

## tf.contrib.distributions.Deterministic

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`allow_nan_stats``atol`Class **Deterministic**Defined in [tensorflow/contrib/distributions/python/ops/deterministic.py](#).Scalar **Deterministic** distribution on the real line.

The scalar **Deterministic** distribution is parameterized by a [batch] point **loc** on the real line. The distribution is supported at this point only, and corresponds to a random variable that is constant, equal to **loc**.

See [Degenerate rv](#).

## Mathematical Details

The probability mass function (pmf) and cumulative distribution function (cdf) are

```
pmf(x; loc) = 1, if x == loc, else 0
cdf(x; loc) = 1, if x >= loc, else 0
```

## Examples

```
# Initialize a single Deterministic supported at zero.
constant = tf.contrib.distributions.Deterministic(0.)
constant.prob(0.)
==> 1.
constant.prob(2.)
==> 0.

# Initialize a [2, 2] batch of scalar constants.
loc = [[0., 1.], [2., 3.]]
x = [[0., 1.1], [1.99, 3.]]
constant = tf.contrib.distributions.Deterministic(loc)
constant.prob(x)
==> [[1., 0.], [0., 1.]]
```

## Properties

**allow\_nan\_stats**Python **bool** describing behavior when a stat is undefined.

Stats return +/- infinity when it makes sense. E.g., the variance of a Cauchy distribution is infinity. However, sometimes the statistic is undefined, e.g., if a distribution's pdf does not achieve a maximum within the support of the distribution, the mode is undefined. If the mean is undefined, then by definition the variance is undefined. E.g. the mean for Student's T for  $df = 1$  is undefined (no clear way to say it is either + or - infinity), so the variance =  $E[(X - \text{mean})^2]$  is also undefined.

Returns:

- `allow_nan_stats`: Python `bool`.

## **atol**

Absolute tolerance for comparing points to `self.loc`.

## **batch\_shape**

Shape of a single sample from a single event index as a `TensorShape`.

May be partially defined or unknown.

The batch dimensions are indexes into independent, non-identical parameterizations of this distribution.

Returns:

- `batch_shape`: `TensorShape`, possibly unknown.

## **dtype**

The `DType` of `Tensor`s handled by this `Distribution`.

## **event\_shape**

Shape of a single sample from a single batch as a `TensorShape`.

May be partially defined or unknown.

Returns:

- `event_shape`: `TensorShape`, possibly unknown.

## **loc**

Point (or batch of points) at which this distribution is supported.

## **name**

Name prepended to all ops created by this `Distribution`.

## **parameters**

Dictionary of parameters used to instantiate this `Distribution`.

## reparameterization\_type

Describes how samples from the distribution are reparameterized.

Currently this is one of the static instances `distributions.FULLY_REPARAMETERIZED` or `distributions.NOT_REPARAMETERIZED`.

Returns:

An instance of `ReparameterizationType`.

## rtol

Relative tolerance for comparing points to `self.loc`.

## validate\_args

Python `bool` indicating possibly expensive checks are enabled.

## Methods

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### \_\_init\_\_

```
__init__(
    loc,
    atol=None,
    rtol=None,
    validate_args=False,
    allow_nan_stats=True,
    name='Deterministic'
)
```

Initialize a scalar `Deterministic` distribution.

The `atol` and `rtol` parameters allow for some slack in `pmf`, `cdf` computations, e.g. due to floating-point error.

```
pmf(x; loc)
= 1, if Abs(x - loc) <= atol + rtol * Abs(loc),
= 0, otherwise.
```

Args:

- `loc`: Numeric `Tensor` of shape `[B1, ..., Bb]`, with `b >= 0`. The point (or batch of points) on which this distribution is supported.
- `atol`: Non-negative `Tensor` of same `dtype` as `loc` and broadcastable shape. The absolute tolerance for comparing closeness to `loc`. Default is `0`.
- `rtol`: Non-negative `Tensor` of same `dtype` as `loc` and broadcastable shape. The relative tolerance for comparing closeness to `loc`. Default is `0`.
- `validate_args`: Python `bool`, default `False`. When `True` distribution parameters are checked for validity despite possibly degrading runtime performance. When `False` invalid inputs may silently render incorrect outputs.
- `allow_nan_stats`: Python `bool`, default `True`. When `True`, statistics (e.g., mean, mode, variance) use the value `"NaN"` to indicate the result is undefined. When `False`, an exception is raised if one or more of the statistic's batch

members are undefined.

