

1 The value of information for spatial conservation
2 planning

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Abstract

Spatial conservation plans are typically based upon uncertain inputs and may benefit from additional data to inform them. However, the toolset of spatial prioritization does not yet contain a method for assessing the value of new information to a spatial conservation plan. If the value of information were to be calculated, then conservation plans would more effectively benefit from a more optimal amount of information. Here, for the first time we demonstrate how a formal value of information analysis can be applied to a spatial conservation plan. We show how a value of information analysis can be combined with traditional conservation planning tools to map species distributions and optimize a reserve network to protect them. We incorporate uncertainty into conservation planning with Monte Carlo sampling of the planning inputs and then test the effects of uncertainty reduction to calculate the value of additional information to a conservation plan. The impact of optimally incorporating additional information into conservation plans, will be more effective plans where additional information is beneficial, and avoiding the loss of resources to unnecessary information gathering where new data has no benefit to the fundamental objectives of the plan.

18 Introduction

19 The field of science that focuses on developing methods to select candidate sites for protection and other
20 conservation actions is called spatial conservation planning (Moilanen et al., 2009). Spatial conservation
21 plans are complex and their inputs are sometimes uncertain or based on few data. The outcomes of spatial
22 conservation plans could be improved if they incorporated additional information. For example, additional
23 occurrence data could be included for species of concern to the conservation planner so that the input layers
24 of the spatial plan were more precise. But additional information comes at a cost. And that cost may have
25 to be traded-off against implementing the conservation plan itself. Therefore, it is crucial to measure the
26 value of potential new information to the conservation plan. If the value of new information is too low, that
27 is, it does not significantly improve the conservation outcome, it may be more optimal to implement a plan
28 based on the original information alone.

29 Spatial conservation planning and imperfect information

30 Nearly all conservation actions include a spatial component: that is, decision about where to act. Spatial
31 conservation planning originally focused on designing networks of conservation reserves, but has since then
32 expanded to cover also other conservation actions and multi-action planning e.g. (Kujala et al., 2015). The
33 aim of conservation is to preserve a representative subset of a region's biota by separating its constituents
34 from threatening processes. Conservation does not occur in a vacuum. States and non-state actors practicing
35 conservation do so with limited budgets and resources. Also, previous conservation actions need to be
36 accounted for to target resources where they are most critically needed. Therefore, conservation planning
37 must be systematic (Margules and Pressey, 2000)

38 A typical (systematic) spatial conservation plan will assess a pool of candidate locations for reservation (or
39 some equivalent action). The planner will either find a set of locations that maximize conservation benefits
40 within a given budget, or prioritize locations in order to meet a conservation target as cost effectively as
41 possible.

The information needed to make a spatial conservation plan

A systematic spatial conservation plan is in essence a classic decision analysis requiring optimization. Like any decision analysis it first requires a comprehensive problem definition. In defining the problem the conservation planner requires five types of information to proceed.

- **Objectives:** The objective may be a target (e.g., protect 20% of the habitat of a set of species) or a goal to maximize some gain or minimize some loss (e.g. protect locations so as to minimize the average loss of habitat for a set of species.)
- **Constraints:** The bounds in which the plan operates. Including but not limited to, the spatial and temporal frame the plan will operate in, and the resources (e.g., monetary) available to the planner.
- **Actions:** The actions the planner can take (e.g., protect, not protect, restore habitat, etc.) to meet their objectives within the given constraints.
- **State variables:** The components of the system in which the plan will operate that planner seeks to effect and against which, the performance of the plan will be measured. In a spatial conservation plan the state variables are typically the distribution of a set of species the plan is seeking to protect.
- **System models:** A system model links the actions the planner will take and the state variables. With a system model the planner can predict what the outcome of any given plan will be with respect to the state variables of interest (e.g., what will be the effect of protecting certain areas on the distribution of species).

Uncertainty in spatial conservation planning.

Of the components in the list above, it is the last two, state variables and system models, where the most critical uncertainty lies. Here we focus on the uncertainty in state variables and leave the treatment of system model uncertainty for another forum.

State variables (typically modeled species distributions) are almost always based on imperfect knowledge. Conservation planners do not know with certainty where the species they seek to protect occur and must rely on models to predict their occurrence and abundance. Such models may themselves be based on uncertain

and imperfect inputs (e.g., the distribution of a species may be predicted from a climate envelope that is based on uncertain climate data)(Guillera-Arroita et al., 2015). Uncertainty also arises in state variables such as species distribution maps because the models used to build them are trained with few data points. For example, a common approach to predicting the distribution of species is to use so called presence-only species distribution models (often with the software MaxEnt). In such models, the environment of locations where a species is known to occur, is compared to the environment overall. Ignoring for a moment any uncertainty in the nature of the environment, the fewer locations a species is known to be present at, the more imprecise and uncertain the predictions of its overall distribution from such models will be.

Accounting for uncertainty in spatial conservation planning

Ultimately a conservation planner, like any decision maker, can do one of two things in the face of uncertainty. They can make a decision (formulate a plan) with the uncertainty or try to reduce the uncertainty. Even if they take the second option, rarely is uncertainty completely resolved and the plan must be made with imperfect information. More often than not, spatial conservation planning is done in spite of uncertainty rather than with uncertainty. Uncertainty, whether or not explicitly acknowledged, is not often quantified for state variables or any of the other decision components. For example, a set of predictive species distribution maps will be produced on top of which a spatial plan is built. However, only one map per species is typically produced and these maps will be implicitly treated as the true state of the system. When in reality the maps represent one possible, and at best average or most likely (though typically not both and perhaps not either), version of the system state under the assumption that the data used to produce them was unbiased. If instead, a set of maps was produced that reflected the uncertainty (multiple maps for each species) then a complementary set of plans could be produced from them, that reflected the uncertainty in state variables. It is only at this point having quantified uncertainty, that uncertainty can truly be addressed and an assessment made of whether and/or how to reduce it by acquiring additional information. To know whether or how to reduce uncertainty we must measure the value of information.

The value of information

Value of information analysis is a tool used to quantify how much reducing the uncertainty in a predictive model is worth to a decision maker. The value of information is the difference between the final outcome of a decision (or plan) with or without additional information. Value, in and of itself, cannot be known in advance of any decision problem, including a spatial conservation plan, playing out. Therefore, decision theorists work with expected value. Expected value is the mean of all possible outcomes weighted by their probability of occurring. For example, if a person will earn a dollar when a fair coin toss is heads, and nothing if it is tails, the expected value of the toss is 50 cents. When making a decision with multiple alternatives, assuming the decision maker is risk neutral, it is always best to take the action that maximizes the expected value.

The expected value with original information

The expected value (see Box 1) with original information, EVWOI, is the maximum expected value if no additional information is gathered before a decision is made (see Box 1 for more information). In the case of spatial conservation planning, EVWOI is the default. Typically, a conservation plan maximizes the expected value using the information at hand. For example, species occurrence data (point locations of places where each species of concern has been observed) is used to build a set of species habitat suitability maps, using a species distribution modelling algorithm such as MaxEnt. A second algorithm, such as Zonation or Marxan, is used to construct a plan that maximizes the expected outcome with respect to some objective/target. The key, is that in the default case there is only one map used per species. The one-per-species map set represents the expected outcome under this level of uncertainty. Any uncertainty is averaged over and the map delineating the spatial conservation plan will indicate the expected value with original information.

The expected value with perfect information

Having perfect information is to have complete knowledge—no uncertainty. While in practice this is unlikely to ever occur, the expected value with perfect information (EVWPI, see Box 1 for a formal definition) is a useful construct as it allows to calculate the expected value of information

The expected value of perfect information

If we can estimate the value of having perfect information, that is knowing what it is worth to resolve all uncertainty before enacting a conservation plan, then will have an idea of the upper bound on what we should be willing to do to reduce uncertainty. If the expected value of perfect information is relatively small then it is less likely to be worth resolving uncertainty than if the value of perfect information was relatively large.

