CS 4240 Phase 1

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1 Lexical Rules

Pre-parse the input to remove comments with the following DFA. The resulting NOT-COMMENT tokens are concatenated together.

Everything under the token column represents either generated tokens or custom table actions on the character buffer used to produce the text associated with tokens.

start state	symbol	next state	token
START	$\Sigma - \{/, "\}$	START	NOT-COMMENT
START	"	STRING	
START	/	SLASH	
STRING	$\Sigma - \{\setminus, "\}$	STRING	
STRING		STRING-SLASH	
STRING	,,	START	NOT-COMMENT
STRING-SLASH	Σ	STRING	
SLASH	$\Sigma - \{*\}$	START	NOT-COMMENT
SLASH	*	COMMENT	
COMMENT	$\Sigma - \{*\}$	COMMENT	
COMMENT	*	COMMENT-END	
COMMENT-END	$\Sigma - \{*,/\}$	COMMENT	
COMMENT-END	*	COMMENT-END	
COMMENT-END	/	START	COMMENT

The DFA for uncommented code.

Note, any time backtracking is mentioned, it essentially is the same as treating the current state as the start state and doing the corresponding transitions or token generations. This is included to simplify the table by removing duplication of the start state transitions.

Note, all ids are later matched character by character with keywords to determine if they are keywords.

Note, drop character for the error state means that the last read character is ignored, and the state remains unchanged.

start state	symbol	next state	token
START	+	START	PLUS
START	-	START	MIN
START	*	START	MULT
START	/	START	DIV
START	=	START	EQ
START		START	LPAREN
START		START	RPAREN
START	,	START	COMMA

START	&	START	AND
START	_	START	OR
START		START	LSQUARE
START		START	RSQUARE
START	:	START	SEMI
START	(LANGLE	
START	\ \ \	RANGLE	
START	:	COLON	
START	0-9	INT-LIT	
START	"	STRING-LIT	
START	a-zA-Z	ID	
START	whitespace	START	ignore
START	others	ERROR	drop character
LANGLE	$\Sigma - \{=, \rangle\}$	START	LESS, backtrack
LANGLE	>	START	NOTEQ
LANGLE	=	START	LESSEQ
RANGLE	$\Sigma - \{=\}$	START	GREATER, backtrack
RANGLE	=	START	GREATEREQ
COLON	=	START	ASSIGN
COLON	$\Sigma - \{=\}$	START	COLON, backtrack
INT-LIT	0-9	INT-LIT	·
INT-LIT	$\Sigma - 0 - 9$	START	INT-LIT, backtrack
ID	a-zA-Z0-9_	ID	·
ID	$\Sigma - a - zA - Z0 - 9$	START	ID, backtrack
STRING-LIT	$\Sigma - \setminus$	STRING-LIT	
STRING-LIT	"	START	STRING-LIT
STRING-LIT	\	STRING-LIT-SLASH	
STRING-LIT-SLASH	n	STRING-LIT	
STRING-LIT-SLASH	t	STRING-LIT	
STRING-LIT-SLASH	"	STRING-LIT	
STRING-LIT-SLASH	\	STRING-LIT	
STRING-LIT-SLASH	^	STRING-LIT-CTL	
STRING-LIT-SLASH	0-9	STRING-LIT-CODE-1	
STRING-LIT-SLASH	whitespace	STRING-LIT-SPACE	ignore 2 characters
STRING-LIT-SLASH	others	ERROR	drop character
STRING-LIT-CTL	@A-Z[\]^	STRING-LIT	
STRING-LIT-CTL	others	ERROR	drop character
STRING-LIT-CODE-1	0-9	STRING-LIT-CODE-2	
STRING-LIT-CODE-1	others	ERROR	drop character
STRING-LIT-CODE-2	0-9	STRING-LIT	
STRING-LIT-CODE-2	others	ERROR	drop character
STRING-LIT-SPACE	whitespace	STRING-LIT-SPACE	ignore
STRING-LIT-SPACE		STRING-LIT	ignore
STRING-LIT-SPACE	others	ERROR	drop character

2 Grammar Rules

Raw Grammar:

