

# A Structural Model of Liquidity in Over-the-Counter Markets

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Views are solely those of the authors and so cannot be taken to represent those of  
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# Market Liquidity

Corporate bonds:

- Key **source of financing** for firms in the real economy.
- Key **investment** for financial institutions.
- Trade in **over-the-counter markets**.

**Market liquidity:** firms can trade quickly and at low cost.

Illiquidity in corporate bond markets:

- ① Undermines firms' abilities to **issue debt**.
- ② Threatens **financial stability**.

# Market Liquidity

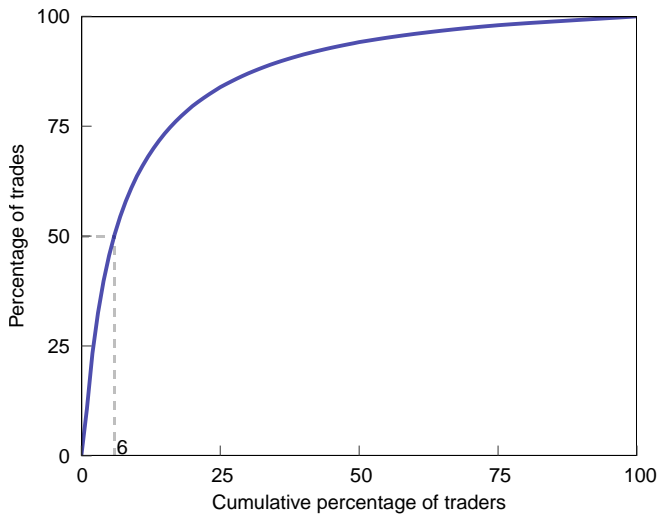
Liquidity is an equilibrium outcome which is shaped by:

- ① Financial conditions.
- ② Trading technologies.
- ③ Regulatory policy.

## This Paper

Combine theory with unique dataset on **secondary market for sterling corporate bonds** to study liquidity and its determinants.

# Firm Heterogeneity



# Research Questions

**Firm heterogeneity:** a small subset of frequent traders do the bulk of trading.

**Q1:** To what extent is **liquidity** reliant on a small subset of frequent traders?

**Q2:** How does this heterogeneity interact with:

- ① Financial shocks?
- ② Trading platforms?
- ③ Banking regulation?

# Approach

- ① Data on **all firms' trading** in sterling corporate bonds.
- ② Empirical facts on trader heterogeneity, intermediation, and trading activity.
- ③ Search & matching model of trading informed by the data.  
→ **Heterogeneous search costs** across traders.
- ④ Structural estimation.  
→ Pin down search cost distribution.
- ⑤ Counterfactual analyses.

Literature

# Findings

**Q1:** Is liquidity reliant on a small subset of traders? 8% most frequent traders supply as much liquidity as the remaining 92%.

**Q2:** How does this heterogeneity interact with:

- ① Financial shocks? Market highly vulnerable to shocks to frequent traders.
- ② Trading platforms? Platforms efficiency-enhancing, but harm frequent traders → will resist their introduction.
- ③ Bank capital regulation? Reduces liquidity, but market responses reduce costs by 30%. Costs increase in a stress.

# Literature & Contribution

## OTC Market liquidity and its determinants.

**Market features.** Di Maggio, Kermani & Song (2017), Li & Schürhoff (2019), Fontaine & Walton (2020).

**Post-crisis regulation.** Adrian, Fleming, Shachar & Vogt (2017), Bao, O'Hara & Zhou (2018), Bessembinder, Jacobsen, Maxwell & Venkataraman (2018), Choi & Huh (2021), Schultz (2017).

**Financial shocks.** Eisfeldt, Herskovic, Rajan & Siriwardane (2021).

**Trading mechanisms.** Allen & Wittwer (2021), Barclay, Hendershott & Madhavan (2015), Plante (2018).

Innovation:

- 1 Structurally estimate model of liquidity.

Contribution:

- 1 Explain mechanisms.
- 2 Counterfactual scenarios.



# Literature & Contribution

## Search models of financial markets.

Duffie, Gârleanu & Pedersen (2005, 2007), Afonso & Lagos (2015); Lagos & Rochetau (2009), Vayanos & Weill (2008), Uslu (2019). Neklyudov (2019), Farboodi, Jarosch & Shimer (2021), Liu (2020). Brancaccio, Li & Schürhoff (2020), Allen, Clark & Houde (2019), Gavazza (2016).

