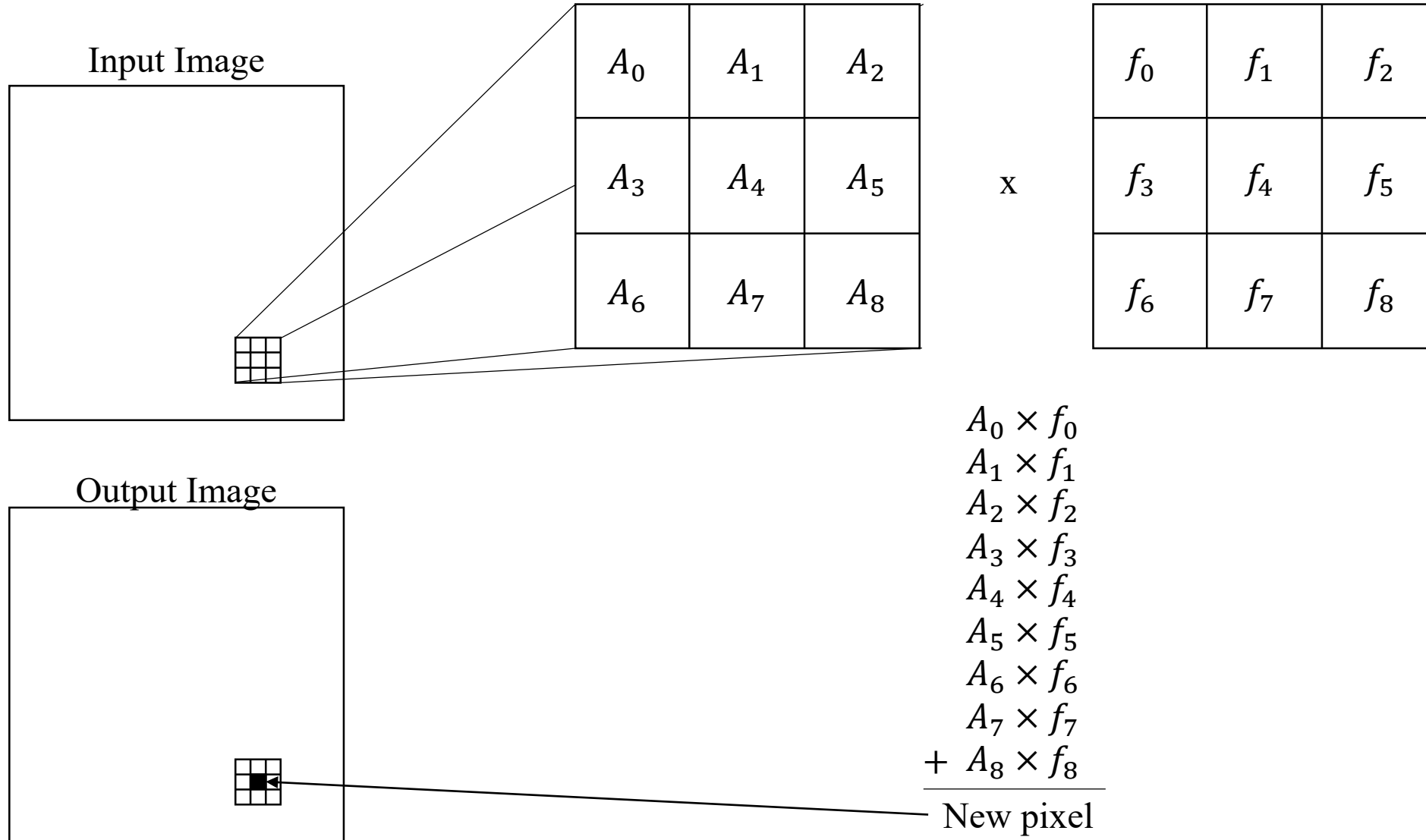


# Window Operation

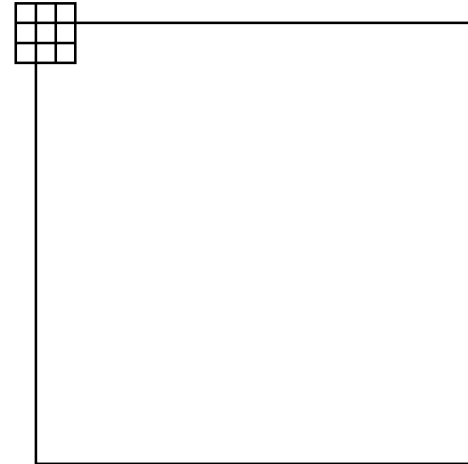
강석원

# Convolution



# Convolution

- Edge에서의 Convolution
  1. Zero Padding
  2. Edge의 pixel 복사 또는 Round
  3. (0, 0) 대신 (1,1)화소에서의 시작



