

## tf.contrib.distributions.SinhArcsinh

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Class **SinhArcsinh**Inherits From: **TransformedDistribution**Defined in `tensorflow/contrib/distributions/python/ops/sinh_arcsinh.py`.The SinhArcsinh transformation of a distribution on `(-inf, inf)`.

This distribution models a random variable, making use of a **SinhArcsinh** transformation (which has adjustable tailweight and skew), a rescaling, and a shift.

The **SinhArcsinh** transformation of the Normal is described in great depth in [Sinh-arcsinh distributions](#). Here we use a slightly different parameterization, in terms of **tailweight** and **skewness**. Additionally we allow for distributions other than Normal, and control over **scale** as well as a "shift" parameter **loc**.

## Mathematical Details

Given random variable **Z**, we define the SinhArcsinh transformation of **Z**, **Y**, parameterized by **(loc, scale, skewness, tailweight)**, via the relation:

```
Y := loc + scale * F(Z) * (2 / F(2))
F(Z) := Sinh( (Arcsinh(Z) + skewness) * tailweight )
```

This distribution is similar to the location-scale transformation **L(Z) := loc + scale \* Z** in the following ways:

- If **skewness = 0** and **tailweight = 1** (the defaults), **F(Z) = Z**, and then **Y = L(Z)** exactly.
- **loc** is used in both to shift the result by a constant factor.
- Our definition of **C** ensures that **P[Y - loc <= 2 \* scale] = P[L(Z) - loc <= 2 \* scale]**. Thus it can be said that the weights in the tails of **Y** and **L(Z)** beyond **loc + 2 \* scale** are the same.

This distribution is different than **loc + scale \* Z** due to the reshaping done by **F**:

- Positive (negative) **skewness** leads to positive (negative) skew.
- positive skew means, the mode of **F(Z)** is "tilted" to the right.
- positive skew means positive values of **F(Z)** become more likely, and negative values become less likely.
- Larger (smaller) **tailweight** leads to fatter (thinner) tails.
- Fatter tails mean larger values of **|F(Z)|** become more likely.
- **tailweight < 1** leads to a distribution that is "flat" around **Y = loc**, and a very steep drop-off in the tails.

- `tailweight > 1` leads to a distribution more peaked at the mode with heavier tails.

To see the argument about the tails, note that for  $|Z| \gg 1$  and  $|Z| \gg (|\text{skewness}| * \text{tailweight})^{1/\text{tailweight}}$ , we have  $Y \approx 0.5 Z^{\text{tailweight}} e^{(\text{sign}(Z) \text{ skewness} * \text{tailweight})}$ .

To see the argument about `C` and quantiles, note that

$$\begin{aligned} P[(Y - \text{loc}) / \text{scale} \leq 2] &= P[F(Z) \leq 2 * \text{scale} / C] \\ &= P[Z \leq F^{-1}(2 * \text{scale} / C)] \\ &= P[Z \leq 2]. \end{aligned}$$

## Properties

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### `allow_nan_stats`

Python `bool` describing behavior when a stat is undefined.

Stats return +/- infinity when it makes sense. E.g., the variance of a Cauchy distribution is infinity. However, sometimes the statistic is undefined, e.g., if a distribution's pdf does not achieve a maximum within the support of the distribution, the mode is undefined. If the mean is undefined, then by definition the variance is undefined. E.g. the mean for Student's T for  $df = 1$  is undefined (no clear way to say it is either + or - infinity), so the variance =  $E[(X - \text{mean})^2]$  is also undefined.

Returns:

- `allow_nan_stats`: Python `bool`.

### `batch_shape`

Shape of a single sample from a single event index as a `TensorShape`.

May be partially defined or unknown.

The batch dimensions are indexes into independent, non-identical parameterizations of this distribution.

Returns:

- `batch_shape`: `TensorShape`, possibly unknown.

### `bijector`

Function transforming  $x \Rightarrow y$ .

