

**Problem 15.** Show that Theorem 2.36 and its Corolary become false (in  $\mathbb{R}$ , for example) if the word "compact" is replaced by "closed" or "bounded."

*Proof.* Bruh □

**Problem 16.** Regard  $\mathbb{Q}$ , the set of all rational numbers, as a metric space, with  $d(p, q) = |p - q|$ . let  $E$  be the set of all  $p \in \mathbb{Q}$  such that  $2 < p^2 < 3$ . Show that  $E$  is closed and bounded in  $\mathbb{Q}$ , but that  $E$  is not compact. Is  $E$  open in  $\mathbb{Q}$ .