CS 4240 Phase 1

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The lexer/parser is run by compiling all the Java files and running the General.Runner class. The program takes in one argument for the tiger file, which must have a .tiger extension. The program outputs two files programname.tokens and programname.tokens.err, the first is a list of tokens. The second is any error output if it exists.

1 Lexical Rules

Pre-parse the input to remove comments with the following DFA. The resulting NOT-COMMENT tokens are concatenated together.

Everything under the token column represents either generated tokens or custom table actions on the character buffer used to produce the text associated with tokens.

start state	symbol	next state	token
START	$\Sigma - \{/, "\}$	START	NOT-COMMENT
START	"	STRING	
START	/	SLASH	
STRING	$\Sigma - \{\setminus, "\}$	STRING	
STRING	\	STRING-SLASH	
STRING	"	START	NOT-COMMENT
STRING-SLASH	Σ	STRING	
SLASH	$\Sigma - \{*\}$	START	NOT-COMMENT
SLASH	*	COMMENT	
COMMENT	$\Sigma - \{*\}$	COMMENT	
COMMENT	*	COMMENT-END	
COMMENT-END	$\Sigma - \{*,/\}$	COMMENT	
COMMENT-END	*	COMMENT-END	
COMMENT-END	/	START	COMMENT

The DFA for uncommented code.

Note, any time backtracking is mentioned, it essentially is the same as treating the current state as the start state and doing the corresponding transitions or token generations. This is included to simplify the table by removing duplication of the start state transitions.

Note, all ids are later matched character by character with keywords to determine if they are keywords.

Note, drop character for the error state means that the last read character is ignored, and the state remains unchanged.

start state	symbol	next state	token
START	+	START	PLUS
START	-	START	MIN

CTA DT	*	START	MULT
START			DIV
START	/	START	
START	= (START	EQ
START		START	LPAREN
START)	START	RPAREN
START	,	START	COMMA
START	&	START	AND
START		START	OR
START		START	LSQUARE
START		START	RSQUARE
START	;	START	SEMI
START	(LANGLE	
START)	RANGLE	
START	:	COLON	
START	0-9	INT-LIT	
START	"	STRING-LIT	
START	a-zA-Z	ID	
START	whitespace	START	ignore
START	others	ERROR	drop character
LANGLE	$\Sigma - \{=, \rangle\}$	START	LESS, backtrack
LANGLE	>	START	NOTEQ
LANGLE	=	START	LESSEQ
RANGLE	$\Sigma - \{=\}$	START	GREATER, backtrack
RANGLE	=	START	GREATEREQ
COLON	=	START	ASSIGN
COLON	$\Sigma - \{=\}$	START	COLON, backtrack
INT-LIT	0-9	INT-LIT	, in the second
INT-LIT	$\Sigma - 0 - 9$	START	INT-LIT, backtrack
ID	a-zA-Z0-9_	ID	,
ID	$\Sigma - a - zA - Z0 - 9$	START	ID, backtrack
STRING-LIT	$\Sigma - \setminus$	STRING-LIT	,
STRING-LIT	"	START	STRING-LIT
STRING-LIT	\	STRING-LIT-SLASH	
STRING-LIT-SLASH	n	STRING-LIT	
STRING-LIT-SLASH	t	STRING-LIT	
STRING-LIT-SLASH	"	STRING-LIT	
STRING-LIT-SLASH	\	STRING-LIT	
STRING-LIT-SLASH	^	STRING-LIT-CTL	
STRING-LIT-SLASH	0-9	STRING-LIT-CODE-1	
STRING-LIT-SLASH	whitespace	STRING-LIT-SPACE	ignore 2 characters
STRING-LIT-SLASH	others	ERROR	drop character
STRING-LIT-CTL	@A-Z[\]^	STRING-LIT	arop enaracee
STRING-LIT-CTL	others	ERROR	drop character
STRING-LIT-CODE-1	0-9	STRING-LIT-CODE-2	drop character
STRING-LIT-CODE-1	others	ERROR	drop character
STRING-LIT-CODE-2	0-9	STRING-LIT	arop character
STRING-LIT-CODE-2	others	ERROR	drop character
STRING-LIT-SPACE	whitespace	STRING-LIT-SPACE	ignore
STRING-LIT-SPACE	\ \	STRING-LIT-STACE STRING-LIT	ignore
STRING-LIT-SPACE	others	ERROR	drop character
DITHING-LII-SFACE	Officia	EILLOIL	drop character

2 Grammar Rules

Given the raw grammar for the Tiger Language, provided in the Tiger Language Reference Manual, and shown below, we have generated a new grammar, by modifying it in order to ensure that it is not ambiguous, by enforcing operator precedences and left associativity, and to ensure that the grammar supports LL(1) parsing, by removing any left recursion and performing left factoring.