- `name` : Python `str` name prefixed to Ops created by this class.

## **batch\_shape\_tensor**

```
batch_shape_tensor(name='batch_shape_tensor')
```

Shape of a single sample from a single event index as a 1-D `Tensor`.

The batch dimensions are indexes into independent, non-identical parameterizations of this distribution.

Args:

- `name` : name to give to the op

Returns:

- `batch_shape` : `Tensor`.

## **cdf**

```
cdf(  
    value,  
    name='cdf'  
)
```

Cumulative distribution function.

Given random variable `X`, the cumulative distribution function `cdf` is:

```
cdf(x) := P[X <= x]
```

Args:

- `value` : `float` or `double Tensor`.
- `name` : The name to give this op.

Returns:

- `cdf` : a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## **copy**

```
copy(**override_parameters_kwargs)
```

Creates a deep copy of the distribution.

★ **Note:** the copy distribution may continue to depend on the original initialization arguments.

Args:

- `**override_parameters_kwargs`: String/value dictionary of initialization arguments to override with new values.

Returns:

- `distribution`: A new instance of `type(self)` initialized from the union of `self.parameters` and `override_parameters_kwargs`, i.e., `dict(self.parameters, **override_parameters_kwargs)`.

## covariance

```
covariance(name='covariance')
```

Covariance.

Covariance is (possibly) defined only for non-scalar-event distributions.

For example, for a length-`k`, vector-valued distribution, it is calculated as,

```
Cov[i, j] = Covariance(X_i, X_j) = E[(X_i - E[X_i]) (X_j - E[X_j])]
```

where `Cov` is a (batch of) `k x k` matrix, `0 <= (i, j) < k`, and `E` denotes expectation.

Alternatively, for non-vector, multivariate distributions (e.g., matrix-valued, Wishart), `Covariance` shall return a (batch of) matrices under some vectorization of the events, i.e.,

```
Cov[i, j] = Covariance(Vec(X)_i, Vec(X)_j) = [as above]
```

where `Cov` is a (batch of) `k' x k'` matrices, `0 <= (i, j) < k' = reduce_prod(event_shape)`, and `Vec` is some function mapping indices of this distribution's event dimensions to indices of a length-`k'` vector.

Args:

- `name`: The name to give this op.

Returns:

- `covariance`: Floating-point `Tensor` with shape `[B1, ..., Bn, k', k']` where the first `n` dimensions are batch coordinates and `k' = reduce_prod(self.event_shape)`.

## entropy

```
entropy(name='entropy')
```

Shannon entropy in nats.

## event\_shape\_tensor

```
event_shape_tensor(name='event_shape_tensor')
```

Shape of a single sample from a single batch as a 1-D int32 `Tensor`.

Args:

- `name`: name to give to the op

Returns:

- `event_shape`: `Tensor` .

## `is_scalar_batch`

```
is_scalar_batch(name='is_scalar_batch')
```

Indicates that `batch_shape == []` .

Args:

- `name`: The name to give this op.

Returns:

- `is_scalar_batch`: `bool` scalar `Tensor` .

## `is_scalar_event`

```
is_scalar_event(name='is_scalar_event')
```

Indicates that `event_shape == []` .

Args:

- `name`: The name to give this op.

Returns:

- `is_scalar_event`: `bool` scalar `Tensor` .

## `log_cdf`

```
log_cdf(  
    value,  
    name='log_cdf'  
)
```

Log cumulative distribution function.

Given random variable `X` , the cumulative distribution function `cdf` is:

```
log_cdf(x) := Log[ P[X <= x] ]
```

Often, a numerical approximation can be used for `log_cdf(x)` that yields a more accurate answer than simply taking the logarithm of the `cdf` when `x << -1` .

Args:

- `value`: `float` or `double Tensor` .
- `name`: The name to give this op.

Returns:

- `logcdf`: a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## `log_prob`

```
log_prob(  
    value,  
    name='log_prob'  
)
```

Log probability density/mass function.

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

- `log_prob`: a `Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## `log_survival_function`

```
log_survival_function(  
    value,  
    name='log_survival_function'  
)
```

Log survival function.

