



UNDERSTAND

10. **Generalize** Explain two methods by which $(2m^3 + 4n^2)^2$ can be simplified. Which method do you prefer and why?
11. **Use Structure** Polynomial function P is the sum of two polynomial functions, one with degree 2 and a positive leading coefficient and one with degree 3 and a negative leading coefficient. Describe the end behavior of P . Write an example of two polynomial functions and their sum, P , to justify your description.
12. **Generalize** Multiply the polynomials $(a + b)(a + b)(a + b)$ to develop a general formula for cubing a binomial, $(a + b)^3$.
13. **Reason** Polynomial function R is the difference of two degree-two polynomial functions. What are the possible degrees for R ? Explain.
14. **Error Analysis** Describe and correct the error a student made in multiplying the polynomials.

$$\begin{aligned}
 &(y - 2)(3y^2 - y - 7) \\
 &= y(3y^2 - y - 7) - 2(3y^2 - y - 7) \\
 &= 3y^3 - y^2 - 7y + (-6y^2) + (-2y) - 14 \\
 &= 3y^3 - 7y^2 - 9y - 14
 \end{aligned}$$



15. **Higher Order Thinking** Do you think polynomials are closed under division? Explain why you think so, or provide a counterexample.
16. **Construct Arguments** Explain why the expression $9x^3 + \frac{1}{2}x^2 + 3x^{-1}$ is not a polynomial.
17. **Communicate Precisely** Explain the difference between the graphs of polynomial functions with a degree of 3 that have a positive leading coefficient and the graphs of those with a negative leading coefficient.

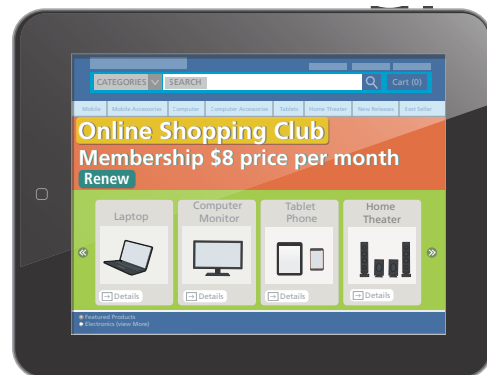
PRACTICE

Add or subtract the polynomials. SEE EXAMPLE 1

18. $(2x^3 + 3x^2 + 4) + (6x^3 - x^2 - 5x)$
19. $(5y^4 + 3y^3 - 6y^2 + 14) - (-y^4 + y^2 - 7y - 1)$
20. $(4p^2q^2 + 2p^2q - 7pq) - (9p^2q^2 + 5pq^2 - 11pq)$

Multiply the polynomials. SEE EXAMPLE 2

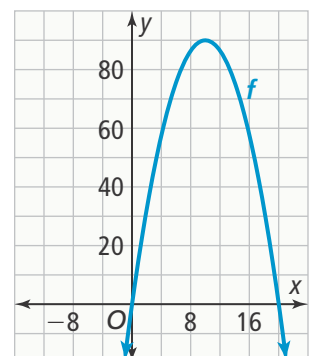
21. $-4xy(5x^2 - 9xy - y^2)$
22. $(3c - 4)(2c^2 - 5c + 7)$
23. $(z + 5)(z - 9)(1 - z)$
24. Is the set of monomials closed under addition? Explain why you think so, or provide a counterexample. SEE EXAMPLE 3
25. An online shopping club has 13,500 members when it charges \$8 per month for membership. For each \$1 monthly increase in membership fee, the club loses approximately 500 of its existing members.



Write and simplify a function R to represent the monthly revenue received by the club when x represents the price increase.

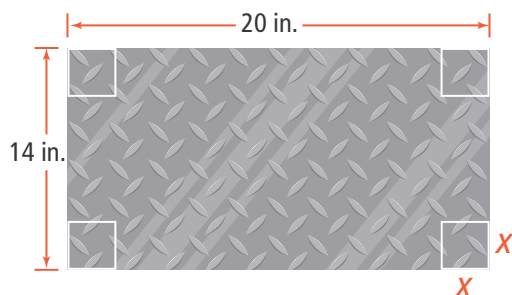
Hint Monthly revenue = # members • monthly fee SEE EXAMPLE 4

26. The graph shows a polynomial function f . Polynomial function $g = x^2(6 - x)$. Compare the maximum values and the end behavior of the functions f and g when $x > 0$. SEE EXAMPLE 5



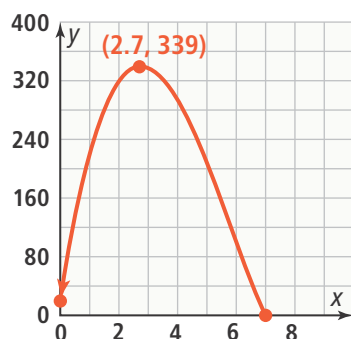
APPLY

Use this information for 27 and 28. A foundry manufactures aluminum trays from pieces of sheet metal as shown.



27. Model With Mathematics Let x represent the side length of each square.

- Write expressions for the length, width, and height of the metal tray.
- Write and simplify a polynomial function V to represent the volume of the tray.
- Using the graph of the function V , explain what the marked vertex represents.



28. Reason Suppose the foundry manufacturer has a new design where the squares cut from the corners have sides that are half the length of the squares in the previous design.

- Write expressions for the length, width, and height of this tray.
- Write and simplify the polynomial function $v(x)$, to represent the volume of the new tray.
- Write the function $D(x)$ that represents the difference, $V(x) - v(x)$.

29. Make Sense and Persevere Jacy has \$1,000 to invest in a fund that pays approximately 4.6% per year or in a savings account with an annual interest rate of 1.8%. Write a polynomial function $S(x)$ to represent the interest Jacy will earn in 1 year by investing x dollars in the fund and the remainder in the savings account.

ASSESSMENT PRACTICE

30. Are polynomials open or closed under each operation? Classify each operation as *open* or *closed*.

- addition
- subtraction
- multiplication
- division

31. SAT/ACT Which of the following functions is NOT a polynomial function?

- $2y^2 + 9y - 8$
- $-\frac{1}{2}x^3 + 8$
- $(x - 1)(5 - x)(x + 4)$
- $9z^4 + 2z + \frac{1}{z}$

32. Performance Task Consider the polynomial functions $P(x) = x^2 - 4$ and $R(x) = -x^2 - 2x$.

Part A Write and simplify a polynomial function $T(x)$ that is the product of P and R .

Part B Copy and complete the table of values for all three functions.

x	$P(x)$	$R(x)$	$T(x)$
-3			
-2			
-1			
0			
1			
2			
3			

Part C Graph the functions on the same coordinate grid.

Part D How do the zeros of T relate to the zeros of P and R ?

Part E Explain how you can identify the intervals in which T is positive by analyzing the R and P .