symbol	rule
$\langle \text{tiger-program} \rangle$	let (declaration-segment) in (stat-seq) end
$\langle declaration\text{-segment} \rangle$	\langle \text{type-declaration-list} \langle \text{var-declaration-list} \langle \text{funct-declaration-list} \rangle
(type-declaration-list)	(type-declaration) (type-declaration-list)
(type-declaration-list)	NULL
(var-declaration-list)	(var-declaration) (var-declaration-list)
(var-declaration-list)	NULL
(funct-declaration-list)	\langle \text{funct-declaration} \langle \text{funct-declaration-list} \rangle
(funct-declaration-list)	NULL
(type-declaration)	type $id = \langle type \rangle$;
$\langle \text{type} \rangle$	(type-id)
$\langle \text{type} \rangle$	array [INTLIT] (type-dim) of (type-id)
$\langle \text{type-dim} \rangle$	[INTLIT] \(\text{type-dim}\)
$\langle \text{type-dim} \rangle$	NULL
(type-id)	int
$\langle \text{type-id} \rangle$	string
$\langle \text{type-id} \rangle$	id
(var-declaration)	$ \operatorname{var} \langle \operatorname{id-list} \rangle : \langle \operatorname{type-id} \rangle \langle \operatorname{optional-init} \rangle ;$
$\langle id-list \rangle$	id
$\langle id-list \rangle$	id , ⟨id-list⟩
$\langle \text{optional-init} \rangle$	NULL
$\langle \text{optional-init} \rangle$	$:=\langle \text{const} \rangle$
$\langle \text{funct-declaration} \rangle$	function id (\(\param-\list \rangle \) \(\rangle \text{ret-type} \rangle \text{begin \(\stat-\seq \rangle \text{ end } ;} \)
$\langle param-list \rangle$	NULL
$\langle param-list \rangle$	\(\rho\rho\rangle\) \(\rho\rangle\) \(\rho\rangle\) \(\rho\rho\rangle\) \(\rho\rangle\) \(\rho\rho\rho\rho\rho\rho\rho\rho\rho\rho
⟨param-list-tail⟩	NULL
(param-list-tail)	$\langle param \rangle \langle param-list-tail \rangle$
⟨ret-type⟩	NULL
⟨ret-type⟩	$: \langle \text{type-id} \rangle$
$\langle param \rangle$	id: ⟨type-id⟩
$\langle \text{stat-seq} \rangle$	$\langle \text{stat} \rangle \langle \text{stat-seq} \rangle$
$\langle \text{stat-seq} \rangle$	$\langle \operatorname{stat} \rangle$
$\langle \text{stat} \rangle$	$\langle \text{lvalue} \rangle := \langle \text{expr} \rangle$;
$\langle \text{stat} \rangle$	$ if\langle \exp \rangle $ then $\langle \operatorname{stat-seq} \rangle$ endif;
$\langle \text{stat} \rangle$	$ \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stat-seq} \rangle \text{ else } \langle \text{stat-seq} \rangle \text{ endif };$
$\langle \text{stat} \rangle$	while $\langle \exp \rangle$ do $\langle \operatorname{stat-seq} \rangle$ enddo;
$\langle \text{stat} \rangle$	for id := $\langle \exp r \rangle$ to $\langle \exp r \rangle$ do $\langle \operatorname{stat-seq} \rangle$ enddo;
$\langle \text{stat} \rangle$	\langle \text{opt-prefix} \text{ id (\langle \text{expr-list}\rangle);
$\langle \text{stat} \rangle$	break;
$\langle \text{stat} \rangle$	return (expr);
$\langle \exp r \rangle$	$\langle \exp r \rangle$ $\langle \exp r \rangle$ $\langle \exp r \rangle$
$\langle \exp r \rangle$	(const)
$\langle \exp r \rangle$	\(\lambda \text{lvalue}\rangle
$\langle \exp r \rangle$	$-\langle \exp r \rangle$
$\langle \exp r \rangle$	$(\langle \exp \rangle)$
(binary-operator)	(\\cxpi /) *
(Sinary Operator)	

```
⟨binary-operator⟩
⟨binary-operator⟩
                                     +
⟨binary-operator⟩
                                     _
⟨binary-operator⟩
                                     =
                                     <
⟨binary-operator⟩
                                     >
⟨binary-operator⟩
(binary-operator)
                                     <=
                                     >=
⟨binary-operator⟩
(binary-operator)
                                     <>
⟨binary-operator⟩
                                     &
⟨binary-operator⟩
⟨binary-operator⟩
                                     :=
⟨opt-prefix⟩
                                     \langle lvalue \rangle :=
                                     NULL
(opt-prefix)
\langle const \rangle
                                     INTLIT
\langle const \rangle
                                     {\bf STRLIT}
\langle const \rangle
                                     nil
                                     \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
\langle \text{expr-list} \rangle
⟨expr-list⟩
                                     NULL
                                     , \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
\langle \text{expr-list-tail} \rangle
⟨expr-list-tail⟩
                                     NULL
                                     id \langle lvalue-tail \rangle
(lvalue)
                                     [\langle \expr \rangle] \langle \text{lvalue-tail} \rangle
(lvalue-tail)
⟨lvalue-tail⟩
                                     NULL
```

