#### Contents #define lsort(a) sort(iter(a)) #define gsort(a) sort(riter(a)) 1 Basic 1 #define pb(a) push\_back(a) 1.1 Default Code . . . . . . . . . . . . . . . . . #define eb(a) emplace\_back(a) 2 #define pf(a) push\_front(a) 2 #define ef(a) emplace\_front(a) #define pob pop\_back() $^{2}$ #define pof pop\_front() #define mp(a, b) make\_pair(a, b) 2 Data Structure $\mathbf{2}$ #define F first 2.1 Binary Indexed Tree . . . . . . . . . . . . 2 #define S second 2.2 Disjoint Set Union-Find . . . . . . . . . #define mt make tuple 2.3 Segment Tree . . . . . . . . . . . . . . . . . #define gt(t, i) get<i>(t) #define iceil(a, b) (((a) + (b) - 1) / (3 Graph 3 3 #define tomax(a, b) ((a) = max((a), (b))3.2 Floyd-Warshall . . . . . . . . . . . . . . . . 4 4 #define tomin(a, b) ((a) = min((a), (b))4 4 #define topos(a) ((a) = (((a) % MOD + 3.6 Block-cut Tree . . . . . . . . . . . . . . . . MOD) % MOD)) #define uni(a) a.resize(unique(iter(a)) 4 String 5 - a.begin()) 4.1 KMP...... 5 #define printv(a, b) {bool pvaspace= 6 false; \ 4.3 Longest Palindromic Substring . . . . . . 6 for(auto pva : a){ \ 4.4 Suffix Array . . . . . . . . . . . . . . . . . 6 if(pvaspace) b << " "; pvaspace=true;\</pre> b << pva; \ Math and Geometry 7 }\ 5.1 Vector Operations . . . . . . . . . . . . 7 b << "\n";} 7 5.2 Convex Hull . . . . . . . . . . . . . . . . . using namespace std; using namespace \_\_gnu\_pbds; 6 DP Trick 8 typedef long long 11; 6.1 Dynamic Convex Hull . . . . . . . . . . . 8 typedef unsigned long long ull; typedef long double ld; 7 Numbers and Math Formulae 8 using pii = pair<int, int>; 9 using pll = pair<11, 11>; 7.4 Prime Numbers . . . . . . . . . . . . . . . using pdd = pair<ld, ld>; 9 7.5 Number Theory . . . . . . . . . . . . . . . . 9 using tiii = tuple<int, int, int>; 7.6 Combinatorics . . . . . . . . . . . . . . . . const 11 MOD = 1000000007; const 11 MAX = 2147483647; **Basic** 1 template < typename A, typename B> 1.1 Default Code ostream& operator << (ostream& o, pair < A, B> p){ #include <bits/stdc++.h> return o << '(' << p.F << ',' << p.S #include <bits/extc++.h> << ')'; #define StarBurstStream ios\_base:: sync\_with\_stdio(false); cin.tie(0); int main(){ cout.tie(0); StarBurstStream #define iter(a) a.begin(), a.end()

#define riter(a) a.rbegin(), a.rend()

return 0;

```
1.2 .vimrc

:set nu
:set ai
:set cursorline
:set tabstop=4
:set shiftwidth=4
:set mouse=a
:set expandtab
hi CursorLine cterm=none ctermbg=
```

#### 1.3 PBDS

DarkMagenta

#### 1.4 Random

```
mt19937 rnd(chrono::steady_clock::now().
    time_since_epoch().count());
uniform_int_distribution<int> dis(1,
    100);
cout << dis(rnd) << "\n";</pre>
```

#### 1.5 Clock

```
int st = clock();
int ed = clock();
if(ed - st >= CLOCKS_PER_SEC * 1);
```

## 2 Data Structure

#### 2.1 Binary Indexed Tree

```
template < typename T>
struct BIT{

private:
   vector < T > bit;
   int lowbit(int x) {
      return x & (-x);
   }

public:
   explicit BIT(int sz) {
      bit.resize(sz + 1);
   }

void modify(int x, T v) {
```

```
for(; x < bit.size(); x += lowbit(x)
) bit[x] += v;
}

T get(int x){
   T ans = T();
   for(; x; x -= lowbit(x)) ans += bit[x];
   return ans;
}
};</pre>
```

