}) = 100.0$

Knowing Starter Motor = faulty explains away the probability of Battery Voltage indicating Starter System.

$P(\text{Starter system} = \text{okay} | \text{Battery Voltage} = \text{strong}) = 96.5$

$P(\text{Starter system} = \text{okay} | \text{Battery Voltage} = \text{strong}, \text{Starter Motor} = \text{faulty}) = 2.0$

(3) Sequence of accumulated evidence items Fuel System = okay, Car Cranks = true, Air System = okay increases the probability that Car Starts = true.

$$P(\text{Car Starts} = \text{true}) = 28$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}) = 30.9$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}, \text{Car Cranks} = \text{true}) = 62.2$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}, \text{Car Cranks} = \text{true}, \text{Air System} = \text{okay}) = 64.0$$

(4) Sequence of accumulated evidence items Fuel System = okay, Spark Timing = bad, Spark Quality = good causes the probability that Car Starts = true to increase and decrease.

$$P(\text{Car Starts} = \text{true}) = 28$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}) = 30.9$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}, \text{Spark Timing} = \text{bad}) = 29.2$$

$$P(\text{Car starts} = \text{true} \mid \text{Fuel System} = \text{okay}, \text{Spark Timing} = \text{bad}, \text{Spark Quality} = \text{good}) = 73.7$$