

Distributed Algorithms for Dynamic Networks

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Abstract

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1 High-Level Description of Goal

The goal of this paper is to simplify the creation of distributed algorithms for dynamic networks by demonstrating that any algorithm that works for the broadcast variant of the synchronous model with a star topology can be made to work for the broadcast variant of the synchronous model with any topology. We will do so by describing a simulation algorithm that, if run on every node in the broadcast model, will match perfectly the output of the nodes of the centrally controlled model.

2 Models

Distributed Model

1. We are considering the broadcast variant of the synchronous model, defined with respect to a connected network topology $G=(V,E)$.
2. The broadcast variant is defined such that a given node has no knowledge of its neighbors but may send a single message per round that all of its neighbors will receive.
3. Nodes in the network have unique identification numbers (UIDs) and they have knowledge of their own UID.

3 Problem Definition

1. We are considering the main execution to be the distributed model as defined in the Models section with n processes.
2. We are also considering a reference execution of the distributed model with a star topology and $n+1$ processes. The processes in this reference execution will run a given algorithm A and each process will keep an individual communication log, in which it will write its input and output for every round.
3. The main execution will run some algorithm S , which will take as input A , the algorithm run on the reference execution. The processes in the main execution will keep individual communication logs, which do not have the restriction of those in the reference execution that they must contain the given process' input and output for every round.
4. The problem is defined as solved if for the communication log of every process in the main execution, there is at least one identical communication log in the leaf processes of the reference execution and vice-versa.

4 Algorithm

1. Run unmodified Leader Election without Network Information
 - (a) Assume nodes have UIDs (which is also assumed for the distributed model)
 - (b) Each process runs Terminating Synchronous Breadth First Search and the node that manages to terminate elects itself leader and tells the other nodes to terminate
2. The Simulation
 - (a) Assume that each and every round of the given algorithm has a finite repetitions of a step, which is comprised of two parts
 - i. The star node sends a broadcast message to all the leaf nodes (Broadcast part)
 - ii. All leaf nodes send a receive message to the star node in response to the broadcast message (Receive part)
 - (b) Each step is simulated by the leader node running a modified instance of terminating synchronous BFS
 - i. The search message sent by a parent node to its children nodes is modified to be "search" plus the broadcast message, which is dictated by the output of the input algorithm A_1

- ii. Upon receiving a search message, a node runs the input algorithm A2 on the broadcast message portion and then creates the receive message portion using the output of A2
- iii. The done message sent by a child node to its parent node is modified to be “done” plus both the UID and the receive message of the child node as well as any done messages received by the child node
- iv. Upon receiving a search message, a node writes the broadcast message portion to its communication log
- v. Upon sending a done message, a node writes the receive message portion to its communication log
- vi. The leader simulates sending a search message to itself and then simulates sending a done message back to itself
- vii. This algorithm terminates when the leader has received done messages from all of its children and a simulated done message from itself

Static Model - All the nodes turn on at the same time

Simulation Algorithm takes one input, algorithm A, the algorithm to be simulated. Algorithm A can be broken into two distinct algorithms, A1, the algorithm run by the star process, and A2, the algorithm run by the leaf processes.

Member Variables - maxID (UID); parent (UID); totalChildren (int); childCount (int); wait (int); Message has a root (a round, the UID); a id of the sender (UID); a type search, choose, done; a receiver (UID), defaults to NULL;

Dynamic Addition Model - Nodes turn on at various times but they don't turn off The leader elected will be the node with the highest UID out of all of the nodes that turned on at round 1

Variables - maxRoot - (a round, the UID); parent (UID); totalChildren (int); childCount (int); wait (int); Message has a root (a round, the UID); a id of the sender (UID); a type search, choose, done; a receiver (UID);

```

initVariables() ;
for round 1 ... r do
    for each message m in Inbox do
        if m.maxID > maxID then
            | updateMaxRoot() ;
        end
        if m.maxID == maxID then
            if m.type == choose AND receiver == myUID then
                | childCount++ ;
                | totalChildren++ ;
            end
            if m.type == done AND receiver == myUID then
                | childCount- ;
                if childCount == 0 then
                    | sendDoneMsg() ;
                end
            end
        end
        if m.maxID < maxID then
            | msg = (type=search, sender=myUID, maxID=maxID) ;
            | Outbox.enqueue(msg) ;
        end
    end
    if wait != 0 AND childCount == 0 then
        | wait- ;
        if wait == 0 then
            | sendDoneMsg() ;
        end
    end
    for each message m in Outbox do
        | broadcast(m);
    end
    myRound++ ;
end

```

Algorithm 1: Simulation Algorithm for Static Model

```

myRound == 0 ;
maxID = myUID ;
message m = (type=search, sender=myUID, maxID=maxID) ;

```

Algorithm 2: initVariables method

```

maxID = m.maxID;
parent = m.sender;
childCount = totalChildren = 0; msg1 = (type=choose, sender=myUID,
maxID=maxID, receiver=m.sender) ;
Outbox.enqueue(msg1) ;
msg2 = (type=search, sender=myUID, maxID=maxID) ;
Outbox.enqueue(msg2) ;
wait = 3 ;

```

Algorithm 3: updateMaxRoot method

```

msg = ( type=done, sender=myUID, maxID=maxID ) ;
Outbox.enqueue( msg ) ;

```

Algorithm 4: sendDoneMsg method

```

initVariables() ;
for round 1...r do
    for each message m in Inbox do
        if m.root > maxRoot then
            | updateMaxRoot() ;
        end
        if m.root == maxRoot then
            if m.type == choose AND receiver == myUID then
                | childCount++ ;
                | totalChildren++ ;
            end
            if m.type == done AND receiver == myUID then
                | childCount- ;
                | if childCount == 0 then
                    | | sendDoneMsg() ;
                end
            end
        end
        if m.root < maxRoot then
            | msg = (type=search, sender=myUID, root=(r=maxRoot.r+1,
            | id=maxRoot.id) ) ;
            | Outbox.enqueue(msg) ;
        end
    end
    if wait != 0 AND childCount == 0 then
        | wait- ;
        | if wait == 0 then
            | | sendDoneMsg() ;
        end
    end
    for each message m in Outbox do
        | broadcast(m);
    end
    myRound++ ;
    maxRoot = (r=maxRoot.r+1, id=maxRoot.id) ;
end

```

Algorithm 5: Simulation Algorithm for the Dynamic Addition Model

```

myRound == 0 ;
maxRoot = (r=myRound, sender=myUID) ;
message m = (type=search, id=myUID, root=maxRoot) ;
Algorithm 6: initVariables method for Dynamic Addition Model

```

```

maxRoot = m.root;
parent = m.sender;
childCount = totalChildren = 0; msg1 = (type=choose, sender=myUID,
root=(r=maxRoot.r+1, id=maxRoot.id), receiver=m.id) ;
Outbox.enqueue(msg1) ;
msg2 = (type=search, sender=myUID, root=(r=maxRoot.r+1,
id=maxRoot.id) ) ;
Outbox.enqueue(msg2) ;
wait = 3 ;

```

Algorithm 7: updateMaxRoot method for Dynamic Addition Model

```

msg = ( type=done, sender=myUID, root=(r=maxRoot.r+1,
id=maxRoot.id), receiver=parent ) ;
Outbox.enqueue( msg ) ;

```

Algorithm 8: sendDoneMsg method for Dynamic Addition Model