

HPCA translocation biophysics examination

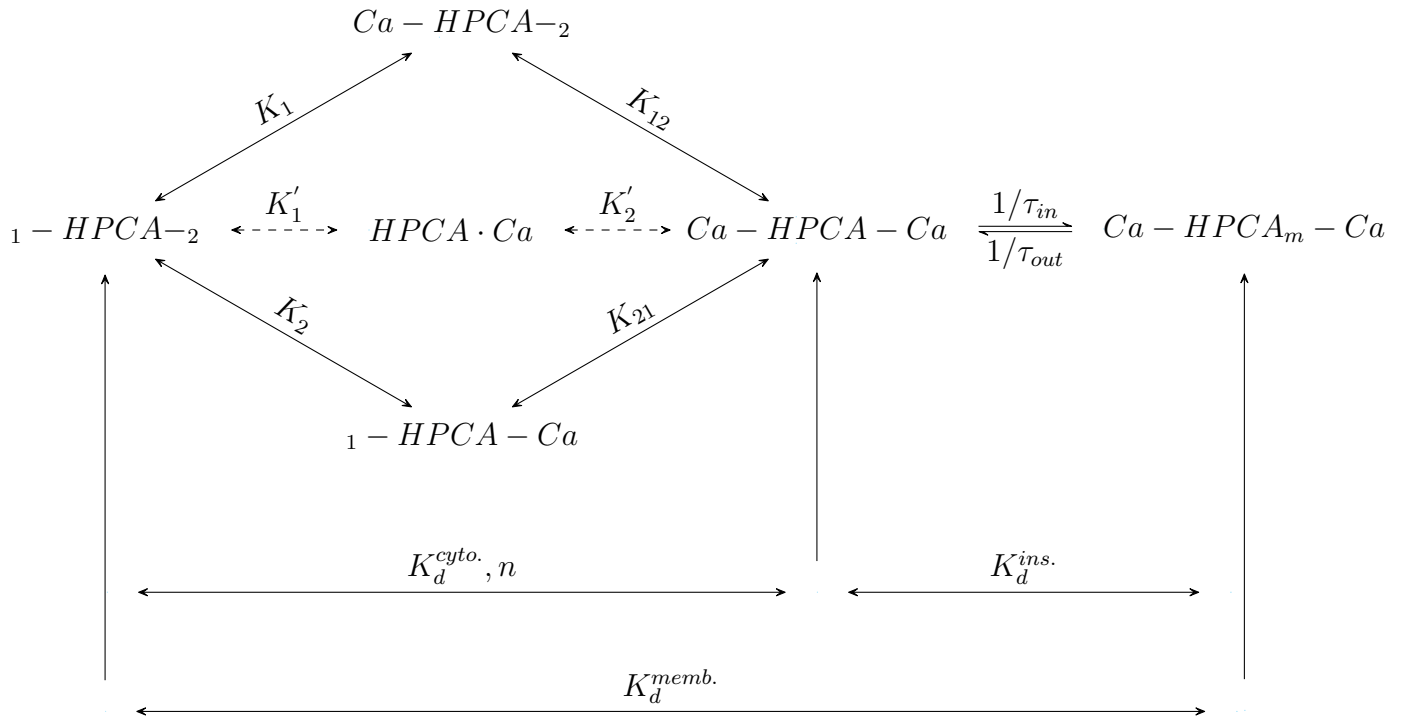
War, day 41

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General scheme



Kinetic model

Calcium binding

$$K_1 = \frac{[HPCA]_0[Ca^{2+}]}{[Ca - HPCA-2]} \quad (1)$$

$$[Ca - HPCA-2] = \frac{[HPCA]_0[Ca^{2+}]}{K_1} \quad (2)$$

$$K_2 = \frac{[HPCA]_0[Ca^{2+}]}{[1-HPCA - Ca]} \quad (3)$$

$$[1-HPCA - Ca] = \frac{[HPCA]_0[Ca^{2+}]}{K_2} \quad (4)$$

$$K'_1 = \frac{[HPCA]_0[Ca^{2+}]}{[HPCA \cdot Ca]} = \frac{[HPCA]_0[Ca^{2+}]}{[Ca - HPCA-2] + [1-HPCA - Ca]} \quad (5)$$

$$K'_1 = \frac{[HPCA]_0[Ca^{2+}]}{\frac{[HPCA]_0[Ca^{2+}]}{K_1} + \frac{[HPCA]_0[Ca^{2+}]}{K_2}} = \frac{1}{\frac{1}{K_1} + \frac{1}{K_2}} = \frac{K_1 K_2}{K_1 + K_2} \quad (6)$$

Cooperativity

Membrane insertion

$$\tau_{in} \propto \frac{a^2}{D} \quad (7)$$

$$\tau_{out} \propto e^{\frac{\Delta E}{kT}} \quad (8)$$

General model

$$Y = \frac{\frac{\tau_{out}}{\tau_{in}} \left(\frac{[Ca^{2+}]}{K_d^{cyto.}} \right)^n}{1 + \left(\frac{[Ca^{2+}]}{K_d^{cyto.}} \right)^n + \frac{\tau_{out}}{\tau_{in}} \left(\frac{[Ca^{2+}]}{K_d^{cyto.}} \right)^n} \quad (9)$$

$$\frac{\tau_{out}}{\tau_{in}} \gg 1 \Rightarrow Y \approx \frac{\frac{\tau_{out}}{\tau_{in}} \left(\frac{[Ca^{2+}]}{K_d^{cyto.}} \right)^n}{1 + \frac{\tau_{out}}{\tau_{in}} \left(\frac{[Ca^{2+}]}{K_d^{cyto.}} \right)^n} \quad (10)$$

$$Y \approx \frac{\left(\frac{[Ca^{2+}]}{K_d^{cyto.} \sqrt[n]{\frac{\tau_{in}}{\tau_{out}}}} \right)^n}{1 + \left(\frac{[Ca^{2+}]}{K_d^{cyto.} \sqrt[n]{\frac{\tau_{in}}{\tau_{out}}}} \right)^n} = \frac{\left(\frac{[Ca^{2+}]}{K_d^{memb.}} \right)^n}{1 + \left(\frac{[Ca^{2+}]}{K_d^{memb.}} \right)^n} \quad (11)$$

$$K_d^{memb.} = K_d^{cyto.} \sqrt[n]{\frac{\tau_{in}}{\tau_{out}}} = K_d^{cyto.} \sqrt[n]{\frac{a^2}{D\tau_{out}}} \quad (12)$$