### `distribution`

Base distribution,  $p(x)$ .

### `dtype`

The `DType` of `Tensor`s handled by this `Distribution`.

### `event_shape`

Shape of a single sample from a single batch as a `TensorShape`.

May be partially defined or unknown.

Returns:

- `event_shape`: `TensorShape`, possibly unknown.

## **loc**

The `loc` in  $Y := \text{loc} + \text{scale} @ F(Z) * (2 / F(2))$ .

## **name**

Name prepended to all ops created by this `Distribution`.

## **parameters**

Dictionary of parameters used to instantiate this `Distribution`.

## **reparameterization\_type**

Describes how samples from the distribution are reparameterized.

Currently this is one of the static instances `distributions.FULLY_REPARAMETERIZED` or `distributions.NOT_REPARAMETERIZED`.

Returns:

An instance of `ReparameterizationType`.

## **scale**

The `LinearOperator` `scale` in  $Y := \text{loc} + \text{scale} @ F(Z) * (2 / F(2))$ .

## **skewness**

Controls the skewness. `Skewness > 0` means right skew.

## **tailweight**

Controls the tail decay. `tailweight > 1` means faster than Normal.

## **validate\_args**

Python `bool` indicating possibly expensive checks are enabled.

## Methods

---

### **`__init__`**

```

__init__(
    loc,
    scale,
    skewness=None,
    tailweight=None,
    distribution=None,
    validate_args=False,
    allow_nan_stats=True,
    name='MultivariateNormalLinearOperator'
)

```

Construct SinhArcsinh distribution on  $(-\infty, \infty)$ .

Arguments (**loc**, **scale**, **skewness**, **tailweight**) must have broadcastable shape (indexing batch dimensions). They must all have the same **dtype**.

Args:

- **loc**: Floating-point **Tensor**.
- **scale**: **Tensor** of same **dtype** as **loc**.
- **skewness**: Skewness parameter. Default is **0.0** (no skew).
- **tailweight**: Tailweight parameter. Default is **1.0** (unchanged tailweight)
- **distribution**: **tf.Distribution**-like instance. Distribution that is transformed to produce this distribution. Default is **ds.Normal(0., 1.)**. Must be a scalar-batch, scalar-event distribution. Typically **distribution.reparameterization\_type = FULLY\_REPARAMETERIZED** or it is a function of non-trainable parameters. WARNING: If you backprop through a **SinhArcsinh** sample and **distribution** is not **FULLY\_REPARAMETERIZED** yet is a function of trainable variables, then the gradient will be incorrect!
- **validate\_args**: Python **bool**, default **False**. When **True** distribution parameters are checked for validity despite possibly degrading runtime performance. When **False** invalid inputs may silently render incorrect outputs.
- **allow\_nan\_stats**: Python **bool**, default **True**. When **True**, statistics (e.g., mean, mode, variance) use the value "**NaN**" to indicate the result is undefined. When **False**, an exception is raised if one or more of the statistic's batch members are undefined.
- **name**: Python **str** name prefixed to Ops created by this class.

## batch\_shape\_tensor

```
batch_shape_tensor(name='batch_shape_tensor')
```

Shape of a single sample from a single event index as a 1-D **Tensor**.

The batch dimensions are indexes into independent, non-identical parameterizations of this distribution.

Args:

- **name**: name to give to the op

Returns:

- **batch\_shape**: **Tensor**.

## cdf

```

cdf(
    value,
    name='cdf'
)

```

Cumulative distribution function.

Given random variable  $X$ , the cumulative distribution function **cdf** is:

```

cdf(x) := P[X <= x]

```

Args:

- **value**: **float** or **double Tensor**.
- **name**: The name to give this op.

Returns:

- **cdf**: a **Tensor** of shape **sample\_shape(x) + self.batch\_shape** with values of type **self.dtype**.

