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Everything Formula – AEON-M Codex
Engine (Unified v2.0)

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License: MIT (change if you need
Business Source later)

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import os, json, math, wave, struct,
argparse
import numpy as np
import matplotlib.pyplot as plt

```
# Core Constants
# -----
PHI = (1 + np.sqrt(5)) / 2 # Golden ratio
GOLDEN_ANGLE_DEG =
137.50776405003785 # degrees between seeds in phyllotaxis
GOLDEN_ANGLE_RAD =
np.deg2rad(GOLDEN_ANGLE_DEG) # radians
ALPHA_INV = 137.036 # Inverse fine-structure constant (as a scale knob)
TAU = 2 * np.pi # 2π
EPS = 1e-12

# Create output dirs
def _ensure_dirs():
    for d in ["assets", "data", "audio"]:
        os.makedirs(d, exist_ok=True)
```

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```
# 1) Kepler Solver (keeps your original,  
adds rad/deg control)
```

```
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```
def solve_kepler(M, e, initial_E=None,  
tol=1e-12, max_iter=40, degrees=True):
```

```
    """
```

Solve Kepler's equation $M = E - e \sin E$
for eccentric anomaly E .

Returns (E_{final} , iteration_log). M may
be degrees or radians.

```
    """
```

```
    M_rad = np.deg2rad(M) if degrees else  
M
```

```
    E = M_rad if initial_E is None else  
initial_E
```

```
    iters = []
```

```
for i in range(max_iter):
    f = E - e * np.sin(E) - M_rad
    fp = 1 - e * np.cos(E)
    step = f / (fp + EPS)
    E_new = E - step
    err = abs(step)
```

```
iters.append({
    "iter": i + 1,
    "E_deg": float(np.rad2deg(E_new)),
    "M_deg": float(np.rad2deg(E_new -
e * np.sin(E_new))),
    "abs_step_deg":
float(np.rad2deg(step))
})
E = E_new
if err < tol:
    break
```

```
return (float(np.rad2deg(E)) if degrees
```

else float(E)), iters

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2) Recursive Field ($r = a\sqrt{n}$, $\theta = n\varphi$ or
golden-angle phyllotaxis)

+ 3–6–9 “square-off” recursion

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def recursive_field_points(N=2000, a=1.0,
mode="golden_angle"):

"""

 mode: "golden_angle" -> $\theta_n = n * \text{golden_angle}$

 "golden_ratio" -> $\theta_n = n * \text{PHI}$

 returns x, y arrays

"""

n = np.arange(1, N + 1, dtype=float)

r = a * np.sqrt(n)

```
if mode == "golden_angle":  
    theta = n * GOLDEN_ANGLE_RAD  
else:  
    theta = n * PHI  
x = r * np.cos(theta)  
y = r * np.sin(theta)  
return x, y
```

```
def rotate_points(x, y, angle_rad):  
    ca, sa = np.cos(angle_rad),  
    np.sin(angle_rad)  
    xr = x * ca - y * sa  
    yr = x * sa + y * ca  
    return xr, yr
```

```
def square_off_369(N=1500, a=1.0,  
depth=2):
```

""""

Build three seed arms (3,6,9) then
'square-off' by rotating each arm by 120°
recursively for 'depth' levels. Returns list

of (x,y) arms.

=====

```
arms = []
base_x, base_y =
recursive_field_points(N=N, a=a,
mode="golden_angle")
```

```
# Seed rotations for 3, 6, 9 (equilateral
spacing)
```

```
seeds_deg = [0.0, 120.0, 240.0]
```

```
for sd in seeds_deg:
```

```
    x1, y1 = rotate_points(base_x,
base_y, np.deg2rad(sd))
    arms.append((x1, y1))
```

```
# Recursive square-off: at each depth,
rotate each arm by ±90° (squaring gesture)
```

```
for d in range(1, depth + 1):
```

```
    new_arms = []
```

```
    for (x, y) in arms[-3:]: # work from
last level's three
```

```
    for rot_deg in (90, -90):
        xr, yr = rotate_points(x, y,
np.deg2rad(rot_deg))
            new_arms.append((xr *
(0.85**d), yr * (0.85**d))) # slight scale-
in to nest
    arms.extend(new_arms)
```

return arms

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```
# 3) Rodin Map (mod-9 doubling) + 3/6/9
anchors
```

```
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```
def rodin_doubling_sequence(start=1,
steps=30):
```

```
=====
```

Generate Rodin-style doubling pattern
modulo 9: 1→2→4→8→7→5→1 ...