Box 1: A simple example: value of information for a plan to protect one species at two properties

A conservation planner can afford to protect one piece of land to help save an endangered species from extinction. Two properties are available.

The planner's aim is to maximise the area of habitat protected for the endangered species. The planner is uncertain about each property's **habitat suitability**. A property's habitat suitability can be either one (suitable) or zero (unsuitable). The first property has a 50% chance of being suitable (a 50% chance that habitat suitability is one, and a 50% chance that it is zero). But the planner knows that the second property has a slightly better chance (60%) of being suitable (i.e., a 40% chance it's unsuitable). The properties are identical in all other ways. A property can be protected **with original information** (i.e., choosing a property while still ignorant of the habitat suitabilities) or **with perfect information** (i.e., knowing the actual habitat suitabilities of each property in advance). The **value** of protecting a property is the same as its habitat suitability (i.e., the value can be zero or one) Regardless of their habitat suitability, an unprotected property has no value to the planner. The conservation planner must decide which property to protect.

Expected value

The **expected value** (EV) is the value the planner expects (but not necessarily what they get), given the outcome of their decision is uncertain. An **expected value** is a value weighted (multiplied) by a probability.

Before they make a decision, the planner can work out the **expected value with original information** (EVWOI) or the **expected value with perfect information** (EVWPI). The **expected value of perfect information** (EVPI) is the difference between the EVWPI and the EVWOI. If the EVPI is positive, it means it is worth (up to a point) learning before making a decision. For this example, if the EVPI is large enough, it is worth the planner working out what the habitat suitabilities of the two properties are, before they decide which one to protect. But if the EVPI is too low (when there is little difference between EVWOI and EVWPI) they should just decide which one to protect straightaway.

Expected value with original information

The EVWOI is the highest value the planner expects they could get, on average (the **maximum expected value**), by protecting a property when they don't know the habitat suitabilities. To work out the expected value of protecting a property, the planner weights (i.e., multiplies) the values that are possible by their probabilities and adds them together.

In this case, protecting the first property has a $1 - 0.5 = 0.5$ probability of having a value of 0, and a 0.5 probability of having a value of 1. So, the expected value is:

$$1 \times 0.5 + 0 \times (1 - 0.5) = 0.5.$$

The calculation for the second property is:

$$1 \times 0.6 + 0 \times (1 - 0.6) = 0.6,$$

meaning the maximum expected value, EVWOI, is also **0.6**. Formally, using mathematical notation, the calculation can be expressed as:

$$\text{EVWOI} = \max_a \mathbb{E}_s[U(a, s)]. \quad (1)$$

Where a represents the **action** taken by the conservation planner, s represents a **state** (or scenario) (i.e., in this case it describes the information the planner has on the properties' habitat suitabilities), U represents the **utility** (or the value to the planner) of taking action a , and \mathbb{E} is the mathematical symbol for **expectation**.

Expected value with perfect information

The EVWPI is the value the planner expects if they knew the properties' habitat suitabilities before deciding which one to protect.

In this case, there are four possible scenarios:

1. both properties are suitable,
2. the first is suitable while the second is not,
3. the second is suitable while the first is not, and
4. neither is suitable.

Because the planner is only protecting one property, the value the planner gets from any one of these scenarios is the highest of the values of the two properties for that scenario (i.e., the value for scenarios 1, 2 and 3 is one, since there is at least one suitable property, while the value for scenario 4 is zero, since neither property is suitable). To work out the EVWPI, the planner takes the four maximum values (one for each scenario), and sums them, weighted by the scenarios' respective probabilities. The probability of a given scenario is the probability that the first property has the suitability stated in the scenario, multiplied by the probability that the second property has the suitability stated in the scenario. For scenarios 1 and 3, where the second property is suitable, the probability of the scenario is $0.5 \times 0.6 = 0.3$, irrespective of whether the first property is suitable or not. This is because the probability of the first property being suitable is the same as the probability that it is unsuitable (i.e., 0.5). Similarly, for scenarios 2 and 4, where the second property is unsuitable, the probability is $0.5 \times 0.4 = 0.2$. So, the weighted values for scenarios 1 to 4, respectively, are:

$$\begin{aligned}
1 \times (0.5 \times 0.6) &= 1 \times 0.3 = 0.3, \\
1 \times (0.5 \times 0.4) &= 1 \times 0.2 = 0.2, \\
1 \times (0.5 \times 0.6) &= 1 \times 0.3 = 0.3, \text{ and} \\
0 \times (0.5 \times 0.4) &= 0 \times 0.2 = 0.
\end{aligned} \tag{2}$$

177 The EVWPI is the sum of these weighted values, $0.3 + 0.2 + 0.3 + 0 = \mathbf{0.8}$. In mathematical notation this can
178 be expressed as:

$$\text{EVWPI} = \mathbb{E}_s[\max_a U(a, s)]. \tag{3}$$

179 Here the symbols have the same meaning as in equation 1. But notice that instead of calculating the
180 **action that maximises the expected value** as in EVWOI, EVWPI is the **expected maximum value**
181 **of action**. In other words, the order of maximisation and expectation has been reversed.

182 **Expected value of perfect information**

183 As noted above, the expected value of perfect information (EVPI) is the difference between the EVWPI and
184 the EVWOI. Combining equations 1 and 3, the EVPI can be expressed as:

$$\text{EVPI} = \mathbb{E}_s[\max_a U(a, s)] - \max_a \mathbb{E}_s[U(a, s)]. \tag{4}$$

185 In the conservation planner's case, EVPI is $0.8 - 0.6 = \mathbf{0.2}$, meaning that if they could express habitat value
186 as money, they should be willing to spend up to 20% of the price of a property, on learning about habitat
187 suitability, before they decide what to protect.

188

189 As indicated above spatial conservation planning that explicitly addresses uncertainty in state variables
190 including (but not limited to) species distribution models is atypical. This presents a problem, as without

191 measuring uncertainty we cannot know whether uncertainty is worth addressing. Without doubt there is a
192 motive to reduce uncertainty in general, as decisions made with less uncertainty, all else being equal, will be
193 better ones than decisions made with relatively more uncertainty. In light of these facts we propose that
194 the field of spatial conservation planning should absorb the decision theoretic tools of value of information
195 analyses. However, introducing a new tool into to an established framework is by no means trivial. As such
196 here we seek to incorporate the concepts of value of information in harmony with the norms of systematic
197 spatial conservation planning. In doing so, we outline what we think is a robust and comprehensive method
198 of calculating the value of information for a spatial conservation plan for the first time. Our approach in the
199 following work has to been to balance simplicity with realism. While central case study is contrived it uses
200 real (not simulated data) in a plan to protect species of conservation concern in a region in need of systematic
201 planning. To perform our analysis we combine the use of established software packages MaxEnt (Phillips and
202 Dudík, 2008) and Zonation (?), which are well known to conservation planners, with Monte Carlo sampling
203 methods and value of information analysis. The rest of this text is organized as follows. We introduce the
204 case study briefly and then demonstrate how, within the context of spatial conservation planning, the value
205 of information can be calculated using Monte Carlo methods. To aid understanding we interweave the case
206 study with toy low resolution examples so that reader may gain a deeper understanding of the method we
207 are proposing.

Case study: a spatial conservation plan for the Hunter region, NSW, Australia

To demonstrate how to incorporate the value of information in a systematic spatial conservation plan, we now turn to a case study on prioritizing the Hunter region for the conservation of threatened plants and animals. For the case study we make the simplifying assumptions that the entire region is an original position where no area is protected but the entire region is available for protection in a conservation plan. While this is entirely unrealistic, it would be unnecessary to complicate the demonstration with a more realistic scenario as the complications would only serve to distract the reader from the key components of the method we outline here.

