Modeling interactions and the use of CONTRAST statement for post-fitting comparisons

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Outline

Concepts of effect-measure modification/interaction

SAS coding schemes

 Examples of post-fitting comparisons under different coding schemes

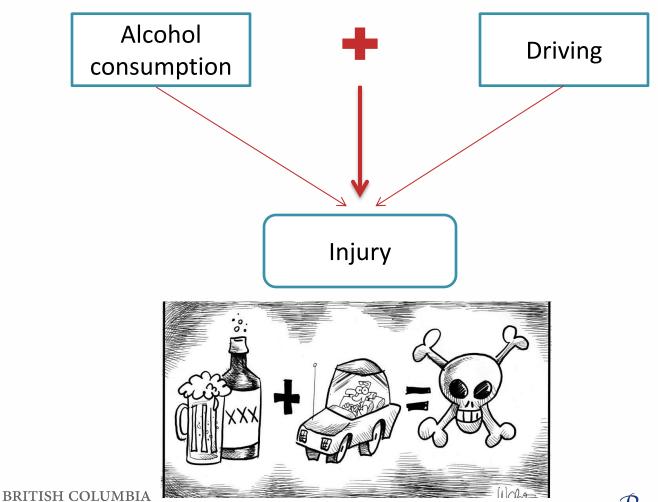
Summary







Examples of effect-measure modification



CENTRE for EXCELLENCE

in HIV/AIDS

Examples of effect-measure modification

- Cigarette smoking during pregnancy is associated with low birth weight
- Maternal age is also associated with variations in birth weight
- Smoking has a bigger effect on risk of low birth weight in older moms than younger moms



Effect-measure modification

 Effect-measure modification refers to the situation in which a measure of effect changes over values of some other variable







Effect-measure modification

 Effect-measure modification refers to the situation in which a measure of effect changes over values of some other variable

- Better understanding of causation
- Identification of "high-risk" groups
- Target interventions at specific subgroups







Measures of interaction

• Example:

Additive statistical model

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 (x_1 * x_2) + \varepsilon$$







Measures of interaction

Example:

Additive statistical model

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \varepsilon$$

Effect x_1 on y is measured by β_1







Measures of interaction

• Example:

Additive statistical model

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 (x_1 * x_2) + \varepsilon$$

Effect x_1 on y is measured by $\beta_1 + \beta_3 x_2$







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Summary







Hypothetical example

```
DATA Injury data;
   INPUT Driving Alcohol Injury Count @@;
   DATALINES;
      1 20
0
   0
                 0 0 46
                 1 0 20
0
   1
      1 20
   2 1 30
                 2 0 30
   0 1 80
                 0 0 30
                 1 0 28
1
   1
      1 70
   2 1 100
                 2 0 11
   0 1 80
                 0 0 60
2
   1 1 450
                 1 0 48
      1 500
                 2 0 52
RUN;
```

Driving Skill:

Driving 0: Excellent

1: Good

2: Bad

Alcohol Consumption:

Alcohol 0: Low

1: Moderate

2: High

Outcome:

Injury 0: No

l: Yes







Coding Schemes

Three coding schemes available in SAS:

- Effect coding
- Reference coding
- Indicator (GLM or dummy) coding







Effect coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving Alcohol / Ref=First;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```







Effect coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving Alcohol / Ref=First;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```

- Default coding for LOGISTIC procedure
- Can be specified with the PARAM=EFFECT option in the CLASS statement for some other procedures (e.g. GENMOD)







Effect coding

Class Level Information

| Class | Value | Design Variables | | |
|---------|-------|---------------------|-------|--|
| | | D_1 | D_2 | |
| Driving | 0 | -1 | -1 | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |

Replace the actual variable in the design matrix with a set of variables that use values of **-1**,**0** or **1**

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$







Reference coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving(Ref='0') Alcohol(Ref='0') / Param=ref;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```







Reference coding

Class Level Information

| Class | Value | Design Variables | | |
|---------|-------|-----------------------|-----------------------|--|
| Driving | 0 | D ₁ | D ₂ | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |
| | | | | |

