

tf.contrib.linalg.LinearOperatorIdentity

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Class **LinearOperatorIdentity**Defined in [tensorflow/contrib/linalg/python/ops/linear_operator_identity.py](#).See the guide: [Linear Algebra \(contrib\)](#) > [LinearOperator](#)**LinearOperator** acting like a [batch] square identity matrix.

This operator acts like a [batch] identity matrix **A** with shape **[B1, ..., Bb, N, N]** for some **b >= 0**. The first **b** indices index a batch member. For every batch index **(i1, ..., ib)**, **A[i1, ..., ib, :, :]** is an **N x N** matrix. This matrix **A** is not materialized, but for purposes of broadcasting this shape will be relevant.

LinearOperatorIdentity is initialized with **num_rows**, and optionally **batch_shape**, and **dtype** arguments. If **batch_shape** is **None**, this operator efficiently passes through all arguments. If **batch_shape** is provided, broadcasting may occur, which will require making copies.

```

# Create a 2 x 2 identity matrix.
operator = LinearOperatorIdentity(num_rows=2, dtype=tf.float32)

operator.to_dense()
==> [[1., 0.]
      [0., 1.]]

operator.shape
==> [2, 2]

operator.log_abs_determinant()
==> 0.

x = ... Shape [2, 4] Tensor
operator.matmul(x)
==> Shape [2, 4] Tensor, same as x.

y = tf.random_normal(shape=[3, 2, 4])
# Note that y.shape is compatible with operator.shape because operator.shape
# is broadcast to [3, 2, 2].
# This broadcast does NOT require copying data, since we can infer that y
# will be passed through without changing shape. We are always able to infer
# this if the operator has no batch_shape.
x = operator.solve(y)
==> Shape [3, 2, 4] Tensor, same as y.

# Create a 2-batch of 2x2 identity matrices
operator = LinearOperatorIdentity(num_rows=2, batch_shape=[2])
operator.to_dense()
==> [[[1., 0.]
      [0., 1.]],
      [[1., 0.]
      [0., 1.]]]

# Here, even though the operator has a batch shape, the input is the same as
# the output, so x can be passed through without a copy. The operator is able
# to detect that no broadcast is necessary because both x and the operator
# have statically defined shape.
x = ... Shape [2, 2, 3]
operator.matmul(x)
==> Shape [2, 2, 3] Tensor, same as x

# Here the operator and x have different batch_shape, and are broadcast.
# This requires a copy, since the output is different size than the input.
x = ... Shape [1, 2, 3]
operator.matmul(x)
==> Shape [2, 2, 3] Tensor, equal to [x, x]

```

Shape compatibility

This operator acts on [batch] matrix with compatible shape. `x` is a batch matrix with compatible shape for `matmul` and `solve` if

```

operator.shape = [B1,...,Bb] + [N, N], with b >= 0
x.shape = [C1,...,Cc] + [N, R],
and [C1,...,Cc] broadcasts with [B1,...,Bb] to [D1,...,Dd]

```

Performance

If `batch_shape` initialization arg is `None`:

- `operator.matmul(x)` is $O(1)$
- `operator.solve(x)` is $O(1)$
- `operator.determinant()` is $O(1)$

If `batch_shape` initialization arg is provided, and static checks cannot rule out the need to broadcast:

- `operator.matmul(x)` is $O(D1*…*Dd*N*R)$
- `operator.solve(x)` is $O(D1*…*Dd*N*R)$
- `operator.determinant()` is $O(B1*…*Bb)$

Matrix property hints

This `LinearOperator` is initialized with boolean flags of the form `is_X`, for `X = non_singular, self_adjoint, positive_definite, square`. These have the following meaning:

- If `is_X == True`, callers should expect the operator to have the property `X`. This is a promise that should be fulfilled, but is *not* a runtime assert. For example, finite floating point precision may result in these promises being violated.
- If `is_X == False`, callers should expect the operator to not have `X`.
- If `is_X == None` (the default), callers should have no expectation either way.

Properties

`batch_shape`

`TensorShape` of batch dimensions of this `LinearOperator`.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `TensorShape([B1, ..., Bb])`, equivalent to `A.get_shape()[:-2]`

Returns:

`TensorShape`, statically determined, may be undefined.

`domain_dimension`

Dimension (in the sense of vector spaces) of the domain of this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `N`.