### Innovation:

- 1 Structural estimation.
- 2 Endogenous search & unconstrained holdings.

### Contribution:

- 1 Quantitative importance.
- 2 Traders vary search intensity to manage balance sheets and respond to shocks.

Approach Findings

## Data & Facts

# The Secondary Market for Sterling Corporate Bonds

**Issuers:** British Petroleum, Manchester United.

**Traders:** Banks, asset managers, hedge funds & insurers.

Trading is **bilateral** and typically **phone-based**.

Rough distinction between **dealers**—who intermediate/supply liquidity—and **customers**—who demand it.

Bond market **dealers tend to be banks**.

# Data

## Trade data

Bank of England transaction-level data on secondary market for **sterling corporate bonds**.

- Any transaction by UK-regulated firm or EU subsidiary of UK-regulated firm.
- 2012-2017.
- **Fields:** price, quantity, time of trade, trader identities.

## Bond characteristics data

Refinitiv Eikon data on primary issuance and bond characteristics.

**Comparative advantage:** Identity of all traders.

# Empirical Facts

- ① Trading is concentrated in a small subset of frequent traders.
- ② Frequent traders intermediate.
- ③ Both dealers & customers demand and supply liquidity.
- ④ Traders vary trading frequency to manage balance sheets.
- ⑤ Dealer trading behaviour varies with capital regulation.

Fact 1

Fact 2

Fact 3

Fact 4

Fact 5

# Endogenous Trading Frequency

|                   | Probability (%) |      |
|-------------------|-----------------|------|
|                   | Theory          | Data |
| Paired trades     | 6.9             | 44   |
| Offsetting trades | 3.5             | 31   |

**Paired:** firm trades same bond more than once on same day.

**Offsetting:** firm buys and sells same bond on same day. [Back](#)

# Empirical Facts

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Fact 1

Fact 2

Fact 3

Fact 4

Fact 5

# Model



# Overview

**Search and matching framework** in the spirit of Duffie, Gârleanu & Pedersen (2005) and Uslu (2019).

- Dynamic model.
- Single tradable asset.
- Continuum of risk-averse traders.
- Shocks to traders' valuations  $\rightarrow$  gains to trade.
- Search frictions  $\rightarrow$  illiquidity.
- Random search  $\rightarrow$  meetings  $\rightarrow$  bilateral bargaining.

# The Model and the Data

Trading is concentrated in small set of firms.

→ **heterogeneous costs** of searching.

Firms adjust trading frequency to manage balance sheets.

→ **endogenous search** intensity.

Dealers & customers demand and supply liquidity.

→ **endogenous intermediation**.

# Components of Equilibrium

**Trader type** (search cost  $z$ , valuation  $\beta$ , holdings  $h$ )  $\equiv \Delta$ .

## Inputs

- Utility parameters.
- Shock frequency.
- Search cost distribution.
- Matching function.

## Equilibrium outcomes

- Quantity  $q(\Delta, \Delta')$  & price  $p(\Delta, \Delta')$ .
- Search intensity  $\gamma(\Delta)$ .
- Value function:  $V(\Delta)$ .
- Distributions:  $\Phi(\Delta)$ .

# Value Function

Equation governing traders' optimal behaviour:

$$\begin{aligned}
 r \underbrace{V(z, \beta, h)}_{\text{Value}} = & \underbrace{u(\beta, h) - s(z, \gamma(z, \beta, h))}_{\text{Flow value \& search costs}} + \\
 & \underbrace{\eta \int (V(z, \beta', h) - V(z, \beta, h)) G(d\beta')}_{\text{Switch type}} + \\
 & \frac{1}{2} \iiint \underbrace{m(\gamma(z, \beta, h), \gamma(z', \beta', h'))}_{\text{Meeting probability}} \underbrace{S((z, \beta, h), (z', \beta', h'))}_{\text{Surplus}} \Phi(dz', d\beta', dh')
 \end{aligned}$$

# Equilibrium Decisions

## Trading Decision Details

- **Nash bargaining** over price  $p(\Delta, \Delta')$  & quantity  $q(\Delta, \Delta')$ .
  - Quantity maximises the surplus. Quantity
  - Price splits the surplus equally. Price

## Search Decision Search

- Search intensity  $\gamma(\Delta) \rightarrow MC=MB$ .
- Traders search harder:
  - if they have **low search cost**.
  - when **gains to trade are higher**.

