

tf.contrib.linalg.LinearOperatorComposition

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Class **LinearOperatorComposition**Inherits From: [LinearOperator](#)Defined in [tensorflow/contrib/linalg/python/ops/linear_operator_composition.py](#).See the guide: [Linear Algebra \(contrib\)](#) > [LinearOperator](#)Composes one or more **LinearOperators**.

This operator composes one or more linear operators $[op_1, \dots, op_J]$, building a new **LinearOperator** with action defined by:

$$op_composed(x) := op_1(op_2(\dots(op_J(x))\dots))$$

If op_j acts like $[batch]$ matrix A_j , then $op_composed$ acts like the $[batch]$ matrix formed with the multiplication $A_1 A_2 \dots A_J$.

If op_j has shape $batch_shape_j + [M_j, N_j]$, then we must have $N_j = M_{j+1}$, in which case the composed operator has shape equal to $broadcast_batch_shape + [M_1, N_J]$, where $broadcast_batch_shape$ is the mutual broadcast of $batch_shape_j$, $j = 1, \dots, J$, assuming the intermediate batch shapes broadcast. Even if the composed shape is well defined, the composed operator's methods may fail due to lack of broadcasting ability in the defining operators' methods.

```

# Create a 2 x 2 linear operator composed of two 2 x 2 operators.
operator_1 = LinearOperatorFullMatrix([[1., 2.], [3., 4.]])
operator_2 = LinearOperatorFullMatrix([[1., 0.], [0., 1.]])
operator = LinearOperatorComposition([operator_1, operator_2])

operator.to_dense()
==> [[1., 2.]
      [3., 4.]]

operator.shape
==> [2, 2]

operator.log_abs_determinant()
==> scalar Tensor

x = ... Shape [2, 4] Tensor
operator.matmul(x)
==> Shape [2, 4] Tensor

# Create a [2, 3] batch of 4 x 5 linear operators.
matrix_45 = tf.random_normal(shape=[2, 3, 4, 5])
operator_45 = LinearOperatorFullMatrix(matrix_45)

# Create a [2, 3] batch of 5 x 6 linear operators.
matrix_56 = tf.random_normal(shape=[2, 3, 5, 6])
operator_56 = LinearOperatorFullMatrix(matrix_56)

# Compose to create a [2, 3] batch of 4 x 6 operators.
operator_46 = LinearOperatorComposition([operator_45, operator_56])

# Create a shape [2, 3, 6, 2] vector.
x = tf.random_normal(shape=[2, 3, 6, 2])
operator.matmul(x)
==> Shape [2, 3, 4, 2] Tensor

```

Performance

The performance of `LinearOperatorComposition` on any operation is equal to the sum of the individual operators' operations.

Matrix property hints

This `LinearOperator` is initialized with boolean flags of the form `is_X`, for `X = non_singular, self_adjoint, positive_definite, square`. These have the following meaning:

- If `is_X == True`, callers should expect the operator to have the property `X`. This is a promise that should be fulfilled, but is *not* a runtime assert. For example, finite floating point precision may result in these promises being violated.
- If `is_X == False`, callers should expect the operator to not have `X`.
- If `is_X == None` (the default), callers should have no expectation either way.

Properties

batch_shape

`TensorShape` of batch dimensions of this `LinearOperator`.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns

`TensorShape([B1, ..., Bb])` , equivalent to `A.get_shape()[: -2]`

Returns:

`TensorShape` , statically determined, may be undefined.

domain_dimension

Dimension (in the sense of vector spaces) of the domain of this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]` , then this returns `N` .

Returns:

`Dimension` object.

dtype

The `DType` of `Tensor` s handled by this `LinearOperator` .

graph_parents

List of graph dependencies of this `LinearOperator` .

is_non_singular

is_positive_definite

is_self_adjoint

is_square

Return `True/False` depending on if this operator is square.

name

Name prepended to all ops created by this `LinearOperator` .

operators

range_dimension

Dimension (in the sense of vector spaces) of the range of this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]` , then this returns `M` .

