```
In [2]: ▶
                1 import numpy as np
                2 import matplotlib.pyplot as plt
                  {\color{red} \textbf{import}} \ {\color{blue} \textbf{matplotlib.gridspec}} \ {\color{red} \textbf{as}} \ {\color{grid} \textbf{gridspec}}
                3
                4
                  import time
                6
                  class State:
                8
                       def __init__(self, positions, masses=1, timestep=0.001, nsteps=10000):
                9
                           Initialize the initial position of each atom\n \,
               10
                           Based on intial positions, calculate interatomic forces acting on the XYZ of each atom
               11
               12
               13
                           self.positions
                                                 = positions
               14
                           self.natm, self.ndim = positions.shape
                           self.update_interatomic_forces()
               15
               16
               17
                           self.masses
                                           = np.ones(shape=self.natm) * masses
               18
                           self.timestep = timestep
               19
                           self.velocities = np.zeros(shape=(self.natm, self.ndim))
               20
                           self.squared_cartesian_distances = np.zeros(shape=(self.natm, self.natm))
               21
               22
                           self.nsteps
                                           = nsteps
               23
                           self.trajectory = np.zeros(shape=(nsteps, self.natm, self.ndim))
               24
                           self.potential_energies = np.zeros(nsteps)
                           self.kinetic_energies = np.zeros(nsteps)
               25
               26
                           self.total_energies
                                                 = np.zeros(nsteps)
               27
               28
                       def step(self):
               29
                           F = m*dv/dt
               30
                           v(t + dt) = v + F*dt/m
               31
               32
                           x(t+dt) = x + v*dt
               33
               34
                           self.velocities += self.forces * self.timestep / 2 / self.masses
                           self.positions += self.velocities * self.timestep
               35
               36
                           self.update_interatomic_forces()
               37
                           self.velocities += self.forces * self.timestep / 2 / self.masses
               38
               39
                       def run(self):
               40
               41
                           The following is the only (one) Python loop used in this program.
               42
                           The heavy lifting is done by NumPy operations.
               43
                           for step in range(self.nsteps):
               44
               45
                               self.step()
               46
                               self.trajectory[step]
                                                              = self.positions
               47
                               self.potential_energies[step] = self.compute_potential_energy()
                               self.kinetic_energies[step] = self.compute_kinetic_energy()
               48
                                                              = self.potential_energies[step] + self.kinetic_energies[step]
               49
                               self.total_energies[step]
               50
               51
                       def update_interatomic_forces(self):
               52
               53
                           Given the xyz coordinates of n atoms,\n
               54
                           Calculate the distances between every pair of atoms.\n
               55
                           For each atom, calculate the forces that other atoms exert on it on the XYZ directions
               56
               57
                           #https://stackoverflow.com/questions/25965329/difference-between-every-pair-of-columns-of-two-numpy-
                                                             = self.positions.reshape(self.natm, 1, self.ndim)#from stack overfl
               58
                           each atom coordinates
               59
                           interatom_distances_per_dimension_per_atom = each_atom_coordinates - self.positions
               60
               61
                           self.squared cartesian distances = np.sum(interatom distances per dimension per atom**2,axis=2)
               62
                                                       = State.gradient_return(self.squared_cartesian_distances, 1, 1)
                           gradients_between_atoms
               63
                           interatom_gradients_per_atom = gradients_between_atoms.reshape(self.natm, self.natm, 1)
               64
               65
                           force_per_dimension_per_atom = interatom_gradients_per_atom * interatom_distances_per_dimension_per_
                           force_per_dimension_per_atom[np.isnan(force_per_dimension_per_atom)] = 0
               66
               67
                           self.forces = np.sum(force_per_dimension_per_atom,axis=0)
               68
               69
                       def compute_potential_energy(self):
               70
                           potentials_between_atoms
                                                        = State.potential_return(self.squared_cartesian_distances, 1, 1)
               71
                           return np.sum(np.triu(potentials_between_atoms,1))
               72
               73
                       def compute_kinetic_energy(self):
               74
                           return 0.5*np.sum(np.dot(self.masses, self.velocities**2))
               75
                       @staticmethod
               76
               77
                       def gradient_return(r_t, epsilon, sigma_t):
               78
                           z = sigma_t/r_t
               79
                           u = z*z*z
                           return 24 * epsilon * u * (1 - 2 * u) / r_t
               80
               81
               82
                       @staticmethod
               83
                       def potential_return(r_t,epsilon,sigma_t):
               84
                           z = sigma_t/r_t
                           u = z*z*z
               85
```

```
Below I execute the program and test the speed for 10000 steps. It is around 1.9 seconds
In [64]:
          Ыv
                1
                   positions = np.array([
                 2
                       [0.5391356726,0.1106588251,-0.4635601962], #atom1
                3
                       [-0.5185079933,0.4850176090,0.0537084789], #atom2
                4
                       [0.0793723207,-0.4956764341,0.5098517173], #atom3
                5
                   ])
                6
                   state = State(positions)
                7
                   start = time.time()
                   state.run()
                9 print(f"Duration: {time.time()-start} seconds")
             <ipython-input-2-340bf0d24bd7>:73: RuntimeWarning: divide by zero encountered in true_divide
               z = sigma t/r t
             <ipython-input-2-340bf0d24bd7>:60: RuntimeWarning: invalid value encountered in multiply
               force_per_dimension_per_atom = interatom_gradients_per_atom * interatom_distances_per_dimension_per_atom
             <ipython-input-2-340bf0d24bd7>:79: RuntimeWarning: divide by zero encountered in true_divide
               z = sigma_t/r_t
             Duration: 1.905918836593628 seconds
         Costa's program takes 0.185 seconds
In [69]: ▶
                1 costaPlot = Image.open('CostaEnergyPlot.png')
                   costaTime = Image.open('CostaTime.png')
                   fig,ax
                            = plt.subplots(figsize=(10,10))
                4 ax.imshow(costaTime)
   Out[69]: <matplotlib.image.AxesImage at 0x17d2e006790>
```

The plot for the energies is similar to the one produced by Costa's C program.

```
In [66]:
                1 fig = plt.figure()
         H
                2 fig.set_figheight(15)
                3
                  fig.set_figwidth(15)
                4 gs = gridspec.GridSpec(100, 100)
                5
                  ax1 = fig.add_subplot(gs[32:64,:40])
                6
                  ax2 = fig.add_subplot(gs[:,50:])
                  ax1.plot(range(10000), state.kinetic_energies, label='kinetic')
                  ax1.plot(range(10000), state.potential_energies, label='potential')
                9 ax1.plot(range(10000), state.total_energies, label='total')
               10 ax1.set(ylabel='Energy', xlabel='Timesteps')
               11 ax1.legend()
               12 ax1.set(title='Mine')
               13 ax2.imshow(costaPlot)
               14 ax2.set(title='Costa\'s')
               15 ax2.axis('off')
```

Out[66]: (-0.5, 579.5, 420.5, -0.5)