symbol	rule
$\overline{\langle \text{tiger-program} \rangle}$	let (declaration-segment) in (stat-seq) end
$\langle declaration\text{-segment} \rangle$	$\langle type\text{-declaration-list}\rangle \ \langle var\text{-declaration-list}\rangle \ \langle funct\text{-declaration-list}\rangle$

```
⟨type-declaration-list⟩
                                         ⟨type-declaration⟩ ⟨type-declaration-list⟩
⟨type-declaration-list⟩
                                         NULL
⟨var-declaration-list⟩
                                         (var-declaration) (var-declaration-list)
⟨var-declaration-list⟩
                                         NULL
(funct-declaration-list)
                                         \(\langle \text{funct-declaration} \rangle \text{funct-declaration-list} \rangle \)
                                         NULL
(funct-declaration-list)
⟨type-declaration⟩
                                         type id = \langle \text{type} \rangle;
\langle type \rangle
                                         ⟨type-id⟩
                                         array [ INTLIT ] of \( \text{type-dim} \) of \( \text{type-id} \)
\langle type \rangle
⟨type-dim⟩
                                         [ INTLIT ] (type-dim)
⟨type-dim⟩
                                         NULL
\langle \text{type-id} \rangle
                                         int
⟨type-id⟩
                                         string
\langle \text{type-id} \rangle
                                         id
(var-declaration)
                                         var (id-list) : (type-id) (optional-init);
\langle id-list \rangle
\langle id-list \rangle
                                         id, \langle id-list \rangle
⟨optional-init⟩
                                         NULL
(optional-init)
                                         := \langle const \rangle
\(\rangle \text{funct-declaration} \rangle \)
                                         function id ( \( \rangle \text{param-list} \rangle ) \( \rangle \text{ret-type} \rangle \text{ begin \( \stat-\text{seq} \rangle \text{ end} \);
(param-list)
                                         NULL
(param-list)
                                         ⟨param⟩ ⟨param-list-tail⟩
⟨param-list-tail⟩
                                         NULL
                                         , (param) (param-list-tail)
⟨param-list-tail⟩
                                         NULL
⟨ret-type⟩
⟨ret-type⟩
                                         : (type-id)
                                         id: \langle type-id \rangle
(param)
                                         ⟨stat⟩ ⟨stat-seq⟩
(stat-seq)
\langle \text{stat-seq} \rangle
                                         \langle stat \rangle
\langle stat \rangle
                                         \langle \text{lvalue} \rangle := \langle \text{expr} \rangle ;
\langle stat \rangle
                                         if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle endif;
                                         if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle else \langle \operatorname{stat-seq} \rangle endif;
\langle stat \rangle
                                         while \langle \exp r \rangle do \langle \operatorname{stat-seq} \rangle enddo;
\langle stat \rangle
                                         for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
\langle stat \rangle
                                         \langle \text{opt-prefix} \rangle \text{ id } (\langle \text{expr-list} \rangle);
\langle stat \rangle
\langle stat \rangle
                                         break;
                                         return (expr);
\langle stat \rangle
                                         ⟨expr⟩ ⟨binary-operator⟩ ⟨expr⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                         \langle const \rangle
                                         ⟨lvalue⟩
\langle \exp r \rangle
                                         - \langle \exp r \rangle
\langle \exp r \rangle
                                         (\langle \exp r \rangle)
\langle \exp r \rangle
(binary-operator)
(binary-operator)
(binary-operator)
                                         +
(binary-operator)
(binary-operator)
                                         =
(binary-operator)
                                         <
(binary-operator)
                                         >
(binary-operator)
                                         <=
(binary-operator)
                                         >=
(binary-operator)
                                         <>
(binary-operator)
                                         &
```

```
\langle \text{binary-operator} \rangle
(binary-operator)
                                                 :=
\langle \text{opt-prefix} \rangle
                                                 \langle lvalue \rangle :=
(opt-prefix)
                                                 NULL
\langle const \rangle
                                                 INTLIT
\langle const \rangle
                                                 STRLIT
\langle const \rangle
                                                 _{\mathrm{nil}}
                                                 \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
⟨expr-list⟩
\langle \text{expr-list} \rangle
                                                 NULL
                                                 , \langle \exp r \rangle \langle \exp r-list-tail\rangle
\langle \text{expr-list-tail} \rangle
\langle \text{expr-list-tail} \rangle
                                                 NULL
                                                 id \langle lvalue-tail \rangle
(lvalue)
                                                 [\langle \expr \rangle] \langle \text{lvalue-tail} \rangle
(lvalue-tail)
                                                 NULL
(lvalue-tail)
```

Modified Grammar:

symbol	rule		
$\langle \text{tiger-program} \rangle$	let (declaration-segment) in (stat-seq) end		
$\langle declaration\text{-segment} \rangle$	(type-declaration-list) (var-declaration-list) (funct-declaration-list)		
$\langle \text{type-declaration-list} \rangle$	$\langle \text{type-declaration} \rangle \langle \text{type-declaration-list} \rangle$		
$\langle \text{type-declaration-list} \rangle$	NULL		
$\langle var-declaration-list \rangle$	(var-declaration) (var-declaration-list)		
$\langle var-declaration-list \rangle$	NULL		
$\langle funct\text{-}declaration\text{-}list \rangle$	$\langle \text{funct-declaration} \rangle \langle \text{funct-declaration-list} \rangle$		
$\langle funct-declaration-list \rangle$	NULL		
$\langle \text{type-declaration} \rangle$	type $id = \langle type \rangle$;		
$\langle var\text{-declaration} \rangle$	$ \operatorname{var} \langle \operatorname{id-list} \rangle : \langle \operatorname{type-id} \rangle \langle \operatorname{optional-init} \rangle ;$		
$\langle funct\text{-}declaration \rangle$	function id ($\langle param-list \rangle$) $\langle ret-type \rangle$ begin $\langle stat-seq \rangle$ end;		
$\langle \mathrm{type} \rangle$	$\langle \text{type-id} \rangle$		
$\langle \mathrm{type} \rangle$	array [INTLIT] of $\langle \text{type-dim} \rangle$ of $\langle \text{type-id} \rangle$		
$\langle { m type-dim} \rangle$	$[INTLIT] \langle type-dim \rangle$		
$\langle { m type-dim} \rangle$	NULL		
$\langle ext{type-id} \rangle$	id		
$\langle id$ -list \rangle	id (id-list-tail)		
$\langle id$ -list-tail \rangle	\mid , id \langle id-list-tail \rangle		
$\langle \mathrm{id} ext{-list-tail} \rangle$	NULL		
$\langle { m optional\text{-}init} \rangle$	$:=\langle \mathrm{const} \rangle$		
$\langle { m optional\text{-}init} \rangle$	NULL		
$\langle \mathrm{param ext{-}list} angle$	$\langle param \rangle \langle param-list-tail \rangle$		
$\langle \mathrm{param ext{-}list} angle$	NULL		
$\langle param-list-tail \rangle$	$\mid , \langle param \rangle \langle param-list-tail \rangle$		
$\langle param-list-tail \rangle$	NULL		
$\langle { m ret-type} \rangle$	$:\langle ext{type-id} \rangle $		
$\langle { m ret-type} \rangle$	NULL		
$\langle \mathrm{param} \rangle$	$ id : \langle type-id \rangle$		
$\langle \text{stat-seq} \rangle$	$\langle \text{stat} \rangle \langle \text{stat-seq-tail} \rangle$		
$\langle \text{stat-seq-tail} \rangle$	$\langle \text{stat} \rangle \langle \text{stat-seq-tail} \rangle$		
$\langle \text{stat-seq-tail} \rangle$	NULL		
$\langle \mathrm{stat} \rangle$	$ if \langle expr \rangle then \langle stat-seq \rangle \langle stat-if-tail \rangle$		
$\langle \mathrm{stat} \rangle$	while $\langle \exp r \rangle$ do $\langle \operatorname{stat-seq} \rangle$ enddo;		
$\langle \mathrm{stat} \rangle$	for id := $\langle \exp r \rangle$ to $\langle \exp r \rangle$ do $\langle \text{stat-seq} \rangle$ enddo;		
$\langle \mathrm{stat} \rangle$	break;		

```
\langle stat \rangle
                                     return (expr);
\langle stat \rangle
                                     id (stat-func-or-assign)
⟨stat-func-or-assign⟩
                                     (\langle \text{expr-list} \rangle);
                                      \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
⟨stat-func-or-assign⟩
⟨stat-if-tail⟩
                                     else (stat-seq) endif;
⟨stat-if-tail⟩
                                     endif;
(stat-assign)
                                     - (unaryminus) (stat-assign-tail)
                                     (\langle \exp r \rangle) \langle \operatorname{stat-assign-tail} \rangle
(stat-assign)
                                      \langle const \rangle \langle stat-assign-tail \rangle
⟨stat-assign⟩
(stat-assign)
                                     id \langle stat-assign-id \rangle
                                      (\langle expr-list \rangle);
(stat-assign-id)
                                      \langle lvalue-tail \rangle \langle stat-assign-tail \rangle
⟨stat-assign-id⟩
(stat-assign-tail)
                                      (expr-tail)
⟨stat-assign-tail⟩
                                      (orexpr-tail)
⟨stat-assign-tail⟩
                                      (andexpr-tail)
⟨stat-assign-tail⟩
                                      ⟨compare-tail⟩
⟨stat-assign-tail⟩
                                      ⟨term-tail⟩
\langle \exp r \rangle
                                      (orexpr) (expr-tail)
                                      ⟨orop⟩ ⟨orexpr⟩ ⟨expr-tail⟩
⟨expr-tail⟩
⟨expr-tail⟩
                                     NULL
                                      ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      \langle andop \rangle \langle andexpr \rangle \langle orexpr-tail \rangle
(orexpr-tail)
(orexpr-tail)
                                     NULL
                                      ⟨compare⟩ ⟨andexpr-tail⟩
\langle and expr \rangle
\langle and expr-tail \rangle
                                      ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
                                     NULL
\langle compare \rangle
                                      ⟨term⟩ ⟨compare-tail⟩
                                      ⟨addop⟩ ⟨term⟩ ⟨compare-tail⟩
(compare-tail)
\langle compare-tail \rangle
                                     NULL
                                      ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
⟨term-tail⟩
                                      ⟨mulop⟩ ⟨factor⟩ ⟨term-tail⟩
⟨term-tail⟩
                                     NULL
                                      (unaryminus)
(factor)
⟨factor⟩
                                     - (unaryminus)
(unaryminus)
                                     (\langle \exp r \rangle)
⟨unaryminus⟩
                                      \langle const \rangle
(unaryminus)
                                      (lvalue)
                                     INTLIT
\langle const \rangle
\langle const \rangle
                                     STRLIT
\langle const \rangle
                                     nil
\langle \text{orop} \rangle
\langle andop \rangle
                                     &
\langle compop \rangle
\langle compop \rangle
                                      <>
\langle compop \rangle
                                      >
\langle compop \rangle
                                      <
\langle compop \rangle
                                      >=
\langle compop \rangle
                                      <=
(addop)
                                      +
\langle addop \rangle
                                      *
\langle \text{mulop} \rangle
\langle \text{mulop} \rangle
                                     ⟨expr⟩ ⟨expr-list-tail⟩
\langle \text{expr-list} \rangle
```