Replace the actual variable in the design matrix with a set of variables that use values of **0** or **1**

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$







Comparisons between effect and reference coding

- Effect coding
 - A main effect parameter is interpreted as the difference of the level's effect from the average effect of all the levels

- Reference coding
 - A main effect parameter is interpreted as the difference in the level's effect compared to the reference level







Comparisons between effect and reference coding

Effect coding

| Parameter | | | DF | Est |
|-----------------|---|---|----|-----|
| Intercept | | | 1 | 0 |
| Driving | 1 | | 1 | 0 |
| Driving | 2 | | 1 | 0 |
| Alcohol | 1 | | 1 | 0 |
| Alcohol | 2 | | 1 | 0 |
| Driving*Alcohol | 1 | 1 | 1 | -0 |
| Driving*Alcohol | 1 | 2 | 1 | 0 |
| Driving*Alcohol | 2 | 1 | 1 | 0 |
| Driving*Alcohol | 2 | 2 | 1 | 0 |
| | | | | |

Estimate 0.8956 0.4725 0.7007 0.1558 0.5946 -0.6077 0.2446 0.4859 0.0724 Reference coding

| Parameter | | | DF | / Estimate |
|-----------------|---|---|----|------------|
| Intercept | | | 1 | -0.8329 |
| Driving | 1 | | 1 | 1.8137 |
| Driving | 2 | | 1 | 1.1205 |
| Alcohol | 1 | | 1 | 0.8329 |
| Alcohol | 2 | | 1 | 0.8329 |
| Driving*Alcohol | 1 | 1 | 1 | -0.8974 |
| Driving*Alcohol | 1 | 2 | 1 | 0.3936 |
| Driving*Alcohol | 2 | 1 | 1 | 1.1175 |
| Driving*Alcohol | 2 | 2 | 1 | 1.1428 |
| | | | | |







Outline

Concepts of effect-measure modification/interaction

SAS coding schemes

 Examples of post-fitting comparisons under different coding schemes

Summary







Hypothetical example

• Question:

What's the odds ratio for having "bad" driving skill compared with "excellent" driving skill, when have "high" level of alcohol consumption before driving?

Driving Skill:

Driving 0: Excellent

1: Good

2: Bad

Alcohol Consumption:

Alcohol 0: Low

1: Moderate

2: High

Driving = 2 & Alcohol = 2

VS.

Driving = 0 & Alcohol = 2

| Class | Value | Desi Varia | |
|---------|-------|---------------|----------------|
| | | D_1 | D_2 |
| Driving | 0 | -1 | -1 |
| | 1 | 1 | 0 |
| | 2 | 0 | 1 |
| | | | |
| | | ${f A_1}$ | \mathbf{A}_2 |
| Alcohol | 0 | -1 | -1 |
| | 1 | 1 | 0 |
| | 2 | 0 | 1 |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$







| Class | Value | Desi Varia | | |
|---------|-------|----------------|----------------|--|
| | | $\mathtt{D_1}$ | D_2 | |
| Driving | 0 | -1 | -1 | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |
| | | | | |
| | | ${f A_1}$ | \mathbf{A}_2 | |
| Alcohol | 0 | -1 | -1 | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

Driving = 2 & Alcohol = 2
$$D_1 = 0, D_2 = 1$$

 $A_1 = 0, A_2 = 1$

$$\log(Odds_{Driving2Alcohol2}) = a + b_2 + c_2 + g_4$$







| Class | Value | Design Variables | | | |
|---------|-------|---------------------|----------------|--|--|
| | | D_1 | D_2 | | |
| Driving | 0 | -1 | -1 | | |
| | 1 | 1 | 0 | | |
| | 2 | 0 | 1 | | |
| | | | | | |
| | | ${f A}_1$ | \mathbf{A}_2 | | |
| Alcohol | 0 | -1 | -1 | | |
| | 1 | 1 | 0 | | |
| | 2 | 0 | 1 | | |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

Driving = 0 & Alcohol = 2
$$D_1 = -1, D_2 = -1$$

$$A_1 = 0, A_2 = 1$$

$$\log(Odds_{Driving0Alcohol2}) = a - b_1 - b_2 + c_2 - g_2 - g_4$$







VS.