Study area

The Hunter is a biodiverse region of north-eastern New South Wales, Australia. The region is home to many threatened species of plants and animals. There are multiple threats to biodiversity in the region. The Hunter is under active development and the area's land users utilize its resources for mining, agriculture, transport, urban infrastructure and conservation. For the analyses we present here we consider the Hunter region to include the local government areas of Cessnock, Dungog, Gloucester, Gosford, Greater Taree, Great Lakes, Lake Macquarie, Maitland, Musselbrook, Newcastle, Port Macquarie-Hastings, Port Stephens, Singleton, Upper Hunter and Wyong.

Study species

Short descriptions of the study species.

- Biology
- Why threatened?

Approximate maximum carrying capacity of the Hunter region

1 pixel is 900 hectare.

Powerful Owl home range is 1e4 to 5e4 hectares Maximum Carrying capacity is probably something $> .001$ birds per hectare, or about .9 birds per pixel.

Tiger Quoll home range is 5e3 to 4e4 hectares. Maximum Carrying capacity is probably something $> .002$ quolls per hectare, or about 1.8 quolls per pixel.

Squirrel Glider maximum carrying capacity is 1.5 gliders per hectare, or at about 1350 gliders per pixel

Regent honeyeater: according to this 0.12 ($\pm .72$) birds per hectare (not normally distributed though). So a rough guess may be 2 birds per hectare or 1800 birds per pixel.

Angophora inopina: according to this 1100 trees where found in 6.2 hectare. So approx 180 plants per hectare and 162000 plants per pixel.

Acacia bynoeana 1600 plants / 650ha So approx plants per 2.5 plants per hectare and 2250 plants per pixel.

Input data for the conservation plan

Predictors of species distributions

We summarise the environment of the Hunter region with six data layers: annual mean solar radiation, annual mean temperature, annual precipitation, precipitation seasonality (coefficient of variation), inherent soil fertility, and topographic wetness index (Figure 3). Each layer is a 104 by 114 grid of 3km by 3km cells. We chose this set of variables as they are publically available, are biologically plausible drivers of the distribution of many taxa, have previously been shown to predict the distributions of the study species in the region and are relatively are uncorrelated with one another (maximum pearson correlaton coefficient = r).

Species occurence data

Background geographic data

Box 2: A slightly less simple example: value of information for a plan to protect one species at two properties with continuous uncertainty

In Box 1 we demonstrated how to calculate the value of information when the uncertainty in value was discrete (value of property could be zero or one). In the following example we increase complexity slightly and demonstrate how to calculate EVPI when uncertainty is continuous.

Modelling species distributions using Maxent

Calculating the expected value with original information

$$\text{EVWOI} = 25\%$$

Box 3: A simple example of calculating the value of information for a conservation plan using Zonation

Expected value with perfect information

$$\text{EVWPI} = 26\%$$

Expected value of perfect information

$$\text{EVPI} = 1\%$$

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List of Figures

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- 2 How to calculate EVWPI. First work out the scenarios that are possible. Then choose the property to protect in each possible scenario. When the properties have equal value it doesn't matter which one is selected (e.g., in scenarios 3 & 4). Next calculate the probability that the scenario occurs by multiplying the probabilities of the property habitat suitabilities (e.g., for scenario 1, the probability is $0.5 \times 0.6 = 0.3$, see the rightmost arrows). Next multiply the scenario probabilities by the value of the properties selected in each scenario. Finally, sum the weighted scenario values (rightmost values). In this case the EVWPI is **0.8**. 20
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- 4 Climate, soil and topographic maps of the Hunter region. These variables were used to model the distribution of the study species used to formulate the spatial conservation plan. 22
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328		average proportion of carrying capacity remaining with all other unprotected cells are removed	
329		(top equation. Next calculate EVWPI. For each set of bootstrapped species carrying capacity	
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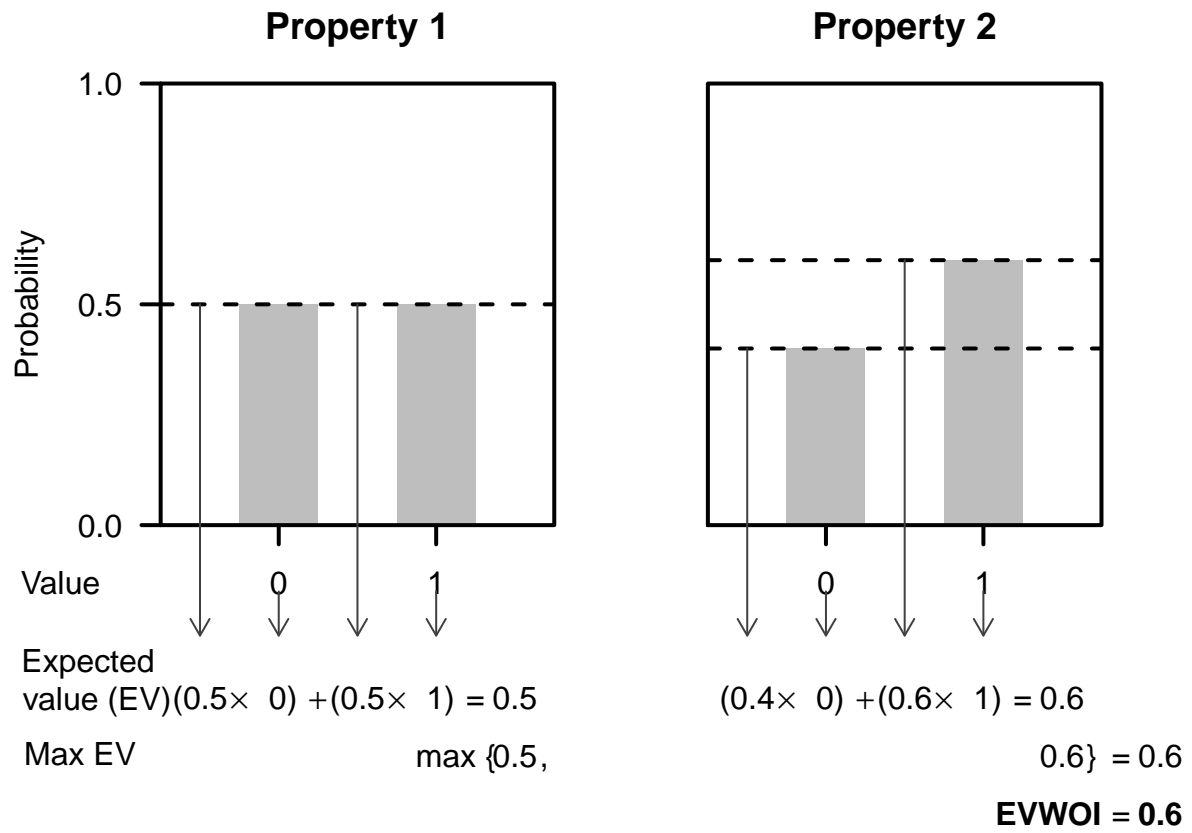


