Contents	<pre>#define pof pop_front()</pre>
1 Template 1	#define mp(a, b) make_pair(a, b)
1 Template 1 1.1 Default Code	#define F first
1.2 .vimrc	#deline b becond
1.2 .VIIIIC	#define mt make_tuple
2 Data Structure 1	#define gt(t, i) get <i>(t)</i>
2.1 Binary Indexed Tree	#define iceil(a, b) (((a) + (b) - 1) / (b))
2.2 Disjoint Set Union-Find	#define tomax(a, b) ((a) = max((a), (b)))
2.3 Segment Tree	<pre>#define printv(a, b) {bool pvaspace=false; \</pre>
2.0 Segment free	for(auto pva : a){ \
3 Graph 3	<pre>if(pvaspace) b << " "; pvaspace=true;\</pre>
3.1 Dijkstra	b << pva;\
3.2 Floyd-Warshall	}\
3.3 Kruskal	b << "\n";}
3.4 Tarjan SCC	////
3.5 SPFA	//#define TEST
	uging nomegness and
4 String 4	<pre>using namespace std; using namespacegnu_pbds;</pre>
4.1 KMP 4	using namespacegnu_pbds;
4.2 Z Value	humadaf lang lang 11.
4.3 Longest Palindromic Substring 4	typedef long long ll;
4.4 Suffix Array 5	typedef unsigned long long ull;
	typedef long double ld;
5 Geometry 5	
5.1 Vector Operations 5	<pre>using pii = pair<int, int="">;</int,></pre>
5.2 Convex Hull 6	using pll = pair <ll, 11="">;</ll,>
	using pdd = pair <ld, ld="">;</ld,>
6 Number Theory 6	<pre>using tiii = tuple<int, int="" int,="">;</int,></pre>
6.1 Prime Sieve 6	. 11 MOD
M DD M'I	const 11 MOD = 1000000007;
7 DP Trick 6	const 11 MAX = 2147483647;
7.1 Dynamic Convex Hull 6	
8 Numbers and Math 7	template < typename A, typename B>
8.1 Fibonacci	ostream& operator << (ostream& o, pair <a, b=""> p</a,>
8.2 Catalan){
8.3 Geometry	return o << '(' << p.F << ',' << p.S << ')
8.4 Prime Numbers	'; }
8.5 Number Theory	J.
6.5 Number Theory	
	int main(){
1 Template	StarBurstStream
•	return 0;
1.1 Default Code	}
//#define NDEBUG	1.2 .vimrc
Himaluda Chiha (adda 1975)	Least my
<pre>#include <bits stdc++.h=""></bits></pre>	:set nu
<pre>#include <bits extc++.h=""></bits></pre>	:set ai
	:set cursorline
#define StarBurstStream ios_base::	:set tabstop=4
<pre>sync_with_stdio(false); cin.tie(0); cout.</pre>	:set shiftwidth=4
tie(0);	:set mouse=a
<pre>#define iter(a) a.begin(), a.end()</pre>	:set expandtab
<pre>#define riter(a) a.rbegin(), a.rend()</pre>	hi CursorLine cterm=none ctermbg=DarkMagenta
<pre>#define lsort(a) sort(iter(a))</pre>	2 Data Structura
<pre>#define gsort(a) sort(riter(a))</pre>	2 Data Structure
<pre>#define pb(a) push_back(a)</pre>	0.1 D: I I I I I
<pre>#define eb(a) emplace_back(a)</pre>	2.1 Binary Indexed Tree
<pre>#define pf(a) push_front(a)</pre>	
<pre>#define pob pop_back()</pre>	template < typename T >

```
struct BIT{
private:
  vector<T> bit;
  int lowbit(int x){
    return x & (-x);
public:
  explicit BIT(int sz){
    bit.resize(sz + 1);
  void modify(int x, T v){
    for(; x < bit.size(); x += lowbit(x))</pre>
   bit[x] += v;
 T get(int x){
    T ans = T();
    for(; x; x -= lowbit(x)) ans += bit[x];
    return ans;
  }
};
```

2.2 Disjoint Set Union-Find

```
vector<int> dsu, rk;

void initDSU(int n){
    dsu.resize(n);
    rk.resize(n);
    for(int i = 0; i < n; i++) dsu[i] = i, rk[
        i] = 1;
}

int findDSU(int x){
    if(dsu[x] == x) return x;
    dsu[x] = findDSU(dsu[x]);
    return dsu[x];
}

void unionDSU(int a, int b){
    int pa = findDSU(a), pb = findDSU(b);
    if(rk[pa] > rk[pb]) swap(pa, pb);
    if(rk[pa] == rk[pb]) rk[pb]++;
    dsu[pa] = pb;
}
```

