Example of performing IMPULSED fitting

This example shows how to (1) how to synthesize dMRI signals based on the IMPULSED method; and (2) how to fit the IMPULSED model to dMRI data to extract microstructural parameters such as mean cell size d, apparent intracellular volume fraction v_{in} , intra- and extra-cellular diffusion coefficients D_{in} and D_{ex} .

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Reference

The main reference that should be cited when using the code in this script is

- 1. Jiang X, et al. Quantification of cell size using temporal diffusion spectroscopy. Magn Reson Med. 2016;75(3):1076-85. PubMed PMID: 25845851.
- 2. Xu J, et al. Magnetic resonance imaging of mean cell size in human breast tumors. Magn Reson Med. 2020;83(6):2002-14. PubMed PMID: 31765494.

Preliminary

```
clear variables ; clear obj ;
```

Generate DiffusionPulseSequence objects

Create a trapezoidal cosine OGSE pulse sequence object for all OGSE acquisitions

```
Nacq = 9;
                   % total number of acquisition points
pulse_tcos = mati.DiffusionPulseSequence(Nacq,...
    'TE',
                       110,...
                                               % echo time [ms]
    'delta',
                       40,...
                                               % gradient duration [ms]
    'Delta',
                       45,...
                                               % separation of two gradients [ms]
    'b',
                         [0.1,0.2,0.3, 0.4, 0.2,0.4,0.6,0.8,1.0], ... % b value [ms/um^2]
    'n',
                         [2,2,2, 2, 1,1,1,1,1],...
                                                              % number of oscillating cycles
    'shape',
                    "tcos",...
                                              % gradient waveform shape
    'gdir',
                       [0 0 1],...
                                                % gradient directions. It should be a Nx3 matrix
    'trise',
                       0.9);
                                               % gradient rise time [ms]
% Create a trapezoidal PGSE pulse sequence object for all PGSE acquisitions
Nacq = 9;
pulse_tpgse = mati.DiffusionPulseSequence(Nacq, ...
    'TE',
                       110,...
    'delta',
                       12, ...
    'Delta',
                       74, ...
                         [0.2:0.2:1.8], ...
    'b',
                    "tpgse",...
    'shape',
    'gdir',
                       [0 0 1],...
    'trise',
                        0.9);
% Combine OGSE and PGSE pulse sequence objects
pulse = mati.PulseSequence.cat(pulse_tcos, pulse_tpgse);
\% An example of choosing a subset of PulseSequence object to meet e.g., hardware limitations
pulse = pulse(pulse.G<80e-5);</pre>
                                 \% 80mT/m = 80 x 10^(-5) gauss/um
% Display the PulseSequence object
pulse.disp(pulse)
```

```
<a href="">Note: PulseSequence properties should be column vectors. They are shown as row vectors here for visualization purpose only
</a>
ans =
```

```
struct with fields:
 delta: [40 40 40 40 40 40 40 12 12 12 12 12 12 12 12]
 Delta: [45 45 45 45 45 45 45 45 74 74 74 74 74 74 74 74]
 shape: [1×16 string]
    b: [1×16 double]
     G: [1×16 double]
    n: [2 2 1 1 1 1 1 0 0 0 0 0 0 0 0 0]
 trise: [1×16 double]
  gdir: [3×16 double]
     f: [1×16 double]
     w: [1×16 double]
    T: [20 20 40 40 40 40 40 0 0 0 0 0 0 0 0 0]
    tp: [1×16 double]
 tdiff: [5 5 10 10 10 10 10 70 70 70 70 70 70 70 70 70]
 gamma: 26.7500
  Nacq: 16
    TR: []
    df: []
```

Generate IMPULSED model object

Choose which specific model to use. Note that IMPULSED can fit up to five parameters, i..e, d, v_{in} , D_{in} , D_{ex} 0, and β_{ex} . Individual parameters could be fixed during fitting to enhance the fitting precision of other parameters.

```
nmodel = 3 ;
switch nmodel
    case 1, structure.modelName = '1compt' ; structure.geometry = 'sphere' ;
    case 2, structure.modelName = 'impulsed_vin_d_Dex' ; structure.Din = 2 ; structure.betaex = 0 ; structure.geometry = 'sphere';
    case 3, structure.modelName = 'impulsed_vin_d_Dex_Din' ; %structure.betaex = 0 ; structure.geometry = 'sphere';
    case 4, structure.modelName = 'impulsed_vin_d_Dex_Din_betaex' ; %structure.geometry = 'sphere';
end

% Create an IMPULSED model object
impulsed = mati.IMPULSED(structure, pulse) ;
```