Figure 1

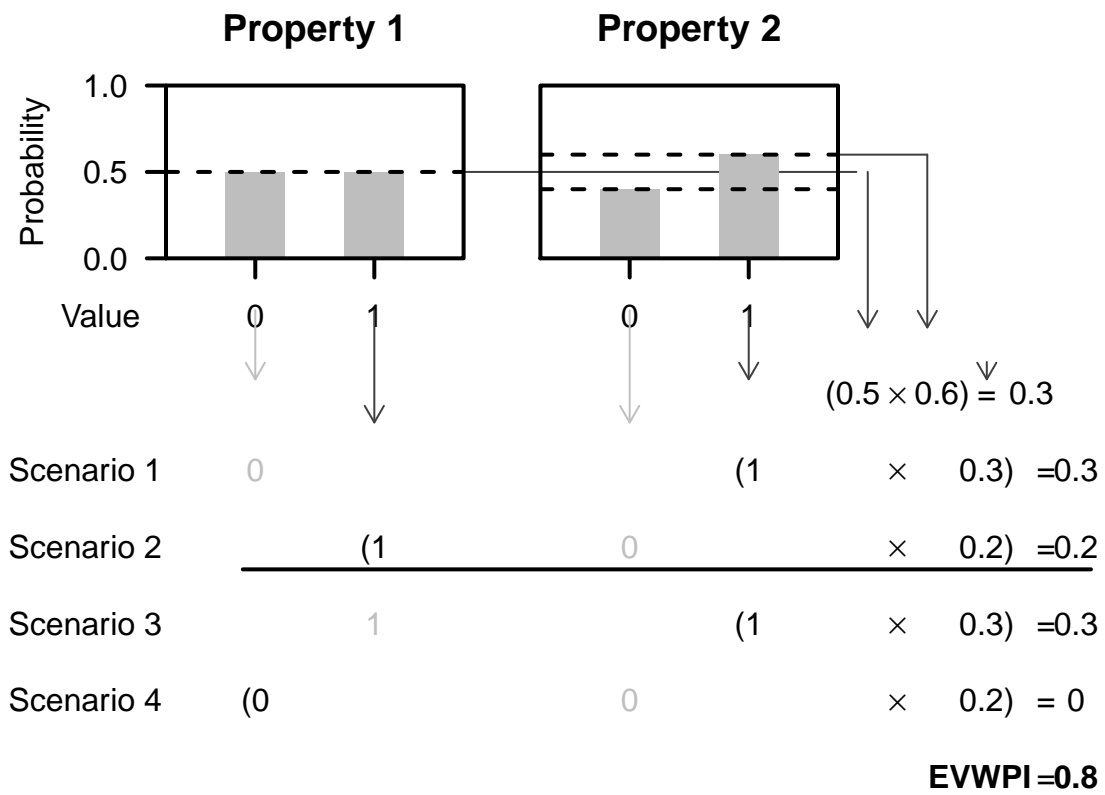
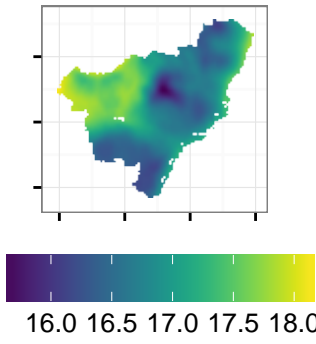
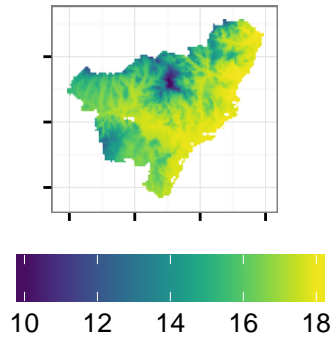