Returns:

`Dimension` object.

shape

`TensorShape` of this `LinearOperator` .

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]` , then this returns `TensorShape([B1, ..., Bb, M, N])` , equivalent to `A.get_shape()` .

Returns:

`TensorShape` , statically determined, may be undefined.

tensor_rank

Rank (in the sense of tensors) of matrix corresponding to this operator.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]` , then this returns `b + 2` .

Args:

- `name` : A name for this `Op`.

Returns:

Python integer, or None if the tensor rank is undefined.

Methods

`__init__`

```
__init__(
    operators,
    is_non_singular=None,
    is_self_adjoint=None,
    is_positive_definite=None,
    is_square=None,
    name=None
)
```

Initialize a `LinearOperatorComposition` .

`LinearOperatorComposition` is initialized with a list of operators `[op_1, ..., op_J]` . For the `matmul` method to be well defined, the composition `op_i.matmul(op_{i+1})(x)` must be defined. Other methods have similar constraints.

Args:

- `operators` : Iterable of `LinearOperator` objects, each with the same `dtype` and composable shape.
- `is_non_singular` : Expect that this operator is non-singular.
- `is_self_adjoint` : Expect that this operator is equal to its hermitian transpose.
- `is_positive_definite` : Expect that this operator is positive definite, meaning the quadratic form $\mathbf{x}^H \mathbf{A} \mathbf{x}$ has positive real part for all nonzero \mathbf{x} . Note that we do not require the operator to be self-adjoint to be positive-definite. See: https://en.wikipedia.org/wiki/Positive-definite_matrix\#Extension_for_non_symmetric_matrices
- `is_square` : Expect that this operator acts like square [batch] matrices.
- `name` : A name for this `LinearOperator` . Default is the individual operators names joined with `_o_` .

Raises:

- `TypeError` : If all operators do not have the same `dtype` .
- `ValueError` : If `operators` is empty.

`add_to_tensor`

```
add_to_tensor(  
    x,  
    name='add_to_tensor'  
)
```

Add matrix represented by this operator to `x` . Equivalent to `A + x` .

Args:

- `x` : `Tensor` with same `dtype` and shape broadcastable to `self.shape` .
- `name` : A name to give this `Op` .

Returns:

A `Tensor` with broadcast shape and same `dtype` as `self` .

`assert_non_singular`

```
assert_non_singular(name='assert_non_singular')
```

Returns an `Op` that asserts this operator is non singular.

This operator is considered non-singular if

```
ConditionNumber < max{100, range_dimension, domain_dimension} * eps,  
eps := np.finfo(self.dtype.as_numpy_dtype).eps
```

Args:

- `name` : A string name to prepend to created ops.

Returns:

An `Assert Op` , that, when run, will raise an `InvalidArgumentError` if the operator is singular.

`assert_positive_definite`

```
assert_positive_definite(name='assert_positive_definite')
```

Returns an `Op` that asserts this operator is positive definite.

Here, positive definite means that the quadratic form $\mathbf{x}^H \mathbf{A} \mathbf{x}$ has positive real part for all nonzero `x` . Note that we do not require the operator to be self-adjoint to be positive definite.

Args:

- `name` : A name to give this `Op` .

Returns:

An `Assert Op` , that, when run, will raise an `InvalidArgumentError` if the operator is not positive definite.

`assert_self_adjoint`

```
assert_self_adjoint(name='assert_self_adjoint')
```

Returns an `Op` that asserts this operator is self-adjoint.

Here we check that this operator is *exactly* equal to its hermitian transpose.

Args:

- `name` : A string name to prepend to created ops.

Returns:

An `Assert Op` , that, when run, will raise an `InvalidArgumentError` if the operator is not self-adjoint.

`batch_shape_tensor`

```
batch_shape_tensor(name='batch_shape_tensor')
```

Shape of batch dimensions of this operator, determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]` , then this returns a `Tensor` holding `[B1, ..., Bb]` .

Args:

- `name` : A name for this `Op`.

Returns:

`int32 Tensor`

`determinant`

```
determinant(name='det')
```

Determinant for every batch member.