## Asset Distributions

- Steady state  $\rightarrow$  **trading flows** perfectly balance **shock flows**.
- Market clears. Details Equilibrium

# Equilibrium Trading & Liquidity

Values  $V(z, \beta, h)$  are concave in holdings.

- Traders have a **target holding** that depends on their search cost and valuation.
- Traders with **low valuations and high holdings sell** the asset.
- Traders with **high valuations hold more** of the asset.

**Market Depth:** maximum amount that could be sold per unit time without depressing price by more than a given amount.

- **Extensive margin:** how frequently can I trade?
- **Intensive margin:** how costly is it for me to trade?

Definition

## Estimation & Results

# Estimation

**Parametric assumptions:** Utility, search cost & shock process parameters.

**GMM:** match theoretical to empirical moments.

Moments summarising the joint distribution of holdings, trading frequency, price and quantity. Search costs Matching Moments



# Interpreting Parameter Values

Estimated model fits data well. Moment Fit Estimates

Highly **skewed distribution of search costs** → large technological advantage for frequent traders.

**Trading more frequent than shocks.**

- Quantity rationing.
- Liquidity supply.

# Research Questions

**Q1:** To what extent is liquidity reliant on a small subset of traders?

**Q2:** How does firm heterogeneity interact with:

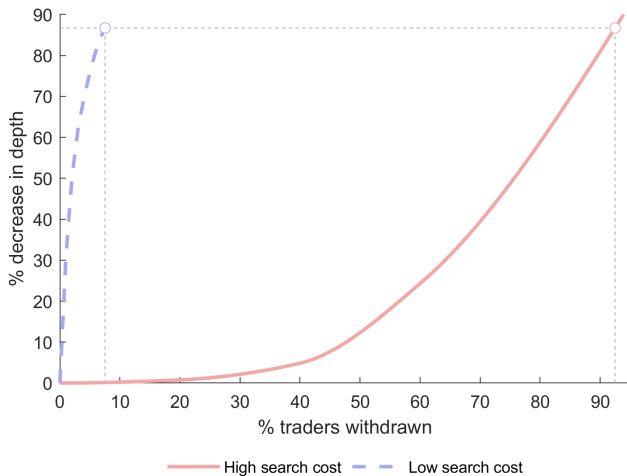
- ① Financial shocks?
- ② Trading platforms?
- ③ Banking regulation?

# Research Questions: Heterogeneity

**Question:** To what extent is liquidity reliant on a small subset of traders?

**Exercise:** Withdraw sets of traders and compute impact on liquidity.

# Contributions to Liquidity



8% of traders supply as much liquidity as the remaining 92%.

# Research Questions: Platforms

**Question:** How does firm heterogeneity interact with **trading platforms**?

**Exercise:** Simulate impact of trading platforms on liquidity & welfare.

# Trading Platforms

Market historically **over-the-counter**: bilateral and phone-based.

Slow increase in **platform-based trading**:

- Multilateral electronic trading platforms.
- Bids posted to all platform members.

Success requires sufficient uptake.

Two types of counterfactual.

- ① Platforms as **reduction & homogenisation of search costs**:  
→ set all search costs to those of the lowest-cost trader.
- ② Platforms as **more efficient trading mechanisms**:  
→ Walrasian equilibrium.

# Trading Platforms: Results

|                     | Baseline |           | Homog. | Walras. |
|---------------------|----------|-----------|--------|---------|
|                     | Low cost | High cost | Agg.   | Agg     |
| Spreads, bps        | 223      | -223      | 0      | 0       |
| Utility             | 16.3     | 13.3      | 14.5   | 14.5    |
| <i>Aggregate</i>    |          |           |        |         |
| Price variance, bps | 378      |           | 90     | 0       |
| Utility             | 13.8     |           | 14.5   | 14.5    |

Platforms improve liquidity and welfare, but **frequent traders worse off**.

# Trading Platforms: Drivers

**Trading platforms a trade-off** for most efficient traders:

- Pro: improved search technology.
- Con: loss of competitive advantage.