Given random variable `X`, the survival function is defined:

```
log_survival_function(x) = Log[ P[X > x] ]  
                        = Log[ 1 - P[X <= x] ]  
                        = Log[ 1 - cdf(x) ]
```

Typically, different numerical approximations can be used for the log survival function, which are more accurate than `1 - cdf(x)` when `x >> 1`.

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

`Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## `mean`

```
mean(name='mean')
```

Mean.

## mode

```
mode(name='mode')
```

Mode.

## param\_shapes

```
param_shapes(  
    cls,  
    sample_shape,  
    name='DistributionParamShapes'  
)
```

Shapes of parameters given the desired shape of a call to `sample()`.

This is a class method that describes what key/value arguments are required to instantiate the given `Distribution` so that a particular shape is returned for that instance's call to `sample()`.

Subclasses should override class method `_param_shapes`.

Args:

- `sample_shape`: `Tensor` or python list/tuple. Desired shape of a call to `sample()`.
- `name`: name to prepend ops with.

Returns:

`dict` of parameter name to `Tensor` shapes.

## param\_static\_shapes

```
param_static_shapes(  
    cls,  
    sample_shape  
)
```

`param_shapes` with static (i.e. `TensorShape`) shapes.

This is a class method that describes what key/value arguments are required to instantiate the given `Distribution` so that a particular shape is returned for that instance's call to `sample()`. Assumes that the sample's shape is known statically.

Subclasses should override class method `_param_shapes` to return constant-valued tensors when constant values are fed.

Args:

- `sample_shape`: `TensorShape` or python list/tuple. Desired shape of a call to `sample()`.

Returns:



**dict** of parameter name to **TensorShape** .

Raises:

- **ValueError** : if **sample\_shape** is a **TensorShape** and is not fully defined.

## prob

```
prob(  
    value,  
    name='prob'  
)
```

Probability density/mass function.

Args:

- **value**: **float** or **double Tensor** .
- **name** : The name to give this op.

Returns:

- **prob**: a **Tensor** of shape **sample\_shape(x) + self.batch\_shape** with values of type **self.dtype** .

## quantile

```
quantile(  
    value,  
    name='quantile'  
)
```

Quantile function. Aka "inverse cdf" or "percent point function".

Given random variable **X** and **p in [0, 1]**, the **quantile** is:

```
quantile(p) := x such that P[X <= x] == p
```

Args:

- **value**: **float** or **double Tensor** .
- **name** : The name to give this op.

Returns:

- **quantile**: a **Tensor** of shape **sample\_shape(x) + self.batch\_shape** with values of type **self.dtype** .

## sample

```
sample(
    sample_shape=(),
    seed=None,
    name='sample'
)
```

Generate samples of the specified shape.

Note that a call to `sample()` without arguments will generate a single sample.

Args:

- `sample_shape`: 0D or 1D `int32 Tensor`. Shape of the generated samples.
- `seed`: Python integer seed for RNG
- `name`: name to give to the op.

Returns:

- `samples`: a `Tensor` with prepended dimensions `sample_shape`.

## stddev

```
stddev(name='stddev')
```

Standard deviation.

Standard deviation is defined as,

$$\text{stddev} = E[(X - E[X])**2]**0.5$$

where  $X$  is the random variable associated with this distribution,  $E$  denotes expectation, and `stddev.shape = batch_shape + event_shape`.

Args:

- `name`: The name to give this op.

Returns:

- `stddev`: Floating-point `Tensor` with shape identical to `batch_shape + event_shape`, i.e., the same shape as `self.mean()`.

## survival\_function

```
survival_function(
    value,
    name='survival_function'
)
```

Survival function.

Given random variable  $X$ , the survival function is defined:

```
survival_function(x) = P[X > x]
                    = 1 - P[X <= x]
                    = 1 - cdf(x).
```

Args:

- `value`: `float` or `double Tensor`.
- `name`: The name to give this op.

Returns:

`Tensor` of shape `sample_shape(x) + self.batch_shape` with values of type `self.dtype`.

## variance

```
variance(name='variance')
```

Variance.

Variance is defined as,

$$\text{Var} = E[(X - E[X])**2]$$

where `X` is the random variable associated with this distribution, `E` denotes expectation, and `Var.shape = batch_shape + event_shape`.

Args:

- `name`: The name to give this op.

Returns:

- `variance`: Floating-point `Tensor` with shape identical to `batch_shape + event_shape`, i.e., the same shape as `self.mean()`.

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