After performing the grammar's modifications, we came to the following grammar.

symbol	rule
$\langle \text{tiger-program} \rangle$	let (declaration-segment) in (stat-seq) end
(declaration-segment)	\langle type-declaration-list \rangle \langle var-declaration-list \rangle \langle funct-declaration-list \rangle
(type-declaration-list)	$\langle \text{type-declaration} \rangle \langle \text{type-declaration-list} \rangle$
$\langle \text{type-declaration-list} \rangle$	NULL
$\langle var\text{-declaration-list} \rangle$	$\langle \text{var-declaration} \rangle \langle \text{var-declaration-list} \rangle$
$\langle var\text{-declaration-list} \rangle$	NULL
$\langle \text{funct-declaration-list} \rangle$	$\langle \text{funct-declaration} \rangle \langle \text{funct-declaration-list} \rangle$
$\langle \text{funct-declaration-list} \rangle$	NULL
$\langle \text{type-declaration} \rangle$	type $id = \langle type \rangle$;
$\langle var\text{-declaration} \rangle$	$ \text{var } \langle \text{id-list} \rangle : \langle \text{type-id} \rangle \langle \text{optional-init} \rangle ;$
$\langle \text{funct-declaration} \rangle$	function id ($\langle param-list \rangle$) $\langle ret-type \rangle$ begin $\langle stat-seq \rangle$ end;
$\langle \mathrm{type} \rangle$	$\langle ext{type-id} \rangle$
$\langle \mathrm{type} \rangle$	array [INTLIT] (type-dim) of (type-id)
$\langle \mathrm{type\text{-}dim} \rangle$	$[INTLIT] \langle type-dim \rangle$
$\langle \mathrm{type\text{-}dim} \rangle$	NULL
$\langle \mathrm{type\text{-}id} \rangle$	id
$\langle id\text{-list} \rangle$	id (id-list-tail)
$\langle id$ -list-tail \rangle	$, id \langle id\text{-list-tail} \rangle $
$\langle id$ -list-tail \rangle	NULL
$\langle { m optional\text{-}init} \rangle$	$:=\langle \mathrm{const} \rangle$
$\langle { m optional\text{-}init} \rangle$	NULL
$\langle param-list \rangle$	$\langle param \rangle \langle param-list-tail \rangle$
$\langle param-list \rangle$	NULL
$\langle param-list-tail \rangle$	$, \langle param \rangle \langle param-list-tail \rangle$
$\langle param-list-tail \rangle$	NULL

```
⟨ret-type⟩
                                     : \langle \text{type-id} \rangle
⟨ret-type⟩
                                     NULL
                                    \mathrm{id}:\,\langle\mathrm{type\text{-}id}\rangle
(param)
                                     ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
⟨stat-seq-tail⟩
                                     ⟨stat⟩ ⟨stat-seq-tail⟩
                                     NULL
⟨stat-seq-tail⟩
\langle stat \rangle
                                     if \langle \exp r \rangle then \langle \text{stat-seq} \rangle \langle \text{stat-if-tail} \rangle
\langle stat \rangle
                                     while \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
                                     for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo ;
\langle stat \rangle
\langle stat \rangle
                                     break;
                                     return \langle \exp r \rangle:
(stat)
                                     id (stat-func-or-assign)
\langle stat \rangle
⟨stat-func-or-assign⟩
                                     (\langle expr-list \rangle);
⟨stat-func-or-assign⟩
                                     \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle ;
⟨stat-if-tail⟩
                                     else (stat-seq) endif;
⟨stat-if-tail⟩
                                     endif;
                                     - (unaryminus) (stat-assign-tail)
(stat-assign)
(stat-assign)
                                     (\langle \exp r \rangle) \langle \operatorname{stat-assign-tail} \rangle
                                     ⟨const⟩ ⟨stat-assign-tail⟩
⟨stat-assign⟩
⟨stat-assign⟩
                                     id (stat-assign-id)
                                     (\langle expr-list \rangle)
⟨stat-assign-id⟩
                                     (lvalue-tail) (stat-assign-tail)
⟨stat-assign-id⟩
⟨stat-assign-tail⟩
                                     ⟨expr-tail⟩
(stat-assign-tail)
                                     (orexpr-tail)
⟨stat-assign-tail⟩
                                     (andexpr-tail)
⟨stat-assign-tail⟩
                                     (compare-tail)
⟨stat-assign-tail⟩
                                     ⟨term-tail⟩
\langle \exp r \rangle
                                     ⟨orexpr⟩ ⟨expr-tail⟩
⟨expr-tail⟩
                                     ⟨orop⟩ ⟨orexpr⟩ ⟨expr-tail⟩
⟨expr-tail⟩
                                     NULL
\langle orexpr \rangle
                                     (andexpr) (orexpr-tail)
                                     ⟨andop⟩ ⟨andexpr⟩ ⟨orexpr-tail⟩
(orexpr-tail)
(orexpr-tail)
                                     NULL
\langle andexpr \rangle
                                     ⟨compare⟩ ⟨andexpr-tail⟩
                                     ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
⟨andexpr-tail⟩
                                     NULL
\langle compare \rangle
                                     ⟨term⟩ ⟨compare-tail⟩
                                     ⟨addop⟩ ⟨term⟩ ⟨compare-tail⟩
⟨compare-tail⟩
                                     NULL
(compare-tail)
\langle \text{term} \rangle
                                     ⟨factor⟩ ⟨term-tail⟩
⟨term-tail⟩
                                     \langle mulop \langle \factor \langle \term-tail \rangle
⟨term-tail⟩
                                     NULL
(factor)
                                     (unaryminus)
\langle factor \rangle
                                     - (unaryminus)
⟨unaryminus⟩
                                     (\langle \exp r \rangle)
(unaryminus)
                                     \langle const \rangle
⟨unaryminus⟩
                                     (lvalue)
                                     INTLIT
\langle const \rangle
\langle const \rangle
                                     STRLIT
\langle const \rangle
                                     nil
\langle \text{orop} \rangle
                                     \&
\langle andop \rangle
\langle compop \rangle
                                     =
```

```
\langle compop \rangle
                                                           <>
\langle compop \rangle
                                                          >
                                                           <
\langle compop \rangle
                                                          >=
\langle compop \rangle
\langle compop \rangle
                                                           <=
                                                          +
\langle addop \rangle
\langle addop \rangle
                                                          -
*
\langle \text{mulop} \rangle
\langle \text{mulop} \rangle
\langle \text{expr-list} \rangle
                                                          \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
\langle \text{expr-list} \rangle
                                                          NULL
                                                          , \langle \exp r \rangle \langle \exp r-list-tail\rangle
\langle \text{expr-list-tail} \rangle
\langle \text{expr-list-tail} \rangle
                                                          NULL
                                                         id (lvalue-tail)
\langle lvalue \rangle
                                                          [\langle \expr \rangle] \langle \text{lvalue-tail} \rangle
\langle lvalue-tail \rangle
\langle lvalue-tail \rangle
                                                          NULL
```