# Smoothing(Blurring)

- 목적
  - Noise 제거 및 윤곽선 제거

- 효과



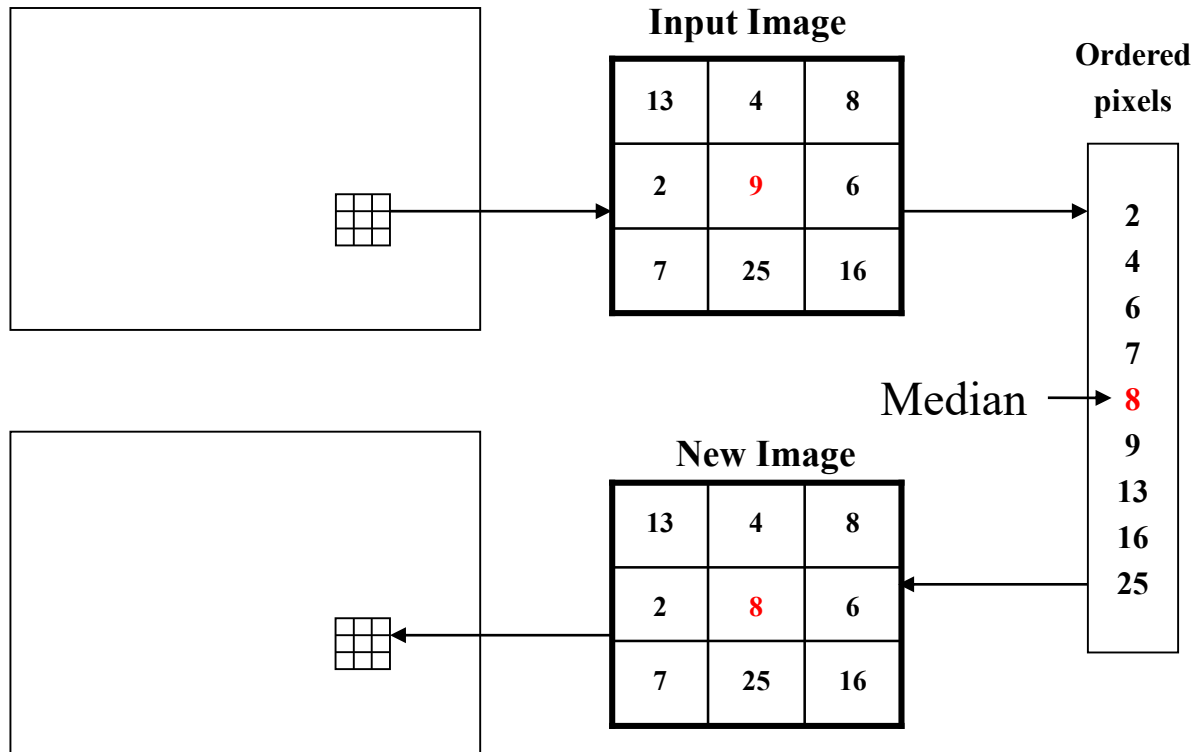
→ Blur Filter Size

# Smoothing(Blurring)

- Mean Filter  $\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$   $\frac{1}{10} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 1 \end{bmatrix}$   $\frac{1}{4} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$
- Gaussian Filter  $\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$

# Smoothing(Blurring)

- Median Filtering



Original image  
(Noise Added)



Median Filter(3x3)

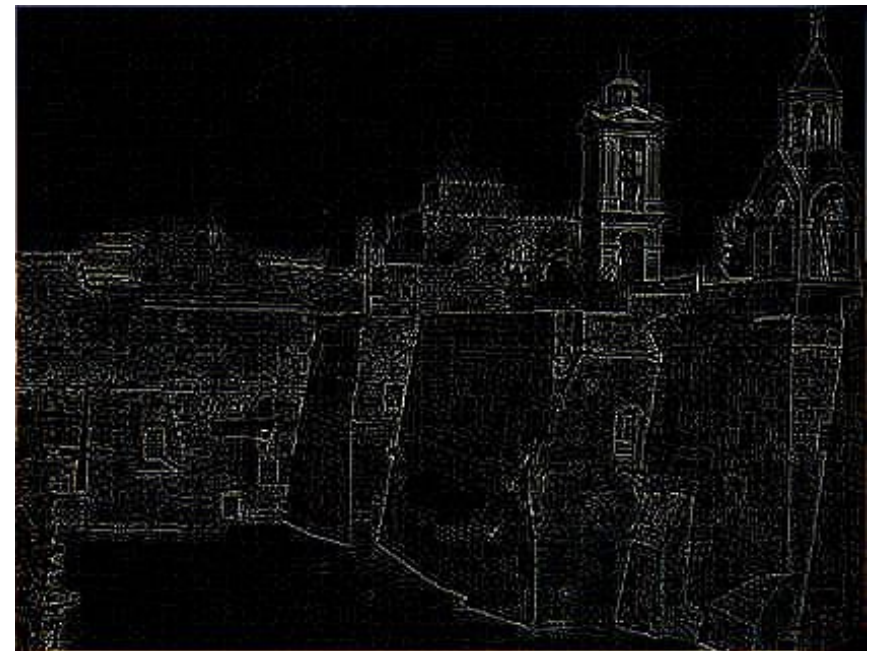


Median Filter(5x5)



Median Filter(9x9)