2.3 Segment Tree

```
template < typename T>
struct Node {
   T v = 0, tag = 0;
   int sz = 1, l = -1, r = -1;
   T rv() {
     return v + tag * sz;
   }
   void addTag(T t) {
     tag += t;
   }
```

```
};
template < typename T>
T pullValue(T b, T c){
  return b + c;
template < typename T>
void pull(Node<T> &a, Node<T> &1, Node<T> &r
   ) {
  a.v = pullValue(l.rv(), r.rv());
  a.sz = 1.sz + r.sz;
template < typename T>
void push(Node<T> &a, Node<T> &l, Node<T> &r
   ) {
  1.addTag(a.tag);
  r.addTag(a.tag);
  a.v = a.rv();
  a.tag = 0;
template < typename T>
struct SegmentTree{
  vector < Node < T >> st;
  int cnt = 0;
  explicit SegmentTree(int sz){
    st.resize(4 * sz);
  }
  int build(int 1, int r, vector<T>& o){
    int id = cnt++;
    if(l == r){
      st[id].v = o[1];
      return id;
    }
    int m = (1 + r) / 2;
    st[id].1 = build(1, m, o);
    st[id].r = build(m + 1, r, o);
    pull(st[id], st[st[id].1], st[st[id].r])
    return id;
  void modify(int 1, int r, int v, int L,
   int R, int id){
    if(1 == L \&\& r == R){
      st[id].addTag(v);
      return;
    }
    int M = (L + R) / 2;
    if(r \le M) \mod ify(1, r, v, L, M, st[id].
    else if (1 > M) modify (1, r, v, M + 1, R,
    st[id].r);
    else{
      modify(1, M, v, L, M, st[id].1);
      modify(M + 1, r, v, M + 1, R, st[id].r
```

|}

```
);
    pull(st[id], st[st[id].1], st[st[id].r])
  }
  T query(int 1, int r, int L, int R, int id
    if(l == L && r == R) return st[id].rv();
    push(st[id], st[st[id].1], st[st[id].r])
    int M = (L + R) / 2;
    if(r <= M) return query(l, r, L, M, st[</pre>
   id].1);
    else if(l > M) return query(l, r, M + 1,
    R, st[id].r);
    else{
      return pullValue(query(1, M, L, M, st[
   id].1), query(M + 1, r, M + 1, R, st[id].
   r));
    }
  }
};
```

3 Graph

3.1 Dijkstra

```
//The first element in pair should be edge
   weight, and the second should be vertex
vector<vector<pii>> g;
int n;
int dijkstra(int start, int end){
  priority_queue<pii, vector<pii>, greater<</pre>
   pii>> q;
  for(pii p : g[start]){
    q.push(p);
  q.push(mp(0, start));
  vector<int> dis(n, -1);
  dis[start] = 0;
  vector<int> visit(n);
  while(q.size()){
    int v = q.top().S;
    int d = q.top().F;
    if(v == end) break;
    q.pop();
    if(visit[v]) continue;
    visit[v] = true;
    for(pii p : g[v]){
      if(visit[p.S]) continue;
      if(dis[p.S] == -1 \mid \mid d + p.F < dis[p.S]
   ]){
        dis[p.S] = d + p.F;
        q.push(mp(dis[p.S], p.S));
    }
  }
  return dis[end];
```

3.2 Floyd-Warshall

```
vector<vector<int>> g;
int n;

void floydwarshall(){
  for(int k = 0; k < n; k++)
    for(int i = 0; i < n; i++)
      for(int j = 0; j < n; j++)
        if(g[i][k] != -MAX && g[k][j] != -
      MAX && (g[i][j] == -MAX || g[i][k] + g[k]
      ][j] < g[i][j]))
        g[i][j] = g[i][k] + g[k][j];
}</pre>
```

3.3 Kruskal

```
int kruskal(){
  int ans = 0;
  lsort(e);
  initDSU();
  for(auto& i : e){
    int a = i.S.F, b = i.S.S;
    if(findDSU(a) == findDSU(b)) continue;
    ans += i.F;
    unionDSU(a, b);
  }
  return ans;
}
```