Example of synthesize dMRI signals based on the IMPULSED model

This is for computer simulations studies to synthesize dMRI signals based on the IMPULSED model. The ground-truth microstructural parameter are determined below. NOTE:

- 1. parms sim is a cell array that contains all microstructual parameters for dMRI signal synthesis
- 2. variables (*_sim) indicate ground-truth microstructural parameters used in the simulations.

```
switch nmodel
   case 1
              % [d, Din]
       d = [10:15]; Din = [1.56 3];
                             [d,Din]=meshgrid(d,Din);
       parms_sim = {d, Din};
       d_sim = d(:)' ; Din_sim = Din(:)' ;
           % [vin, d, Dex]
       vin = [0.6]; d = [10:15]; Dex = [1.56 3];
       parms_sim = {vin, d, Dex}; [vin, d,Dex] = meshgrid(vin, d,Dex);
       d_sim = d(:)' ; vin_sim = vin(:)' ; Dex_sim = Dex(:)' ;
    case 3 % [vin, d, Dex, Din]
       vin = [0.6]; d = [10:15]; Dex = [1.56]; Din = [1.56];
       parms_sim = {vin, d, Dex, Din}; [vin, d,Dex,Din] = ndgrid(vin, d,Dex,Din);
       d_sim = d(:)' ; vin_sim = vin(:)' ; Dex_sim = Dex(:)' ; Din_sim = Din(:)' ;
   vin = [0.6]; d = [8:2:16]; Dex = [2]; Din = [1.56]; betaex = [5];
       parms_sim = {vin, d, Dex, Din, betaex}; [vin, d,Dex,Din,betaex] = ndgrid(vin, d,Dex,Din,betaex);
       d_sim = d(:)' ; vin_sim = vin(:)' ; Dex_sim = Dex(:)' ; Din_sim = Din(:)' ; betaex_sim = betaex(:)' ;
end
% Synthesize IMPULSED signals based on the microstructural parameters determined above
signal_sim = impulsed.FcnSignal(parms_sim, impulsed) ;
% Add Rician noise to synthesized signals
sigma_noise = 0.025;
                       % standard deviation of Gaussian noise in the real and the imaginary images assuming to be equal
```

```
signal_sim = mati.Physics.AddRicianNoise(signal_sim, sigma_noise);

% Create an ImageData object
[Npulse, Nparms] = size(signal_sim);
data = mati.ImageData(reshape(signal_sim',[Nparms, 1, 1, Npulse]), sigma_noise);
```

Fit IMPULSED model to dMRI signals

Create a Fit object

```
fitopts.solverName = 'lsqnonlin'; % {'lsqcurvefit' , 'lsqnonlin' , 'fmincon'}
fitopts.options = optimoptions(fitopts.solverName, 'Display', 'off');
fitopts.noiseModel = 'standard'; %{'none','standard';'logLikelihood'}
fitopts.flag.parfor = 'y';
                                      % If use parallel computing with parfor
fitopts.flag.deivim = 'n';
                                     % if remove IVIM influence
fitopts.flag.multistart = 'y';
                                     % If try fittings multiple times with different initial conditions
fitopts.NumStarts = 5;
                                   % if try multistart=='y', try how many times of different initial conditions?
% Create a data fitting object
fitpars = mati.FitPars(impulsed, fitopts);
warning off;
% Fit model to data
fitout = fitpars.Fit(data) ;
```

Check fitted results

Show the comparison of IMPULSED fitted and ground-truth mean cell size

```
figure(1); clf; hold on;
plot(d_sim, fitout.d, 'o');
plot([0 20],[0 20],'r'); box on;
xlabel('input d [\mum]'); ylabel('fitted d [\mum]'); xlim([0 20]); ylim([0 20]);
legend('fits', 'identity', 'Location','Southeast');
```