$\langle \text{expr-list} \rangle$	NULL
$\langle \text{expr-list-tail} \rangle$, $\langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle$
$\langle \text{expr-list-tail} \rangle$	NULL
$\langle lvalue \rangle$	$id \langle lvalue-tail \rangle$
$\langle lvalue-tail \rangle$	$[\langle \expr \rangle] \langle \text{lvalue-tail} \rangle$
$\langle lvalue-tail \rangle$	NULL

non-terminal	first set
$\langle lvalue-tail \rangle$	$[,\epsilon$
(lvalue)	id
$\langle \text{expr-list-tail} \rangle$	$,, \epsilon$
$\langle \text{expr-list} \rangle$	(, nil, STRLIT, INTLIT, id, -, ϵ
$\langle \mathrm{mulop} \rangle$	*, /
$\langle addop \rangle$	+, -
$\langle \text{compop} \rangle$	=,<,>,<=,>=,<>
$\langle andop \rangle$	&
$\langle \text{orop} \rangle$	
$\langle \text{const} \rangle$	nil, STRLIT, INTLIT
(unaryminus)	(, nil, STRLIT, INTLIT, id
(factor)	(, nil, STRLIT, INTLIT, id, -
(term-tail)	$ *,/,\epsilon $
$\langle \text{term} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle \text{compare-tail} \rangle$	$+,-,\epsilon$
$\langle \text{compare} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle and expr-tail \rangle$	=,<,>,<=,>=,<
$\langle andexpr \rangle$	(, nil, STRLIT, INTLIT, id, -
(orexpr)	(, nil, STRLIT, INTLIT, id, -
(orexpr-tail)	$ \stackrel{\circ}{\&} , \epsilon$
$\langle \exp r \rangle$	(, nil, STRLIT, INTLIT, id, -
(expr-tail)	$ \cdot $, ϵ
$\langle \text{stat-assign} \rangle$	id, -, (, nil, STRLIT, INTLIT
$\langle \text{stat-assign-id} \rangle$	$[, (, *, /, +, -, =, <, >, <=, >=, <>, \&, , \epsilon]$
$\langle \text{stat-assign-tail} \rangle$	*, / , +, -, =, <, >, <=, >=, <>, & , , \epsilon
(stat-if-tail)	else, endif
(stat-func-or-assign)	(, :=, [
$\langle \text{stat} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq-tail} \rangle$	if, while, for, break, return, id, ϵ
(param)	id
⟨ret-type⟩	$:,\epsilon$
(param-list-tail)	$,,\epsilon$
(param-list)	id, ϵ
(optional-init)	$:=,\epsilon$
(id-list-tail)	$ \; ,, \epsilon $
$\langle id$ -list \rangle	id
$\langle \text{type-id} \rangle$	id
$\langle \text{type-dim} \rangle$	$[,\epsilon$
$\langle \text{type} \rangle$	array, id
(funct-declaration)	function
(var-declaration)	var
$\langle \text{type-declaration} \rangle$	type
(funct-declaration-list)	function, ϵ
(var-declaration-list)	$ $ var, ϵ
. ,	1

```
\begin{array}{c|c} \langle \text{type-declaration-list} \rangle & \text{type, } \epsilon \\ \langle \text{declaration-segment} \rangle & \text{function, var, type, } \epsilon \\ \langle \text{tiger-program} \rangle & \text{let} \end{array}
```

Note, the dollar sign is the end of tokens symbol.

