# Quick Look

Wojciech Kołowski

### Old rules

$$\frac{\Gamma, x : A \vdash e \Leftarrow H \Rightarrow B}{\Gamma \vdash \lambda x. e \Leftarrow A \rightarrow H \Rightarrow A \rightarrow B}^{\text{ABS}}$$

$$\frac{\Gamma \vdash f \Leftarrow ? \rightarrow H \Rightarrow A \rightarrow B \quad \Gamma \vdash a \Leftarrow A \Rightarrow A}{\Gamma \vdash f \Rightarrow A \Rightarrow B}^{\text{APP}}$$

$$\frac{\Gamma \vdash a \Leftarrow ? \Rightarrow A \quad \Gamma \vdash f \Leftarrow A \rightarrow H \Rightarrow A \rightarrow B}{\Gamma \vdash f \Rightarrow A \Rightarrow B}^{\text{ALTAPP}}$$

#### Wut

Easy for the original rule APP, but hard for the alternative ALTAPP: f  $e_1$ , f  $e_2$ , etc.

Easy for the alternative rule Altapp, but hard for the original one App:  $(\lambda x. e) y$ ,  $(\lambda x. e) y$  z

Hard for both: case  $(\lambda a. e_1) (\lambda b. e_2) x$ 



# Quick Look at the argument

$$\frac{(x:A) \in \Gamma}{\Gamma \vdash x \Rightarrow A} QL\text{-}ARG\text{-}VAR$$

$$\overline{\Gamma \vdash (e : H) \Rightarrow H}^{\text{QL-Arg-Annot}}$$

$$\overline{\Gamma \vdash \text{unit} \Rightarrow 1}^{\text{QL-Arg-Unit}}$$

$$\frac{e \neq x \quad e \neq (e':H') \quad e \neq \text{unit}}{\Gamma \vdash e \Rightarrow ?} \text{QL-Arg-Fail}$$

## The new rule

$$\frac{\Gamma \vdash a \Rightarrow H_A \quad \Gamma \vdash f \Leftarrow H_A \to H_B \Rightarrow A \to B \quad \Gamma \vdash a \Leftarrow A \Rightarrow A}{\Gamma \vdash f \ a \Leftarrow H_B \Rightarrow B} \text{App-QL-App-QL-App}$$

## Quick Look at the function

$$\frac{\Gamma \vdash f \Rightarrow H_A \rightarrow H_B' \qquad \begin{array}{c} \Gamma \vdash a \Leftarrow H_A \Rightarrow A \\ \Gamma \vdash f \Leftarrow A \rightarrow H_B \sqcup H_B' \Rightarrow A \rightarrow B \\ \hline \Gamma \vdash f \ a \Leftarrow H_B \Rightarrow B \end{array}}{\text{QL-Fun}}$$

## Quick Look

$$\frac{(x:A) \in \Gamma \quad H \sqsubseteq A}{\Gamma \vdash x \Leftarrow H \Rightarrow A} QL\text{-VAR}$$

$$\Gamma \vdash (e: H_1) \Leftarrow H_2 \Rightarrow H_1 \sqcup H_2$$
 QL-Annot

$$\frac{e \neq x \quad e \neq (e' : H')}{\Gamma \vdash e \Leftarrow H \Rightarrow H} QL\text{-Fail}$$

### New rules

$$\frac{\Gamma \vdash f \Leftarrow ? \to H \Rightarrow H_A \to H_B}{\Gamma \vdash f \Leftarrow A \to H_B \Rightarrow A \to B} \frac{\Gamma \vdash a \Leftarrow H_A \Rightarrow A}{\Gamma \vdash f \Leftarrow A \to H_B \Rightarrow A \to B} \text{QL-App}$$

#### Wut

$$\frac{\Gamma \vdash e_{2} \Leftarrow ? \Rightarrow H_{2} \quad \Gamma \vdash e_{1} \Leftarrow H \Rightarrow f \; ; \; \overline{e} \; ; \; H'}{\Gamma \vdash e_{1} \; e_{2} \Leftarrow H \Rightarrow f \; ; \; \overline{e} \; ; \; H'} \text{QLD-APP}$$

$$\frac{(x : A) \in \Gamma \quad H \sqsubseteq A}{x \vdash H \Leftarrow A \Rightarrow ; \; ;} \text{QLD-VAR}$$

$$\overline{\Gamma \vdash (e : H_{1}) \Leftarrow H_{2} \Rightarrow H_{1} \sqcup H_{2}} \text{QL-Annot}$$

$$\frac{e \neq x \quad e \neq (e' : H')}{\Gamma \vdash e \Leftrightarrow H \Rightarrow H} \text{QL-Fail}$$

$$\frac{\Gamma \vdash e_{1} \; e_{2} \Leftarrow H \Rightarrow f \; ; \; \overline{e} \; ; \; H'}{\Gamma \vdash e_{1} \; e_{2} \Leftarrow H \Rightarrow B}$$