4-3 Additional Practice

Multiplying and Dividing Rational Expressions

Write an equivalent expression. Specify the domain.

1.
$$\frac{4x+6}{2x+3}$$

2;
$$x = -\frac{3}{2}$$

2.
$$\frac{3x^2-12}{x^2-x-6}$$

$$\frac{3x-6}{x-3}$$
; $x \neq -2$, 3

$$3. \ \frac{x^2 + 13x + 40}{x^2 - 2x - 35}$$

$$\frac{3x-6}{x-3}$$
; $x \neq -2$, 3 $\frac{x+8}{x-7}$; $x \neq -5$, 7

What is the simplified form of each rational expression? Specify the domain.

4.
$$\frac{2x^2 + 11x + 5}{3x^2 + 17x + 10}$$

$$\frac{2x+1}{3x+2}$$
; $x \neq -5$, $-\frac{2}{3}$

4.
$$\frac{2x^2 + 11x + 5}{3x^2 + 17x + 10}$$
 5. $\frac{6x^2 + 5xy - 6y^2}{3x^2 - 5xy + 2y^2}$ 6. $\frac{x^2 + 3x - 18}{x^2 - 36}$

$$\frac{2x+1}{3x+2}$$
; $x \neq -5$, $-\frac{2}{3}$ $\frac{2x+3y}{x-y}$; $x \neq -y$, $\frac{2}{3}y$ $\frac{x-3}{x-6}$; $x \neq \pm 6$

6.
$$\frac{x^2 + 3x - 18}{x^2 - 36}$$

$$\frac{x-3}{x-6}; x \neq \pm 6$$

Find the product and the domain.

7.
$$\frac{5a}{5a+5}$$
 · (10a + 10) 8. $\frac{x^2-5x}{x^2-3x}$ · $\frac{x+3}{x-5}$

8.
$$\frac{x^2 - 5x}{x^2 - 3x} \cdot \frac{x + 3}{x - 5}$$

10a;
$$a \neq -1$$
, 0

1:
$$x \neq 0$$
, 3, 5

9.
$$\frac{5y-20}{3y+15} \cdot \frac{7y+35}{10y+40}$$

$$\frac{7(y-4)}{6(y+5)}$$
; $x \neq -5, -4$

Find the quotient and the domain.

10.
$$\frac{7x^4}{24y^5} \div \frac{21x}{12y^4}$$

$$\frac{x^3}{6y}$$
; x , $y \neq 0$

11.
$$\frac{y^2 - 49}{(y - 7)^2} \div \frac{5y + 35}{y^2 - 7y}$$

$$\frac{y}{5}$$
; $y \neq 0, \pm 7$

11.
$$\frac{y^2 - 49}{(y - 7)^2} \div \frac{5y + 35}{y^2 - 7y}$$
 12. $\frac{y^2 - 5y + 4}{y^2 - 1} \div \frac{y^2 - 9}{y^2 + 5y + 4}$

$$\frac{y}{5}$$
; $y \neq 0, \pm 7$ $\frac{y^2 - 16}{y^2 - 9}$; $y \neq \pm 1, \pm 3, -4$

- **13.** A farmer must decide whether to build a cylindrical grain silo with radius r, or a rectangular grain silo with width r and length 2r. Both silos have the same height h. Which has the greater ratio of volume to surface area? Explain. The cylinder, because the ratio for the cylinder is $\frac{rh}{2r+2h}$, and the ratio for the rectangular prism is $\frac{rh}{2r+3h}$.
- **14.** How do you know what values to exclude from the domain? Answers may vary: Sample: Any value of the variable that makes the denominator equal to zero.