After ensuring that the new grammar meets all the requirements, the first and follow sets were generated for every non-terminal symbol of the grammar.

non-terminal	first set
$\langle \text{lvalue-tail} \rangle$	$[,\epsilon$
$\langle lvalue \rangle$	id
$\langle \text{expr-list-tail} \rangle$	$ \; ,, \; \epsilon $
$\langle \text{expr-list} \rangle$	(, nil, STRLIT, INTLIT, id, -, ϵ
$\langle \mathrm{mulop} \rangle$	*, /
$\langle \mathrm{addop} \rangle$	+, -
$\langle \mathrm{compop} \rangle$	=,<,>,<=,>=,<>
$\langle andop \rangle$	&
$\langle \mathrm{orop} angle$	
$\langle \mathrm{const} \rangle$	nil, STRLIT, INTLIT
$\langle { m unaryminus} \rangle$	(, nil, STRLIT, INTLIT, id
$\langle factor \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle \text{term-tail} \rangle$	$ *,/,\epsilon $
$\langle \mathrm{term} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle { m compare-tail} \rangle$	$+,-,\epsilon$
$\langle \mathrm{compare} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle and expr-tail \rangle$	$ =, <, >, <=, >=, <>, \epsilon$
$\langle and expr \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle \mathrm{orexpr} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle { m or expr-tail} angle$	$\mid \& \;, \epsilon$
$\langle \mathrm{expr} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle ext{expr-tail} \rangle$	$\mid \mid, \epsilon$
$\langle \text{stat-assign} \rangle$	id, -, (, nil, STRLIT, INTLIT
$\langle \text{stat-assign-id} \rangle$	$ [, (, *, /, +, -, =, <, >, <=, >=, <>, \&, , \epsilon]$
$\langle \text{stat-assign-tail} \rangle$	*, / , +, -, =, <, >, <=, >=, <>, & , , \epsilon
$\langle { m stat} ext{-if-tail} angle$	else, endif
$\langle \text{stat-func-or-assign} \rangle$	$\mid (,:=,[$
$\langle \mathrm{stat} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq-tail} \rangle$	if, while, for, break, return, id, ϵ
$\langle \mathrm{param} \rangle$	id
$\langle \text{ret-type} \rangle$	$:,\epsilon $

```
⟨param-list-tail⟩
                                        ,,~\epsilon
⟨param-list⟩
                                       id, \epsilon
\langle optional-init \rangle
                                       :=, \epsilon
\langle id-list-tail\rangle
                                       ,,\;\epsilon
\langle id-list \rangle
                                       id
\langle \text{type-id} \rangle
                                       id
\langle \text{type-dim} \rangle
                                        [, \epsilon]
⟨type⟩
                                       array, id
\( \) funct-declaration \( \)
                                       function
⟨var-declaration⟩
                                       var
⟨type-declaration⟩
                                        type
\langle funct-declaration-list \rangle
                                       function, \epsilon
\langle var-declaration-list \rangle
                                       var, \epsilon
⟨type-declaration-list⟩
                                       type, \epsilon
(declaration-segment)
                                       function, var, type, \epsilon
⟨tiger-program⟩
                                       let
```