Args:

- `name` : A name for this `Op`.

Returns:

Tensor with shape `self.batch_shape` and same `dtype` as `self`.

Raises:

- `NotImplementedError`: If `self.is_square` is `False`.

diag_part

```
diag_part(name='diag_part')
```

Efficiently get the [batch] diagonal part of this operator.

If this operator has shape `[B1, ..., Bb, M, N]`, this returns a **Tensor** `diagonal`, of shape `[B1, ..., Bb, min(M, N)]`, where `diagonal[b1, ..., bb, i] = self.to_dense()[b1, ..., bb, i, i]`.

```
my_operator = LinearOperatorDiag([1., 2.])

# Efficiently get the diagonal
my_operator.diag_part()
==> [1., 2.]

# Equivalent, but inefficient method
tf.matrix_diag_part(my_operator.to_dense())
==> [1., 2.]
```

Args:

- `name`: A name for this **Op**.

Returns:

- `diag_part`: A **Tensor** of same `dtype` as `self`.

domain_dimension_tensor

```
domain_dimension_tensor(name='domain_dimension_tensor')
```

Dimension (in the sense of vector spaces) of the domain of this operator.

Determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns `N`.

Args:

- `name`: A name for this **Op**.

Returns:

int32 Tensor

log_abs_determinant

```
log_abs_determinant(name='log_abs_det')
```

Log absolute value of determinant for every batch member.

Args:

- `name`: A name for this `Op`.

Returns:

`Tensor` with shape `self.batch_shape` and same `dtype` as `self`.

Raises:

- `NotImplementedError`: If `self.is_square` is `False`.

matmul

```
matmul(  
    x,  
    adjoint=False,  
    adjoint_arg=False,  
    name='matmul'  
)
```

Transform [batch] matrix `x` with left multiplication: `x --> Ax`.

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]  
operator = LinearOperator(...)  
operator.shape = [..., M, N]  
  
X = ... # shape [..., N, R], batch matrix, R > 0.  
  
Y = operator.matmul(X)  
Y.shape  
==> [..., M, R]  
  
Y[..., :, r] = sum_j A[..., :, j] X[j, r]
```

Args:

- `x`: `Tensor` with compatible shape and same `dtype` as `self`. See class docstring for definition of compatibility.
- `adjoint`: Python `bool`. If `True`, left multiply by the adjoint: $A^H x$.
- `adjoint_arg`: Python `bool`. If `True`, compute $A x^H$ where x^H is the hermitian transpose (transposition and complex conjugation).
- `name`: A name for this `Op`.

Returns:

A `Tensor` with shape `[..., M, R]` and same `dtype` as `self`.

matvec

```
matvec(  
    x,  
    adjoint=False,  
    name='matvec'  
)
```

Transform [batch] vector x with left multiplication: $x \mapsto Ax$.

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]  
operator = LinearOperator(...)  
  
X = ... # shape [..., N], batch vector  
  
Y = operator.matvec(X)  
Y.shape  
==> [..., M]  
  
Y[... , :] = sum_j A[... , :, j] X[... , j]
```

Args:

- x : **Tensor** with compatible shape and same **dtype** as **self**. x is treated as a [batch] vector meaning for every set of leading dimensions, the last dimension defines a vector. See class docstring for definition of compatibility.
- **adjoint**: Python **bool**. If **True**, left multiply by the adjoint: $A^H x$.
- **name**: A name for this `Op`.

Returns:

A **Tensor** with shape $[..., M]$ and same **dtype** as **self**.

range_dimension_tensor

```
range_dimension_tensor(name='range_dimension_tensor')
```

Dimension (in the sense of vector spaces) of the range of this operator.

Determined at runtime.

If this operator acts like the batch matrix A with $A.shape = [B1, \dots, Bb, M, N]$, then this returns M .

Args:

- **name**: A name for this `Op`.

Returns:

int32 Tensor

shape_tensor

```
shape_tensor(name='shape_tensor')
```

Shape of this `LinearOperator`, determined at runtime.