non-terminal	follow set
$\langle \text{lvalue-tail} \rangle$:=, *, / , +, -, =, <, >, <=, >=, <>, &
$\langle lvalue-tail \rangle$, if, while, for, break, return, id, endif, end,), ,, ,], then, do, to, ;
$\langle \text{expr-list-tail} \rangle$	
$\langle \text{expr-list} \rangle$	
$\langle \text{expr-tail} \rangle$	if, while, for, break, return, id, endif, end,), ,, ,], then, do, to, ;
$\langle \text{or expr-tail} \rangle$	if, while, for, break, return, id, endif, end, [,), ,, ,], then, do, to, ;
$\langle and expr-tail \rangle$	if, while, for, break, return, id, endif, end, & $, , \rangle, ,, ,]$, then, do, to, ;
$\langle \text{compare-tail} \rangle$	if, while, for, break, return, id, endif, end
$\langle \text{compare-tail} \rangle$	[&,], , , ,], then, do, to, $;, =, <, >, <=, >=, <>$
$\langle ext{term-tail} \rangle$	if, while, for, break, return, id, endif, end, & , ,)
$\langle ext{term-tail} \rangle$, ,], then, do, to, ;, =, <, >, <=, >=, <>, +, -
$\langle stat-assign-tail \rangle$	if, while, for, break, return, id, endif, end
$\langle stat-assign-id \rangle$	if, while, for, break, return, id, endif, end
$\langle \text{stat-seq-tail} \rangle$	endif, end
$\langle { m ret-type} \rangle$	begin
$\langle \text{param-list-tail} \rangle$	
$\langle param-list \rangle$	
$\langle { m optional-init} \rangle$	function, in
$\langle id$ -list-tail \rangle	:
$\langle \text{type-dim} \rangle$	of
$\langle funct-declaration-list \rangle$	in
$\langle var-declaration-list \rangle$	function, in
$\langle \text{type-declaration-list} \rangle$	var, function, in
$\langle declaration\text{-segment} \rangle$	in

Note, if there is no corresponding rule, then that means a parser error is generated.

Note, errors are handled by dropping tokens until a valid token is found.

symbol	next token	rule
$\langle addop \rangle$	+	+
$\langle addop \rangle$	-	-
$\langle \mathrm{andexpr} \rangle$	($\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle \mathrm{andexpr} \rangle$	nil	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle \mathrm{andexpr} \rangle$	STRLIT	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle \mathrm{andexpr} \rangle$	INTLIT	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle \mathrm{andexpr} \rangle$	id	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle \mathrm{andexpr} \rangle$	_	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	<	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	>	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	>=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	<=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle { m andexpr-tail} \rangle$	<>	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	if	ϵ
$\langle \text{andexpr-tail} \rangle$	while	ϵ