3.4 Tarjan SCC

```
vector<vector<int>> g;
vector<int> st;
vector<bool> inst;
vector<int> scc;
vector<int> ts, low;
int tmp = 0;
int sccid = 0;
void initSCC(int n){
 tmp = 0;
  sccid = 0;
  st.clear();
  g.clear();
  g.resize(2 * n + 1);
  inst.clear();
  inst.resize(2 * n + 1);
  scc.clear();
  scc.resize(2 * n + 1);
  ts.clear();
  ts.resize(2 * n + 1, -1);
  low.clear();
  low.resize(2 * n + 1);
}
void dfs(int now){
  st.eb(now);
  inst[now] = true;
```

```
}
  ts[now] = ++tmp;
  low[now] = ts[now];
                                                   }
  for(int i : g[now]){
                                                   return dis[end];
    if(ts[i] == -1){
                                                }
      dfs(i);
                                                    String
                                                4
      low[now] = min(low[now], low[i]);
    else if(inst[i]) low[now] = min(low[now
                                                4.1 KMP
   ], ts[i]);
                                                vector<int> f;
                                                void build(string& t){
  if(low[now] == ts[now]){
                                                   f.clear();
    sccid++;
                                                  f.resize(t.size());
    int t;
                                                   int p = -1;
    do{
                                                  f[0] = -1;
      t = st.back();
                                                   for(int i = 1; i < t.size(); i++){
      st.pob;
                                                     while (p != -1 \&\& t[p + 1] != t[i]) p = f
      inst[t] = false;
      scc[t] = sccid;
                                                     if(t[p + 1] == t[i]) f[i] = p + 1;
                                                     else f[i] = -1;
    while(t != now);
                                                     p = f[i];
                                                  }
                                                }
}
                                                int kmp(string& s, string& t){
3.5 SPFA
                                                   int ans = 0;
                                                   int p = -1;
const 11 INFINITE = 2147483647;
                                                   for(int i = 0; i < s.size(); i++){
                                                     while(p != -1 && t[p + 1] != s[i]) p = f
int n;
                                                    [p];
vector<vector<pii>> g;
                                                     if(t[p + 1] == s[i]) p++;
                                                     if(p + 1 == t.size()){
int spfa(int start, int end){
                                                       ans++;
                                                       p = f[p];
  vector<int> dis(n, INFINITE);
                                                     }
  int start;
                                                  }
  cin >> start;
                                                   return ans;
  dis[start] = 0;
                                                4.2 Z Value
  queue < int > q;
  q.push(start);
  vector < bool > inq(n);
                                                vector<int> z;
  inq[start] = true;
  vector<int> cnt(n);
                                                void build(string s, int n){
                                                  z.clear();
  while(!q.empty()){
                                                   z.resize(n);
    int v = q.front();
                                                   int 1 = 0;
    q.pop();
                                                   for(int i = 1; i < n; i++){
    inq[v] = false;
                                                     if(1 + z[1] >= i) z[i] = min(z[1] + 1 -
    for(pii p : g[v]){
                                                    i, z[i - 1]);
      if(!(dis[p.F] == INFINITE || dis[v] +
                                                     while(i + z[i] < n && s[z[i]] == s[i + z
   p.S < dis[p.F])) continue;</pre>
                                                    [i]]) z[i]++;
      cnt[p.F]++;
                                                     if(i + z[i] > 1 + z[1]) 1 = i;
      if(cnt[p.F] >= n) return -INFINITE; //
   negetive cycle
                                                }
      dis[p.F] = dis[v] + p.S;
```

if(!inq[p.F]){

q.push(p.F);

inq[p.F] = true;

4.3 Longest Palindromic Substring

#define T(x) ((x) % 2 ? s[(x) / 2] : '.')

```
string s;
int L;
int ex(int 1, int r){
  int i = 0;
  while (1 - i \ge 0 \&\& r + i < L \&\& T(1 - i)
   == T(r + i)) i++;
  return i;
int lps(string ss){
  s = ss;
 L = 2 * s.size() + 1;
  int mx = 0;
  int center = 0;
  vector<int> r(L);
  int ans = 1;
 r[0] = 1;
  for(int i = 1; i < L; i++){
    int ii = center - (i - center);
    int len = mx - i + 1;
    if(i > mx){
      r[i] = ex(i, i);
      center = i;
     mx = i + r[i] - 1;
    else if(r[ii] == len){
      r[i] = len + ex(i - len, i + len);
      center = i;
      mx = i + r[i] - 1;
    else r[i] = min(r[ii], len);
    ans = max(ans, r[i]);
  return ans - 1;
}
```