Figure 2

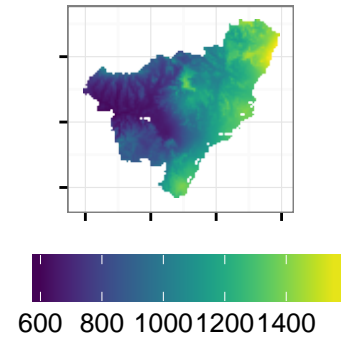
Annual Mean Radiation



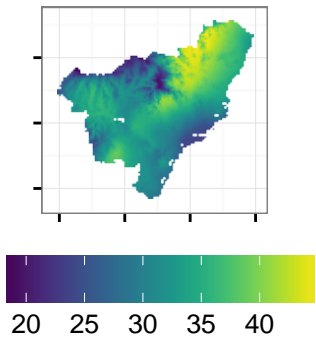
Annual Mean Temperature



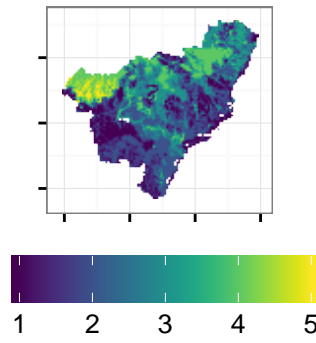
Annual Precipitation



Precipitation Seasonality



Soil Fertility



Topographic Wetness