$\langle and expr-tail \rangle$	for	$\mid \epsilon$
$\langle \text{andexpr-tail} \rangle$	break	ϵ
$\langle \text{andexpr-tail} \rangle$	return	ϵ
$\langle \text{andexpr-tail} \rangle$	id	ϵ
$\langle \text{andexpr-tail} \rangle$	endif	ϵ
$\langle \text{andexpr-tail} \rangle$	end	ϵ
$\langle \text{andexpr-tail} \rangle$	&	ϵ
$\langle \text{andexpr-tail} \rangle$	1	ϵ
$\langle \text{andexpr-tail} \rangle$)	ϵ
$\langle \text{andexpr-tail} \rangle$,	ϵ
$\langle \text{andexpr-tail} \rangle$	1	ϵ
$\langle \text{andexpr-tail} \rangle$	then	ϵ
$\langle andexpr-tail \rangle$	do	ϵ
$\langle and expr-tail \rangle$	to	ϵ
$\langle \text{andexpr-tail} \rangle$;	ϵ
$\langle andop \rangle$	&	&
$\langle \text{compare} \rangle$	($\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare} \rangle$	nil	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare} \rangle$	STRLIT	\langle term \rangle \langle compare-tail \rangle
$\langle \text{compare} \rangle$	INTLIT	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare} \rangle$	id	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare} \rangle$	_	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare-tail} \rangle$	+	$\langle addop \rangle \langle term \rangle \langle compare-tail \rangle$
$\langle \text{compare-tail} \rangle$	-	$\langle addop \rangle \langle term \rangle \langle compare-tail \rangle$
$\langle \text{compare-tail} \rangle$	if	ϵ
$\langle \text{compare-tail} \rangle$	while	ϵ
$\langle \text{compare-tail} \rangle$	for	ϵ
$\langle \text{compare-tail} \rangle$	break	ϵ
$\langle \text{compare-tail} \rangle$	return	ϵ
$\langle \text{compare-tail} \rangle$	id	ϵ
$\langle \text{compare-tail} \rangle$	endif	ϵ
$\langle \text{compare-tail} \rangle$	end	ϵ
$\langle \text{compare-tail} \rangle$	&	ϵ
$\langle \text{compare-tail} \rangle$		ϵ
$\langle \text{compare-tail} \rangle$)	ϵ
$\langle \text{compare-tail} \rangle$,	ϵ
$\langle \text{compare-tail} \rangle$]	ϵ
$\langle \text{compare-tail} \rangle$	then	ϵ
$\langle \text{compare-tail} \rangle$	do	ϵ
$\langle \text{compare-tail} \rangle$	to	ϵ
$\langle \text{compare-tail} \rangle$;	ϵ
$\langle \text{compare-tail} \rangle$	=	ϵ
$\langle \text{compare-tail} \rangle$	<	ϵ
$\langle \text{compare-tail} \rangle$	>	ϵ
$\langle \text{compare-tail} \rangle$	<=	ϵ
$\langle \text{compare-tail} \rangle$	>=	ϵ
$\langle \text{compare-tail} \rangle$	<>	ϵ
$\langle \text{compop} \rangle$	=	=
$\langle \text{compop} \rangle$	<	<
$\langle \text{compop} \rangle$	>	>
$\langle \text{compop} \rangle$	<=	<=
$\langle \text{compop} \rangle$	>=	<i>></i> =
$\langle \mathrm{compop} \rangle$	<>	<>

```
\langle const \rangle
                                   nil
                                                     nil
\langle const \rangle
                                   STRLIT
                                                     STRLIT
                                   INTLIT
                                                     INTLIT
\langle const \rangle
                                   function
                                                     \langle type-declaration-list \rangle \langle var-declaration-list \rangle \langle funct-declaration-list \rangle
(declaration-segment)
(declaration-segment)
                                   var
                                                     (type-declaration-list) (var-declaration-list) (funct-declaration-list)
(declaration-segment)
                                   type
                                                     (type-declaration-list) (var-declaration-list) (funct-declaration-list)
(declaration-segment)
                                   in
                                                     \epsilon
⟨expr-list⟩
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
⟨expr-list⟩
                                   (
⟨expr-list⟩
                                   nil
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
                                   STRLIT
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
(expr-list)
⟨expr-list⟩
                                   INTLIT
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
(expr-list)
                                   id
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
\langle \text{expr-list} \rangle
                                                     ⟨expr⟩ ⟨expr-list-tail⟩
                                   )
⟨expr-list-tail⟩
                                                     , \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
⟨expr-list-tail⟩
                                   (
                                                     ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                   nil
                                                     (orexpr) (expr-tail)
\langle \exp r \rangle
                                   STRLIT
                                                     (orexpr) (expr-tail)
                                   INTLIT
                                                     (orexpr) (expr-tail)
\langle \exp r \rangle
\langle \exp r \rangle
                                  id
                                                     (orexpr) (expr-tail)
\langle \exp r \rangle
                                                     (orexpr) (expr-tail)
(expr-tail)
                                                     ⟨orop⟩ ⟨orexpr⟩ ⟨expr-tail⟩
                                   if
(expr-tail)
(expr-tail)
                                   while
                                                     \epsilon
(expr-tail)
                                   for
                                                     \epsilon
⟨expr-tail⟩
                                   break
                                                     \epsilon
(expr-tail)
                                   return
                                                     \epsilon
⟨expr-tail⟩
                                   id
                                                     \epsilon
                                   endif
(expr-tail)
                                                     \epsilon
(expr-tail)
                                   end
                                                     \epsilon
⟨expr-tail⟩
                                   )
                                                     \epsilon
(expr-tail)
                                                     \epsilon
(expr-tail)
                                                     \epsilon
(expr-tail)
                                   then
                                                     \epsilon
(expr-tail)
                                   do
                                                     \epsilon
(expr-tail)
                                   to
                                                     \epsilon
(expr-tail)
                                   (
(factor)
                                                     (unaryminus)
                                                     ⟨unaryminus⟩
\langle factor \rangle
                                   nil
(factor)
                                   STRLIT
                                                     (unaryminus)
(factor)
                                   INTLIT
                                                     (unaryminus)
                                                     (unaryminus)
(factor)
                                   id
(factor)
                                                     - (unaryminus)
(funct-declaration)
                                   function
                                                     function id (\langle param-list\rangle ) \langle ret-type \rangle begin \langle stat-seq \rangle end ;
                                                     \( \) funct-declaration \( \) \( \) \( \) \( \) \( \) \( \) declaration-list \( \)
(funct-declaration-list)
                                   function
(funct-declaration-list)
                                   in
⟨id-list⟩
                                   id
                                                     id (id-list-tail)
(id-list-tail)
                                   :
                                                     , id (id-list-tail)
(id-list-tail)
                                  id
                                                     id (lvalue-tail)
(lvalue)
                                                     [\langle \expr \rangle] \langle \text{lvalue-tail} \rangle
(lvalue-tail)
                                   [
(lvalue-tail)
                                  :=
                                                     \epsilon
```

```
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      +
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      =
                                                          \epsilon
(lvalue-tail)
                                      <
                                                          \epsilon
(lvalue-tail)
                                      >
                                                          \epsilon
(lvalue-tail)
                                      <=
                                                          \epsilon
(lvalue-tail)
                                      >=
