CS 4240 Phase 1

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1 Lexical Rules

Pre-parse the input to remove comments with the following DFA. The resulting NOT-COMMENT tokens are concatenated together.

Everything under the token column represents either generated tokens or custom table actions on the character buffer used to produce the text associated with tokens.

start state	symbol	next state	token
START	$\Sigma - \{/, "\}$	START	NOT-COMMENT
START	"	STRING	
START	/	SLASH	
STRING	$\Sigma - \{\setminus, "\}$	STRING	
STRING		STRING-SLASH	
STRING	,,	START	NOT-COMMENT
STRING-SLASH	Σ	STRING	
SLASH	$\Sigma - \{*\}$	START	NOT-COMMENT
SLASH	*	COMMENT	
COMMENT	$\Sigma - \{*\}$	COMMENT	
COMMENT	*	COMMENT-END	
COMMENT-END	$\Sigma - \{*,/\}$	COMMENT	
COMMENT-END	*	COMMENT-END	
COMMENT-END	/	START	COMMENT

The DFA for uncommented code.

Note, any time backtracking is mentioned, it essentially is the same as treating the current state as the start state and doing the corresponding transitions or token generations. This is included to simplify the table by removing duplication of the start state transitions.

Note, all ids are later matched character by character with keywords to determine if they are keywords.

Note, drop character for the error state means that the last read character is ignored, and the state remains unchanged.

start state	symbol	next state	token
START	+	START	PLUS
START	-	START	MIN
START	*	START	MULT
START	/	START	DIV
START	=	START	EQ
START		START	LPAREN
START		START	RPAREN
START	,	START	COMMA

START	&	START	AND
START	_	START	OR
START		START	LSQUARE
START		START	RSQUARE
START	:	START	SEMI
START	(LANGLE	
START	\ \ \	RANGLE	
START	:	COLON	
START	0-9	INT-LIT	
START	"	STRING-LIT	
START	a-zA-Z	ID	
START	whitespace	START	ignore
START	others	ERROR	drop character
LANGLE	$\Sigma - \{=, \rangle\}$	START	LESS, backtrack
LANGLE	>	START	NOTEQ
LANGLE	=	START	LESSEQ
RANGLE	$\Sigma - \{=\}$	START	GREATER, backtrack
RANGLE	=	START	GREATEREQ
COLON	=	START	ASSIGN
COLON	$\Sigma - \{=\}$	START	COLON, backtrack
INT-LIT	0-9	INT-LIT	·
INT-LIT	$\Sigma - 0 - 9$	START	INT-LIT, backtrack
ID	a-zA-Z0-9_	ID	·
ID	$\Sigma - a - zA - Z0 - 9$	START	ID, backtrack
STRING-LIT	$\Sigma - \setminus$	STRING-LIT	
STRING-LIT	"	START	STRING-LIT
STRING-LIT	\	STRING-LIT-SLASH	
STRING-LIT-SLASH	n	STRING-LIT	
STRING-LIT-SLASH	t	STRING-LIT	
STRING-LIT-SLASH	"	STRING-LIT	
STRING-LIT-SLASH	\	STRING-LIT	
STRING-LIT-SLASH	^	STRING-LIT-CTL	
STRING-LIT-SLASH	0-9	STRING-LIT-CODE-1	
STRING-LIT-SLASH	whitespace	STRING-LIT-SPACE	ignore 2 characters
STRING-LIT-SLASH	others	ERROR	drop character
STRING-LIT-CTL	@A-Z[\]^	STRING-LIT	
STRING-LIT-CTL	others	ERROR	drop character
STRING-LIT-CODE-1	0-9	STRING-LIT-CODE-2	
STRING-LIT-CODE-1	others	ERROR	drop character
STRING-LIT-CODE-2	0-9	STRING-LIT	
STRING-LIT-CODE-2	others	ERROR	drop character
STRING-LIT-SPACE	whitespace	STRING-LIT-SPACE	ignore
STRING-LIT-SPACE		STRING-LIT	ignore
STRING-LIT-SPACE	others	ERROR	drop character

2 Grammar Rules

Raw Grammar:

symbol	rule
$\overline{\langle \text{tiger-program} \rangle}$	let (declaration-segment) in (stat-seq) end
$\langle declaration\text{-segment} \rangle$	$\langle type\text{-declaration-list}\rangle \ \langle var\text{-declaration-list}\rangle \ \langle funct\text{-declaration-list}\rangle$

```
⟨type-declaration-list⟩
                                         ⟨type-declaration⟩ ⟨type-declaration-list⟩
⟨type-declaration-list⟩
                                         NULL
⟨var-declaration-list⟩
                                         (var-declaration) (var-declaration-list)
⟨var-declaration-list⟩
                                         NULL
\( \) funct-declaration-list \( \)
                                         \(\langle \text{funct-declaration} \rangle \text{funct-declaration-list} \rangle \)
                                         NULL
\( \) funct-declaration-list \( \)
⟨type-declaration⟩
                                         type id = \langle \text{type} \rangle;
\langle type \rangle
                                         ⟨type-id⟩
                                         array [ INTLIT ] of \( \text{type-dim} \) of \( \text{type-id} \)
\langle type \rangle
⟨type-dim⟩
                                         [INTLIT] \(\text{type-dim}\)
⟨type-dim⟩
                                         NULL
\langle \text{type-id} \rangle
                                         int
⟨type-id⟩
                                         string
\langle \text{type-id} \rangle
                                         id
(var-declaration)
                                         var (id-list) : (type-id) (optional-init);
\langle id-list \rangle
\langle id-list \rangle
                                         id, \langle id-list \rangle
⟨optional-init⟩
                                         NULL
(optional-init)
                                         := \langle const \rangle
\(\funct-declaration\)
                                         function id ( \( \rangle \text{param-list} \rangle ) \( \rangle \text{ret-type} \rangle \text{ begin \( \stat-\text{seq} \rangle \text{ end} \);
(param-list)
                                         NULL
(param-list)
                                         ⟨param⟩ ⟨param-list-tail⟩
⟨param-list-tail⟩
                                         NULL
                                         , (param) (param-list-tail)
⟨param-list-tail⟩
                                         NULL
⟨ret-type⟩
⟨ret-type⟩
                                         : (type-id)
                                         id: \langle type-id \rangle
(param)
                                         ⟨stat⟩ ⟨stat-seq⟩
(stat-seq)
\langle \text{stat-seq} \rangle
                                         \langle stat \rangle
\langle stat \rangle
                                         \langle \text{lvalue} \rangle := \langle \text{expr} \rangle ;
\langle stat \rangle
                                         if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle endif;
                                         if \langle \exp r \rangle then \langle \operatorname{stat-seq} \rangle else \langle \operatorname{stat-seq} \rangle endif;
\langle stat \rangle
                                         while \langle \exp r \rangle do \langle \operatorname{stat-seq} \rangle enddo;
\langle stat \rangle
                                         for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
\langle stat \rangle
                                         \langle \text{opt-prefix} \rangle \text{ id } (\langle \text{expr-list} \rangle);
\langle stat \rangle
\langle stat \rangle
                                         break;
                                         return (expr);
\langle stat \rangle
                                         ⟨expr⟩ ⟨binary-operator⟩ ⟨expr⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                         \langle const \rangle
                                         ⟨lvalue⟩
\langle \exp r \rangle
                                         - \langle \exp r \rangle
\langle \exp r \rangle
                                         (\langle \exp r \rangle)
\langle \exp r \rangle
(binary-operator)
(binary-operator)
(binary-operator)
                                         +
(binary-operator)
(binary-operator)
                                         =
(binary-operator)
                                         <
(binary-operator)
                                         >
(binary-operator)
                                         <=
(binary-operator)
                                         >=
(binary-operator)
                                         <>
(binary-operator)
                                         &
```

```
\langle \text{binary-operator} \rangle
(binary-operator)
                                                 :=
\langle \text{opt-prefix} \rangle
                                                 \langle lvalue \rangle :=
(opt-prefix)
                                                 NULL
\langle const \rangle
                                                 INTLIT
\langle const \rangle
                                                 STRLIT
\langle const \rangle
                                                 _{\mathrm{nil}}
                                                 \langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle
⟨expr-list⟩
\langle \text{expr-list} \rangle
                                                 NULL
                                                 , \langle \exp r \rangle \langle \exp r-list-tail\rangle
\langle \text{expr-list-tail} \rangle
\langle \text{expr-list-tail} \rangle
                                                 NULL
                                                 id \langle lvalue-tail \rangle
(lvalue)
                                                 [\langle \expr \rangle] \langle \text{lvalue-tail} \rangle
(lvalue-tail)
                                                 NULL
(lvalue-tail)
```

Modified Grammar:

symbol	rule		
$\langle \text{tiger-program} \rangle$	let (declaration-segment) in (stat-seq) end		
$\langle declaration\text{-segment} \rangle$	\langle \text{type-declaration-list} \langle \text{var-declaration-list} \langle \text{funct-declaration-list} \rangle		
$\langle \text{type-declaration-list} \rangle$	$\langle \text{type-declaration} \rangle \langle \text{type-declaration-list} \rangle$		
$\langle \text{type-declaration-list} \rangle$	NULL		
$\langle var-declaration-list \rangle$	(var-declaration) (var-declaration-list)		
$\langle var-declaration-list \rangle$	NULL		
$\langle funct\text{-}declaration\text{-}list \rangle$	$\langle \text{funct-declaration} \rangle \langle \text{funct-declaration-list} \rangle$		
$\langle funct-declaration-list \rangle$	NULL		
$\langle \text{type-declaration} \rangle$	type $id = \langle type \rangle$;		
$\langle var\text{-declaration} \rangle$	$ \operatorname{var} \langle \operatorname{id-list} \rangle : \langle \operatorname{type-id} \rangle \langle \operatorname{optional-init} \rangle ;$		
$\langle funct\text{-}declaration \rangle$	function id ($\langle param-list \rangle$) $\langle ret-type \rangle$ begin $\langle stat-seq \rangle$ end;		
$\langle \mathrm{type} \rangle$	$\langle \text{type-id} \rangle$		
$\langle \mathrm{type} \rangle$	array [INTLIT] of $\langle \text{type-dim} \rangle$ of $\langle \text{type-id} \rangle$		
$\langle { m type-dim} \rangle$	$[INTLIT] \langle type-dim \rangle$		
$\langle { m type-dim} \rangle$	NULL		
$\langle ext{type-id} \rangle$	id		
$\langle id$ -list \rangle	id (id-list-tail)		
$\langle id$ -list-tail \rangle	\mid , id \langle id-list-tail \rangle		
$\langle \mathrm{id} ext{-list-tail} \rangle$	NULL		
$\langle { m optional\text{-}init} \rangle$	$:=\langle \mathrm{const} \rangle$		
$\langle { m optional\text{-}init} \rangle$	NULL		
$\langle { m param-list} \rangle$	$\langle param \rangle \langle param-list-tail \rangle$		
$\langle { m param-list} \rangle$	NULL		
$\langle param-list-tail \rangle$	$\mid , \langle param \rangle \langle param-list-tail \rangle$		
$\langle param-list-tail \rangle$	NULL		
$\langle { m ret-type} \rangle$	$:\langle ext{type-id} \rangle $		
$\langle { m ret-type} \rangle$	NULL		
$\langle \mathrm{param} \rangle$	$ id : \langle type-id \rangle$		
$\langle \text{stat-seq} \rangle$	$\langle \text{stat} \rangle \langle \text{stat-seq-tail} \rangle$		
$\langle \text{stat-seq-tail} \rangle$	$\langle \text{stat} \rangle \langle \text{stat-seq-tail} \rangle$		
$\langle \text{stat-seq-tail} \rangle$	NULL		
$\langle \mathrm{stat} \rangle$	$ if \langle expr \rangle then \langle stat-seq \rangle \langle stat-if-tail \rangle$		
$\langle \mathrm{stat} \rangle$	while $\langle \exp r \rangle$ do $\langle \operatorname{stat-seq} \rangle$ enddo;		
$\langle \mathrm{stat} \rangle$	for id := $\langle \exp r \rangle$ to $\langle \exp r \rangle$ do $\langle \text{stat-seq} \rangle$ enddo;		
$\langle \mathrm{stat} \rangle$	break;		

```
\langle stat \rangle
                                     return (expr);
\langle stat \rangle
                                     id (stat-func-or-assign)
⟨stat-func-or-assign⟩
                                     (\langle expr-list \rangle);
                                      \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
⟨stat-func-or-assign⟩
⟨stat-if-tail⟩
                                     else (stat-seq) endif;
⟨stat-if-tail⟩
                                     endif;
(stat-assign)
                                     - (unaryminus) (stat-assign-tail)
                                     (\langle \exp r \rangle) \langle \operatorname{stat-assign-tail} \rangle
(stat-assign)
                                      \langle const \rangle \langle stat-assign-tail \rangle
⟨stat-assign⟩
(stat-assign)
                                     id \langle stat-assign-id \rangle
                                      (\langle expr-list \rangle);
(stat-assign-id)
                                      \langle lvalue-tail \rangle \langle stat-assign-tail \rangle
⟨stat-assign-id⟩
(stat-assign-tail)
                                      (expr-tail)
⟨stat-assign-tail⟩
                                      (orexpr-tail)
⟨stat-assign-tail⟩
                                      (andexpr-tail)
⟨stat-assign-tail⟩
                                      ⟨compare-tail⟩
⟨stat-assign-tail⟩
                                      ⟨term-tail⟩
\langle \exp r \rangle
                                      (orexpr) (expr-tail)
                                      ⟨orop⟩ ⟨orexpr⟩ ⟨expr-tail⟩
⟨expr-tail⟩
⟨expr-tail⟩
                                     NULL
                                      ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      \langle andop \rangle \langle andexpr \rangle \langle orexpr-tail \rangle
(orexpr-tail)
(orexpr-tail)
                                     NULL
                                      ⟨compare⟩ ⟨andexpr-tail⟩
\langle and expr \rangle
\langle and expr-tail \rangle
                                      ⟨compop⟩ ⟨compare⟩ ⟨andexpr-tail⟩
(andexpr-tail)
                                     NULL
\langle compare \rangle
                                      ⟨term⟩ ⟨compare-tail⟩
                                      ⟨addop⟩ ⟨term⟩ ⟨compare-tail⟩
(compare-tail)
\langle compare-tail \rangle
                                     NULL
                                      ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
⟨term-tail⟩
                                      ⟨mulop⟩ ⟨factor⟩ ⟨term-tail⟩
⟨term-tail⟩
                                     NULL
                                      (unaryminus)
(factor)
⟨factor⟩
                                     - (unaryminus)
(unaryminus)
                                     (\langle \exp r \rangle)
⟨unaryminus⟩
                                      \langle const \rangle
(unaryminus)
                                      (lvalue)
                                     INTLIT
\langle const \rangle
\langle const \rangle
                                     STRLIT
\langle const \rangle
                                     nil
\langle \text{orop} \rangle
\langle andop \rangle
                                     &
\langle compop \rangle
\langle compop \rangle
                                      <>
\langle compop \rangle
                                      >
\langle compop \rangle
                                      <
\langle compop \rangle
                                      >=
\langle compop \rangle
                                      <=
(addop)
                                      +
\langle addop \rangle
                                      *
\langle \text{mulop} \rangle
\langle \text{mulop} \rangle
                                     ⟨expr⟩ ⟨expr-list-tail⟩
\langle \text{expr-list} \rangle
```