Returns:

`Dimension` object.

`dtype`

The `DType` of `Tensor`s handled by this `LinearOperator`.

`graph_parents`

List of graph dependencies of this `LinearOperator`.

is_non_singular

is_positive_definite

is_self_adjoint

is_square

Return `True/False` depending on if this operator is square.

name

Name prepended to all ops created by this `LinearOperator`.

range_dimension

Dimension (in the sense of vector spaces) of the range of this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `M`.

Returns:

`Dimension` object.

shape

`TensorShape` of this `LinearOperator`.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `TensorShape([B1, ..., Bb, M, N])`, equivalent to `A.get_shape()`.

Returns:

`TensorShape`, statically determined, may be undefined.

tensor_rank

Rank (in the sense of tensors) of matrix corresponding to this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `b + 2`.

Args:

- `name`: A name for this `Op`.

Returns:

Python integer, or None if the tensor rank is undefined.

Methods

`__init__`

```
__init__(
    num_rows,
    batch_shape=None,
    dtype=None,
    is_non_singular=True,
    is_self_adjoint=True,
    is_positive_definite=True,
    is_square=True,
    assert_proper_shapes=False,
    name='LinearOperatorIdentity'
)
```

Initialize a `LinearOperatorIdentity`.

The `LinearOperatorIdentity` is initialized with arguments defining `dtype` and shape.

This operator is able to broadcast the leading (batch) dimensions, which sometimes requires copying data. If `batch_shape` is `None`, the operator can take arguments of any batch shape without copying. See examples.

Args:

- `num_rows`: Scalar non-negative integer `Tensor`. Number of rows in the corresponding identity matrix.
- `batch_shape`: Optional 1-D integer `Tensor`. The shape of the leading dimensions. If `None`, this operator has no leading dimensions.
- `dtype`: Data type of the matrix that this operator represents.
- `is_non_singular`: Expect that this operator is non-singular.
- `is_self_adjoint`: Expect that this operator is equal to its hermitian transpose.
- `is_positive_definite`: Expect that this operator is positive definite, meaning the quadratic form $\mathbf{x}^H \mathbf{A} \mathbf{x}$ has positive real part for all nonzero \mathbf{x} . Note that we do not require the operator to be self-adjoint to be positive-definite. See: https://en.wikipedia.org/wiki/Positive-definite_matrix\#Extension_for_non_symmetric_matrices
- `is_square`: Expect that this operator acts like square [batch] matrices.
- `assert_proper_shapes`: Python `bool`. If `False`, only perform static checks that initialization and method arguments have proper shape. If `True`, and static checks are inconclusive, add asserts to the graph.
- `name`: A name for this `LinearOperator`

Raises:

- `ValueError`: If `num_rows` is determined statically to be non-scalar, or negative.
- `ValueError`: If `batch_shape` is determined statically to not be 1-D, or negative.
- `ValueError`: If any of the following is not `True`: `{is_self_adjoint, is_non_singular, is_positive_definite}`.

`add_to_tensor`

```
add_to_tensor(
    mat,
    name='add_to_tensor'
)
```

Add matrix represented by this operator to `mat`. Equiv to `I + mat`.

Args:

- `mat` : `Tensor` with same `dtype` and shape broadcastable to `self`.
- `name` : A name to give this `Op`.

Returns:

A `Tensor` with broadcast shape and same `dtype` as `self`.

`assert_non_singular`

```
assert_non_singular(name='assert_non_singular')
```

Returns an `Op` that asserts this operator is non singular.

This operator is considered non-singular if

```
ConditionNumber < max{100, range_dimension, domain_dimension} * eps,  
eps := np.finfo(self.dtype.as_numpy_dtype).eps
```

Args:

- `name` : A string name to prepend to created ops.

Returns:

An `Assert Op`, that, when run, will raise an `InvalidArgumentError` if the operator is singular.

`assert_positive_definite`

```
assert_positive_definite(name='assert_positive_definite')
```

Returns an `Op` that asserts this operator is positive definite.

Here, positive definite means that the quadratic form $\mathbf{x}^H \mathbf{A} \mathbf{x}$ has positive real part for all nonzero \mathbf{x} . Note that we do not require the operator to be self-adjoint to be positive definite.

Args:

- `name` : A name to give this `Op`.