Estimation:

- Frequent traders can trade more frequently than shocked.  
→ **Benefits are small.**
- Skewed search cost distribution → large competitive advantage.  
→ **Costs are large.**

Frequent traders will resist introduction of platforms.



# Trading Platforms: Implications

## How do frequent traders block platforms?

- Intermediaries' balance sheet capacity required on platform.
- Intermediaries hold more of bond at issuance.
- Intermediaries generate as well as satisfy trading volume.

## Can traders find a way around this?

- Recent collaborations between platform companies and investment banks.

# Research Questions: Banking Regulation

**Question:** How does firm heterogeneity interact with **bank capital regulation**?

**Exercise:** Simulate impact of capital regulation on liquidity & welfare. [Details](#)

# Capital Regulation and Bond markets

Rationalises recent trends in markets:

- Capital **regulation reduces liquidity**, but **markets adjust** to reduce the costs.
  - Adjust search to better control balance sheet.
  - Bonds pass to non-dealers.
  - Non-dealers supply liquidity.
- **In sell-offs**, dealers are called upon to buy assets, and are less willing to do so → **costs go up**.

# Findings

**Q1:** Is liquidity reliant on a small subset of traders? 8% most frequent traders supply as much liquidity as the remaining 92%.

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Literature

# Conclusion

Combine theory and data to quantitatively study **liquidity in OTC markets**.

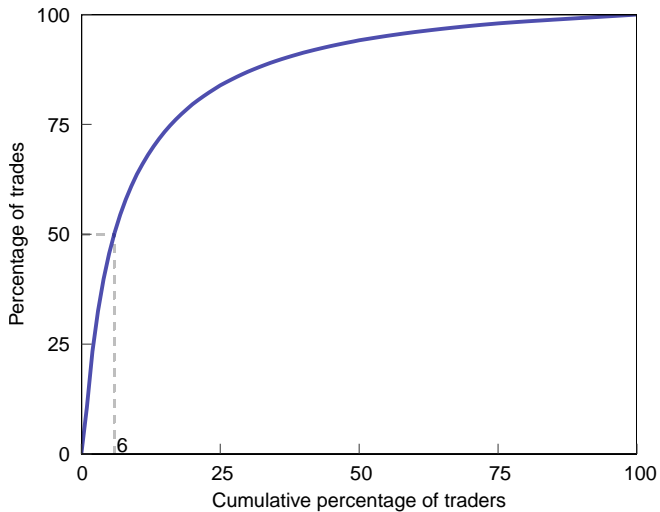


Study implications for:

- ① Resilience of liquidity.
- ② Trading technologies.
- ③ Regulatory policy.

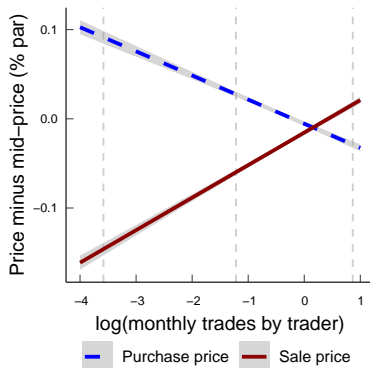
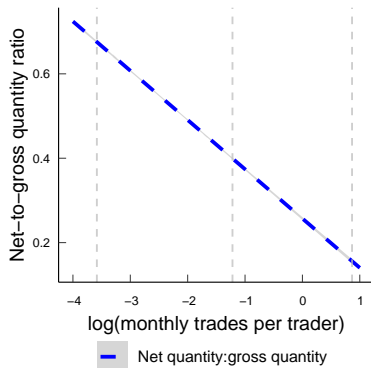
Thanks!  
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# Firm Heterogeneity



[Back](#)

# Intermediation & Trading Frequency



Frequent traders earn money by transferring bonds from sellers to buyers. [Back](#)



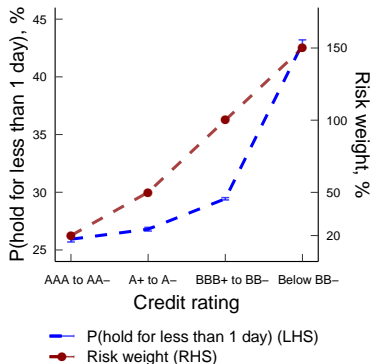
# Trading by Firm Type

| Buyer\ Seller | Customer | Dealer |
|---------------|----------|--------|
| Customer      | 23       | 30     |
| Dealer        | 33       | 14     |