## copy

```

copy(**override_parameters_kwargs)

```

Creates a deep copy of the distribution.

★ **Note:** the copy distribution may continue to depend on the original initialization arguments.

Args:

- **\*\*override\_parameters\_kwargs**: String/value dictionary of initialization arguments to override with new values.

Returns:

- **distribution**: A new instance of **type(self)** initialized from the union of **self.parameters** and **override\_parameters\_kwargs**, i.e., **dict(self.parameters, \*\*override\_parameters\_kwargs)**.

## covariance

```

covariance(name='covariance')

```

Covariance.

Covariance is (possibly) defined only for non-scalar-event distributions.

For example, for a length-**k**, vector-valued distribution, it is calculated as,

```

Cov[i, j] = Covariance(X_i, X_j) = E[(X_i - E[X_i]) (X_j - E[X_j])]

```

where **Cov** is a (batch of) **k x k** matrix,  $0 \leq (i, j) < k$ , and **E** denotes expectation.

Alternatively, for non-vector, multivariate distributions (e.g., matrix-valued, Wishart), **Covariance** shall return a (batch of)

matrices under some vectorization of the events, i.e.,

```
Cov[i, j] = Covariance(Vec(X)_i, Vec(X)_j) = [as above]
```

where **Cov** is a (batch of)  $k' \times k'$  matrices,  $0 \leq (i, j) < k' = \text{reduce\_prod}(\text{event\_shape})$ , and **Vec** is some function mapping indices of this distribution's event dimensions to indices of a length- $k'$  vector.

Args:

- **name** : The name to give this op.

Returns:

- **covariance** : Floating-point **Tensor** with shape  $[B_1, \dots, B_n, k', k']$  where the first  $n$  dimensions are batch coordinates and  $k' = \text{reduce\_prod}(\text{self.event\_shape})$ .

## entropy

```
entropy(name='entropy')
```

Shannon entropy in nats.

## event\_shape\_tensor

```
event_shape_tensor(name='event_shape_tensor')
```

Shape of a single sample from a single batch as a 1-D int32 **Tensor**.

Args:

- **name** : name to give to the op

Returns:

- **event\_shape** : **Tensor**.

## is\_scalar\_batch

```
is_scalar_batch(name='is_scalar_batch')
```

Indicates that **batch\_shape** ==  $[]$ .

Args:

- **name** : The name to give this op.

Returns:

- **is\_scalar\_batch** : **bool** scalar **Tensor**.

## is\_scalar\_event

```
is_scalar_event(name='is_scalar_event')
```

Indicates that `event_shape == []`.

Args:

- `name`: The name to give this op.

Returns:

- `is_scalar_event`: `bool` scalar `Tensor`.

## log\_cdf

```
log_cdf(  
    value,  
    name='log_cdf'  
)
```

Log cumulative distribution function.

Given random variable `X`, the cumulative distribution function `cdf` is:

```
log_cdf(x) := Log[ P[X <= x] ]
```

Often, a numerical approximation can be used for `log_cdf(x)` that yields a more accurate answer than simply taking the logarithm of the `cdf` when `x << -1`.

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

- `logcdf`: a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## log\_prob

```
log_prob(  
    value,  
    name='log_prob'  
)
```

Log probability density/mass function.

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

- `log_prob`: a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## log\_survival\_function

```
log_survival_function(  
    value,  
    name='log_survival_function'  
)
```

Log survival function.

Given random variable `X`, the survival function is defined:

```
log_survival_function(x) = Log[ P[X > x] ]  
                        = Log[ 1 - P[X <= x] ]  
                        = Log[ 1 - cdf(x) ]
```

Typically, different numerical approximations can be used for the log survival function, which are more accurate than `1 - cdf(x)` when `x >> 1`.

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

`Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## mean

```
mean(name='mean')
```

Mean.

## mode

```
mode(name='mode')
```

Mode.

