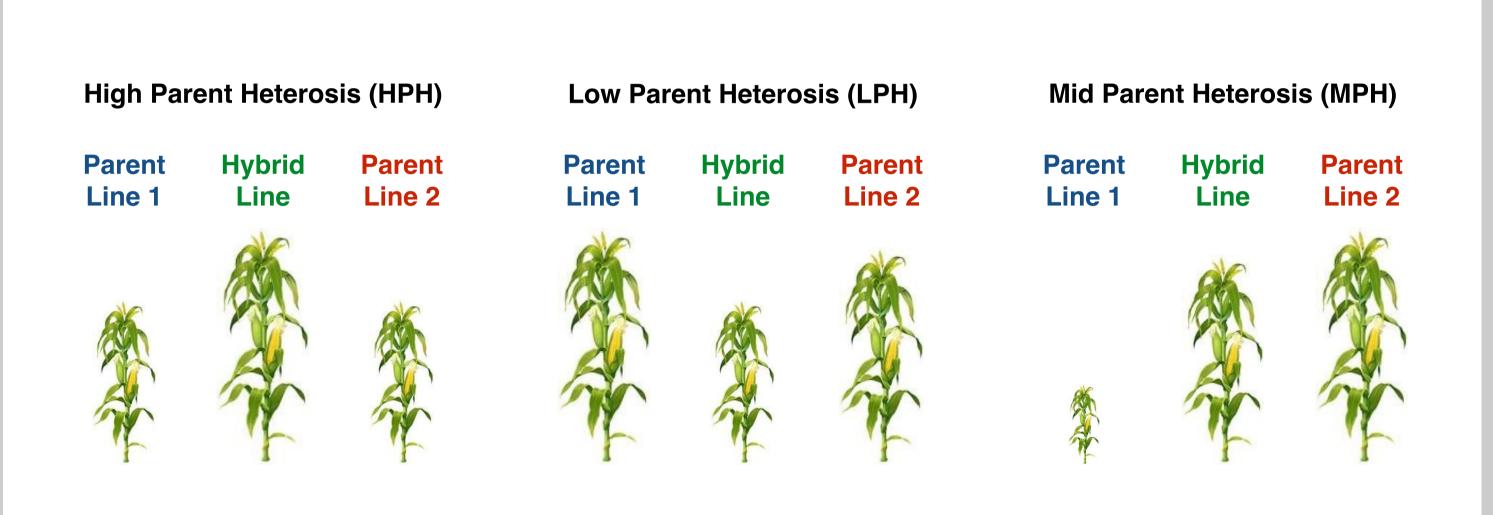
A Hierarchical Modeling Strategy for Identifying Gene Expression Heterosis using Parallel Computing with Graphics Processing Units (GPUs)

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Abstract

Heterosis, or hybrid vigor, occurs when the mean trait value of offspring is more extreme than that of either parent. Well before heterosis was first scientifically described by Darwin in 1876, people used it for practical purposes. Within the last century, heterosis has been used to improve many crop species for food, feed, and fuel industries. Despite intensive study and successful utilization of heterosis, the basic molecular genetic mechanisms responsible for heterosis remain unclear. To learn about these mechanisms, researchers have begun to measure the expression levels of thousands of genes in parental lines and their hybrid offspring. The expression level of each gene can be viewed as a trait alongside more traditional traits like plant height, grain yield, and drought tolerance. This approach presents challenges, such as the simultaneous analysis of tens of thousands of gene expression traits. The main focus of this presentation is a hierarchical modeling strategy for modeling count-based expression data from next-generation RNA sequencing. Also featured are the high performance computing methods that make this method tractable.

Phenotypic Heterosis



Gene Expression Heterosis in RNA Sequencing Data

		Parent Line 1			Hybrid Line		Parent Line 2	
	Gene 1	100	225	0	70	279	300	106
	Gene 2	0	1	1	50	501	2	1
HPH	Gene 3	3	4	2	700	900	0	0
LPH	Gene 4	893	400	760	5	5	1000	513
MPH	Gene 34897	10	13	6	819	761	902	912