#### 2.2 Disjoint Set Union-Find

```
vector<int> dsu, rk;
void initDSU(int n){
  dsu.resize(n);
  rk.resize(n);
  for(int i = 0; i < n; i++) dsu[i] = i,
    rk[i] = 1;
}
int findDSU(int x){
  if(dsu[x] == x) return x;
  dsu[x] = findDSU(dsu[x]);
  return dsu[x];
void unionDSU(int a, int b){
  int pa = findDSU(a), pb = findDSU(b);
  if(rk[pa] > rk[pb]) swap(pa, pb);
  if(rk[pa] == rk[pb]) rk[pb]++;
  dsu[pa] = pb;
```

#### 2.3 Segment Tree

```
template < typename T >
struct Node {
    T v = 0, tag = 0;
    int sz = 1, l = -1, r = -1;
    T rv() {
        return v + tag * sz;
    }
    void addTag(T t) {
        tag += t;
    }
};

template < typename T >
T pullValue(T b, T c) {
    return b + c;
}

template < typename T >
void pull(Node < T > &a, Node < T > &1, Node < T > &r) {
```

```
a.v = pullValue(1.rv(), r.rv());
  a.sz = 1.sz + r.sz;
}
template < typename T>
void push(Node<T> &a, Node<T> &l, Node<T</pre>
   > &r){
  1.addTag(a.tag);
 r.addTag(a.tag);
  a.v = a.rv();
  a.tag = 0;
}
template < typename T>
struct SegmentTree{
  vector<Node<T>> st;
  int cnt = 0;
  explicit SegmentTree(int sz){
    st.resize(4 * sz);
  int build(int 1, int r, vector<T>& o){
    int id = cnt++;
    if(1 == r){
      st[id].v = o[1];
      return id;
    }
    int m = (1 + r) / 2;
    st[id].1 = build(1, m, o);
    st[id].r = build(m + 1, r, o);
    pull(st[id], st[st[id].1], st[st[id
   ].r]);
    return id;
  void modify(int 1, int r, int v, int L
   , int R, int id){
    if(1 == L \&\& r == R){
      st[id].addTag(v);
      return;
    }
    int M = (L + R) / 2;
    if(r <= M) modify(l, r, v, L, M, st[</pre>
   id].1);
    else if (1 > M) modify (1, r, v, M +
   1, R, st[id].r);
      modify(1, M, v, L, M, st[id].1);
      modify(M + 1, r, v, M + 1, R, st[
   id].r);
    pull(st[id], st[st[id].1], st[st[id
   ].r]);
  }
```

```
T query(int 1, int r, int L, int R,
   int id){
    if(1 == L \&\& r == R) return st[id].
   rv();
    push(st[id], st[st[id].1], st[st[id
    int M = (L + R) / 2;
    if(r <= M) return query(1, r, L, M,</pre>
   st[id].1);
    else if(1 > M) return query(1, r, M
   + 1, R, st[id].r);
    else{
      return pullValue(query(1, M, L, M,
    st[id].1), query(M + 1, r, M + 1, R,
    st[id].r));
  }
};
```

# 3 Graph

#### 3.1 Dijkstra

```
//The first element in pair should be
   edge weight, and the second should be
    vertex
vector<vector<pii>> g;
int n;
int dijkstra(int start, int end){
  priority_queue<pii, vector<pii>,
   greater<pii>> q;
  for(pii p : g[start]){
    q.push(p);
  q.push(mp(0, start));
  vector<int> dis(n, -1);
  dis[start] = 0;
  vector<int> visit(n);
  while(q.size()){
    int v = q.top().S;
    int d = q.top().F;
    if(v == end) break;
    q.pop();
    if(visit[v]) continue;
    visit[v] = true;
    for(pii p : g[v]){
      if(visit[p.S]) continue;
      if(dis[p.S] == -1 \mid \mid d + p.F < dis
   [p.S]){
        dis[p.S] = d + p.F;
        q.push(mp(dis[p.S], p.S));
      }
    }
  }
  return dis[end];
```