                                                          \epsilon
(lvalue-tail)
                                      <>
                                                          \epsilon
(lvalue-tail)
                                      &
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
                                      if
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      while
                                                          \epsilon
(lvalue-tail)
                                      for
                                                          \epsilon
(lvalue-tail)
                                      break
                                                          \epsilon
(lvalue-tail)
                                      return
                                                          \epsilon
(lvalue-tail)
                                      id
                                                          \epsilon
(lvalue-tail)
                                      endif
                                                          \epsilon
(lvalue-tail)
                                      end
                                                          \epsilon
(lvalue-tail)
                                      )
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      then
                                                          \epsilon
(lvalue-tail)
                                      do
                                                          \epsilon
(lvalue-tail)
                                      to
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
\langle \text{mulop} \rangle
\langle \text{mulop} \rangle
                                                          := \langle const \rangle
(optional-init)
                                      :=
⟨optional-init⟩
                                      function
(optional-init)
                                      in
                                                          ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      (
                                                          ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      nil
\langle orexpr \rangle
                                      STRLIT
                                                          (andexpr) (orexpr-tail)
                                      INTLIT
\langle orexpr \rangle
                                                          ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      id
                                                          (andexpr) (orexpr-tail)
                                                          ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      &
                                                          ⟨andop⟩ ⟨andexpr⟩ ⟨orexpr-tail⟩
(orexpr-tail)
(orexpr-tail)
                                      if
(orexpr-tail)
                                      while
                                                          \epsilon
(orexpr-tail)
                                      for
                                                          \epsilon
(orexpr-tail)
                                      break
                                                          \epsilon
(orexpr-tail)
                                      return
                                                          \epsilon
(orexpr-tail)
                                      id
                                                          \epsilon
                                      endif
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                      end
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                      )
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                      then
                                                          \epsilon
(orexpr-tail)
                                      do
                                                          \epsilon
```

```
(orexpr-tail)
                               to
                                                \epsilon
(orexpr-tail)
                                                \epsilon
\langle \text{orop} \rangle
(param)
                               id
                                                id: (type-id)
(param-list)
                               )
                               id
(param-list)
                                                ⟨param⟩ ⟨param-list-tail⟩
(param-list-tail)
                               )
                                                , (param) (param-list-tail)
(param-list-tail)
⟨ret-type⟩
                               begin
⟨ret-type⟩
                                                : \langle \text{type-id} \rangle
                               id
                                                id (stat-assign-id)
(stat-assign)
                                                - (unaryminus) (stat-assign-tail)
(stat-assign)
                               (
(stat-assign)
                                                (\langle \exp r \rangle) \langle \operatorname{stat-assign-tail} \rangle
⟨stat-assign⟩
                               nil
                                                \langle const \rangle \langle stat-assign-tail \rangle
                               STRLIT
                                                ⟨const⟩ ⟨stat-assign-tail⟩
(stat-assign)
(stat-assign)
                               INTLIT
                                                \langle const \rangle \langle stat-assign-tail \rangle
(stat-assign-id)
                               end
(stat-assign-id)
                               endif
(stat-assign-id)
                               id
                                                \epsilon
(stat-assign-id)
                               return
                                                \epsilon
                               break
(stat-assign-id)
                                                \epsilon
(stat-assign-id)
                               for
                                                \epsilon
(stat-assign-id)
                               while
                                                \epsilon
                               if
(stat-assign-id)
(stat-assign-id)
                                                (lvalue-tail) (stat-assign-tail)
                               &
(stat-assign-id)
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                               <>
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                               >=
                                                (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                               <=
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                               >
(stat-assign-id)
                               <
                                                (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                               =
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                                (lvalue-tail) (stat-assign-tail)
                               +
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
(stat-assign-id)
                                                (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                               (
                                                (\langle \text{expr-list} \rangle);
                                                ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
(stat-assign-tail)
                               end
                               endif
(stat-assign-tail)
                                                \epsilon
(stat-assign-tail)
                               id
(stat-assign-tail)
                               return
                                                \epsilon
                               break
(stat-assign-tail)
                                                \epsilon
(stat-assign-tail)
                               for
                                                \epsilon
                               while
(stat-assign-tail)
                                                \epsilon
(stat-assign-tail)
                               if
(stat-assign-tail)
                                                ⟨expr-tail⟩
                               &
(stat-assign-tail)
                                                (orexpr-tail)
(stat-assign-tail)
                               <>
                                                (andexpr-tail)
                                                ⟨andexpr-tail⟩
(stat-assign-tail)
                               >=
(stat-assign-tail)
                               \leq =
                                                (andexpr-tail)
(stat-assign-tail)
                               >
                                                (andexpr-tail)
                               <
(stat-assign-tail)
                                                (andexpr-tail)
```

```
(stat-assign-tail)
                                                         (andexpr-tail)
                                     =
(stat-assign-tail)
                                                         (compare-tail)