non-terminal	follow set
$\langle \text{lvalue-tail} \rangle$:=, *, / , +, -, =, <, >, <=, >=, <>, & ,
$\langle lvalue-tail \rangle$,), ,, ,], then, do, to, ;
$\langle \text{expr-list-tail} \rangle$	
$\langle \text{expr-list} \rangle$	
$\langle \text{expr-tail} \rangle$), ,, ,], then, do, to, ;
$\langle \text{or expr-tail} \rangle$	[,), ,, ,], then, do, to, ;
$\langle { m andexpr-tail} \rangle$	& , ,), ,,], then, do, to, ;
$\langle \text{compare-tail} \rangle$	& , ,), ,,], then, do, to, ;, =, <, >, <=, >=, <>
$\langle ext{term-tail} \rangle$	[&, ,), .,], then, do, to, ;, =, <, >, <=, >=, <>, +, -
$\langle \text{term-tail} \rangle$	
$\langle \text{stat-assign-tail} \rangle$;
$\langle stat-assign-id \rangle$;
$\langle \text{stat-seq-tail} \rangle$	endif, end, enddo, else
$\langle { m ret-type} \rangle$	begin
$\langle param-list-tail \rangle$	
$\langle param-list \rangle$	
$\langle { m optional\text{-}init} angle$;
$\langle id$ -list-tail \rangle	:
$\langle \mathrm{type\text{-}dim} \rangle$	of
$\langle \text{funct-declaration-list} \rangle$	in
$\langle var-declaration-list \rangle$	function, in
$\langle \text{type-declaration-list} \rangle$	var, function, in
$\langle declaration\text{-segment} \rangle$	in

At last, the LL(1) parser table for Tiger was generated, as shown below.

Note that if there is no corresponding rule, then that means a parser error is generated. Also note that errors are handled by dropping tokens until a valid token is found.