$\langle \text{expr-list} \rangle$	NULL
$\langle \text{expr-list-tail} \rangle$, $\langle \exp r \rangle \langle \exp r - \operatorname{list-tail} \rangle$
$\langle \text{expr-list-tail} \rangle$	NULL
$\langle lvalue \rangle$	$id \langle lvalue-tail \rangle$
$\langle lvalue-tail \rangle$	$[\langle \expr \rangle] \langle \text{lvalue-tail} \rangle$
$\langle lvalue-tail \rangle$	NULL

non-terminal	first set
$\langle lvalue-tail \rangle$	$[,\epsilon$
(lvalue)	id
$\langle \text{expr-list-tail} \rangle$	$,, \epsilon$
$\langle \text{expr-list} \rangle$	(, nil, STRLIT, INTLIT, id, -, ϵ
$\langle \mathrm{mulop} \rangle$	*, /
$\langle addop \rangle$	+, -
$\langle \text{compop} \rangle$	=,<,>,<=,>=,<>
$\langle andop \rangle$	&
$\langle \text{orop} \rangle$	
$\langle \text{const} \rangle$	nil, STRLIT, INTLIT
(unaryminus)	(, nil, STRLIT, INTLIT, id
(factor)	(, nil, STRLIT, INTLIT, id, -
(term-tail)	$ *,/,\epsilon $
$\langle \text{term} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle \text{compare-tail} \rangle$	$+,-,\epsilon$
$\langle \text{compare} \rangle$	(, nil, STRLIT, INTLIT, id, -
$\langle and expr-tail \rangle$	=, <, >, <=, >=, <>, ε
$\langle andexpr \rangle$	(, nil, STRLIT, INTLIT, id, -
(orexpr)	(, nil, STRLIT, INTLIT, id, -
(orexpr-tail)	$ \stackrel{\circ}{\&} , \epsilon$
$\langle \exp r \rangle$	(, nil, STRLIT, INTLIT, id, -
(expr-tail)	$ \cdot $, ϵ
$\langle \text{stat-assign} \rangle$	id, -, (, nil, STRLIT, INTLIT
$\langle \text{stat-assign-id} \rangle$	$[, (, *, /, +, -, =, <, >, <=, >=, <>, \&, , \epsilon]$
$\langle \text{stat-assign-tail} \rangle$	*, / , +, -, =, <, >, <=, >=, <>, & , , \epsilon
(stat-if-tail)	else, endif
(stat-func-or-assign)	(, :=, [
$\langle \text{stat} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq} \rangle$	if, while, for, break, return, id
$\langle \text{stat-seq-tail} \rangle$	if, while, for, break, return, id, ϵ
(param)	id
⟨ret-type⟩	$:, \epsilon$
(param-list-tail)	$,,\epsilon$
(param-list)	id, ϵ
(optional-init)	$:=,\epsilon$
(id-list-tail)	$ \; ,, \epsilon $
$\langle id$ -list \rangle	id
$\langle \text{type-id} \rangle$	id
$\langle \text{type-dim} \rangle$	$[,\epsilon$
$\langle \text{type} \rangle$	array, id
(funct-declaration)	function
(var-declaration)	var
$\langle \text{type-declaration} \rangle$	type
(funct-declaration-list)	function, ϵ
(var-declaration-list)	$ $ var, ϵ
. ,	1

```
 \begin{array}{c|c} \langle \text{type-declaration-list} \rangle & \text{type, } \epsilon \\ \langle \text{declaration-segment} \rangle & \text{function, var, type, } \epsilon \\ \langle \text{tiger-program} \rangle & \text{let} \\ \end{array}
```