=====

```
seq = []
v = start % 9
if v == 0: v = 9
for _ in range(steps):
    seq.append(v)
    v = (2 * v) % 9
    if v == 0: v = 9
return seq
```

```
def digital_root(n):
    s = n % 9
    return 9 if s == 0 and n != 0 else s
```

```
def mod9_map(N=100):
    return [digital_root(i) for i in range(1, N + 1)]
```

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# 4) Frequency Engines (equal-
temperament & golden scaling)
# + WAV sonification
#
=====

=====

def notes_equal_temperament(n_steps,
f0=220.0): # A3 default
    # semitone steps around f0 over
n_steps
    return [f0 * (2 ** (k/12)) for k in
range(n_steps)]

def notes_golden(n_steps, f0=220.0):
    return [f0 * (PHI ** k) for k in
range(n_steps)]

def sequence_from_mod9(mods,
base=110.0, scheme="et12"):
```

=====

Map mod-9 digits to a scale. 1..9 → offsets.

scheme: "et12" (equal temperament) or "golden"

=====

```
freqs = []
```

```
for d in mods:
```

```
    offset = {1:0, 2:2, 3:3, 4:5, 5:7, 6:8,  
7:10, 8:12, 9:14}[d] # a musical-ish  
mapping
```

```
    if scheme == "et12":
```

```
        freqs.append(base * (2 ** (offset/  
12)))
```

```
    else:
```

```
        freqs.append(base * (PHI ** (offset/  
12)))
```

```
return freqs
```

```
def synth_wav_mono(filename, freqs,  
seconds_each=0.25, fs=44100,
```

fade=0.01, vol=0.3):

=====

 Render a simple sine sweep across
 freqs → WAV mono.

=====

 _ensure_dirs()

 with wave.open(os.path.join("audio",
 filename), "w") as wf:

 wf.setnchannels(1);

 wf.setsampwidth(2); wf.setframerate(fs)

 for f in freqs:

 n = int(seconds_each * fs)

 t = np.arange(n) / fs

 sig = np.sin(2*np.pi*f*t)

 # quick fade-in/out

 fade_n = max(1, int(fade * fs))

 env = np.ones_like(sig)

 env[:fade_n] = np.linspace(0, 1,
 fade_n)

 env[-fade_n:] = np.linspace(1, 0,
 fade_n)

```
    sig = vol * sig * env
    # write int16
    chunk = (sig *
32767).astype(np.int16).tolist()
    wf.writeframes(struct.pack("<" +
"h"*len(chunk), *chunk))
    return os.path.join("audio", filename)
```

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```
# 5) Kepler-corrected spiral &
Zero-point-style phase toy
```

```
#
```

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```
def kepler_corrected_spiral(N=600,
scale=1.0, M_deg=66.0, e=0.21):
```

```
    E_deg, _ = solve_kepler(M_deg, e,
degrees=True)
```

```
    phase = np.deg2rad(E_deg)
```

```
n = np.arange(1, N+1, dtype=float)
r = scale * np.sqrt(n)
theta = n * GOLDEN_ANGLE_RAD +
phase
return r * np.cos(theta), r * np.sin(theta)
```

```
def zero_point_phase(n, omega=1.0,
phase=0.0):
    # simple complex wave as a diagnostic
toy (no claims)
    return np.exp(1j * (phase + n * omega))
```

```
#
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=====
# 6) DNA waveform mapper (lightweight)
#
=====
=====
def dna_waveform(seq,
base_freq=2*np.pi*0.5, phase=0.0):
```

=====

Map ATCG into amplitude weights over a sine spine.

=====

```
weight = {'A': 1.0, 'T': 0.8, 'C': 0.6, 'G': 0.9}
y = []
for i, base in enumerate(seq.upper()):
    y.append(weight.get(base, 0.0) *
np.sin(base_freq*i + phase))
return np.array(y)
```

#

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7) Visualizations

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=====

```
def plot_recursive_field(arms, title="3-6-9
Square-Off Recursive Field"):
    _ensure_dirs()
```

```
plt.figure(figsize=(8,8))
for (x, y) in arms:
    plt.scatter(x, y, s=2, alpha=0.6)
plt.axis("equal")
plt.title(title)
plt.tight_layout()
out = "assets/recursive_field_369.png"
plt.savefig(out, dpi=180); plt.close()
return out
```

```
def plot_kepler_spiral(x, y,
title="Kepler-Corrected Spiral"):
    _ensure_dirs()
    plt.figure(figsize=(7,7))
    plt.scatter(x, y, s=6, alpha=0.75)
    plt.axis("equal")
    plt.title(title)
    plt.tight_layout()
    out = "assets/kepler_spiral.png"
    plt.savefig(out, dpi=180); plt.close()
    return out
```

