## Computer Number Systems Worksheet Created by Sam Craig for the West Lafayette High School ACSL Club of 2014-2015

A subscript after a number designates what base it is in. For example,  $20_{10}$  is 20 in base ten, but usually base ten is assumed and left out.  $10_{16}$  is 10 in base 16, or 16 in base ten. A **bit** is a **bin**ary (base 2) digit.

## Questions

- 1. Convert  $15F_{16}$  to octal.
- 2. Convert  $101000100011_2$  to hexadecimal.
- 3. Evaluate  $21A7_{16} 110_{16}$  in hexadecimal.
- 4. Evaluate  $10531_8 + 12414_8$  in octal.
- 5. Evaluate  $1101111_2 111011_2$  in binary.
- 6. Evaluate  $3C0_{16} + 340_8$  in hexadecimal.
- 7. In the Technology Department's new computer, each "word" of memory contains 16 bits representing 4 pieces of information. The first 5 bits represent Field A; the next 3 bits, Field B; the next 3 bits, Field C; and the last 5 bits, Field D. For example, the 16 bits comprising the "word" 9699<sub>16</sub> has fields with values of 19<sub>16</sub>, 4<sub>16</sub>, 6<sub>16</sub>, and A<sub>16</sub>. What is Field C in 6FAC<sub>16</sub>? (Express your answer as a base 16 number.)

## Answers

1.

$$15F_{16} = 0001 \ 0101 \ 1111_2$$
  
= 101 011 111<sub>2</sub>  
= 537<sub>8</sub>

2.

$$\begin{aligned} 101000100011_2 &= 1010\ 0010\ 0011_2 \\ &= \text{A23}_{16} \end{aligned}$$

3.

$$21A7 \\ -\frac{110}{2097}$$

4.

$$\begin{array}{r}
 1 \\
 10531 \\
 + 12414 \\
 \hline
 23145
 \end{array}$$

5.

$$\begin{matrix} \cancel{1} \cancel{1}^{1} 0 1 1 1 1 \\ - \underline{111011} \\ 110100 \end{matrix}$$

6.

$$3C0_{16} = 0011\ 1100\ 0000_2$$

$$340_8 = 011\ 100\ 000_2$$

$$+ \underbrace{\frac{1111000000}{1101000000}}_{100101000000}$$

7.

$$\begin{aligned} 6\mathrm{FAC}_{16} &= 0110\ 1111\ 1010\ 1100_2 \\ &= 01101\ 111\ 101\ 01100 \end{aligned}$$

SO

$$\begin{aligned} & \text{Field A} = D_{16} \\ & \textbf{Field B} = 7_{16} \\ & \text{Field C} = 5_{16} \\ & \text{Field D} = C_{16} \end{aligned}$$