4.4 Suffix Array

```
#include <bits/stdc++.h>

#define eb(a) emplace_back(a)

using namespace std;

vector<int> sa(string s){
    s += '$';
    int n = s.size();
    int t = __lg(n) + 1;

    vector<vector<int>> rk(t + 1, vector<int>(
        n)), b;

    vector<vector<int>> c1(27);
    for(int i = 0; i < n; i++) c1[s[i] == '$'
        ? 0 : s[i] - 'a' + 1].eb(i);;
    for(int i = 0; i < 27; i++){
        if(!c1[i].empty()) b.eb(c1[i]);
    }</pre>
```

```
b.resize(n);
  for(int i = 0; i < n; i++){
    for(int k : b[i]) rk[0][k] = i;
  for(int i = 1; i <= t; i++){</pre>
    vector<vector<int>> tb(n);
    for(int j = 0; j < n; j++){
      for(int k : b[j]){
        int tmp = ((k - (1 << (i - 1))) \% n
   + n) % n;
        int now = rk[i - 1][tmp];
        tb[now].eb(tmp);
    }
    b = tb;
    int cnt = -1;
    for(int j = 0; j < n; j++){
      int lst = -1;
      for(int k : b[j]){
        int now = rk[i - 1][(k + (1 << (i -
   1))) % n];
        if(now != lst) cnt++;
        rk[i][k] = cnt;
        lst = now;
      }
    }
  }
  return rk[t];
}
```

5 Geometry

5.1 Vector Operations

```
template < typename T>
pair<T, T> operator+(pair<T, T> a, pair<T, T</pre>
  return mp(a.F + b.F, a.S + b.S);
template < typename T>
pair <T, T > operator - (pair <T, T > a, pair <T, T
   > b){
  return mp(a.F - b.F, a.S - b.S);
}
template < typename T>
pair<T, T> operator*(pair<T, T> a, T b){
  return mp(a.F * b, a.S * b);
template < typename T>
pair<T, T> operator/(pair<T, T> a, T b){
  return mp(a.F / b, a.S / b);
template < typename T>
T dot(pair<T, T> a, pair<T, T> b){
  return a.F * b.F + a.S * b.S;
```

```
template < typename T>
T cross(pair < T, T > a, pair < T, T > b) {
  return a.F * b.S - a.S * b.F;
}

template < typename T >
T abs2(pair < T, T > a) {
  return a.F * a.F + a.S * a.S;
}
```

5.2 Convex Hull

```
template < typename T>
pair <T, T > operator - (pair <T, T > a, pair <T, T
   > b){
  return mp(a.F - b.F, a.S - b.S);
template < typename T>
T cross(pair<T, T> a, pair<T, T> b){
  return a.F * b.S - a.S * b.F;
}
template < typename T>
vector<pair<T, T>> getConvexHull(vector<pair</pre>
   <T, T>>& pnts){
  int n = pnts.size();
  lsort(pnts);
  vector<pair<T, T>> hull;
  hull.reserve(n);
  for(int i = 0; i < 2; i++){
    int t = hull.size();
    for(pair<T, T> pnt : pnts){
      while(hull.size() - t >= 2 && cross(
   hull.back() - hull[hull.size() - 2], pnt
   - hull[hull.size() - 2]) <= 0){
        hull.pop_back();
      hull.pb(pnt);
    hull.pop_back();
    reverse(iter(pnts));
  return hull;
}
```

6 Number Theory

6.1 Prime Sieve

```
vector<int> prime;
vector<int> p;
void sieve(int n){
  prime.resize(n + 1, 1);
  for(int i = 2; i <= n; i++){</pre>
```

```
if(prime[i] == 1){
    p.push_back(i);
    prime[i] = i;
}
for(int j : p){
    if((ll)i * j > n || j > prime[i])
break;
    prime[i * j] = j;
}
}
```