non-terminal	follow set
$\langle \text{lvalue-tail} \rangle$:=, *, / , +, -, =, <, >, <=, >=, <>, &
$\langle lvalue-tail \rangle$, if, while, for, break, return, id, endif, end,), ,, ,], then, do, to, ;
$\langle \text{expr-list-tail} \rangle$	
$\langle \text{expr-list} \rangle$	
$\langle \text{expr-tail} \rangle$	if, while, for, break, return, id, endif, end,), ,, ,], then, do, to, ;
$\langle \text{or expr-tail} \rangle$	if, while, for, break, return, id, endif, end, ,), ,, ,], then, do, to, ;
$\langle and expr-tail \rangle$	if, while, for, break, return, id, endif, end, & $, , \rangle, ,, , $, then, do, to, ;
$\langle \text{compare-tail} \rangle$	if, while, for, break, return, id, endif, end
$\langle \text{compare-tail} \rangle$	[&,],,,,,], then, do, to, ;, =, <, >, <=, >=, <>
$\langle \text{term-tail} \rangle$	if, while, for, break, return, id, endif, end, & $, ,$
$\langle \text{term-tail} \rangle$	$[\ ,\ ,\], \text{ then, do, to, };,=,<,>,<=,>=,<>,+,-$
$\langle \text{stat-assign-tail} \rangle$	if, while, for, break, return, id, endif, end
$\langle stat-assign-id \rangle$	if, while, for, break, return, id, endif, end
$\langle \text{stat-seq-tail} \rangle$	endif, end
$\langle { m ret-type} \rangle$	begin
$\langle \text{param-list-tail} \rangle$	
$\langle param-list \rangle$	
$\langle { m optional\mbox{-}init} angle$	function, in
$\langle id$ -list-tail \rangle	:
$\langle { m type-dim} \rangle$	of
$\langle funct-declaration-list \rangle$	in
$\langle var\text{-declaration-list} \rangle$	function, in
$\langle \text{type-declaration-list} \rangle$	var, function, in
$\langle {\rm declaration\text{-}segment} \rangle$	in

Note, if there is no corresponding rule, then that means a parser error is generated.

Note, errors are handled by dropping tokens until a valid token is found.

symbol	next token	rule
$\langle addop \rangle$	+	+
$\langle \mathrm{addop} \rangle$	-	-
$\langle and expr \rangle$	($\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	nil	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	STRLIT	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	INTLIT	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	id	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr \rangle$	-	$\langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	<	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	>	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	>=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	<=	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	<>	$\langle \text{compop} \rangle \langle \text{compare} \rangle \langle \text{andexpr-tail} \rangle$
$\langle and expr-tail \rangle$	if	ϵ
$\langle and expr-tail \rangle$	while	ϵ
$\langle \text{andexpr-tail} \rangle$	for	ϵ