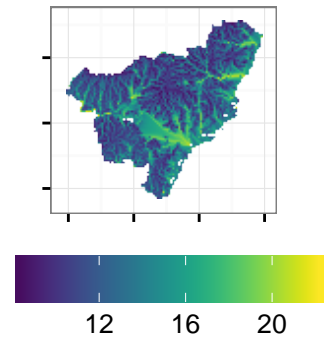


Figure 3

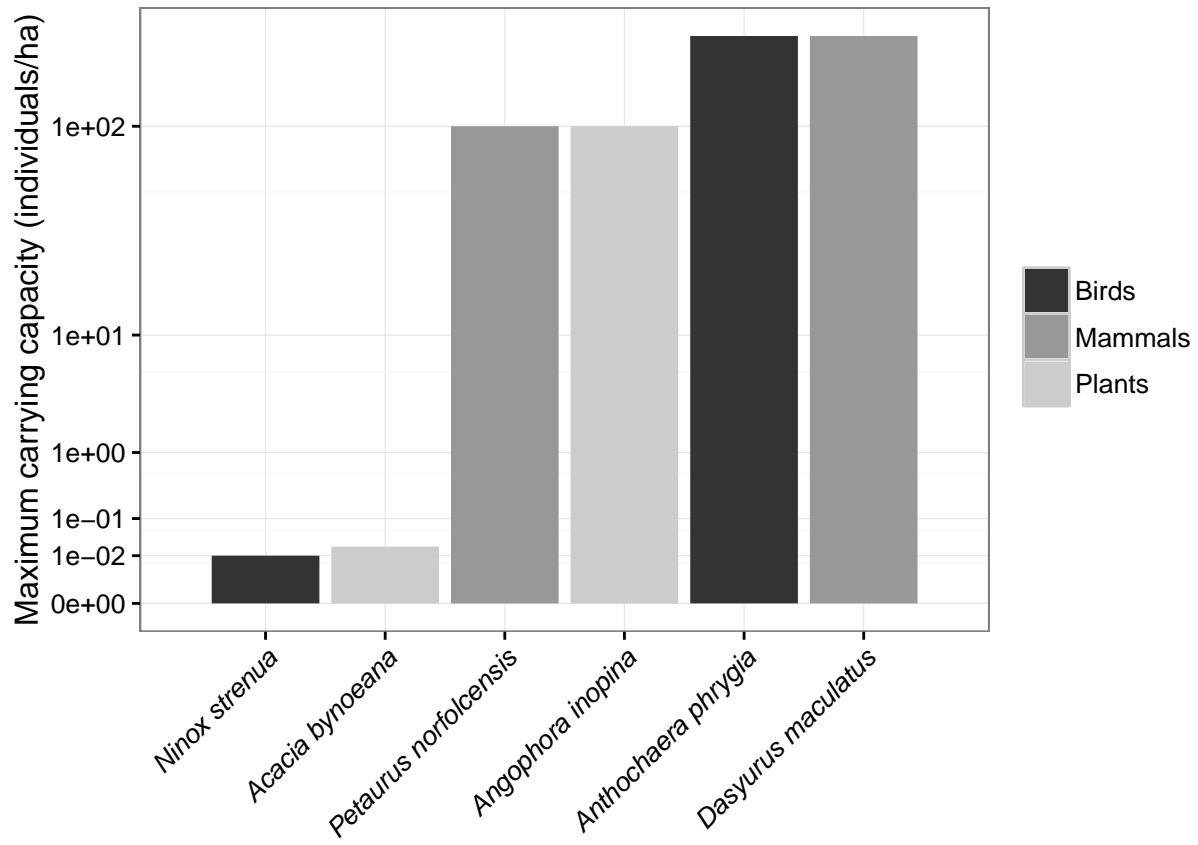


Figure 4

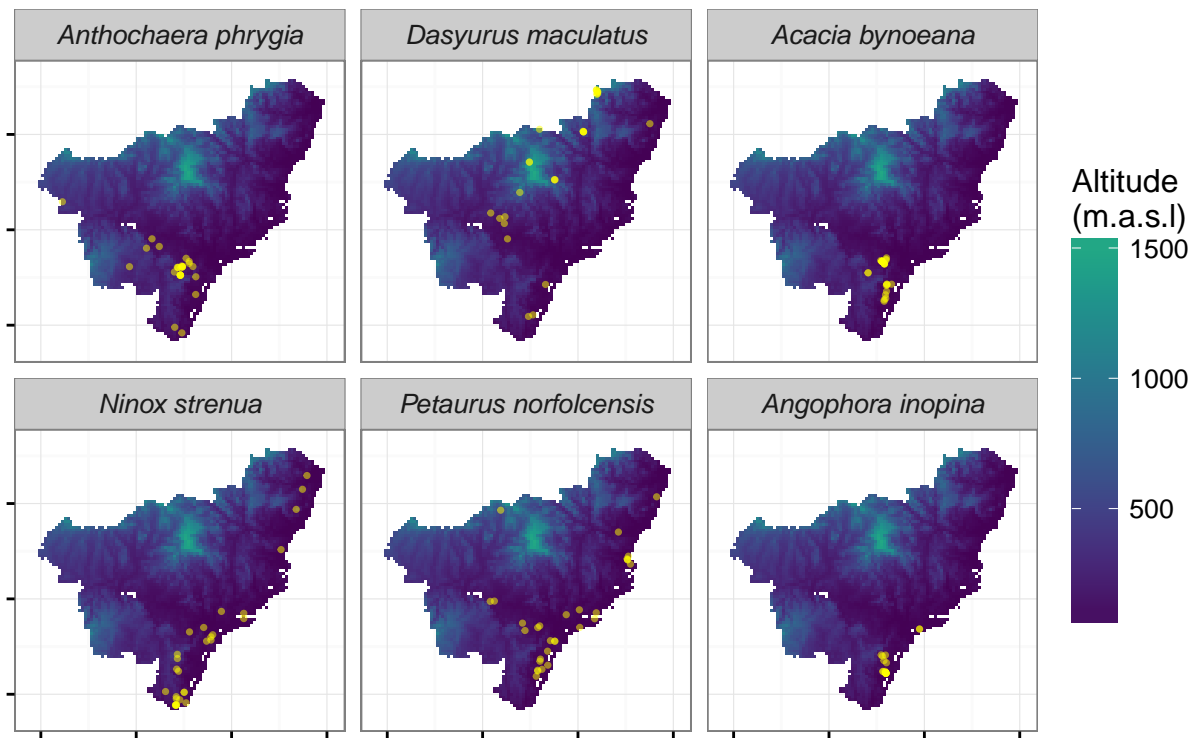


Figure 5

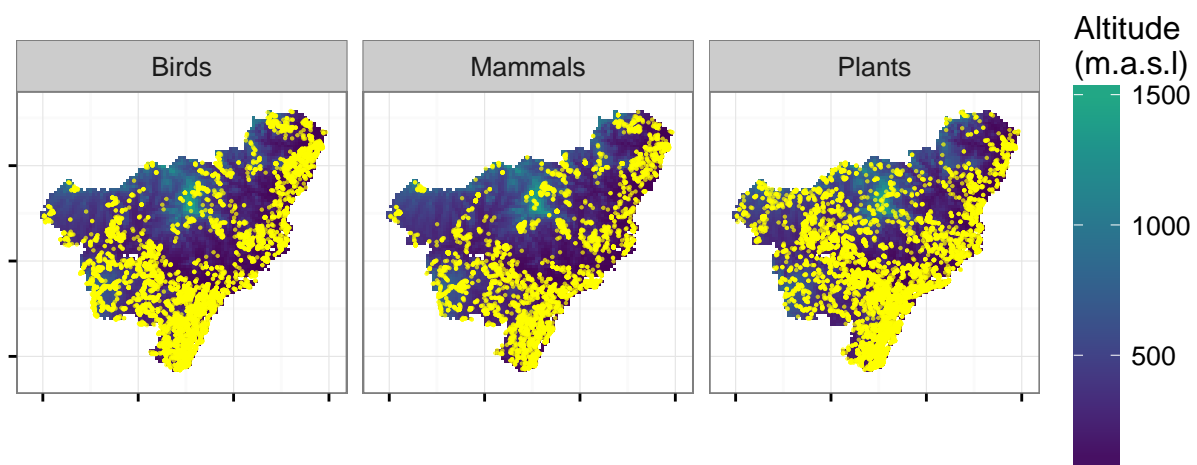


Figure 6

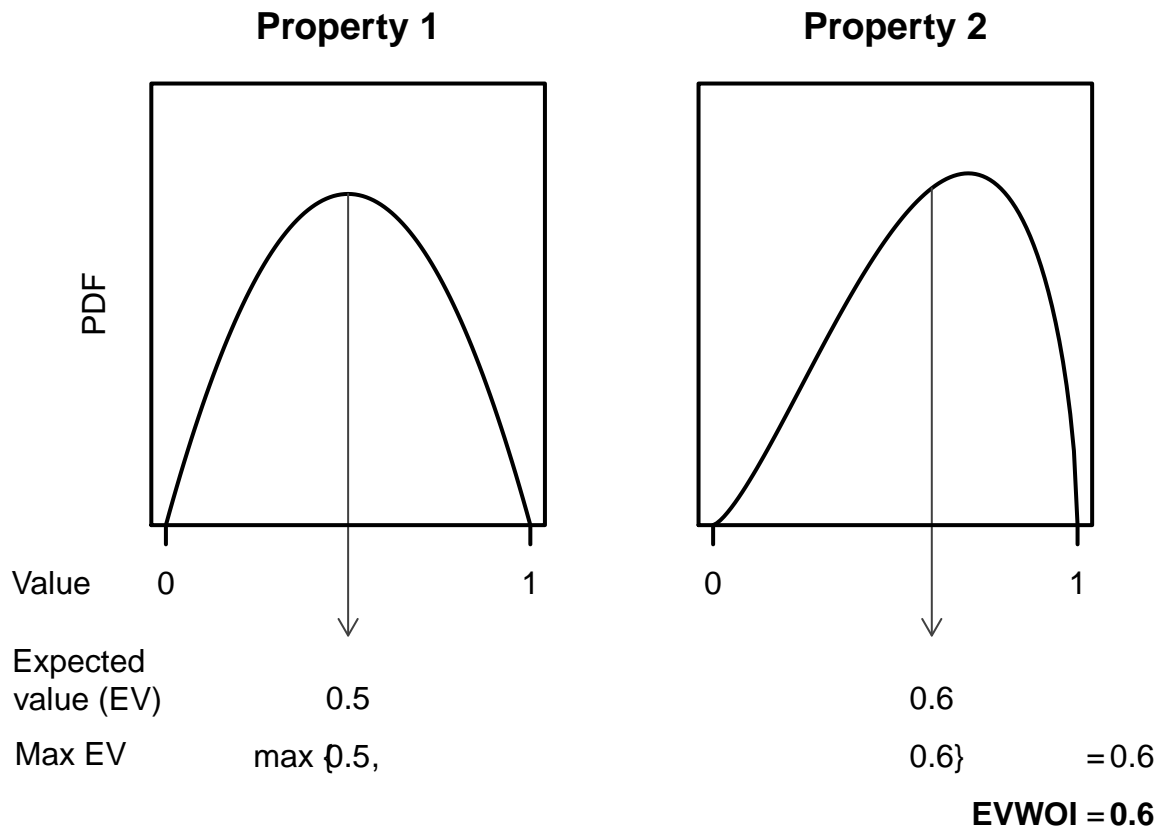
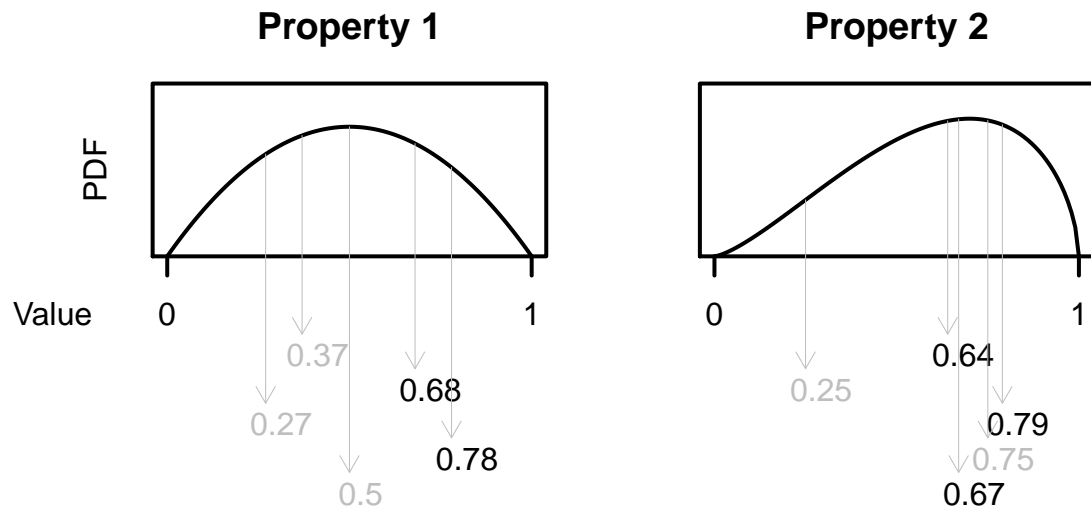