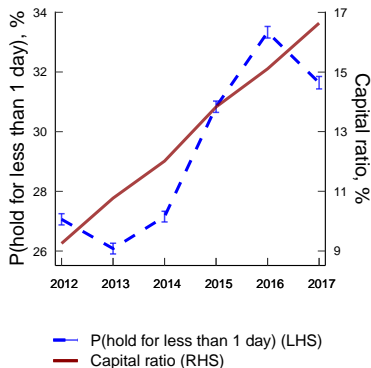
All traders face incentives to demand and supply liquidity.

Firms that are not traditional 'dealers' seek to make money by supplying liquidity (BlackRock, 2015). [Back](#)

# Dealer Trading and Capital Regulation



By risk weight



Through time

Traders condition their trading behaviour on regulation.

[Back](#)

# Trading Quantity

**Nash bargaining:** price  $p(\Delta, \Delta')$  & quantity  $q(\Delta, \Delta')$  maximise product of traders' surpluses.

Quantity maximises the trading surplus. [Further Details](#)

$$\underbrace{V_3(z, \beta, h - q(\Delta, \Delta'))}_{\Delta \text{ marginal valuation}} = \underbrace{V_3(z', \beta', h' + q(\Delta, \Delta'))}_{\Delta' \text{ marginal valuation}}$$

$\Delta$  sells more to  $\Delta'$  when

- 1  $\beta < \beta'$ .
- 2  $h > h'$ .

[Back](#)

# Trading Price

Price determined by traders' changes in values.

$$p(\Delta, \Delta') = \frac{1}{2} \left( \overbrace{\frac{V(z', \beta', h' + q(\Delta, \Delta')) - V(\Delta')}{q(\Delta, \Delta')}}^{\approx \text{slope of } \Delta' \text{ value in } h'} + \underbrace{\frac{V(\Delta) - V(z, \beta, h - q(\Delta, \Delta'))}{q(\Delta, \Delta')}}_{\approx \text{slope of } \Delta \text{ value in } h} \right)$$

Price is:

- Higher when  $\beta$  &  $\beta'$  are higher.
- More variable when the slope of  $V(z, \beta, h)$  is more variable.

# Trading Decisions

**Nash bargaining:** price  $p(\Delta, \Delta')$  & quantity  $q(\Delta, \Delta')$  maximise product of traders' surpluses.

**Quantity maximises the surplus.** [Details](#)

→  $\Delta$  sells more to  $\Delta'$  when  $\beta < \beta'$  and/or  $h > h'$ .

**Price splits the surplus.** [Details](#)

→ Price is higher when  $\beta$  &  $\beta'$  are higher and/or  $h$  &  $h'$  are lower.

Let  $S(\Delta, \Delta')$  denote surplus at the optimal quantity. [Back](#)

# Endogenous Search

FOC of value function:

$$\underbrace{s_2(z, \gamma(\Delta))}_{\text{Marginal cost of search}} = \frac{1}{2} \int \underbrace{\frac{\partial m(\gamma(\Delta), \gamma(\Delta'))}{\partial \gamma(\Delta)}}_{\text{Increase in meetings}} \underbrace{S(\Delta, \Delta') \Phi(d\Delta')}_{\text{Surplus from meeting}}$$

Traders search harder:

- 1 if they have **low search cost**.
- 2 when **gains to trade are higher**.

[Back](#)

# Asset Distributions

Steady state: zero net inflows into all types.

→ **Trading flows** perfectly balance **shock flows**. Equation

Market clearing:

$$\iiint h \Phi(dz, d\beta, dh) = a$$

[Back](#)

# Equilibrium

Steady state such that:

- Value functions solve the trader problem.
- Prices and quantities are determined by Nash bargaining.
- Search is chosen optimally.
- The market clears.