Driving = 0 & Alcohol = 2

$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = b_1 + 2b_2 + g_2 + 2g_4$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(b_1 + 2b_2 + g_2 + 2g_4)$$







$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = b_1 + 2b_2 + g_2 + 2g_4$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(b_1 + 2b_2 + g_2 + 2g_4)$$

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

Driving*Alcohol: 0







CONTRAST Statement:

CONTRAST 'label' row-description<,...,row-description></ options>;

```
PROC LOGISTIC Data=Injury_data Descending;
Freq count;
Class Driving Alcohol / Ref=First;
Model Injury= Driving Alcohol Driving*Alcohol;
Contrast "D 2vs0 at A 2"
Driving 1 2
Driving*Alcohol 0 1 0 2 /Estimate=both;
RUN;
```







Contrast Estimation and Testing Results by Row

| | Standard | | | | | | Wald | | | |
|----------------------------------|-----------|------------------|------------------|----------|------------------|---------------------------|--------------------|------------------|--|--|
| Contrast Ty | ype Row I | Estimate | Error | Alpha Co | onfidence | Limits Cl | ni-Square P | r > ChiSq | | |
| D 2vs0 at A 2 P. D 2vs0 at A 2 E | | 2.2634 9.6154 | 0.2965 2.8507 | | 1.6823 5.3778 | 2.8 444 17.1920 | 58.2818 58.2818 | <.0001 <.0001 | | |

| Class | Value | Design Variables | | | |
|---------|-------|---------------------|----------------|--|--|
| | | D_1 | D_2 | | |
| Driving | 0 | 0 | 0 | | |
| | 1 | 1 | 0 | | |
| | 2 | 0 | 1 | | |
| | | | | | |
| | | ${f A}_1$ | \mathbf{A}_2 | | |
| Alcohol | 0 | 0 | 0 | | |
| | 1 | 1 | 0 | | |
| | 2 | 0 | 1 | | |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$







| Class | Value | Design Variables | | |
|---------|-------|---------------------|----------------|--|
| | | D_1 | D_2 | |
| Driving | 0 | 0 | 0 | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |
| | | | | |
| | | ${f A}_1$ | \mathbf{A}_2 | |
| Alcohol | 0 | 0 | 0 | |
| | 1 | 1 | 0 | |
| | 2 | 0 | 1 | |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

$$D_1 = 0, D_2 = 1$$

 $A_1 = 0, A_2 = 1$

$$\log(Odds_{Driving2Alcohol2}) = a + b_2 + c_2 + g_4$$







| Class | Value | Desi Varia | |
|---------|-------|---------------|----------------|
| | | D_1 | D_2 |
| Driving | 0 | 0 | 0 |
| | 1 | 1 | 0 |
| | 2 | 0 | 1 |
| | | | |
| | | ${f A}_1$ | \mathbf{A}_2 |
| Alcohol | 0 | 0 | 0 |
| | 1 | 1 | 0 |
| | 2 | 0 | 1 |

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

Driving = 0 & Alcohol = 2
$$D_1 = 0, D_2 = 0$$

$$A_1 = 0, A_2 = 1$$

$$\log(Odds_{Driving0Alcohol2}) = a + c_2$$







VS.