symbol	next token	rule
$\langle addop \rangle$	+	+
$\langle \mathrm{addop} \rangle$	-	-
$\langle and expr \rangle$	($\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	nil	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	STRLIT	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$

```
\langle andexpr \rangle
                                                                 INTLIT
                                                                                                   ⟨compare⟩ ⟨andexpr-tail⟩
\langle andexpr \rangle
                                                                 id
                                                                                                   ⟨compare⟩ ⟨andexpr-tail⟩
\langle andexpr \rangle
                                                                                                   ⟨compare⟩ ⟨andexpr-tail⟩
                                                                 _
(andexpr-tail)
                                                                 =
                                                                                                   ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
                                                                 <
                                                                                                   ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
                                                                 >
(andexpr-tail)
                                                                                                   ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
                                                                 >=
                                                                                                   ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
                                                                                                   ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
                                                                 <=
                                                                                                   \langle compop \rangle \langle compare \rangle \langle and expr-tail \rangle
(andexpr-tail)
                                                                 <>
(andexpr-tail)
                                                                 &
                                                                                                   \epsilon
(andexpr-tail)
                                                                                                   \epsilon
(andexpr-tail)
                                                                 )
                                                                                                   \epsilon
(andexpr-tail)
                                                                                                   \epsilon
(andexpr-tail)
                                                                                                   \epsilon
(andexpr-tail)
                                                                 then
                                                                                                   \epsilon
(andexpr-tail)
                                                                 do
                                                                                                   \epsilon
(andexpr-tail)
                                                                 to
                                                                                                   \epsilon
(andexpr-tail)
                                                                                                   \epsilon
                                                                 &
                                                                                                   &
\langle andop \rangle
\langle compare \rangle
                                                                 (
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
(compare)
                                                                 nil
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
\langle compare \rangle
                                                                 STRLIT
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
\langle compare \rangle
                                                                 INTLIT
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
\langle compare \rangle
                                                                 id
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
                                                                                                   ⟨term⟩ ⟨compare-tail⟩
\langle compare \rangle
(compare-tail)
                                                                 +
                                                                                                   ⟨addop⟩ ⟨term⟩ ⟨compare-tail⟩
                                                                                                   ⟨addop⟩ ⟨term⟩ ⟨compare-tail⟩
(compare-tail)
                                                                 &
(compare-tail)
                                                                                                   \epsilon
⟨compare-tail⟩
                                                                                                   \epsilon
                                                                 )
(compare-tail)
                                                                                                   \epsilon
(compare-tail)
                                                                                                   \epsilon
(compare-tail)
                                                                                                   \epsilon
(compare-tail)
                                                                 then
                                                                                                   \epsilon
(compare-tail)
                                                                 do
                                                                                                   \epsilon
(compare-tail)
                                                                 to
                                                                                                   \epsilon
(compare-tail)
                                                                                                   \epsilon
(compare-tail)
                                                                 =
                                                                                                   \epsilon
                                                                 <
(compare-tail)
                                                                                                   \epsilon
                                                                 >
(compare-tail)
                                                                                                   \epsilon
(compare-tail)
                                                                 <=
                                                                                                   \epsilon
(compare-tail)
                                                                 >=
                                                                                                   \epsilon
(compare-tail)
                                                                 <>
                                                                                                   \epsilon
\langle compop \rangle
                                                                 =
                                                                                                   =
\langle compop \rangle
                                                                 <
                                                                                                   <
                                                                 >
                                                                                                   >
\langle compop \rangle
\langle compop \rangle
                                                                 \leq =
                                                                                                   <=
\langle compop \rangle
                                                                 >=
                                                                                                   >=
                                                                 <>
                                                                                                   <>
\langle compop \rangle
\langle const \rangle
                                                                 nil
                                                                                                   nil
\langle const \rangle
                                                                 STRLIT
                                                                                                   STRLIT
\langle const \rangle
                                                                 INTLIT
                                                                                                   INTLIT
(declaration-segment)
                                                                 function
                                                                                                   \langle type-declaration-list \rangle \langle var-declaration-list \rangle \langle funct-declaration-list \rangle \langle \text{funct-declaration-list} \rangle \text{funct-declaration-
(declaration-segment)
                                                                                                   ⟨type-declaration-list⟩ ⟨var-declaration-list⟩ ⟨funct-declaration-list⟩