$\langle and expr-tail \rangle$	break	$\mid \epsilon$
(andexpr-tail)	return	ϵ
(andexpr-tail)	id	ϵ
(andexpr-tail)	endif	ϵ
(andexpr-tail)	end	ϵ
(andexpr-tail)	&	ϵ
(andexpr-tail)		ϵ
(andexpr-tail))	ϵ
(andexpr-tail)	,	ϵ
$\langle \text{andexpr-tail} \rangle$	ĺĺ	ϵ
$\langle \text{andexpr-tail} \rangle$	then	ϵ
$\langle and expr-tail \rangle$	do	ϵ
$\langle and expr-tail \rangle$	to	ϵ
$\langle and expr-tail \rangle$;	ϵ
$\langle andop \rangle$	&	&
$\langle \text{compare} \rangle$	($\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle compare \rangle$	nil	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle compare \rangle$	STRLIT	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle compare \rangle$	INTLIT	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle compare \rangle$	id	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare} \rangle$	_	$\langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare-tail} \rangle$	+	$\langle \text{addop} \rangle \langle \text{term} \rangle \langle \text{compare-tail} \rangle$
$\langle \text{compare-tail} \rangle$		\langle addop \rangle \text{\term} \rangle
$\langle \text{compare-tail} \rangle$	if	ϵ
$\langle \text{compare-tail} \rangle$	while	ϵ
$\langle \text{compare-tail} \rangle$	for	ϵ
$\langle \text{compare-tail} \rangle$	break	ϵ
$\langle \text{compare-tail} \rangle$	return	ϵ
$\langle \text{compare-tail} \rangle$	id	ϵ
⟨compare-tail⟩	endif	ϵ
⟨compare-tail⟩	end	ϵ
⟨compare-tail⟩	&	ϵ
$\langle \text{compare-tail} \rangle$		ϵ
$\langle \text{compare-tail} \rangle$		ϵ
$\langle \text{compare-tail} \rangle$,	ϵ
$\langle \text{compare-tail} \rangle$, 1	ϵ
$\langle \text{compare-tail} \rangle$	then	ϵ
$\langle \text{compare-tail} \rangle$	do	ϵ
$\langle \text{compare-tail} \rangle$	to	ϵ
$\langle \text{compare-tail} \rangle$		ϵ
$\langle \text{compare-tail} \rangle$; =	ϵ
$\langle \text{compare-tail} \rangle$	<	ϵ
$\langle \text{compare-tail} \rangle$	>	ϵ
$\langle \text{compare-tail} \rangle$		ϵ
$\langle \text{compare-tail} \rangle$	_ _	ϵ
$\langle \text{compare-tail} \rangle$	<>	ϵ
$\langle \text{compare-vari} \rangle$	=	=
$\langle \text{compop} \rangle$	<	_ <
$\langle \text{compop} \rangle$	>	>
(compop)		
(compop)		
(compop)	>= <>	>= <>
/	nil	nil
$\langle \text{const} \rangle$	1111	1111

```
\langle const \rangle
                                  STRLIT
                                                    STRLIT
\langle const \rangle
                                  INTLIT
                                                    INTLIT
(declaration-segment)
                                                    \(\lambda\) type-declaration-list\(\rangle\) \(\lambda\) ar-declaration-list\(\rangle\) \(\lambda\) funct-declaration-list\(\rangle\)
                                  function
                                                    \(\lambda\) type-declaration-list\(\rangle\) \(\lambda\) declaration-list\(\rangle\)
(declaration-segment)
                                  var
(declaration-segment)
                                  type
                                                    \langle type-declaration-list \rangle \langle var-declaration-list \rangle \langle funct-declaration-list \rangle
(declaration-segment)
                                  in
⟨expr-list⟩
                                  )
⟨expr-list⟩
                                  (
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
(expr-list)
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
                                  nil
⟨expr-list⟩
                                  STRLIT
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
⟨expr-list⟩
                                  INTLIT
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
⟨expr-list⟩
                                  id
⟨expr-list⟩
                                                    ⟨expr⟩ ⟨expr-list-tail⟩
                                  )
⟨expr-list-tail⟩
⟨expr-list-tail⟩
                                                      ⟨expr⟩ ⟨expr-list-tail⟩
                                  (
\langle \exp r \rangle
                                                    ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
                                                    ⟨orexpr⟩ ⟨expr-tail⟩
                                  nil
\langle \exp r \rangle
                                  STRLIT
                                                    (orexpr) (expr-tail)
                                  INTLIT
                                                    ⟨orexpr⟩ ⟨expr-tail⟩
\langle \exp r \rangle
\langle \exp r \rangle
                                                    (orexpr) (expr-tail)
                                  id
\langle \exp r \rangle
                                                    (orexpr) (expr-tail)
(expr-tail)
                                                    ⟨orop⟩ ⟨orexpr⟩ ⟨expr-tail⟩
(expr-tail)
                                  if
                                  while
(expr-tail)
                                                    \epsilon
⟨expr-tail⟩
                                  for
⟨expr-tail⟩
                                  break
                                                    \epsilon
⟨expr-tail⟩
                                  return
                                                    \epsilon
(expr-tail)
                                  id
                                                    \epsilon
⟨expr-tail⟩
                                  endif
                                                    \epsilon
⟨expr-tail⟩
                                  end
                                                    \epsilon
(expr-tail)
                                  )
                                                    \epsilon
⟨expr-tail⟩
                                                    \epsilon
(expr-tail)
                                                    \epsilon
⟨expr-tail⟩
                                  then
                                                    \epsilon
(expr-tail)
                                  do
                                                    \epsilon
(expr-tail)
                                  to
                                                    \epsilon
(expr-tail)
\langle factor \rangle
                                  (
                                                    ⟨unaryminus⟩
(factor)
                                  nil
                                                    (unaryminus)
\langle factor \rangle
                                  STRLIT
                                                    ⟨unaryminus⟩
(factor)
                                  INTLIT
                                                    ⟨unaryminus⟩
(factor)
                                  id
                                                    (unaryminus)
(factor)
                                                    - (unaryminus)
(funct-declaration)
                                  function
                                                    function id (\langle param-list\rangle ) \langle ret-type \rangle begin \langle stat-seq \rangle end ;
⟨funct-declaration-list⟩
                                  function
                                                    ⟨funct-declaration⟩ ⟨funct-declaration-list⟩
⟨funct-declaration-list⟩
                                  in
                                                    \epsilon
⟨id-list⟩
                                  id
                                                    id (id-list-tail)
(id-list-tail)
⟨id-list-tail⟩
                                                    , id (id-list-tail)
                                  id
                                                    id (lvalue-tail)
(lvalue)
(lvalue-tail)
                                                    [ \langle expr \rangle ] \langle lvalue-tail \rangle
(lvalue-tail)
                                  :=
                                                    \epsilon
                                  *
(lvalue-tail)
                                                    \epsilon
```

```
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      +
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      =
                                                          \epsilon
(lvalue-tail)
                                      <
                                                          \epsilon
                                      >
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      \leq =
                                                          \epsilon
(lvalue-tail)
                                      >=
                                                          \epsilon
(lvalue-tail)
                                      <>
                                                          \epsilon
(lvalue-tail)
                                      &
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      if
                                                          \epsilon
(lvalue-tail)
                                      while
                                                          \epsilon
(lvalue-tail)
                                      for
                                                          \epsilon
(lvalue-tail)
                                      break