Driving = 0 & Alcohol = 2

$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = b_2 + g_4$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(b_2 + g_4)$$







$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = b_2 + g_4$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(b_2 + g_4)$$

Driving:

$$\log(Odds) = a + b_1D_1 + b_2D_2 + c_1A_1 + c_2A_2 + g_1D_1A_1 + g_2D_1A_2 + g_3D_2A_1 + g_4D_2A_2$$

Driving*Alcohol: 0







CONTRAST Statement:

CONTRAST 'label' row-description<,...,row-description></ options>;

```
PROC LOGISTIC Data=Injury_data Descending;
Freq count;
Class Driving(Ref='0') Alcohol(Ref='0') / Param=ref;
Model Injury= Driving Alcohol Driving*Alcohol;
Contrast "D 2vs0 at A 2"
Driving 0 1
Driving*Alcohol 0 0 0 1 / Estimate=both;
RUN;
```







Contrast Estimation and Testing Results by Row

| | | | | Standard | | | | Wald | | | |
|---------------|------|-----|-----------------|----------|-------|------------|---------|------------|------|---------|--|
| Contrast | Type | Row | Estimate | Error | Alpha | Confidence | Limits | Chi-Square | Pr 3 | > ChiSq | |
| D 2vs0 at A 2 | PARM | 1 | 2.2634 | 0.2965 | 0.05 | 1.6823 | 2.8444 | 58.2818 | | <.0001 | |
| D 2vs0 at A 2 | EXP | 1 | 9.6154 | 2.8507 | 0.05 | 5.3778 | 17.1920 | 58.2818 | | <.0001 | |

Summary

- Effect-measure modification is an important concept in public health research
- Understanding SAS coding scheme can help better interpret the parameter estimates
- Pay attention to the design matrix
- The selected parameterization method has a profound effect on how CONTRAST statements are specified and the associated hypothesis tests







References

- Rothman, K. J. (2012). *Epidemiology: an introduction*. Oxford University Press.
- Rothman, K. J., Greenland, S., & Lash, T. L. (Eds.). (2008). *Modern epidemiology*. Lippincott Williams & Wilkins.
- Kiernan, K. (2011). CONTRAST and ESTIMATE statements made easy: the LSMESTRIMATE statement. In *Statistics and Data Analysis SAS Global Forum*.
- Pritchard, M.L., Pasta, D.J. Head of the CLASS: Impress your colleagues with a superior understanding of the CLASS statement in PROC LOGISTIC. Statistics and Data Analysis.
- Pasta, D. J. (2011). Those confounded interactions: building and interpreting a model with many potential confounders and interactions. In Statistics and Data Analysis SAS Global Forum.
- Pasta, D. J. (2005). Parameterizing models to test the hypotheses you want: coding indicator variables and modified continuous variables. In *Proceedings of the Thirtieth Annual SAS Users Group International Conference* (pp. 212-30).
- Fox, S. H., Koepsell, T. D., & Daling, J. R. (1994). Birth weight and smoking during pregnancy-effect modification by maternal age. American journal of epidemiology, 139(10), 1008-1015.







Additional information







Indicator (GLM or dummy) coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving Alcohol / Param=glm;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```







Indicator (GLM or dummy) coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving Alcohol / Param=glm;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```

- In PROC LOGISTIC, this can be specified with the PARAM=GLM option
- Default coding in procedures including GLM, MIXED, GLMMIX, GENMOD







Indicator (GLM or dummy) coding

```
PROC LOGISTIC Data=Injury_data Descending;
   Freq count;
   Class Driving Alcohol / Param=glm;
   Model Injury= Driving Alcohol Driving*Alcohol;
RUN;
```

Class Level Information

| Class | Value | Design Variables | | | | | |
|---------|--------|---------------------|--------|--------|--|--|--|
| Driving | 0 | 1 | 0 | 0 | | | |
| | 1 2 | 0 | 1 0 | 1 | | | |
| Alcohol | 0 | 1 | 0 | 0 | | | |
| | 1 2 | 0 | 0 | 0 1 | | | |