(stat-assign-tail)
                                     +
                                                         (compare-tail)
(stat-assign-tail)
                                                         ⟨term-tail⟩
(stat-assign-tail)
                                                         ⟨term-tail⟩
                                                         (\langle expr-list \rangle);
⟨stat-func-or-assign⟩
                                     (
⟨stat-func-or-assign⟩
                                                         \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
                                     :=
⟨stat-func-or-assign⟩
                                                         \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
⟨stat-if-tail⟩
                                     else
                                                         else (stat-seq) endif;
⟨stat-if-tail⟩
                                     endif
                                                         endif;
⟨stat⟩
                                     if
                                                         if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle \langle \operatorname{stat-if-tail} \rangle
⟨stat⟩
                                     while
                                                         while \langle \exp r \rangle do \langle \operatorname{stat-seq} \rangle enddo;
\langle stat \rangle
                                     for
                                                         for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
\langle stat \rangle
                                     break
                                                         break:
⟨stat⟩
                                                         return (expr);
                                     return
\langle stat \rangle
                                     id
                                                         id (stat-func-or-assign)
⟨stat-seq⟩
                                     if
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
                                     while
                                                         (stat) (stat-seq-tail)
                                     for
⟨stat-seg⟩
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seg⟩
                                     break
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seg⟩
                                     return
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seg⟩
                                     id
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                     endif
                                                         \epsilon
(stat-seq-tail)
                                     end
                                     if
(stat-seq-tail)
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seg-tail)
                                     while
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                     for
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
                                     break
(stat-seq-tail)
                                                         (stat) (stat-seq-tail)
⟨stat-seq-tail⟩
                                     return
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                     id
                                                         ⟨stat⟩ ⟨stat-seq-tail⟩
\langle \text{term} \rangle
                                                         \langle factor \rangle \langle term-tail \rangle
\langle \text{term} \rangle
                                     id
                                                         ⟨factor⟩ ⟨term-tail⟩
                                     INTLIT
\langle \text{term} \rangle
                                                         \(\factor\) \(\text{term-tail}\)
\langle \text{term} \rangle
                                     STRLIT
                                                         ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
                                     nil
                                                         ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
                                                         ⟨factor⟩ ⟨term-tail⟩
⟨term-tail⟩
                                                         \langle mulop \langle \text{factor} \langle \text{term-tail} \rangle
⟨term-tail⟩
                                                         ⟨mulop⟩ ⟨factor⟩ ⟨term-tail⟩
⟨term-tail⟩
                                     )
⟨term-tail⟩
                                                         \epsilon
⟨term-tail⟩
                                     &
                                                         \epsilon
⟨term-tail⟩
                                     end
                                                         \epsilon
⟨term-tail⟩
                                     endif
                                                         \epsilon
⟨term-tail⟩
                                     id
                                                         \epsilon
⟨term-tail⟩
                                     return
                                                         \epsilon
⟨term-tail⟩
                                     break
                                                         \epsilon
⟨term-tail⟩
                                     for
                                                         \epsilon
⟨term-tail⟩
                                     while
                                                         \epsilon
⟨term-tail⟩
                                     if
                                                         \epsilon
⟨term-tail⟩
                                                         \epsilon
⟨term-tail⟩
                                     +
                                                         \epsilon
⟨term-tail⟩
                                     <>
                                                         \epsilon
⟨term-tail⟩
                                     >=
                                                         \epsilon
```

```
⟨term-tail⟩
                                <=
                                                 \epsilon
⟨term-tail⟩
                                >
                                                 \epsilon
⟨term-tail⟩
                                <
                                                 \epsilon
⟨term-tail⟩
                                =
                                                 \epsilon
⟨term-tail⟩
                                                 \epsilon
⟨term-tail⟩
                                to
                                                 \epsilon
⟨term-tail⟩
                                do
                                                 \epsilon
⟨term-tail⟩
                                then
                                                 \epsilon
⟨term-tail⟩
                                                 \epsilon
⟨term-tail⟩
                                let
⟨tiger-program⟩
                                                 let (declaration-segment) in (stat-seq) end
                                                 array [ INTLIT ] of \langle \text{type-dim} \rangle of \langle \text{type-id} \rangle
(type)
                                array
(type)
                                id
                                                 ⟨type-id⟩
                                                 ⟨type-declaration⟩ ⟨type-declaration-list⟩
⟨type-declaration-list⟩
                                type
⟨type-declaration-list⟩
                                var
⟨type-declaration-list⟩
                                function
⟨type-declaration-list⟩
                                in
⟨type-declaration⟩
                                type
                                                 type id = \langle type \rangle;
                                                 [INTLIT] \langle type-dim \rangle
⟨type-dim⟩
⟨type-dim⟩
                                of
                                                \epsilon
                                id
                                                id
⟨type-id⟩
(unaryminus)
                                                 (\langle \exp r \rangle)
                                (
(unaryminus)
                                _{\rm nil}
                                                 \langle const \rangle
                                STRLIT
                                                 \langle const \rangle
(unaryminus)
(unaryminus)
                                INTLIT
                                                 \langle const \rangle
(unaryminus)
                                id
                                                 (lvalue)
⟨var-declaration-list⟩
                                function
(var-declaration-list)
                                in
(var-declaration-list)
                                                 ⟨var-declaration⟩ ⟨var-declaration-list⟩
                                var
(var-declaration)
                                                 var (id-list) : (type-id) (optional-init);
                                var
```