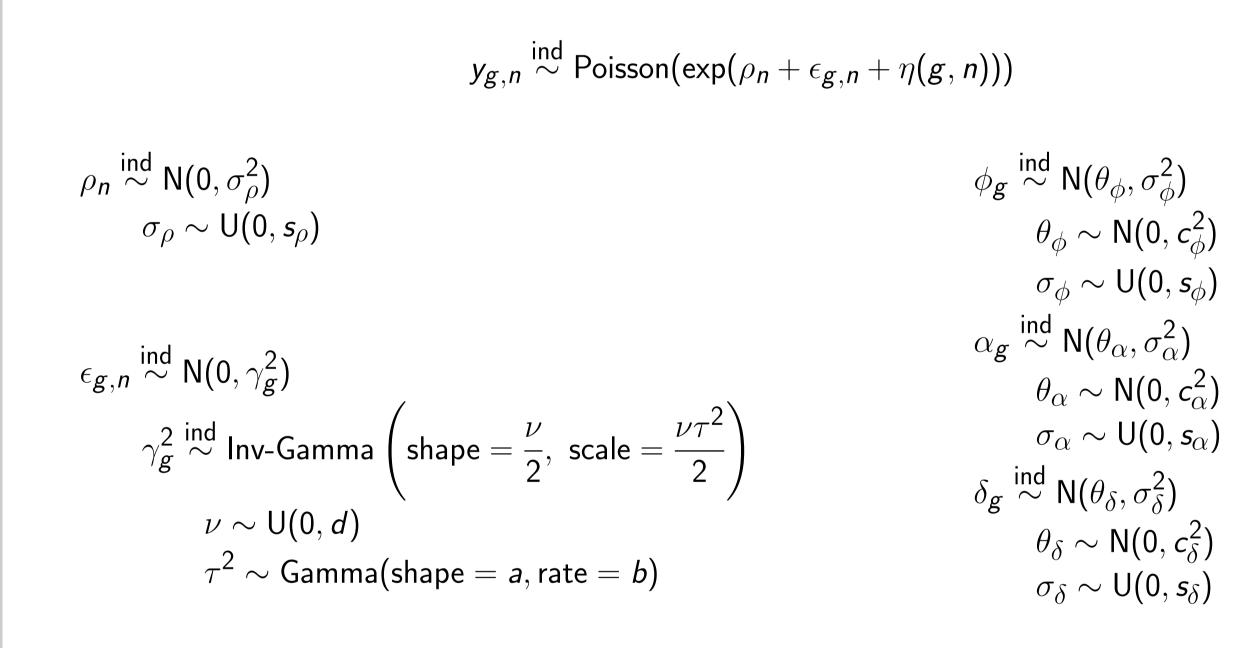
Notation

- ▶ $y_{g,n}$: observed count (gene g, library n).
- $\rightarrow \eta(g, n)$: expression effect.
- ▶ Parameterize $\eta(g, n)$:

$$\eta(\mathbf{g}, \mathbf{n}) = \begin{cases} \phi_{\mathbf{g}} - \alpha_{\mathbf{g}} & \text{if library } n \text{ came from parent 1} \\ \phi_{\mathbf{g}} + \delta_{\mathbf{g}} & \text{if library } n \text{ came from the hybrid} \\ \phi_{\mathbf{g}} + \alpha_{\mathbf{g}} & \text{if library } n \text{ came from parent 2} \end{cases}$$

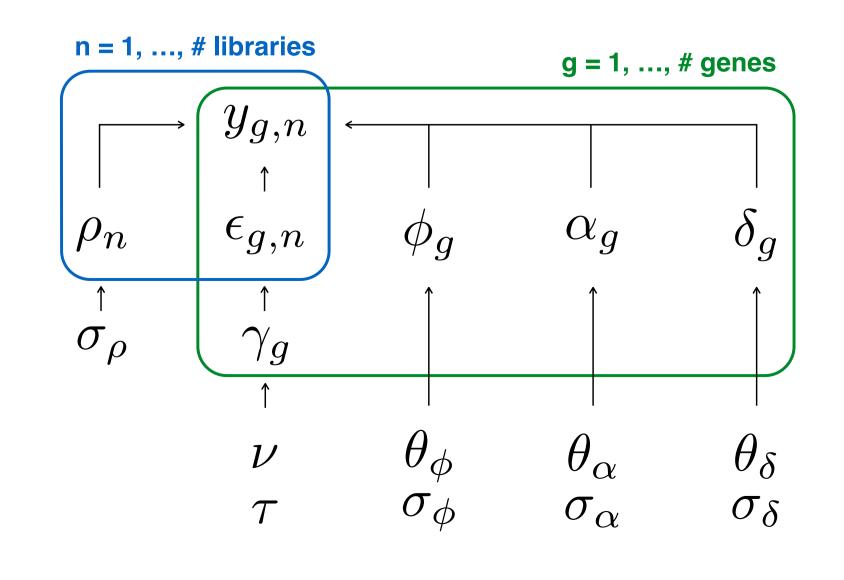
- $ightharpoonup \alpha_{g}$: half parental difference
- $lackbox{\ } \delta_{g}$: difference between hybrid and parental mean

