UNIVERSITY OF TWENTE

Faculty of Engineering Technology Minor Aircraft Engineering



Aircraft Structures (202000157)

Final Exam - January 2021

Available Time: Two hours

Permitted Materials: Calculator, Formula Sheet

Generic guidelines:

- 1. The front page lists the materials you can use during this exam. Any other materials are not allowed. This includes mobile devices.
- 2. When asked, elaborate your answers by providing the equations used or listing the assumptions made.
- 3. Please write clearly. I am an engineer not an archaeologist.

NB. This is an individual exam. Good luck!

Question 1. [15/100 points] The two dimensional stress state at a particular point in a structure equals $\sigma_x = 350$ MPa, $\sigma_y = 225$ MPa and $\tau_{xy} = 100$ MPa.

1. [10 points] Calculate the principal stresses and the orientation of the corresponding principal planes.

Answer

The principal stresses are: $\sigma_{\rm I}=405$ MPa and $\sigma_{\rm II}=170$ MPa, while the principal planes are oriented at $\theta=0.51\pm\pi/2$ or $\theta=29^{\circ}\pm90^{\circ}$.

As a reminder, the equations for the principal stresses are:

$$\sigma_{\rm I,II} = \frac{\sigma_{\rm x} + \sigma_{\rm y}}{2} \pm \frac{1}{2} \sqrt{(\sigma_{\rm x} - \sigma_{\rm y})^2 + 4\tau_{\rm xy}^2},$$

while the principal planes can be found using:

$$\tan 2\theta = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}.$$

Points: Award 3 points for the correct equation for the principal stresses, 3 points for the correct equation for the principal planes and 2 points for each correct answer.

2. [5 points] What is the magnitude of the shear stress acting on the principal planes?

Answer

The shear stress on the principal planes equals 0 MPa.

Points: 5 points for the correct answer, otherwise 0.

Question 2. [15/100 points] The turbine blades in modern jet engines are subjected to intense heat and extreme loads...