Figure 7



$$\text{EVWPI} = \frac{0.64 + 0.68 + 0.79 + 0.78 + 0.67}{5}$$

$$= 0.71$$

Figure 8

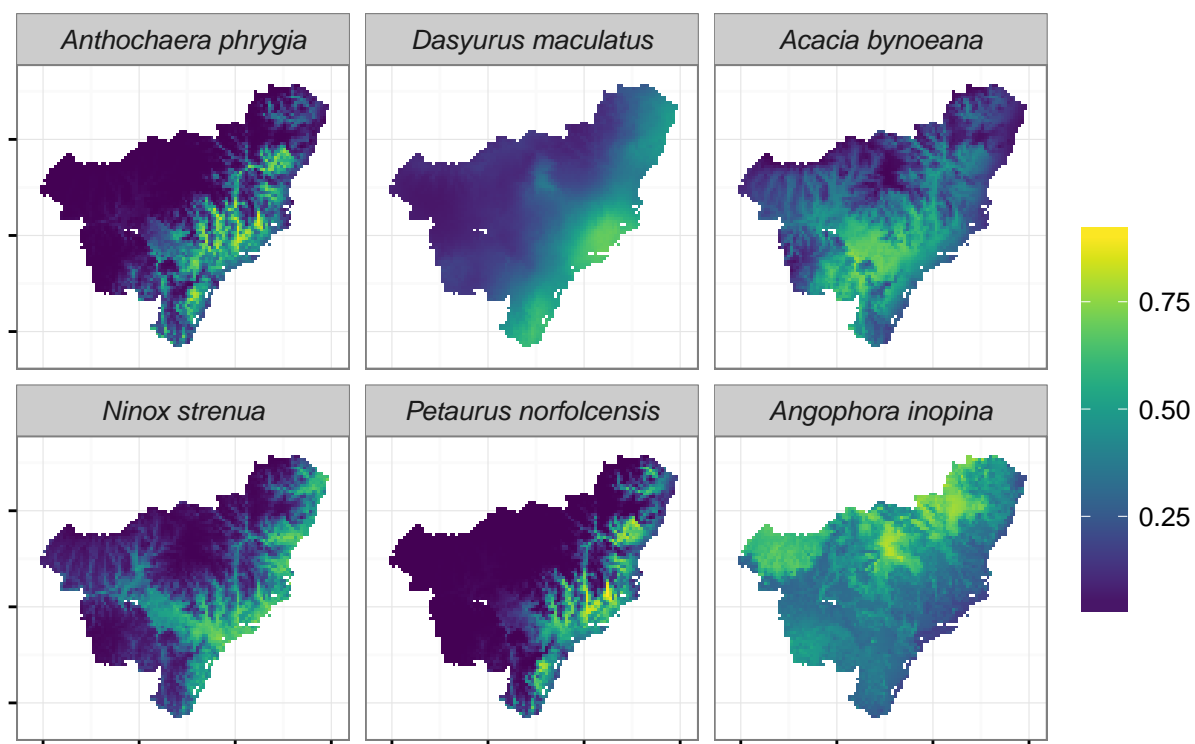


Figure 9

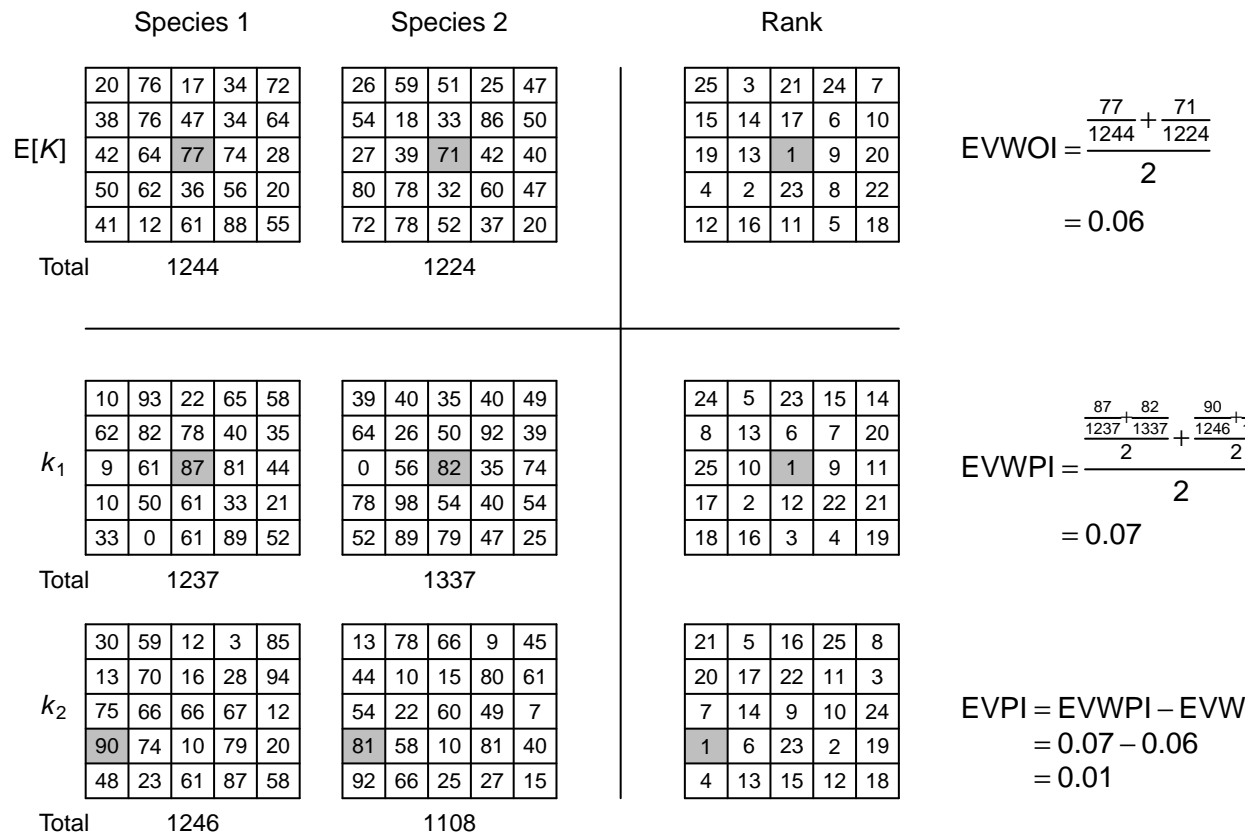


Figure 10

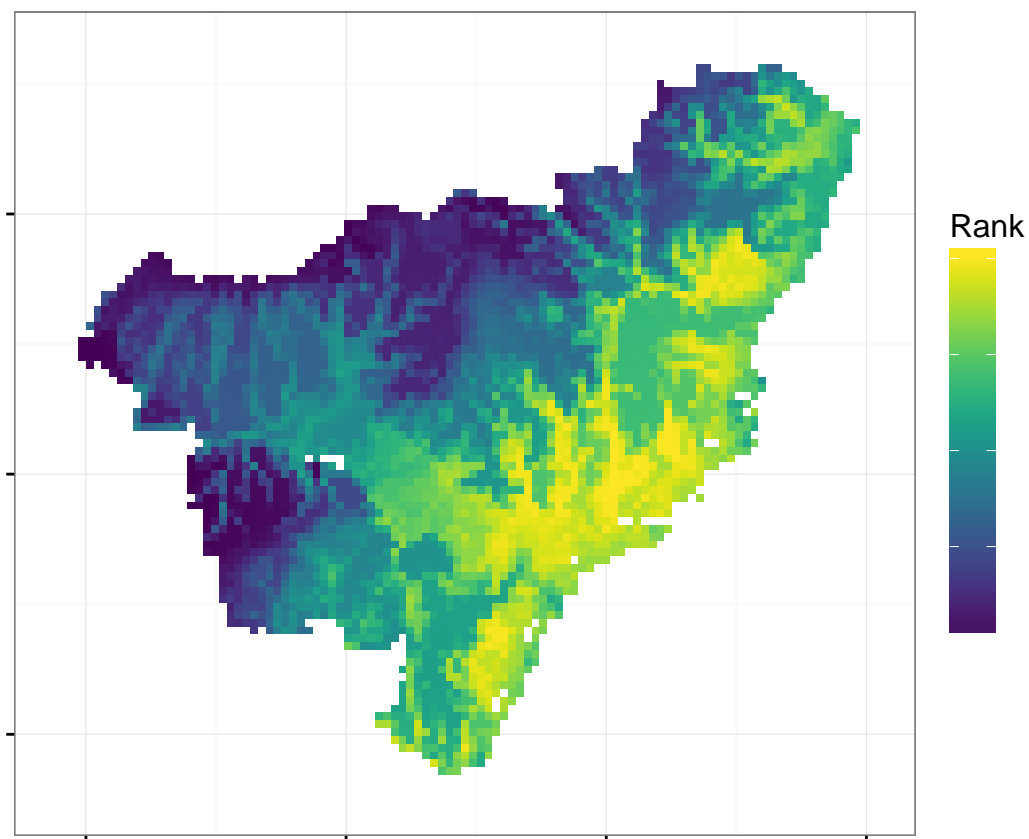