The Hierarchical Model



- ► Greek letters are parameters,
- Roman letters are assumed constant

Directed Acyclic Graph: Opportunities for Parallelism



Fitting the Model: Metropolis-within-Gibbs

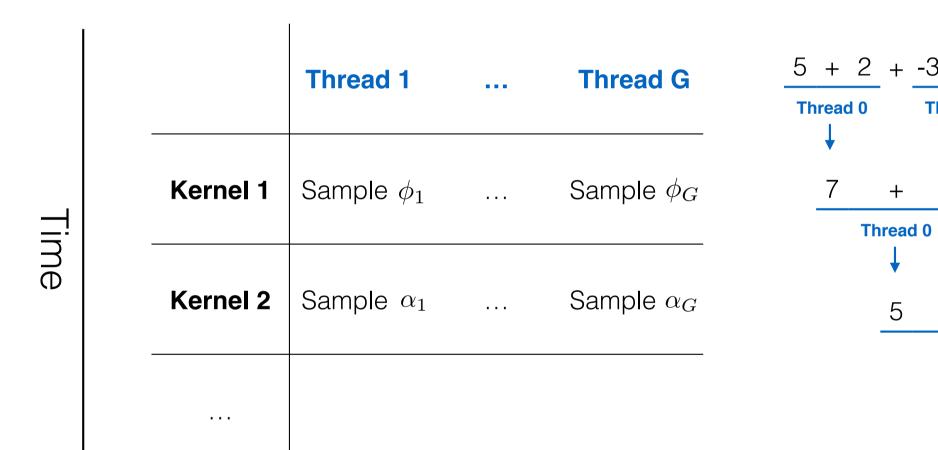
▶ Iteratively sample parameters from their full conditional posterior distributions.

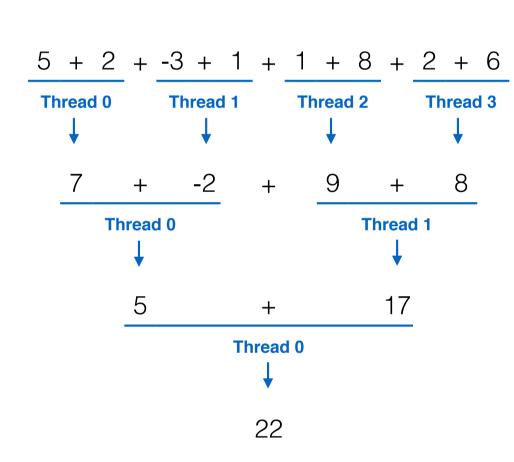
Parameters	Full Conditional Posterior Distributions	Parallel Computing		
$\epsilon_{\mathbf{g},\mathbf{n}},\phi_{\mathbf{g}},\alpha_{\mathbf{g}},\delta_{\mathbf{g}}$		Simultaneous Gibbs step		
ρ_{n}, ν	Approximate (independence proposal Metropolis-Hastings)	Parallel reductions		
$ heta_{\phi}$, $ heta_{lpha}$, $ heta_{\delta}$	Normal distributions	Parallel reductions		
•	Gamma distribution	Parallel reductions		
$\gamma_{m{arphi}}^2$	Inverse gamma distributions	Parallel reductions		
$\sigma_{ ho}^2$, σ_{ϕ}^2 , σ_{lpha}^2 , σ_{δ}^2	Inverse gamma distributions Inverse gamma distributions truncated above	Parallel reductions		

Parallel Computing: CUDA Graphics Processing Units

Simultaneous Gibbs Steps

Parallel Reductions





Inference

▶ Using samples $\phi_g^{(m)}$, $\alpha_g^{(m)}$, and $\delta_g^{(m)}$ ($m=1,\ldots,M$) from the appropriate posterior predictive distributions, we can calculate the posterior probabilities that gene g has...

Heterosis	HPH	LPH	MPH
Probability	$\frac{1}{M} \sum_{m=1}^{M} I\left(\delta_{g}^{(m)} > \left \alpha_{g}^{(m)} \right \right)$	$\frac{1}{M} \sum_{m=1}^{M} I\left(\delta_{g}^{(m)} < -\left \alpha_{g}^{(m)}\right \right)$	$\frac{1}{M}\sum_{m=1}^{M}I\left(\left \delta_{\mathbf{g}}^{(m)} ight >\epsilon ight)$

 \blacktriangleright $I(\cdot)$ is the indicator function, and $\epsilon > 0$ is an appropriate threshold for mid parent heterosis.

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