# Edge Detection



# Edge Detection

- Gradient Filter

$$G[f(x, y)] = \begin{bmatrix} \frac{\partial f(x, y)}{\partial x} \\ \frac{\partial f(x, y)}{\partial y} \end{bmatrix}$$

$$\frac{\partial f(x, y)}{\partial x} \cong \frac{f(x, y) - f(x+1, y)}{\Delta x} = \frac{f(x, y) - f(x+1, y)}{1} = f(x, y) - f(x+1, y)$$

$$\frac{\partial f(x, y)}{\partial y} \cong \frac{f(x, y) - f(x, y+1)}{\Delta y} = \frac{f(x, y) - f(x, y+1)}{1} = f(x, y) - f(x, y+1)$$

$$\frac{\partial f(x, y)}{\partial x} \cong f(x, y) - f(x+1, y) \Rightarrow \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & -1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\frac{\partial f(x, y)}{\partial y} \cong f(x, y) - f(x, y+1) \Rightarrow \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -1 & 0 \end{bmatrix}$$

$$\frac{\partial f(x, y)}{\partial x} \cong f(x+1, y) - f(x-1, y) \Rightarrow \begin{bmatrix} 0 & 0 & 0 \\ -1 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\frac{\partial f(x, y)}{\partial y} \cong f(x, y+1) - f(x, y-1) \Rightarrow \begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$



# Edge Detection

$$\frac{\partial f(x, y)}{\partial x} \cong f(x, y) - f(x+1, y+1) \Rightarrow \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

- Roberts Operator

$$\frac{\partial f(x, y)}{\partial y} \cong f(x+1, y) - f(x, y+1) \Rightarrow \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix}$$

# Edge Detection

- Sobel Operator

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- Prewitt Operator

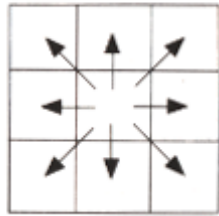
$$\begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

- Frei-Chen Operator

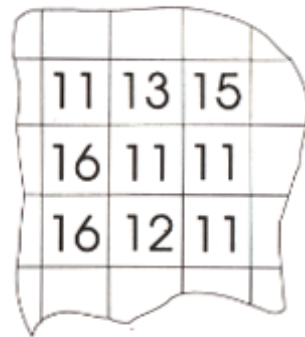
$$\begin{bmatrix} -1 & 0 & 1 \\ -\sqrt{2} & 0 & \sqrt{2} \\ -1 & 0 & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & \sqrt{2} & 1 \\ 0 & 0 & 0 \\ -1 & -\sqrt{2} & -1 \end{bmatrix}$$

# Edge Detection

homogeneity operator



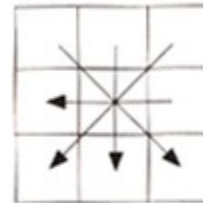
image



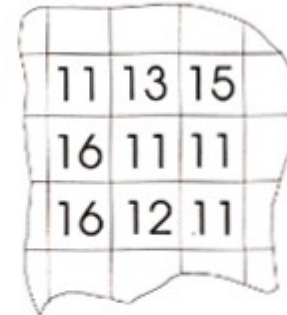
$$\text{new pixel} = \text{maximum of } \{ |11-11| \quad |11-13| \quad |11-15| \\ |11-16| \quad |11-11| \\ |11-16| \quad |11-12| \quad |11-11| \} =$$

유사 연산자의 수행 방법

difference operator



image



$$\text{new pixel} = \text{maximum of } \{ |11-11| \quad |13-12| \quad |15-16| \quad |11-16| \} = 5$$

차연산자의 수행 방법

# Edge Detection

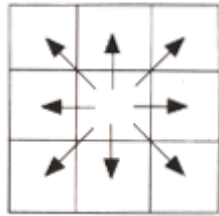
- Laplace Operator

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

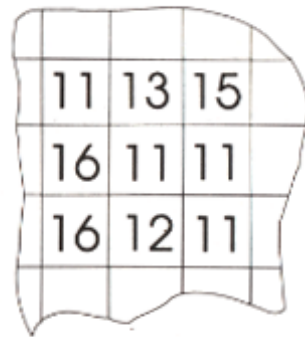
$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -8 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

# Edge Detection

homogeneity operator



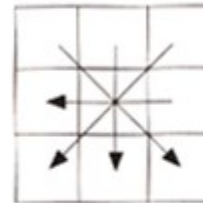
image



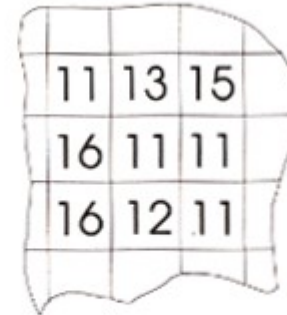
$$\text{new pixel} = \text{maximum of } \{ |11-11| \quad |11-13| \quad |11-15| \\ |11-16| \quad |11-11| \\ |11-16| \quad |11-12| \quad |11-11| \} =$$

유사 연산자의 수행 방법

difference operator



image



$$\text{new pixel} = \text{maximum of } \{ |11-11| \quad |13-12| \quad |15-16| \quad |11-16| \} = 5$$

차연산자의 수행 방법