## param\_shapes

```
param_shapes(  
    cls,  
    sample_shape,  
    name='DistributionParamShapes'  
)
```

Shapes of parameters given the desired shape of a call to `sample()`.



This is a class method that describes what key/value arguments are required to instantiate the given **Distribution** so that a particular shape is returned for that instance's call to **sample()** .

Subclasses should override class method **\_param\_shapes** .

Args:

- **sample\_shape** : **Tensor** or python list/tuple. Desired shape of a call to **sample()** .
- **name** : name to prepend ops with.

Returns:

**dict** of parameter name to **Tensor** shapes.

## **param\_static\_shapes**

```
param_static_shapes(  
    cls,  
    sample_shape  
)
```

**param\_shapes** with static (i.e. **TensorShape** ) shapes.

This is a class method that describes what key/value arguments are required to instantiate the given **Distribution** so that a particular shape is returned for that instance's call to **sample()** . Assumes that the sample's shape is known statically.

Subclasses should override class method **\_param\_shapes** to return constant-valued tensors when constant values are fed.

Args:

- **sample\_shape** : **TensorShape** or python list/tuple. Desired shape of a call to **sample()** .

Returns:

**dict** of parameter name to **TensorShape** .

Raises:

- **ValueError** : if **sample\_shape** is a **TensorShape** and is not fully defined.

## **prob**

```
prob(  
    value,  
    name='prob'  
)
```

Probability density/mass function.

Args:

- **value** : **float** or **double Tensor** .

- `name` : The name to give this op.

Returns:

- `prob` : a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype` .

## quantile

```
quantile(
    value,
    name='quantile'
)
```

Quantile function. Aka "inverse cdf" or "percent point function".

Given random variable `X` and `p in [0, 1]`, the `quantile` is:

```
quantile(p) := x such that P[X <= x] == p
```

Args:

- `value` : `float` or `double Tensor` .
- `name` : The name to give this op.

Returns:

- `quantile` : a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype` .

## sample

```
sample(
    sample_shape=(),
    seed=None,
    name='sample'
)
```

Generate samples of the specified shape.

Note that a call to `sample()` without arguments will generate a single sample.

Args:

- `sample_shape` : 0D or 1D `int32 Tensor` . Shape of the generated samples.
- `seed` : Python integer seed for RNG
- `name` : name to give to the op.

Returns:

- `samples` : a `Tensor` with prepended dimensions `sample_shape` .

## stddev

```
stddev(name='stddev')
```

Standard deviation.

Standard deviation is defined as,

$$\text{stddev} = E[(X - E[X])**2]**0.5$$

where **X** is the random variable associated with this distribution, **E** denotes expectation, and **stddev.shape = batch\_shape + event\_shape**.

Args:

- **name** : The name to give this op.

Returns:

- **stddev** : Floating-point **Tensor** with shape identical to **batch\_shape + event\_shape**, i.e., the same shape as **self.mean()**.

## survival\_function

```
survival_function(  
    value,  
    name='survival_function'  
)
```

Survival function.

Given random variable **X**, the survival function is defined:

$$\begin{aligned}\text{survival\_function}(x) &= P[X > x] \\ &= 1 - P[X \leq x] \\ &= 1 - \text{cdf}(x).\end{aligned}$$

Args:

- **value** : **float** or **double Tensor**.
- **name** : The name to give this op.

Returns:

**Tensor** of shape **sample\_shape(x) + self.batch\_shape** with values of type **self.dtype**.

## variance

```
variance(name='variance')
```

Variance.

Variance is defined as,

$$\text{Var} = E[(X - E[X])**2]$$

where `X` is the random variable associated with this distribution, `E` denotes expectation, and `Var.shape = batch_shape + event_shape`.

Args:

- `name`: The name to give this op.

Returns:

- `variance`: Floating-point `Tensor` with shape identical to `batch_shape + event_shape`, i.e., the same shape as `self.mean()`.

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