```
def plot_rodin_map(seq, title="Rodin Doubling (mod 9)":  
    _ensure_dirs()  
    plt.figure(figsize=(8,3))  
    plt.plot(seq, marker="o");  
    plt.yticks(range(1,10))  
    plt.grid(True, alpha=0.3); plt.title(title);  
    plt.tight_layout()  
    out = "assets/rodin_doubling.png"  
    plt.savefig(out, dpi=180); plt.close()  
    return out
```

```
def plot_dna(y, title="DNA Waveform Mapper"):  
    _ensure_dirs()  
    plt.figure(figsize=(9,3))  
    plt.plot(y)  
    plt.title(title); plt.tight_layout()  
    out = "assets/dna_waveform.png"  
    plt.savefig(out, dpi=180); plt.close()
```

```
return out
```

```
#
```

```
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```

```
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```

8) Master run

```
#
```

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```

```
def main():
```

```
    parser =
```

```
argparse.ArgumentParser(description="Ev  
erything Formula – AEON-M Unified v2.0")
```

```
    parser.add_argument("--N", type=int,  
default=1800, help="points per arm")
```

```
    parser.add_argument("--depth",  
type=int, default=2, help="square-off  
recursion depth")
```

```
    parser.add_argument("--a", type=float,  
default=1.0, help="spiral scale a in r =  
a $\sqrt{n}$ ")
```

```
parser.add_argument("--keplerM",
type=float, default=66.0, help="mean
anomaly (deg)")

parser.add_argument("--keplere",
type=float, default=0.21,
help="eccentricity")

parser.add_argument("--dna", type=str,
default="ATCGATGCACTG", help="DNA toy
sequence")

parser.add_argument("--audio",
action="store_true", help="render mod-9
sonification")

args = parser.parse_args()

_ensure_dirs()

# 3-6-9 recursive field
arms = square_off_369(N=args.N,
a=args.a, depth=args.depth)
img1 = plot_recursive_field(arms)
```

```
# Kepler-corrected spiral
kx, ky = kepler_corrected_spiral(N=800,
scale=args.a, M_deg=args.keplerM,
e=args.keplere)
img2 = plot_kepler_spiral(kx, ky)
```

```
# Rodin doubling + mod9 mapping
rodin_seq =
rodin_doubling_sequence(start=1,
steps=60)
img3 = plot_rodin_map(rodin_seq)
```

```
mod9 = mod9_map(64)
# Build two audio sequences
if args.audio:
    freqs_et =
sequence_from_mod9(mod9,
base=110.0, scheme="et12")
    freqs_phi =
sequence_from_mod9(mod9,
base=110.0, scheme="golden")
```

```
    wav1 =  
synth_wav_mono("mod9_equal_tempera  
ment.wav", freqs_et, seconds_each=0.22)  
    wav2 =  
synth_wav_mono("mod9_golden_scaling.  
wav", freqs_phi, seconds_each=0.22)  
else:  
    wav1 = wav2 = None
```

```
# DNA toy  
y = dna_waveform(args.dna,  
base_freq=np.pi/6, phase=0.0)  
img4 = plot_dna(y)
```

```
# Kepler iteration log (for provenance)  
E_final, klog =  
solve_kepler(args.keplerM, args.keplere,  
degrees=True)  
with open(os.path.join("data",  
"kepler_iterations.json"), "w") as f:  
    json.dump({"E_final_deg": E_final,
```

```
"iterations": klog}, f, indent=2)
```

```
# Summary
```

```
summary = {
```

```
    "images": [img1, img2, img3, img4],
```

```
    "audio": [wav1, wav2],
```

```
    "kepler_E_final_deg": E_final
```

```
}
```

```
with open(os.path.join("data",
```

```
"run_summary.json"), "w") as f:
```

```
    json.dump(summary, f, indent=2)
```

```
print("\n==== AEON-M Unified v2.0 ===")
```

```
print(f"Recursive field image: {img1}")
```

```
print(f"Kepler spiral image : {img2}")
```

```
print(f"Rodin map image : {img3}")
```

```
print(f"DNA waveform image : {img4}")
```

```
if wav1 or wav2:
```

```
    print(f"Audio (ET12) : {wav1}")
```

```
    print(f"Audio (Golden) : {wav2}")
```

```
print(f"Kepler E_final (deg) :
```

```
{E_final:.6f}")  
    print("Artifacts written to ./assets, ./  
audio, ./data\n")
```

```
if __name__ == "__main__":  
    main()
```