Returns:

An `Assert Op`, that, when run, will raise an `InvalidArgumentError` if the operator is not positive definite.

`assert_self_adjoint`

```
assert_self_adjoint(name='assert_self_adjoint')
```

Returns an `Op` that asserts this operator is self-adjoint.

Here we check that this operator is *exactly* equal to its hermitian transpose.

Args:

- `name` : A string name to prepend to created ops.

Returns:

An `Assert Op`, that, when run, will raise an `InvalidArgumentError` if the operator is not self-adjoint.

batch_shape_tensor

```
batch_shape_tensor(name='batch_shape_tensor')
```

Shape of batch dimensions of this operator, determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns a `Tensor` holding `[B1, ..., Bb]`.

Args:

- `name` : A name for this `Op`.

Returns:

`int32 Tensor`

determinant

```
determinant(name='det')
```

Determinant for every batch member.

Args:

- `name` : A name for this `Op`.

Returns:

`Tensor` with shape `self.batch_shape` and same `dtype` as `self`.

Raises:

- `NotImplementedError` : If `self.is_square` is `False`.

diag_part

```
diag_part(name='diag_part')
```

Efficiently get the [batch] diagonal part of this operator.

If this operator has shape `[B1, ..., Bb, M, N]`, this returns a `Tensor` `diagonal`, of shape `[B1, ..., Bb, min(M, N)]`, where `diagonal[b1, ..., bb, i] = self.to_dense()[b1, ..., bb, i, i]`.

```
my_operator = LinearOperatorDiag([1., 2.])

# Efficiently get the diagonal
my_operator.diag_part()
==> [1., 2.]

# Equivalent, but inefficient method
tf.matrix_diag_part(my_operator.to_dense())
==> [1., 2.]
```

Args:

- `name`: A name for this `Op`.

Returns:

- `diag_part`: A `Tensor` of same `dtype` as self.

domain_dimension_tensor

```
domain_dimension_tensor(name='domain_dimension_tensor')
```

Dimension (in the sense of vector spaces) of the domain of this operator.

Determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `N`.

Args:

- `name`: A name for this `Op`.

Returns:

`int32 Tensor`

log_abs_determinant

```
log_abs_determinant(name='log_abs_det')
```

Log absolute value of determinant for every batch member.

Args:

- `name`: A name for this `Op`.

Returns:

`Tensor` with shape `self.batch_shape` and same `dtype` as `self`.

Raises:

- `NotImplementedError`: If `self.is_square` is `False`.

matmul

```
matmul(
    x,
    adjoint=False,
    adjoint_arg=False,
    name='matmul'
)
```

Transform [batch] matrix `x` with left multiplication: `x --> Ax`.

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]
operator = LinearOperator(...)
operator.shape = [..., M, N]

X = ... # shape [..., N, R], batch matrix, R > 0.

Y = operator.matmul(X)
Y.shape
==> [..., M, R]

Y[..., :, r] = sum_j A[..., :, j] X[j, r]
```

Args:

- `x`: `Tensor` with compatible shape and same `dtype` as `self`. See class docstring for definition of compatibility.
- `adjoint`: Python `bool`. If `True`, left multiply by the adjoint: `AH x`.
- `adjoint_arg`: Python `bool`. If `True`, compute `A xH` where `xH` is the hermitian transpose (transposition and complex conjugation).
- `name`: A name for this `Op`.

Returns:

A `Tensor` with shape `[..., M, R]` and same `dtype` as `self`.

matvec

```
matvec(
    x,
    adjoint=False,
    name='matvec'
)
```

Transform [batch] vector `x` with left multiplication: `x --> Ax`.

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]
operator = LinearOperator(...)

X = ... # shape [..., N], batch vector

Y = operator.matvec(X)
Y.shape
==> [..., M]

Y[..., :] = sum_j A[..., :, j] X[..., j]
```

Args:

- `x`: **Tensor** with compatible shape and same `dtype` as `self`. `x` is treated as a [batch] vector meaning for every set of leading dimensions, the last dimension defines a vector. See class docstring for definition of compatibility.
- `adjoint`: Python `bool`. If `True`, left multiply by the adjoint: $A^H x$.
- `name`: A name for this `Op`.