[Formal Definition](#) [Back](#)



# Terms of trade

Nash bargaining:

$$\begin{aligned} \max_{p,q} \quad & \overbrace{(V(z, \beta, h - q) - V(\Delta) + pq)}^{\text{type } \Delta \text{ surplus}} \overbrace{(V(z', \beta', h' + q) - V(\Delta') - pq)}^{\text{type } \Delta' \text{ surplus}} \\ \text{s.t.} \quad & V(z, \beta, h - q) - V(\Delta) + pq \geq 0, \\ & V(z', \beta', h' + q) - V(\Delta') - pq \geq 0. \end{aligned}$$

$p(\Delta, \Delta')$  is per-unit price.

$q(\Delta, \Delta')$  is quantity sold from  $\Delta$  to  $\Delta'$ .

[Back](#)

# Steady state

$$\begin{aligned}
 & \iint_{\underline{\beta}}^{\beta^*} \int_{h^*}^{\infty} m(\gamma(\Delta), \gamma(\Delta')) \phi(\Delta) \phi(\Delta') \mathbb{1}(q(\Delta, \Delta') \geq h - h^*) dh d\beta d\Delta' - \\
 & \iint_{\underline{\beta}}^{\beta^*} \int_{-\infty}^{h^*} m(\gamma(\Delta), \gamma(\Delta')) \phi(\Delta) \phi(\Delta') \mathbb{1}(q(\Delta, \Delta') < h - h^*) dh d\beta d\Delta' \\
 & = \eta(1 - G(\beta^*)) \int_{\underline{\beta}}^{\beta^*} \int_{-\infty}^{h^*} \phi(\Delta) dh d\beta - \eta G(\beta^*) \int_{\beta^*}^{\bar{\beta}} \int_{-\infty}^{h^*} \phi(\Delta) dh d\beta
 \end{aligned}$$

Back

# Equilibrium

Let  $\mathcal{T} \equiv \mathbb{R}^+ \times [\beta_L, \beta_H] \times \mathbb{R}$  be the type space.

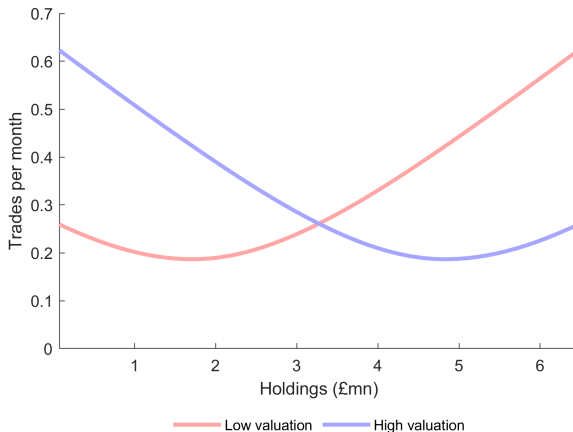
An equilibrium is

- ❶ distribution function  $\Phi : \mathcal{T} \rightarrow [0, 1]$ ;
- ❷ value function  $V : \mathcal{T} \rightarrow \mathbb{R}$ ;
- ❸ search intensity function  $\gamma : \mathcal{T} \rightarrow \mathbb{R}^+$ ;
- ❹ pricing  $p : \mathcal{T}^2 \rightarrow \mathbb{R}^+$  and trade quantity  $q : \mathcal{T}^2 \rightarrow \mathbb{R}$ ;

such that

- Value functions solve the trader problem.
- Price and quantities are determined by Nash bargaining.
- Search is chosen optimally.
- The system is in steady state.
- The market clears. [Back](#)

# Search in Equilibrium



Traders vary search to manage holdings around a target:

- 1 Respond to shocks.
- 2 Offset trades.

[Back](#)

# Market Depth

Maximum willingness to pay:

$$\frac{V(z, \beta, h + q) - V(z, \beta, h)}{q} \xrightarrow{q \rightarrow 0} V_3(z, \beta, h)$$

Maximum  $q^\pi(\Delta, D)$  that can be sold to this trader at price discount no greater than  $D$ :

$$\underbrace{\frac{V(z, \beta, h + q^\pi(\Delta, D)) - V(z, \beta, h)}{q^\pi(\Delta, D)}}_{\text{price for } q^\pi(\Delta, D)} = \underbrace{V_3(z, \beta, h)}_{\text{current price}} - D,$$

**Market depth** is the trade-weighted average of  $q^\pi(\Delta, D)$  times the average frequency of trading  $2\Gamma$ :

$$\Pi(D) = 2\Gamma \int \frac{\gamma(\Delta)\phi(\Delta)}{\Gamma} q^\pi(\Delta, D) d\Delta.$$