Replace the actual variable in the design matrix with a set of variables that use values of 0 or 1

| Value | Design Variables | | | | | |
|-------|-----------------------|--|---|--|--|--|
| | D_1 | D_2 | D_3 | | | |
| 0 | 1 | 0 | 0 | | | |
| 1 | 0 | 1 | 0 | | | |
| 2 | 0 | 0 | 1 | | | |
| | ${\mathtt A}_1$ | \mathbf{A}_2 | A ₃ | | | |
| 0 | 1 | 0 | 0 | | | |
| 1 | 0 | 1 | 0 | | | |
| 2 | 0 | 0 | 1 | | | |
| | 0 1 2 0 1 | Value Varial D1 0 1 0 2 0 A1 0 1 0 1 0 | Value Variables D1 D2 0 1 0 1 0 1 2 0 0 A1 A2 0 1 0 1 0 1 0 1 0 1 0 1 | | | |

$$\begin{aligned} \log(Odds) &= a + b_1 D_1 + b_2 D_2 + b_3 D_3 \\ + c_1 A_1 + c_2 A_2 + c_3 A_3 \\ + g_1 D_1 A_1 + g_2 D_1 A_2 + g_3 D_1 A_3 \\ + g_4 D_2 A_1 + g_5 D_2 A_2 + g_6 D_2 A_3 \\ + g_7 D_3 A_1 + g_8 D_3 A_2 + g_9 D_3 A_3 \end{aligned}$$







| Class | Design Value Variables | | | | | | | |
|---------|---------------------------|-----------------|----------------|-----------------------|--|--|--|--|
| | | D_1 | D_2 | D_3 | | | | |
| Driving | 0 | 1 | 0 | 0 | | | | |
| | 1 | 0 | 1 | 0 | | | | |
| | 2 | 0 | 0 | 1 | | | | |
| | | ${\mathtt A}_1$ | \mathbf{A}_2 | A ₃ | | | | |
| Alcohol | 0 | 1 | 0 | 0 | | | | |
| | 1 | 0 | 1 | 0 | | | | |
| | 2 | 0 | 0 | 1 | | | | |

$$\begin{aligned} \log(Odds) &= a + b_1 D_1 + b_2 D_2 + b_3 D_3 \\ + c_1 A_1 + c_2 A_2 + c_3 A_3 \\ + g_1 D_1 A_1 + g_2 D_1 A_2 + g_3 D_1 A_3 \\ + g_4 D_2 A_1 + g_5 D_2 A_2 + g_6 D_2 A_3 \\ + g_7 D_3 A_1 + g_8 D_3 A_2 + g_9 D_3 A_3 \end{aligned}$$

Driving = 2 & Alcohol = 2
$$D_1 = 0, D_2 = 0, D_3 = 1$$

$$A_1 = 0, A_2 = 0, A_3 = 1$$

$$\log(Odds_{Driving2Alcohol2}) = a + b_3 + c_3 + g_9$$







| Class | Design Value Variables | | | | | | | |
|---------|---------------------------|-----------|----------------|-----------------------|--|--|--|--|
| | | D_1 | D_2 | D_3 | | | | |
| Driving | 0 | 1 | 0 | 0 | | | | |
| | 1 | 0 | 1 | 0 | | | | |
| | 2 | 0 | 0 | 1 | | | | |
| | | ${f A}_1$ | \mathbf{A}_2 | A ₃ | | | | |
| Alcohol | 0 | 1 | 0 | 0 | | | | |
| | 1 | 0 | 1 | 0 | | | | |
| | 2 | 0 | 0 | 1 | | | | |

$$\begin{aligned} \log(Odds) &= a + b_1 D_1 + b_2 D_2 + b_3 D_3 \\ + c_1 A_1 + c_2 A_2 + c_3 A_3 \\ + g_1 D_1 A_1 + g_2 D_1 A_2 + g_3 D_1 A_3 \\ + g_4 D_2 A_1 + g_5 D_2 A_2 + g_6 D_2 A_3 \\ + g_7 D_3 A_1 + g_8 D_3 A_2 + g_9 D_3 A_3 \end{aligned}$$

Driving = 0 & Alcohol = 2
$$D_1 = 1, D_2 = 0, D_3 = 0$$

$$A_1 = 0, A_2 = 0, A_3 = 1$$

$$\log(Odds_{Driving0Alcohol2}) = a + b_1 + c_3 + g_3$$







VS.