# 3.2 Floyd-Warshall

```
vector<vector<int>> g;
int n;

void floydwarshall(){
  for(int k = 0; k < n; k++)
    for(int i = 0; i < n; i++)
      for(int j = 0; j < n; j++)
        if(g[i][k] != -MAX && g[k][j] !=
      -MAX && (g[i][j] == -MAX || g[i][k]
      + g[k][j] < g[i][j]))
        g[i][j] = g[i][k] + g[k][j];
}</pre>
```

## 3.3 Kruskal

```
int kruskal(){
  int ans = 0;
  lsort(e);
  initDSU();
  for(auto& i : e){
    int a = i.S.F, b = i.S.S;
    if(findDSU(a) == findDSU(b))
    continue;
    ans += i.F;
    unionDSU(a, b);
  }
  return ans;
}
```

# 3.4 Tarjan SCC

```
vector<vector<int>> g;
vector<int> st;
vector<bool> inst;
vector<int> scc;
vector<int> ts, low;
int tmp = 0;
int sccid = 0;
void initSCC(int n){
  tmp = 0;
  sccid = 0;
  st.clear();
  g.clear();
  g.resize(2 * n + 1);
  inst.clear();
  inst.resize(2 * n + 1);
  scc.clear();
  scc.resize(2 * n + 1);
  ts.clear();
  ts.resize(2 * n + 1, -1);
  low.clear();
  low.resize(2 * n + 1);
}
```

```
void dfs(int now){
  st.eb(now);
  inst[now] = true;
  ts[now] = ++tmp;
  low[now] = ts[now];
  for(int i : g[now]){
    if(ts[i] == -1){
      dfs(i);
      low[now] = min(low[now], low[i]);
    else if(inst[i]) low[now] = min(low[
   now], ts[i]);
  if(low[now] == ts[now]){
    sccid++;
    int t;
    do{
      t = st.back();
      st.pob;
      inst[t] = false;
      scc[t] = sccid;
    }
    while(t != now);
}
```

#### 3.5 SPFA

```
const 11 INFINITE = 2147483647;
int n;
vector<vector<pii>> g;
int spfa(int start, int end){
  vector<int> dis(n, INFINITE);
  int start;
  cin >> start;
  dis[start] = 0;
  queue < int > q;
  q.push(start);
  vector < bool > inq(n);
  inq[start] = true;
  vector<int> cnt(n);
  while(!q.empty()){
    int v = q.front();
    q.pop();
    inq[v] = false;
    for(pii p : g[v]){
      if(!(dis[p.F] == INFINITE || dis[v
```

```
in[now] = low[now] = ts++;
   ] + p.S < dis[p.F])) continue;
                                              st.push(now);
      cnt[p.F]++;
      if(cnt[p.F] >= n) return -INFINITE
                                              for(int i : tg[now]){
                                                if(i == p) continue;
   ; //negetive cycle
      dis[p.F] = dis[v] + p.S;
                                                if(in[i]) low[now] = min(low[now],
      if(!inq[p.F]){
                                                in[i]);
        inq[p.F] = true;
                                                else{
        q.push(p.F);
                                                   dfs(i, now);
      }
                                                   low[now] = min(low[now], low[i]);
    }
                                                   if((now != p && low[i] >= in[now])
                                                 || (now == p && cnt[now] > 1)){
                                                     int nowid = bccid++;
  return dis[end];
}
                                                     while(true){
                                                       int x = st.top();
3.6 Block-cut Tree
                                                       if(iscut[x]) id[x] = nowid;
                                                       else addedge(nowid, id[x]);
int n;
                                                       st.pop();
                                                       if(x == i) break;
vector<vector<int>> g;
vector<int> id;
                                                     iscut[now] = true;
vector<bool> iscut, bcccut;
                                                     if(id[now] == -1) id[now] =
                                                bccid++;
vector<vector<int>> tg;
                                                     bcccut[id[now]] = true;
vector<int> in, low, cnt;
                                                     addedge(id[now], nowid);
vector < bool > vst;
                                                  }
int ts = 1;
stack<int> st;
int bccid = 1;
                                              if (now == p && cnt[now] == 1 && !iscut
                                                [now]){
void init(){
                                                int nowid = bccid++;
 tg.resize(n + 1);
                                                while(!st.empty()){
  in.resize(n + 1);
                                                   int x = st.top();
  low.resize(n + 1);
                                                   if(!iscut[x]) id[x] = nowid;
  cnt.resize(n + 1);
                                                   else addedge(nowid, id[x]);
  vst.resize(n + 1);
                                                   st.pop();
  id.resize(n + 1, -1);
                                                }
  g.resize(2 * n + 1);
                                              }
  iscut.resize(n + 1);
                                            }
  bcccut.resize(2 * n + 1);
                                                String
                                            4.1 KMP
void addedge(int u, int v){
  g[u].eb(v);
  g[v].eb(u);
                                            vector<int> f;
                                            void build(string& t){
                                              f.clear();
void dfsc(int now, int p){
                                              f.resize(t.size());
  vst[now] = true;
                                              int p = -1;
  for(int i : tg[now]){
                                              f[0] = -1;
    if(i == p || vst[i]) continue;
                                              for(int i = 1; i < t.size(); i++){</pre>
    cnt[now]++;
                                                while (p != -1 \&\& t[p + 1] != t[i]) p
    dfsc(i, now);
                                                 = f[p];
  }
                                                if(t[p + 1] == t[i]) f[i] = p + 1;
}
                                                else f[i] = -1;
```