                                                          \epsilon
(lvalue-tail)
                                      return
                                                          \epsilon
(lvalue-tail)
                                      id
                                                          \epsilon
(lvalue-tail)
                                      endif
                                                          \epsilon
(lvalue-tail)
                                      end
                                                          \epsilon
(lvalue-tail)
                                      )
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
(lvalue-tail)
                                      then
                                                          \epsilon
(lvalue-tail)
                                      do
                                                          \epsilon
(lvalue-tail)
                                      to
                                                          \epsilon
(lvalue-tail)
                                                          \epsilon
\langle \text{mulop} \rangle
\langle \text{mulop} \rangle
                                                          := \langle const \rangle
⟨optional-init⟩
                                      :=
(optional-init)
                                      function
⟨optional-init⟩
                                      in
\langle orexpr \rangle
                                      (
                                                           ⟨andexpr⟩ ⟨orexpr-tail⟩
                                      nil
                                                           ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                      STRLIT
                                                           ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
\langle orexpr \rangle
                                      INTLIT
                                                           (andexpr) (orexpr-tail)
\langle orexpr \rangle
                                      id
                                                           ⟨andexpr⟩ ⟨orexpr-tail⟩
\langle orexpr \rangle
                                                           (andexpr) (orexpr-tail)
(orexpr-tail)
                                      &
                                                           ⟨andop⟩ ⟨andexpr⟩ ⟨orexpr-tail⟩
                                      if
(orexpr-tail)
(orexpr-tail)
                                      while
                                                          \epsilon
(orexpr-tail)
                                      for
                                                          \epsilon
(orexpr-tail)
                                      break
                                                          \epsilon
(orexpr-tail)
                                      return
                                                          \epsilon
(orexpr-tail)
                                      id
                                                          \epsilon
(orexpr-tail)
                                      endif
                                                          \epsilon
(orexpr-tail)
                                      end
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                      )
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                                          \epsilon
                                      then
(orexpr-tail)
                                                          \epsilon
(orexpr-tail)
                                      do
                                                          \epsilon
(orexpr-tail)
                                      to
                                                          \epsilon
```

```
(orexpr-tail)
                                               \epsilon
\langle \text{orop} \rangle
                               id
                                               id: \langle type-id \rangle
(param)
(param-list)
                               )
(param-list)
                               id
                                               ⟨param⟩ ⟨param-list-tail⟩
(param-list-tail)
                               )
(param-list-tail)
                                                 ⟨param⟩ ⟨param-list-tail⟩
⟨ret-type⟩
                               begin
(ret-type)
                                               : (type-id)
(stat-assign)
                               id
                                               id (stat-assign-id)
                                               - (unaryminus) (stat-assign-tail)
(stat-assign)
                               (
                                               (\langle \expr \rangle) \langle \operatorname{stat-assign-tail} \rangle
(stat-assign)
(stat-assign)
                               nil
                                               (const) (stat-assign-tail)
⟨stat-assign⟩
                               STRLIT
                                               \langle const \rangle \langle stat-assign-tail \rangle
                               INTLIT
                                               ⟨const⟩ ⟨stat-assign-tail⟩
(stat-assign)
⟨stat-assign-id⟩
                               end
(stat-assign-id)
                               endif
                                               \epsilon
(stat-assign-id)
                               id
(stat-assign-id)
                               return
                                               \epsilon
(stat-assign-id)
                               break
                                               \epsilon
(stat-assign-id)
                               for
                                               \epsilon
(stat-assign-id)
                               while
                                               \epsilon
(stat-assign-id)
                               if
(stat-assign-id)
                                               (lvalue-tail) (stat-assign-tail)
                               &
(stat-assign-id)
                                               (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                               <>
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                               >=
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                               <=
                                               (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                               >
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                               <
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
(stat-assign-id)
                               =
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
(stat-assign-id)
                                               ⟨lvalue-tail⟩ ⟨stat-assign-tail⟩
                               +
(stat-assign-id)
                                               (lvalue-tail) (stat-assign-tail)
(stat-assign-id)
                                               (lvalue-tail) (stat-assign-tail)
                                               \langle lvalue-tail \rangle \langle stat-assign-tail \rangle
(stat-assign-id)
(stat-assign-id)
                               (
                                               (\langle expr-list \rangle);
⟨stat-assign-id⟩
                                               (lvalue-tail) (stat-assign-tail)
(stat-assign-tail)
                               end
                                               \epsilon
(stat-assign-tail)
                               endif
                                               \epsilon
                               id
(stat-assign-tail)
                                               \epsilon
(stat-assign-tail)
                               return
(stat-assign-tail)
                               break
                                               \epsilon
                               for
(stat-assign-tail)
                                               \epsilon
                               while
(stat-assign-tail)
                                               \epsilon
                               if
(stat-assign-tail)
(stat-assign-tail)
                                               (expr-tail)
(stat-assign-tail)
                               &
                                               (orexpr-tail)
(stat-assign-tail)
                               <>
                                               (andexpr-tail)
(stat-assign-tail)
                                               (andexpr-tail)
                               >=
(stat-assign-tail)
                                               (andexpr-tail)
                               <=
(stat-assign-tail)
                               >
                                               (andexpr-tail)
(stat-assign-tail)
                               <
                                               (andexpr-tail)
(stat-assign-tail)
                               =
                                               (andexpr-tail)
```

```
(stat-assign-tail)
                                                          ⟨compare-tail⟩
(stat-assign-tail)
                                      +
                                                          ⟨compare-tail⟩