7 DP Trick

7.1 Dynamic Convex Hull

```
const ll INF = 1LL << 60;</pre>
template < typename T>
struct Line{
  mutable T a, b, r = 0;
  Line(T a, T b) : a(a), b(b){}
  bool operator < (Line < T > 1) const{
    return a < 1.a;
  bool operator<(T v)const{</pre>
    return r < v;
  }
};
template < typename T>
T divfloor(T a, T b){
  return a / b - ((a ^ b) < 0 && a % b);
template < typename T>
struct DynamicHull{
  multiset <Line <T>, less <>> s;
  int size(){
    return s.size();
  bool intersect(typename set<Line<T>>::
    iterator a, typename set<Line<T>>::
    iterator &b){
    if(b == s.end()){
       a \rightarrow r = INF;
       return false;
    if(a->a == b->a){
       if(a->b > b->b) a->r = INF;
       else a \rightarrow r = -INF;
    else{
       a\rightarrow r = divfloor(b\rightarrow b - a\rightarrow b, a\rightarrow a - b
    ->a);
    }
```

```
return a->r >= b->r;
  void insert(T a, T b){
    Line \langle T \rangle l(a, b);
    auto it = s.insert(1), after = next(it),
    while(intersect(it, after)) after = s.
   erase(after);
    if(before != s.begin() && intersect(--
   before, it)){
      it = s.erase(it);
      intersect(before, it);
    while((it = before) != s.begin() && (--
   before)->r >= it->r) intersect(before, it
     = s.erase(it));
  T query(T v){
    Line<T> 1 = *s.lower_bound(v);
    return l.a * v + l.b;
  }
};
```

8 Numbers and Math

8.1 Fibonacci

$$f(n) = f(n-1) + f(n-2)$$

$$\begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

1	1	1	2	3	5
6	8	13	21	34	55
11	89	144	233	377	610
16	987	1597	2584	4181	6765
21	10946	17711	28657	46368	75025
26	121393	196418	317811	514229	832040
31	1346269	2178309	3524578	5702887	9227465
f(45)	$\approx 10^9$				
f(88)	$\approx 10^{18}$				

8.2 Catalan

$$C_0 = 1, C_n = \sum_{i=0}^{n-1} C_i C_{n-1-i}$$

$$C_n = C_n^{2n} - C_{n-1}^{2n}$$

8.3 Geometry

• Heron's formula: The area of a triangle whose lengths of sides is a,b,c and s = (a+b+c)/2 is $\sqrt{s(s-a)(s-b)(s-c)}$.

• Vector cross product:

$$v_1 \times v_2 = |v_1||v_2|\sin\theta = (x_1 \times y_2) - (x_2 \times y_1).$$

• Vector dot product: $v_1 \cdot v_2 = |v_1||v_2|\cos\theta = (x_1 \times y_1) + (x_2 \times y_2).$

8.4 Prime Numbers

First 50 prime numbers:

```
23
                                                                 29
 1
      2
            3
                                11
                                       13
                                             17
                                                   19
            37
 11
      31
                   41
                         43
                                47
                                       53
                                             59
                                                   61
                                                          67
                                                                 71
 21
      73
             79
                   83
                         89
                                97
                                       101
                                             103
                                                   107
                                                          109
                                                                 113
 31
      127
                   137
                                149
            131
                         139
                                       151
                                             157
                                                    163
                                                          167
                                                                 173
                                       199
                                                   223
                                                                 229
 41
      179
            181
                   191
                         193
                                197
                                             211
                                                          227
Very large prime numbers:
```

1000001333 1000500889 2000000659 900004151 850001359

8.5 Number Theory

- Inversion: $aa^{-1} \equiv 1 \pmod{m}$. a^{-1} exists iff gcd(a, m) = 1.
- Linear inversion: $a^{-1} \equiv (m \lfloor \frac{m}{a} \rfloor) \times (m \mod a)^{-1} \pmod{m}$
- Fermat's little theorem: $a^p \equiv a \pmod{p}$ if p is prime.
- Euler function: $\phi(n) = n \prod_{p|n} \frac{p-1}{p}$
- Euler theorem: $a^{\phi(n)} \equiv 1 \pmod{n}$ if $\gcd(a, n) = 1$.
- Extended Euclidean algorithm: $ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a \lfloor \frac{a}{b} \rfloor b)y_1 = ay_1 + b(x_1 \lfloor \frac{a}{b} \rfloor y_1)$
- Divisor function: $\sigma_x(n) = \sum_{d|n} d^x. \ n = \prod_{i=1}^r p_i^{a_i}.$ $\sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x} 1}{p_i^x 1} \text{ if } x \neq 0. \ \sigma_0(n) = \prod_{i=1}^r (a_i + 1).$
- Chinese remainder theorem: $x \equiv a_i \pmod{m_i}$. $M = \prod m_i$. $M_i = M/m_i$. $t_i = M_i^{-1}$. $x = kM + \sum a_i t_i M_i$, $k \in \mathbb{Z}$.