p = f[i];

}

void dfs(int now, int p){

```
int kmp(string& s, string& t){
  int ans = 0;
  int p = -1;
  for(int i = 0; i < s.size(); i++){
    while(p != -1 && t[p + 1] != s[i]) p
    = f[p];
    if(t[p + 1] == s[i]) p++;
    if(p + 1 == t.size()){
        ans++;
        p = f[p];
    }
  }
  return ans;
}</pre>
```

#### 4.2 Z Value

```
vector<int> z;

void build(string s, int n){
   z.clear();
   z.resize(n);
   int l = 0;
   for(int i = 1; i < n; i++){
      if(l + z[l] >= i) z[i] = min(z[l] +
      l - i, z[i - l]);
      while(i + z[i] < n && s[z[i]] == s[i
      + z[i]]) z[i]++;
      if(i + z[i] > l + z[l]) l = i;
   }
}
```

#### 4.3 Longest Palindromic Substring

```
#define T(x) ((x) % 2 ? s[(x) / 2] : '.'
   )
string s;
int L;
int ex(int 1, int r){
 int i = 0;
  while (1 - i \ge 0 \&\& r + i < L \&\& T(1 - i)
    i) == T(r + i)) i++;
  return i;
}
int lps(string ss){
 s = ss;
  L = 2 * s.size() + 1;
  int mx = 0;
  int center = 0;
  vector<int> r(L);
  int ans = 1;
```

```
r[0] = 1;
for(int i = 1; i < L; i++){
  int ii = center - (i - center);
  int len = mx - i + 1;
  if(i > mx){
    r[i] = ex(i, i);
    center = i;
    mx = i + r[i] - 1;
}
else if(r[ii] == len){
    r[i] = len + ex(i - len, i + len);
    center = i;
    mx = i + r[i] - 1;
}
else r[i] = min(r[ii], len);
  ans = max(ans, r[i]);
}
return ans - 1;
```

#### 4.4 Suffix Array

```
#include <bits/stdc++.h>
#define eb(a) emplace_back(a)
using namespace std;
vector<int> sa(string s){
  s += '$';
  int n = s.size();
  int t = _-lg(n) + 1;
  vector<vector<int>> rk(t + 1, vector<</pre>
   int>(n)), b;
  vector<vector<int>> c1(27);
  for(int i = 0; i < n; i++) c1[s[i] ==
   '$' ? 0 : s[i] - 'a' + 1].eb(i);;
  for(int i = 0; i < 27; i++){
    if(!c1[i].empty()) b.eb(c1[i]);
  b.resize(n);
  for(int i = 0; i < n; i++){
    for(int k : b[i]) rk[0][k] = i;
  for(int i = 1; i <= t; i++){
    vector < vector < int >> tb(n);
    for(int j = 0; j < n; j++){
      for(int k : b[j]){
        int tmp = ((k - (1 << (i - 1)))
   % n + n) % n;
        int now = rk[i - 1][tmp];
        tb[now].eb(tmp);
      }
```

|}

```
}
b = tb;
int cnt = -1;
for(int j = 0; j < n; j++){
   int lst = -1;
   for(int k : b[j]){
      int now = rk[i - 1][(k + (1 << (i - 1)))) % n];
      if(now != lst) cnt++;
      rk[i][k] = cnt;
      lst = now;
   }
}
return rk[t];
</pre>
```