Driving = 0 & Alcohol = 2

$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = -b_1 + b_3 - g_3 + g_9$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(-b_1 + b_3 - g_3 + g_9)$$

$$\log(Odds) = a + b_1D_1 + b_2D_2 + b_3D_3 + c_1A_1 + c_2A_2 + c_3A_3 + g_1D_1A_1 + g_2D_1A_2 + g_3D_1A_3 + g_4D_2A_1 + g_5D_2A_2 + g_6D_2A_3$$

$$+ g_7 D_3 A_1 + g_8 D_3 A_2 + g_9 D_3 A_3$$







$$\log(Odds_{Driving2Alcohol2}) - \log(Odds_{Driving0Alcohol2}) = -b_1 + b_3 - g_3 + g_9$$

$$Odds_{Driving2Alcohol2}/Odds_{Driving0Alcohol2} = exp(-b_1 + b_3 - g_3 + g_9)$$

$$\begin{split} \log(Odds) &= a + b_1D_1 + b_2D_2 + b_3D_3 + c_1A_1 + c_2A_2 + c_3A_3 \\ &+ g_1D_1A_1 + g_2D_1A_2 + g_3D_1A_3 + \ g_4D_2A_1 + g_5D_2A_2 + g_6D_2A_3 \\ &\quad \mathbf{0} \qquad \mathbf{0} \qquad \mathbf{0} \qquad \mathbf{0} \qquad \mathbf{0} \end{split}$$

$$+g_7D_3A_1+g_8D_3A_2+g_9D_3A_3$$







CONTRAST Statement:

CONTRAST 'label' row-description<,...,row-description></ options>;

```
PROC LOGISTIC Data=Injury_data Descending;

Freq count;

Class Driving Alcohol / Param=glm;

Model Injury= Driving Alcohol Driving*Alcohol;

Contrast "D 2vs0 at A 2"

Driving -1 0 1

Driving*Alcohol 0 0 -1 0 0 0 0 1 /E Estimate=both;

RUN;
```







Coefficients of Contrast D 2vs0 at A 2

| Parameter | Row1 |
|------------------|------|
| Intercept | 0 |
| Driving0 | -1 |
| Driving1 | 0 |
| Driving2 | 1 |
| Alcohol0 | 0 |
| Alcohol1 | 0 |
| Alcohol2 | 0 |
| DrivingOAlcoholO | 0 |
| DrivingOAlcohol1 | 0 |
| DrivingOAlcohol2 | -1 |
| Driving1Alcohol0 | 0 |
| Driving1Alcohol1 | 0 |
| Driving1Alcohol2 | 0 |
| Driving2Alcohol0 | 0 |
| Driving2Alcohol1 | 0 |
| Driving2Alcohol2 | 1 |

Contrast Estimation and Testing Results by Row

| | | | | Standard | | | Wald | | | | |
|-------------|--------|-----|----------|----------|-------|------------|---------|------------|------|-------|--|
| Contrast | Type | Row | Estimate | Error | Alpha | Confidence | Limits | Chi-Square | Pr > | ChiSq | |
| | | | | | | | | | | | |
| D 2vs0 at A | 2 PARM | 1 | 2.2634 | 0.2965 | 0.05 | 1.6823 | 2.8444 | 58.2818 | < | .0001 | |
| D 2vs0 at A | 2 EXP | 1 | 9.6154 | 2.8507 | 0.05 | 5.3778 | 17.1920 | 58.2818 | < | .0001 | |







Modeling interactions (Effect coding)