                                                                 var
```

```
(declaration-segment)
                                     type
                                                         \(\lambda\) type-declaration-list\(\rangle\) \(\lambda\) ar-declaration-list\(\rangle\) \(\lambda\) funct-declaration-list\(\rangle\)
(declaration-segment)
                                     in
⟨expr-list⟩
                                     )
⟨expr-list⟩
                                     (
                                                         ⟨expr⟩ ⟨expr-list-tail⟩
(expr-list)
                                     nil
                                                         ⟨expr⟩ ⟨expr-list-tail⟩
                                     STRLIT
                                                         ⟨expr⟩ ⟨expr-list-tail⟩
(expr-list)
(expr-list)
                                     INTLIT
                                                         ⟨expr⟩ ⟨expr-list-tail⟩
⟨expr-list⟩
                                                         ⟨expr⟩ ⟨expr-list-tail⟩
                                     id
                                                         \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
⟨expr-list⟩
                                     )
⟨expr-list-tail⟩
                                                         , \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
⟨expr-list-tail⟩
                                     (
                                                         ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                     nil
                                                         (orexpr) (expr-tail)
                                     STRLIT
                                                         ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
                                     INTLIT
                                                         ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                     id
                                                         ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
                                                         ⟨orexpr⟩ ⟨expr-tail⟩
                                     )
(expr-tail)
⟨expr-tail⟩
                                                         \epsilon
(expr-tail)
                                                         \epsilon
(expr-tail)
                                     then
                                                         \epsilon
(expr-tail)
                                     do
                                                         \epsilon
⟨expr-tail⟩
                                     to
                                                         \epsilon
⟨expr-tail⟩
\langle factor \rangle
                                     (
                                                         ⟨unaryminus⟩
(factor)
                                     nil
                                                         (unaryminus)
                                     STRLIT
                                                         ⟨unaryminus⟩
(factor)
                                     INTLIT
                                                         ⟨unaryminus⟩
(factor)
(factor)
                                     id
                                                         ⟨unaryminus⟩
(factor)
                                                         - (unaryminus)
(funct-declaration)
                                     function
                                                         function id ( \( \rangle \text{param-list} \rangle ) \( \rangle \text{ret-type} \rangle \text{ begin } \( \stat-\text{seq} \rangle \text{ end} \);
                                                         \( \) funct-declaration \( \) \( \) \( \) \( \) \( \) \( \) declaration-list \( \) \( \)
(funct-declaration-list)
                                     function
⟨funct-declaration-list⟩
                                     in
⟨id-list⟩
                                     id
                                                         id (id-list-tail)
(id-list-tail)
                                     :
⟨id-list-tail⟩
                                                         , id (id-list-tail)
                                     id
                                                         id (lvalue-tail)
(lvalue)
(lvalue-tail)
                                                         [ ⟨expr⟩ ] ⟨lvalue-tail⟩
(lvalue-tail)
                                     :=
                                                         \epsilon
                                     *
(lvalue-tail)
                                                         \epsilon
(lvalue-tail)
                                                         \epsilon
(lvalue-tail)
                                     +
                                                         \epsilon
(lvalue-tail)
                                                         \epsilon
(lvalue-tail)
                                     =
                                                         \epsilon
(lvalue-tail)
                                     <
                                                         \epsilon
(lvalue-tail)
                                     >
                                                         \epsilon
(lvalue-tail)
                                     <=
                                                         \epsilon
(lvalue-tail)
                                     >=
                                                         \epsilon
(lvalue-tail)
                                     <>
                                                         \epsilon
(lvalue-tail)
                                     &
                                                         \epsilon
(lvalue-tail)
                                                         \epsilon
(lvalue-tail)
                                     )
                                                         \epsilon
(lvalue-tail)
                                                         \epsilon
```

```
(lvalue-tail)
                                                 \epsilon
(lvalue-tail)
                                then
                                                 \epsilon
(lvalue-tail)
                                do
                                                 \epsilon
(lvalue-tail)
                                to
                                                 \epsilon
(lvalue-tail)
                                                 \epsilon
(mulop)
\langle \text{mulop} \rangle
⟨optional-init⟩
                                :=
                                                 := \langle const \rangle
(optional-init)
\langle orexpr \rangle
                                (
                                                 ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                nil
                                                 (andexpr) (orexpr-tail)
                                STRLIT
                                                 ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
\langle orexpr \rangle
                                INTLIT
                                                 (andexpr) (orexpr-tail)
                                id
                                                 ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                                 ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                &
                                                 (andop) (andexpr) (orexpr-tail)
(orexpr-tail)
(orexpr-tail)
(orexpr-tail)
                                )
                                                 \epsilon
(orexpr-tail)
                                                 \epsilon
(orexpr-tail)
                                                 \epsilon
(orexpr-tail)
                                then
                                                 \epsilon
(orexpr-tail)
                                do
                                                 \epsilon
(orexpr-tail)
                                to
                                                 \epsilon
(orexpr-tail)
                                                 \epsilon
\langle \text{orop} \rangle
(param)
                                id
                                                 id: \langle type-id \rangle
⟨param-list⟩
                                )
                                id
                                                 ⟨param⟩ ⟨param-list-tail⟩
(param-list)
⟨param-list-tail⟩
                                )
                                                   ⟨param⟩ ⟨param-list-tail⟩
(param-list-tail)
⟨ret-type⟩
                                begin
                                                 : \langle type-id \rangle
(ret-type)
                                id
                                                 id (stat-assign-id)
(stat-assign)
                                                 - (unaryminus) (stat-assign-tail)
(stat-assign)
                                (
                                                 (\langle \exp r \rangle) \langle \operatorname{stat-assign-tail} \rangle
(stat-assign)
(stat-assign)
                                nil
                                                 ⟨const⟩ ⟨stat-assign-tail⟩
(stat-assign)
                                STRLIT
                                                 ⟨const⟩ ⟨stat-assign-tail⟩
                                INTLIT
(stat-assign)
                                                 ⟨const⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
(stat-assign-id)
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                &
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                <>
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                >=
(stat-assign-id)
                                \leq =
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                                >
(stat-assign-id)