If this operator acts like the batch matrix `A` with `A.shape = [B1, ..., Bb, M, N]`, then this returns a `Tensor` holding `[B1, ..., Bb, M, N]`, equivalent to `tf.shape(A)`.

Args:

- `name`: A name for this `Op`.

Returns:

`int32 Tensor`

`solve`

```
solve(
    rhs,
    adjoint=False,
    adjoint_arg=False,
    name='solve'
)
```

Solve (exact or approx) `R` (batch) systems of equations: $A X = rhs$.

The returned `Tensor` will be close to an exact solution if `A` is well conditioned. Otherwise closeness will vary. See class docstring for details.

Examples:

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]
operator = LinearOperator(...)
operator.shape = [..., M, N]

# Solve R > 0 linear systems for every member of the batch.
RHS = ... # shape [..., M, R]

X = operator.solve(RHS)
# X[..., :, r] is the solution to the r'th linear system
# sum_j A[..., :, j] X[..., j, r] = RHS[..., :, r]

operator.matmul(X)
==> RHS
```

Args:

- `rhs`: `Tensor` with same `dtype` as this operator and compatible shape. `rhs` is treated like a [batch] matrix meaning for every set of leading dimensions, the last two dimensions defines a matrix. See class docstring for definition of compatibility.
- `adjoint`: Python `bool`. If `True`, solve the system involving the adjoint of this `LinearOperator`: $A^H X = rhs$.
- `adjoint_arg`: Python `bool`. If `True`, solve $A X = rhs^H$ where rhs^H is the hermitian transpose (transposition and complex conjugation).
- `name`: A name scope to use for ops added by this method.

Returns:

Tensor with shape `[..., N, R]` and same **dtype** as **rhs**.

Raises:

- `NotImplementedError`: If `self.is_non_singular` or `is_square` is False.

solvevec

```
solvevec(  
    rhs,  
    adjoint=False,  
    name='solve'  
)
```

Solve single equation with best effort: $\mathbf{A} \mathbf{X} = \mathbf{rhs}$.

The returned **Tensor** will be close to an exact solution if **A** is well conditioned. Otherwise closeness will vary. See class docstring for details.

Examples:

```
# Make an operator acting like batch matrix A. Assume A.shape = [..., M, N]  
operator = LinearOperator(...)  
operator.shape = [..., M, N]  
  
# Solve one linear system for every member of the batch.  
RHS = ... # shape [..., M]  
  
X = operator.solvevec(RHS)  
# X is the solution to the linear system  
# sum_j A[..., :, j] X[..., j] = RHS[..., :]  
  
operator.matvec(X)  
==> RHS
```

Args:

- **rhs**: **Tensor** with same **dtype** as this operator. **rhs** is treated like a [batch] vector meaning for every set of leading dimensions, the last dimension defines a vector. See class docstring for definition of compatibility regarding batch dimensions.
- **adjoint**: Python **bool**. If **True**, solve the system involving the adjoint of this **LinearOperator**: $\mathbf{A}^H \mathbf{X} = \mathbf{rhs}$.
- **name**: A name scope to use for ops added by this method.

Returns:

Tensor with shape `[..., N]` and same **dtype** as **rhs**.

Raises:

- `NotImplementedError`: If `self.is_non_singular` or `is_square` is False.

tensor_rank_tensor

```
tensor_rank_tensor(name='tensor_rank_tensor')
```

Rank (in the sense of tensors) of matrix corresponding to this operator.

If this operator acts like the batch matrix **A** with **A.shape = [B1, ..., Bb, M, N]**, then this returns **b + 2**.

Args:

- **name** : A name for this `Op`.

Returns:

int32 Tensor, determined at runtime.

to_dense

```
to_dense(name='to_dense')
```

Return a dense (batch) matrix representing this operator.

trace

```
trace(name='trace')
```

Trace of the linear operator, equal to sum of **self.diag_part()**.

If the operator is square, this is also the sum of the eigenvalues.

Args:

- **name** : A name for this `Op`.

Returns:

Shape **[B1, ..., Bb]** **Tensor** of same **dtype** as **self**.

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