# Matching function

Linear matching function:

$$m(\gamma, \gamma') = 2\gamma \frac{\gamma'}{\Gamma}$$

where

$$\Gamma = \int \gamma(\Delta) \Phi(d\Delta)$$

→ Conditional on contact, counterparty chosen randomly with likelihood proportional to  $\gamma'$ . [Back](#)

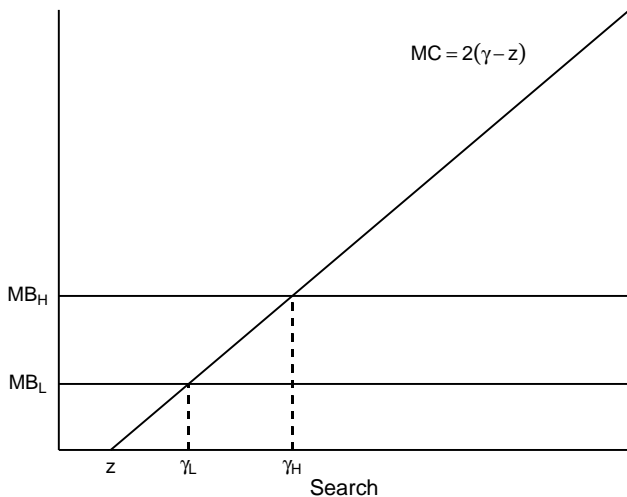
# Search costs

Search cost function given by:

$$s(z, \gamma) = (\gamma - z)^2$$

→ base level of contacts, with constant marginal cost above this base. [Back](#)

# Search technology



[Back](#)



# Moments

## Expectations

- 1 Average trading frequency  $n$ .
- 2 Average trade size  $|q|$ .
- 3 Average price  $p$ .

## Across traders

- 4 Standard deviation of trading frequency  $n$ .

## Within traders

- 5 Standard deviation of holdings  $h$ .
- 6 Standard deviation of prices  $p$ .
- 7 Correlation between quantity sold  $q$  and holdings  $h$ .
- 8 Correlation between absolute inventory  $inv \equiv |h - s|$  and trading frequency  $n$ .

[Back](#)

# Model Fit

| Moment                                    | Data | Model |
|---|------|-------|
| <i>Expectations</i>                       |      |       |
| Price, %                                  | 1.09 | 1.09  |
| Trade size, £mn                           | 0.67 | 0.55  |
| Trading frequency, per month              | 0.44 | 0.43  |
| Holdings, £mn                             | 3.27 | 3.27  |
| <i>Across traders</i>                     |      |       |
| Std. dev. trading frequency, per month    | 0.55 | 0.55  |
| <i>Within traders</i>                     |      |       |
| Std. dev. price, %                        | 0.04 | 0.04  |
| Std. dev. holdings, £mn                   | 1.23 | 1.31  |
| Correlation inventory & trading frequency | 0.08 | 0.09  |
| Correlation holdings & quantity sold      | 0.33 | 0.30  |

[Back](#)

# Parameter Estimates

| Parameter   | Estimate |
|---|----------|
| Search efficiency $z \sim \Gamma(k_z, \theta_z)$                                |          |
| $k_z$   | 0.545    |
| $\theta_z$  | 0.374    |
| Shock frequency $\eta$  |          |
| $\eta$  | 0.040    |
| Utility $u(h) = \beta h - 0.5\kappa h^2; \beta \sim U(\mu_\beta, \sigma_\beta)$ |          |
| $\mu_\beta$   | 0.031    |
| $\sigma_\beta$  | 0.015    |
| $\kappa$  | 0.008    |

[Inference](#)[Back](#)

# Capital Regulation

Concerns tighter capital regulation for dealer-banks has harmed liquidity (Duffie, 2018).

Capital counterfactual:

$$u(h) = \beta h - \tau|h| - \frac{1}{2}\kappa h^2$$

for  $\tau = 0.01$  for 15% of traders with lowest search costs.

Exercise: suppose capital regulation raises cost of inventory by  $\tau$  – what is the impact on markets?

Assessing **cost of capital regulation**—impact on markets—but not the benefits—bank resilience. [Summary](#)