Analysis of Maximum Likelihood Estimates

| | | | | | Standard | Wald | |
|-----------------|---|---|----|----------|----------|------------|------------|
| Parameter | | | DF | Estimate | Error | Chi-Square | Pr > ChiSq |
| | | | | | | | |
| Intercept | | | 1 | 0.8956 | 0.0792 | 127.7505 | <.0001 |
| Driving | 1 | | 1 | 0.4725 | 0.1165 | 16.4577 | <.0001 |
| Driving | 2 | | 1 | 0.7007 | 0.0949 | 54.5624 | <.0001 |
| Alcohol | 1 | | 1 | 0.1558 | 0.1126 | 1.9135 | 0.1666 |
| Alcohol | 2 | | 1 | 0.5946 | 0.1152 | 26.6379 | <.0001 |
| Driving*Alcohol | 1 | 1 | 1 | -0.6077 | 0.1598 | 14.4630 | 0.0001 |
| Driving*Alcohol | 1 | 2 | 1 | 0.2446 | 0.1782 | 1.8825 | 0.1701 |
| Driving*Alcohol | 2 | 1 | 1 | 0.4859 | 0.1341 | 13.1360 | 0.0003 |
| Driving*Alcohol | 2 | 2 | 1 | 0.0724 | 0.1355 | 0.2857 | 0.5930 |







Modeling interactions (Reference coding)

Analysis of Maximum Likelihood Estimates

| | | | | | Standard | Wald | |
|-----------------|---|---|----|----------|----------|------------|------------|
| Parameter | | | DF | Estimate | Error | Chi-Square | Pr > ChiSq |
| | | | | | | | |
| Intercept | | | 1 | -0.8329 | 0.2678 | 9.6692 | 0.0019 |
| Driving | 1 | | 1 | 1.8137 | 0.3429 | 27.9784 | <.0001 |
| Driving | 2 | | 1 | 1.1205 | 0.3177 | 12.4435 | 0.0004 |
| Alcohol | 1 | | 1 | 0.8329 | 0.4144 | 4.0390 | 0.0445 |
| Alcohol | 2 | | 1 | 0.8329 | 0.3720 | 5.0117 | 0.0252 |
| Driving*Alcohol | 1 | 1 | 1 | -0.8974 | 0.5173 | 3.0097 | 0.0828 |
| Driving*Alcohol | 1 | 2 | 1 | 0.3936 | 0.5340 | 0.5433 | 0.4611 |
| Driving*Alcohol | 2 | 1 | 1 | 1.1175 | 0.4732 | 5.5762 | 0.0182 |
| Driving*Alcohol | 2 | 2 | 1 | 1.1428 | 0.4345 | 6.9176 | 0.0085 |







Analysis of Maximum Likelihood Estimates

| | | | | | Standard | Wald | |
|-----------------|---|---|---|----------|----------|------------|------------|
| Parameter | | I | F | Estimate | Error | Chi-Square | Pr > ChiSq |
| | | | | | | | |
| Intercept | | | 1 | 2.2634 | 0.1457 | 241.2922 | <.0001 |
| Driving | 0 | | 1 | -2.2634 | 0.2965 | 58.2818 | <.0001 |
| Driving | 1 | | 1 | -0.0561 | 0.3495 | 0.0258 | 0.8725 |
| Driving | 2 | | 0 | 0 | • | • | • |
| Alcohol | 0 | | 1 | -1.9757 | 0.2245 | 77.4508 | <.0001 |
| Alcohol | 1 | | 1 | -0.0253 | 0.2104 | 0.0145 | 0.9042 |
| Alcohol | 2 | | 0 | 0 | • | • | • |
| Driving*Alcohol | 0 | 0 | 1 | 1.1428 | 0.4345 | 6.9176 | 0.0085 |
| Driving*Alcohol | 0 | 1 | 1 | 0.0253 | 0.4593 | 0.0030 | 0.9560 |
| Driving*Alcohol | 0 | 2 | 0 | 0 | • | • | • |
| Driving*Alcohol | 1 | 0 | 1 | 0.7492 | 0.4440 | 2.8475 | 0.0915 |
| Driving*Alcohol | 1 | 1 | 1 | -1.2657 | 0.4418 | 8.2067 | 0.0042 |
| Driving*Alcohol | 1 | 2 | 0 | 0 | • | • | • |
| Driving*Alcohol | 2 | 0 | 0 | 0 | • | • | • |
| Driving*Alcohol | 2 | 1 | 0 | 0 | • | • | • |
| Driving*Alcohol | 2 | 2 | 0 | 0 | • | • | • |