Returns:

A **Tensor** with shape `[..., M]` and same `dtype` as `self`.

range_dimension_tensor

```
range_dimension_tensor(name='range_dimension_tensor')
```

Dimension (in the sense of vector spaces) of the range of this operator.

Determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `M`.

Args:

- `name`: A name for this `Op`.

Returns:

`int32 Tensor`

shape_tensor

```
shape_tensor(name='shape_tensor')
```

Shape of this **LinearOperator**, determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns a **Tensor** holding `[B1, ..., Bb, M, N]`, equivalent to `tf.shape(A)`.

Args:

- `name`: A name for this `Op`.

Returns:

`int32 Tensor`

solve

```
solve(
    rhs,
    adjoint=False,
    adjoint_arg=False,
    name='solve'
)
```

Solve (exact or approx) **R** (batch) systems of equations: **A X = rhs**.

The returned **Tensor** will be close to an exact solution if **A** is well conditioned. Otherwise closeness will vary. See class docstring for details.

Examples:

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]
operator = LinearOperator(...)
operator.shape = [..., M, N]

# Solve R > 0 linear systems for every member of the batch.
RHS = ... # shape [..., M, R]

X = operator.solve(RHS)
# X[..., :, r] is the solution to the r'th linear system
# sum_j A[..., :, j] X[..., j, r] = RHS[..., :, r]

operator.matmul(X)
==> RHS
```

Args:

- **rhs**: **Tensor** with same **dtype** as this operator and compatible shape. **rhs** is treated like a [batch] matrix meaning for every set of leading dimensions, the last two dimensions defines a matrix. See class docstring for definition of compatibility.
- **adjoint**: Python **bool**. If **True**, solve the system involving the adjoint of this **LinearOperator**: **A^H X = rhs**.
- **adjoint_arg**: Python **bool**. If **True**, solve **A X = rhs^H** where **rhs^H** is the hermitian transpose (transposition and complex conjugation).
- **name**: A name scope to use for ops added by this method.

Returns:

Tensor with shape **[...,N, R]** and same **dtype** as **rhs**.

Raises:

- **NotImplementedError**: If **self.is_non_singular** or **is_square** is False.

solvevec

```
solvevec(
    rhs,
    adjoint=False,
    name='solve'
)
```

Solve single equation with best effort: $\mathbf{A} \mathbf{X} = \mathbf{rhs}$.

The returned `Tensor` will be close to an exact solution if \mathbf{A} is well conditioned. Otherwise closeness will vary. See class docstring for details.

Examples:

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]
operator = LinearOperator(...)
operator.shape = [..., M, N]

# Solve one linear system for every member of the batch.
RHS = ... # shape [..., M]

X = operator.solvevec(RHS)
# X is the solution to the linear system
# sum_j A[..., :, j] X[..., j] = RHS[..., :]

operator.matvec(X)
==> RHS
```

Args:

- `rhs`: `Tensor` with same `dtype` as this operator. `rhs` is treated like a [batch] vector meaning for every set of leading dimensions, the last dimension defines a vector. See class docstring for definition of compatibility regarding batch dimensions.
- `adjoint`: Python `bool`. If `True`, solve the system involving the adjoint of this `LinearOperator`: $\mathbf{A}^H \mathbf{X} = \mathbf{rhs}$.
- `name`: A name scope to use for ops added by this method.

Returns:

`Tensor` with shape `[...,N]` and same `dtype` as `rhs`.

Raises:

- `NotImplementedError`: If `self.is_non_singular` or `is_square` is False.

tensor_rank_tensor

```
tensor_rank_tensor(name='tensor_rank_tensor')
```

Rank (in the sense of tensors) of matrix corresponding to this operator.

If this operator acts like the batch matrix \mathbf{A} with `A.shape = [B1, ..., Bb, M, N]`, then this returns `b + 2`.

Args:

- `name`: A name for this `Op`.

Returns:

`int32 Tensor`, determined at runtime.

to_dense

```
to_dense(name='to_dense')
```

Return a dense (batch) matrix representing this operator.

trace

```
trace(name='trace')
```

Trace of the linear operator, equal to sum of `self.diag_part()`.

If the operator is square, this is also the sum of the eigenvalues.

Args:

- `name`: A name for this `Op`.

Returns:

Shape `[B1, ..., Bb]` `Tensor` of same `dtype` as `self`.

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