(stat-assign-tail)
                                                          ⟨term-tail⟩
(stat-assign-tail)
                                                          ⟨term-tail⟩
⟨stat-func-or-assign⟩
                                      (
                                                          (\langle \text{expr-list} \rangle);
⟨stat-func-or-assign⟩
                                                          \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
                                      :=
⟨stat-func-or-assign⟩
                                                          \langle \text{lvalue-tail} \rangle := \langle \text{stat-assign} \rangle
⟨stat-if-tail⟩
                                      else
                                                          else (stat-seg) endif;
⟨stat-if-tail⟩
                                      endif
                                                          endif;
                                                          if \langle \exp r \rangle then \langle \text{stat-seq} \rangle \langle \text{stat-if-tail} \rangle
\langle stat \rangle
                                      if
                                      while
                                                          while \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
(stat)
                                                          for id := \langle \exp r \rangle to \langle \exp r \rangle do \langle \text{stat-seq} \rangle enddo;
⟨stat⟩
                                      for
\langle stat \rangle
                                      break
                                                          break:
\langle stat \rangle
                                      return
                                                          return (expr);
                                                          id (stat-func-or-assign)
\langle stat \rangle
                                      id
⟨stat-seq⟩
                                      if
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
                                      while
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq⟩
⟨stat-seq⟩
                                      for
                                                          (stat) (stat-seq-tail)
⟨stat-seg⟩
                                      break
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seg⟩
                                      return
⟨stat-seg⟩
                                      id
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                      endif
(stat-seq-tail)
                                      end
                                                          \epsilon
                                      if
(stat-seq-tail)
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
                                      while
(stat-seq-tail)
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
⟨stat-seq-tail⟩
                                      for
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                      break
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
(stat-seq-tail)
                                      return
                                                          (stat) (stat-seq-tail)
⟨stat-seq-tail⟩
                                      id
                                                          ⟨stat⟩ ⟨stat-seq-tail⟩
                                                          ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
\langle \text{term} \rangle
                                      id
                                                          \(\factor\) \(\text{term-tail}\)
                                      INTLIT
\langle \text{term} \rangle
                                                          ⟨factor⟩ ⟨term-tail⟩
                                      STRLIT
                                                          ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
\langle \text{term} \rangle
                                      nil
                                                          ⟨factor⟩ ⟨term-tail⟩
\langle \text{term} \rangle
                                                          ⟨factor⟩ ⟨term-tail⟩
                                      (
⟨term-tail⟩
                                                          \langle mulop \langle \langle factor \rangle \langle term-tail \rangle
⟨term-tail⟩
                                                          \langle mulop \langle \text{factor} \langle \text{term-tail} \rangle
⟨term-tail⟩
                                      )
                                                          \epsilon
⟨term-tail⟩
                                                          \epsilon
                                      &
⟨term-tail⟩
                                                          \epsilon
⟨term-tail⟩
                                      end
                                                          \epsilon
⟨term-tail⟩
                                      endif
                                                          \epsilon
⟨term-tail⟩
                                      id
                                                          \epsilon
⟨term-tail⟩
                                      return
                                                          \epsilon
⟨term-tail⟩
                                      break
                                                          \epsilon
⟨term-tail⟩
                                      for
                                                          \epsilon
⟨term-tail⟩
                                      while
                                                          \epsilon
⟨term-tail⟩
                                      if
                                                          \epsilon
⟨term-tail⟩
                                                          \epsilon
⟨term-tail⟩
                                      +
                                                          \epsilon
⟨term-tail⟩
                                      <>
                                                          \epsilon
⟨term-tail⟩
                                      >=
                                                          \epsilon
⟨term-tail⟩
                                      <=
                                                          \epsilon
```

```
⟨term-tail⟩
                               >
                                                \epsilon
⟨term-tail⟩
                               <
                                                \epsilon
⟨term-tail⟩
                               =
                                                \epsilon
⟨term-tail⟩
                                                \epsilon
⟨term-tail⟩
                               to
                                                \epsilon
⟨term-tail⟩
                               do
                                                \epsilon
⟨term-tail⟩
                               then
                                                \epsilon
⟨term-tail⟩
                                                \epsilon
⟨term-tail⟩
                                                let (declaration-segment) in (stat-seq) end
⟨tiger-program⟩
                               let
                                                array [ INTLIT ] of \( \text{type-dim} \) of \( \text{type-id} \)
⟨type⟩
                               array
                                                \langle \text{type-id} \rangle
(type)
                               id
                                                ⟨type-declaration⟩ ⟨type-declaration-list⟩
⟨type-declaration-list⟩
                               type
⟨type-declaration-list⟩
                               var
⟨type-declaration-list⟩
                               function
⟨type-declaration-list⟩
                               in
                                                type id = \langle type \rangle;
(type-declaration)
                               type
                                                [INTLIT] \langle type-dim \rangle
⟨type-dim⟩
⟨type-dim⟩
                               of
⟨type-id⟩
                               id
                                                id
                                                (\langle expr \rangle)
⟨unaryminus⟩
                               (
                                                \langle const \rangle
(unaryminus)
                               nil
(unaryminus)
                               STRLIT
                                                \langle const \rangle
                                                \langle const \rangle
(unaryminus)
                               INTLIT
(unaryminus)
                               id
                                                (lvalue)
(var-declaration-list)
                               function
⟨var-declaration-list⟩
                               in
(var-declaration-list)
                                                (var-declaration) (var-declaration-list)
                               var
(var-declaration)
                                                var (id-list) : (type-id) (optional-init) ;
                               var
```