# 5 Math and Geometry

## 5.1 Vector Operations

```
template < typename T>
pair<T, T> operator+(pair<T, T> a, pair<
   T, T > b
 return mp(a.F + b.F, a.S + b.S);
}
template < typename T>
pair<T, T> operator-(pair<T, T> a, pair<</pre>
   T, T > b
  return mp(a.F - b.F, a.S - b.S);
}
template < typename T>
pair<T, T> operator*(pair<T, T> a, T b){
 return mp(a.F * b, a.S * b);
template < typename T >
pair<T, T> operator/(pair<T, T> a, T b){
 return mp(a.F / b, a.S / b);
template < typename T>
T dot(pair<T, T> a, pair<T, T> b){
 return a.F * b.F + a.S * b.S;
}
template < typename T>
T cross(pair<T, T> a, pair<T, T> b){
  return a.F * b.S - a.S * b.F;
template < typename T>
T abs2(pair<T, T> a){
 return a.F * a.F + a.S * a.S;
```

## 5.2 Convex Hull

```
template < typename T >
pair <T, T> operator - (pair <T, T> a, pair <
   T, T > b
  return mp(a.F - b.F, a.S - b.S);
}
template < typename T >
T cross(pair<T, T> a, pair<T, T> b){
  return a.F * b.S - a.S * b.F;
template < typename T>
vector<pair<T, T>> getConvexHull(vector<
   pair<T, T>>& pnts){
  int n = pnts.size();
  lsort(pnts);
  vector<pair<T, T>> hull;
  hull.reserve(n);
  for(int i = 0; i < 2; i++){
    int t = hull.size();
    for(pair<T, T> pnt : pnts){
      while(hull.size() - t >= 2 \&\&
   cross(hull.back() - hull[hull.size()
   - 2], pnt - hull[hull.size() - 2]) <=
        hull.pop_back();
      }
      hull.pb(pnt);
    hull.pop_back();
    reverse(iter(pnts));
  return hull;
5.3 Prime Sieve
```

```
vector<int> prime;
vector<int> p;
void sieve(int n){
  prime.resize(n + 1, 1);
  for(int i = 2; i <= n; i++){
    if(prime[i] == 1){
      p.push_back(i);
      prime[i] = i;
    }
  for(int j : p){
      if((ll)i * j > n || j > prime[i])
      break;
```

```
prime[i * j] = j;
}
}
```

#### 5.4 XOR Basis

```
const int mxdigit = 50;
vector<ll> b(mxdigit + 1);
void add(ll t){
  for(int i = mxdigit; i >= 0; i--){
    if(!(1LL << i & t)) continue;</pre>
    if(b[i] != 0){
      t ^= b[i];
      continue;
    }
    for(int j = 0; j < i; j++){
      if(1LL << j & t) t ^= b[j];</pre>
    for(int j = i + 1; j \le mxdigit; j
      if(1LL << i & b[j]) b[j] ^= t;</pre>
    b[i] = t;
    break;
  }
}
```