                                <
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                                =
(stat-assign-id)
                                                 (lvalue-tail) (stat-assign-tail)
                                                 ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                +
(stat-assign-id)
                                /
*
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                                 (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                                 (\langle expr-list \rangle)
```

```
(stat-assign-tail)
(stat-assign-tail)
                                                        ⟨expr-tail⟩
                                    &
(stat-assign-tail)
                                                        (orexpr-tail)
                                     <>
(stat-assign-tail)
                                                        (andexpr-tail)
(stat-assign-tail)
                                    >=
                                                        (andexpr-tail)
(stat-assign-tail)
                                    <=
                                                        (andexpr-tail)
(stat-assign-tail)
                                                        (andexpr-tail)
                                    >
(stat-assign-tail)
                                     <
                                                        (andexpr-tail)
(stat-assign-tail)
                                    =
                                                        (andexpr-tail)
(stat-assign-tail)
                                                        (compare-tail)
(stat-assign-tail)
                                    +
                                                        (compare-tail)
(stat-assign-tail)
                                                        ⟨term-tail⟩
(stat-assign-tail)
                                                        ⟨term-tail⟩
⟨stat-func-or-assign⟩
                                    (
                                                        (\langle \text{expr-list} \rangle);
⟨stat-func-or-assign⟩
                                                        \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle;
                                    :=
⟨stat-func-or-assign⟩
                                                        \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle;
⟨stat-if-tail⟩
                                    else
                                                        else (stat-seq) endif;
⟨stat-if-tail⟩
                                    endif
                                                        endif;
                                    if
                                                        if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle \langle \operatorname{stat-if-tail} \rangle
(stat)
⟨stat⟩
                                    while
                                                        while \langle \exp r \rangle do \langle \text{stat-seg} \rangle enddo;
⟨stat⟩
                                    for
                                                        for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \operatorname{stat-seg} \rangle enddo;
⟨stat⟩
                                    break
                                                        break:
\langle stat \rangle
                                    return
                                                        return \langle \exp r \rangle;
\langle stat \rangle
                                    id
                                                        id (stat-func-or-assign)
                                    if
\langle \text{stat-seq} \rangle
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
                                    while
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
                                    for
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
                                    break
                                                        (stat) (stat-seq-tail)
⟨stat-seq⟩
                                    return
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
                                    id
                                                        (stat) (stat-seq-tail)
(stat-seq-tail)
                                    endif
                                                        \epsilon
(stat-seq-tail)
                                    end
                                                        \epsilon
                                    enddo
(stat-seq-tail)
                                                        \epsilon
                                    else
(stat-seq-tail)
                                    if
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
(stat-seq-tail)
                                    while
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                    for
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                    break
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                    return
                                    id
(stat-seq-tail)
                                                        ⟨stat⟩ ⟨stat-seq-tail⟩
\langle \text{term} \rangle
                                                        ⟨factor⟩ ⟨term-tail⟩
                                    id
                                                        ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
                                    INTLIT
⟨term⟩
                                                        (factor) (term-tail)
\langle \text{term} \rangle
                                    STRLIT
                                                        ⟨factor⟩ ⟨term-tail⟩
                                                        ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
                                    nil
\langle \text{term} \rangle
                                    (
                                                        (factor) (term-tail)
⟨term-tail⟩
                                                        \langle mulop \langle \factor \rangle \text{\term-tail} \rangle
                                                        \langle mulop \langle \factor \rangle \text{\term-tail} \rangle
⟨term-tail⟩
⟨term-tail⟩
                                                        \epsilon
\langle \text{term-tail} \rangle
                                                        \epsilon
                                    &
⟨term-tail⟩
                                                        \epsilon
\langle \text{term-tail} \rangle
                                                        \epsilon
                                    +
⟨term-tail⟩
                                                        \epsilon
```

```
⟨term-tail⟩
                                <>
                                                 \epsilon
⟨term-tail⟩
                                >=
                                                 \epsilon
⟨term-tail⟩
                                \leq =
                                                 \epsilon
⟨term-tail⟩
                                >
                                                 \epsilon
⟨term-tail⟩
                                <
                                                 \epsilon
⟨term-tail⟩
                                                 \epsilon
⟨term-tail⟩
                                                 \epsilon
⟨term-tail⟩
                                to
                                                 \epsilon
⟨term-tail⟩
                                do
                                                 \epsilon
⟨term-tail⟩
                                then
                                                 \epsilon
⟨term-tail⟩
                                                 \epsilon
⟨term-tail⟩
                                let
⟨tiger-program⟩
                                                 let (declaration-segment) in (stat-seq) end
                                                 array [ INTLIT ] \langle \text{type-dim} \rangle of \langle \text{type-id} \rangle
(type)
                                array
(type)
                                id
                                                 ⟨type-id⟩
⟨type-declaration-list⟩
                                type
                                                 ⟨type-declaration⟩ ⟨type-declaration-list⟩
⟨type-declaration-list⟩
                                var
⟨type-declaration-list⟩
                                function
⟨type-declaration-list⟩
                                in
(type-declaration)
                                                 type id = \langle type \rangle;
                                type
⟨type-dim⟩
                                                 [ INTLIT ] (type-dim)
⟨type-dim⟩
                                of
\langle \text{type-id} \rangle
                                id
                                                 id
(unaryminus)
                                                 (\langle \exp r \rangle)
                                (
(unaryminus)
                                nil
                                                 \langle const \rangle
                                STRLIT
(unaryminus)
                                                 \langle const \rangle
⟨unaryminus⟩
                                INTLIT
                                                 \langle const \rangle
(unaryminus)
                                id
                                                 (lvalue)
(var-declaration-list)
                                function
(var-declaration-list)
                                in
(var-declaration-list)
                                var
                                                 ⟨var-declaration⟩ ⟨var-declaration-list⟩
(var-declaration)
                                                 var (id-list) : (type-id) (optional-init);
                                var
```