Figure 11

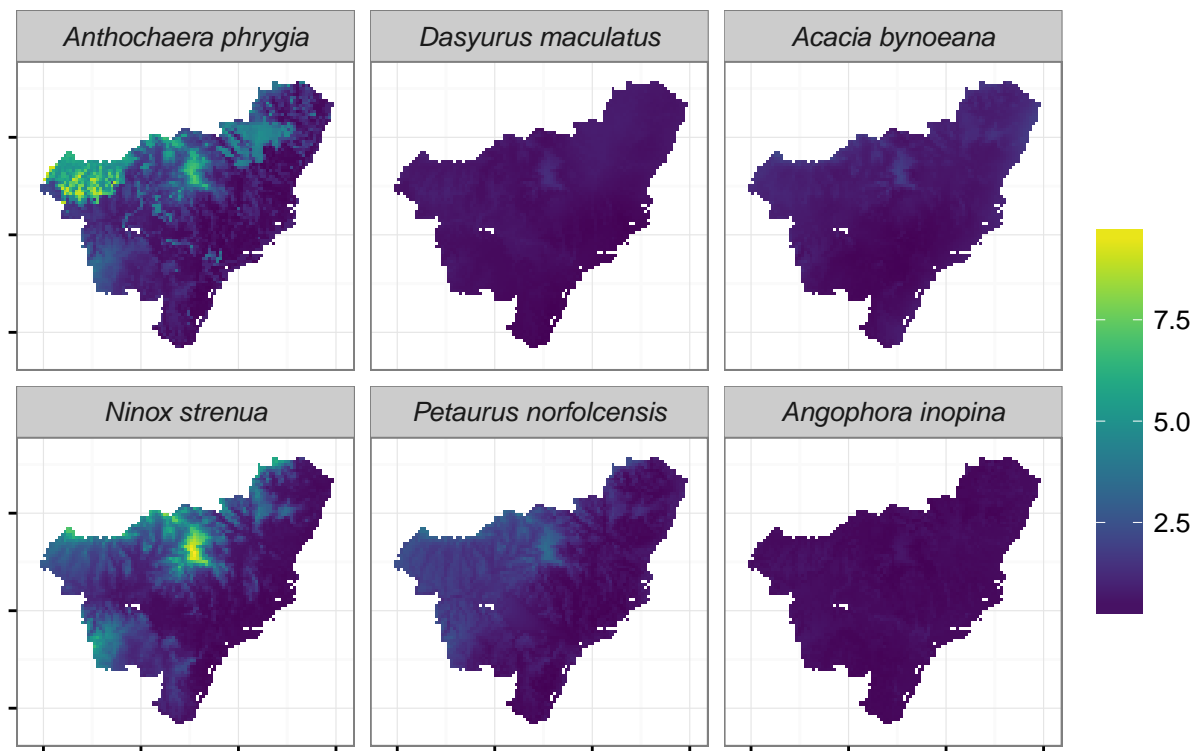


Figure 12

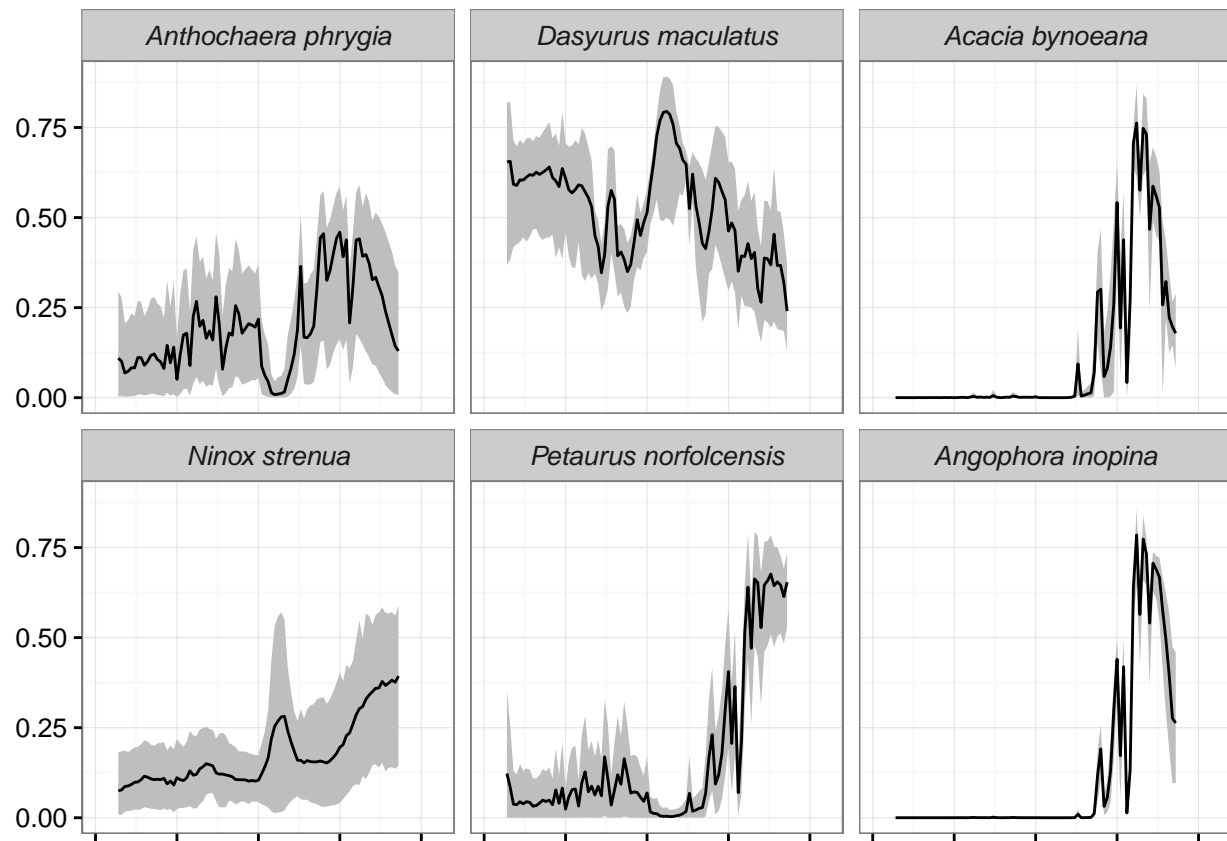


Figure 13

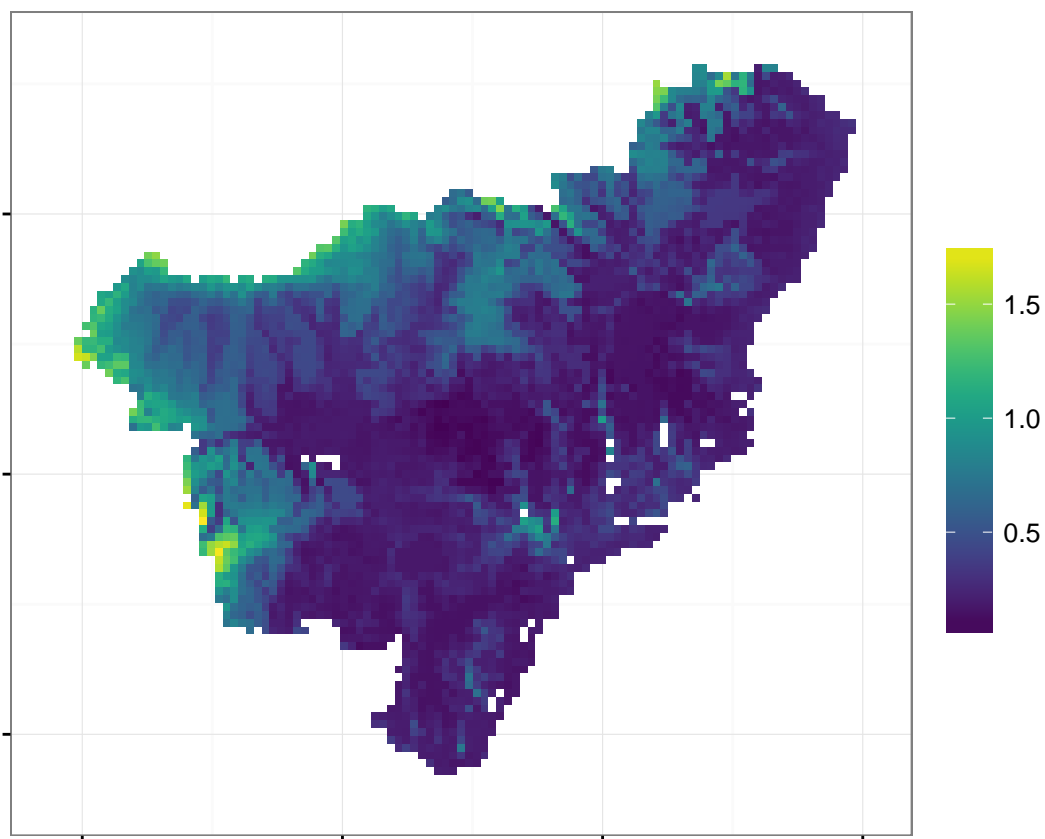


Figure 14

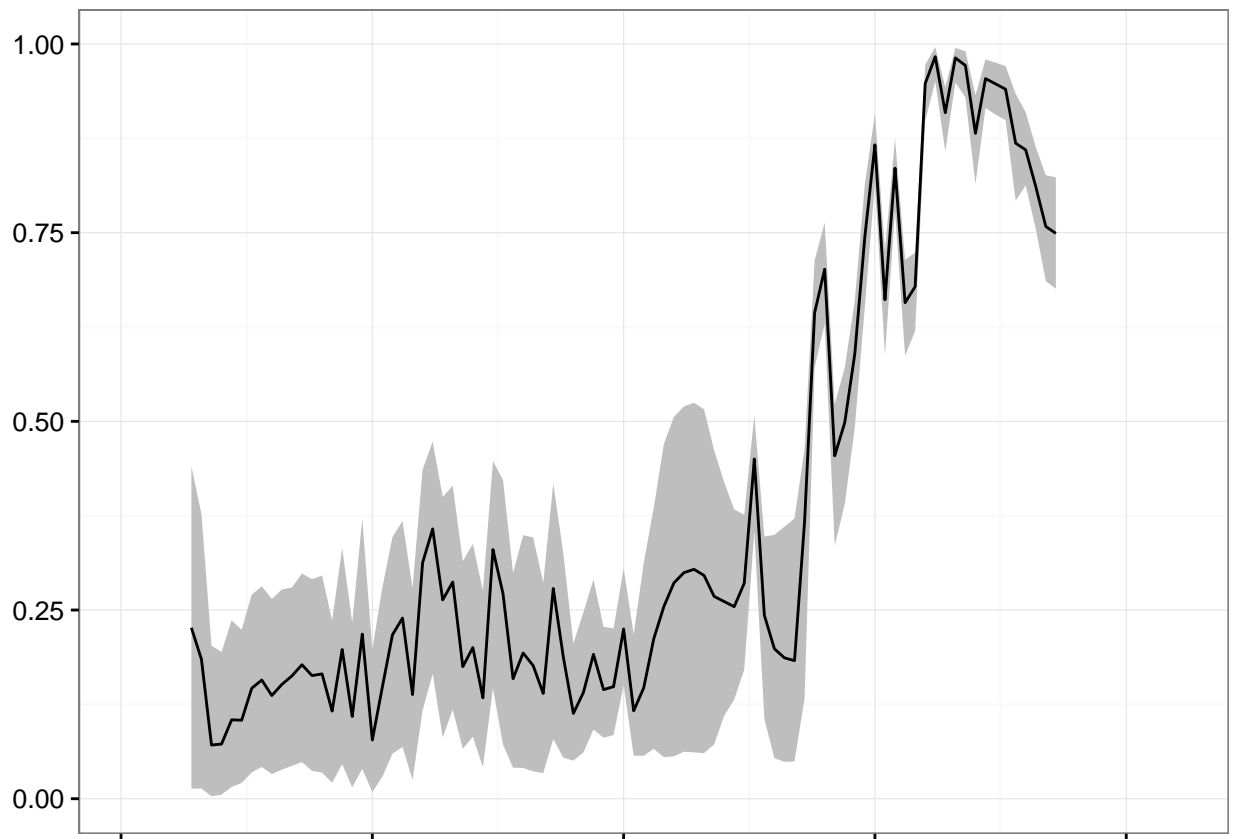


Figure 15