#### 6 DP Trick

## 6.1 Dynamic Convex Hull

```
const ll INF = 1LL << 60;</pre>
template < typename T>
struct Line{
  mutable T a, b, r = 0;
  Line(T a, T b) : a(a), b(b){}
  bool operator < (Line < T > 1) const{
    return a < 1.a;
 bool operator<(T v)const{</pre>
    return r < v;
  }
};
template < typename T>
T divfloor(T a, T b){
  return a / b - ((a ^ b) < 0 && a % b);
}
template < typename T>
```

```
struct DynamicHull{
  multiset <Line <T>, less <>> s;
  int size(){
    return s.size();
  bool intersect(typename set<Line<T>>::
   iterator a, typename set<Line<T>>::
   iterator &b){
    if(b == s.end()){}
      a \rightarrow r = INF;
      return false;
    }
    if(a->a == b->a){
      if(a->b > b->b) a->r = INF;
      else a \rightarrow r = -INF;
    else{
      a->r = divfloor(b->b - a->b, a->a
    - b->a);
    }
    return a \rightarrow r >= b \rightarrow r;
  void insert(T a, T b){
    Line<T> l(a, b);
    auto it = s.insert(1), after = next(
   it), before = it;
    while(intersect(it, after)) after =
   s.erase(after);
    if(before != s.begin() && intersect
    (--before, it)){
      it = s.erase(it);
      intersect(before, it);
    while((it = before) != s.begin() &&
    (--before)->r >= it->r) intersect(
   before, it = s.erase(it));
  }
  T query(T v){
    Line<T> l = *s.lower_bound(v);
    return l.a * v + l.b;
  }
};
```

#### 7 Numbers and Math Formulae

## 7.1 Fibonacci

$$f(n) = f(n-1) + f(n-2)$$
$$\begin{bmatrix} f(n) \\ f(n-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$f(45) \approx 10^9$$
  
 $f(88) \approx 10^{18}$ 

## 7.2 Catalan

$$C_0 = 1, C_n = \sum_{i=0}^{n-1} C_i C_{n-1-i}$$

$$C_n = C_n^{2n} - C_{n-1}^{2n}$$

# 7.3 Geometry

- Heron's formula: The area of a triangle whose lengths of sides is a,b,cand s = (a+b+c)/2 is  $\sqrt{s(s-a)(s-b)(s-c)}$ .
- Vector cross product:  $v_1 \times v_2 = |v_1||v_2|\sin\theta = (x_1 \times y_2) - (x_2 \times y_1).$
- Vector dot product:  $v_1 \cdot v_2 = |v_1||v_2|\cos\theta = (x_1 \times y_1) + (x_2 \times y_2).$

#### 7.4 Prime Numbers

First 50 prime numbers:

Very large prime numbers:

 $\begin{array}{cccc} 1000001333 & 1000500889 & 2500001909 \\ 2000000659 & 900004151 & 850001359 \end{array}$ 

## 7.5 Number Theory

- Inversion:  $aa^{-1} \equiv 1 \pmod{m}$ .  $a^{-1}$  exists iff gcd(a, m) = 1.
- Linear inversion:  $a^{-1} \equiv (m \lfloor \frac{m}{a} \rfloor) \times (m \mod a)^{-1} \pmod{m}$
- Fermat's little theorem:  $a^p \equiv a \pmod{p}$  if p is prime.
- Euler function:  $\phi(n) = n \prod_{p|n} \frac{p-1}{p}$
- Euler theorem:  $a^{\phi(n)} \equiv 1 \pmod{n}$  if  $\gcd(a, n) = 1$ .
- Extended Euclidean algorithm:  $ax + by = \gcd(a, b) = \gcd(b, a \mod b) = \gcd(b, a \lfloor \frac{a}{b} \rfloor b) = bx_1 + (a \lfloor \frac{a}{b} \rfloor b)y_1 = ay_1 + b(x_1 \lfloor \frac{a}{b} \rfloor y_1)$
- Divisor function:  $\sigma_x(n) = \sum_{d|n} d^x$ .  $n = \prod_{i=1}^r p_i^{a_i}$ .  $\sigma_x(n) = \prod_{i=1}^r \frac{p_i^{(a_i+1)x}-1}{p_i^x-1}$  if  $x \neq 0$ .  $\sigma_0(n) = \prod_{i=1}^r (a_i+1)$ .
- Chinese remainder theorem:  $x \equiv a_i \pmod{m_i}$ .  $M = \prod m_i$ .  $M_i = M/m_i$ .  $t_i = M_i^{-1}$ .  $x = kM + \sum a_i t_i M_i$ ,  $k \in \mathbb{Z}$ .

#### 7.6 Combinatorics

- $\bullet \ P_k^n = \frac{n!}{(n-k)!}$
- $C_k^n = \frac{n!}{(n-k)!k!}$
- $H_k^n = C_k^{n+k-1} = \frac{(n+k-1)!}{k!(n-1)!}$