

# 1 The Simulation Study

We compare our method to existing ones in a simulation study. We generate thirty datasets using simulation parameters calculated from real data and analyze the pseudo-data using our method and the popular R language packages `edgeR`, `baySeq`, and `ShrinkBayes` [6] [1]. Using ROC (receiver operating characteristic) curves, we rank the methods' abilities to identify heterosis genes.

## 2 Simulated Data

We begin with a real heterosis RNA-seq dataset from a study by Paschold, Jia, Marcon, and others [5]. We select four libraries from each parent genotype and from the hybrid genotype, totaling twelve libraries for analysis. After library selection, we trim low-count features (genes): that is, we remove all the features with mean expression level below  $\exp(1)$  or with more than three zero counts, leaving 27888 features. Using the `calcNormFactors()`, `estimateGLMTagwiseDisp()`, and `glmFit()` functions in the `edgeR` package, we calculate normalization factors  $c_1, \dots, c_{12}$ , dispersion parameters  $\psi_f$  for feature  $f = 1, \dots, 27888$ , and main effects  $\mu_{f,t}$  for each  $f$  and treatment group  $t = 1$  (parent 1), 2 (parent 2), 3 (hybrid). These estimates serve as simulation parameters for all of our thirty pseudo-datasets.

To simulate a dataset with  $N$  libraries per treatment group ( $3N$  total libraries), the count for feature  $f$  and library  $i$  is drawn from a  $\text{NB}(\exp(c_{\lceil 4i/N \rceil} + \mu_{f,\lceil i/N \rceil}), \psi_f)$  distribution independently of the other counts. Note that feature  $f$  is a heterosis feature if  $\mu_{f,3} > \max(\mu_{f,1}, \mu_{f,2})$  or if  $\mu_{f,3} < \min(\mu_{f,1}, \mu_{f,2})$ . Lastly, we apply the same trimming procedure as before and select a random subset of 25000 of the remaining features. For that dataset, we maintain a "truth vector"  $H = (h_1, \dots, h_{25000})$ , where  $h_f = 1$  if feature  $f$  of the simulated dataset is a heterosis feature and  $h_f = 0$  otherwise.

We simulate 30 datasets total: 10 with  $N = 4$ , 10 with  $N = 8$ , and 10 with  $N = 16$ .

## 3 edgeR

`edgeR` is one of the most popular R packages in RNA-sequencing data analysis. Its newest implementation applies a negative binomial loglinear model to the data. It uses a Cox-Reid adjusted profile likelihood to estimate dispersion parameters, and in the case of `estimateGLMTagwiseDisp()`, shrinks the final dispersion estimates towards those of neighboring features on a common trend. It then estimates main effects using a Fisher scoring algorithm [7] [4].

Using the `calcNormFactors()`, `estimateGLMTagwiseDisp()`, and `glmFit()` functions in the `edgeR` package, we calculate normalization factor estimates  $\hat{c}_i$  for  $i = 1, \dots, 3N$ , dispersion parameter estimates  $\psi_f$  for feature  $f = 1, \dots, 25000$ , and main effects  $\hat{\mu}_{f,t}$  for each  $f$  and treatment group  $t = 1$  (parent 1), 2 (parent 2), 3 (hybrid). Using the `glmLRT()` function, we use likelihood ratio tests to perform the following hypothesis tests.

$$\begin{aligned} H_{0,f,1} : \mu_{f,3} - \mu_{f,1} = 0 \text{ vs } H_{a,f,1} : \mu_{f,3} - \mu_{f,1} \neq 0 \\ H_{0,f,2} : \mu_{f,3} - \mu_{f,2} = 0 \text{ vs } H_{a,f,2} : \mu_{f,3} - \mu_{f,2} \neq 0 \end{aligned}$$

We obtain p-values  $p_{f,1}$  and  $p_{f,2}$ , respectively, from each of the above tests. To translate the results into a test for heterosis for each feature, we compute the following p-values

$$p_{f,\text{edgeR}} = \begin{cases} p_{f,1}/2 & \hat{\mu}_{f,3} < \hat{\mu}_{f,1} \leq \hat{\mu}_{f,2} \text{ or } \hat{\mu}_{f,3} > \hat{\mu}_{f,1} \geq \hat{\mu}_{f,2} \\ p_{f,2}/2 & \hat{\mu}_{f,3} < \hat{\mu}_{f,2} \leq \hat{\mu}_{f,1} \text{ or } \hat{\mu}_{f,3} > \hat{\mu}_{f,2} \geq \hat{\mu}_{f,1} \\ 1 & \hat{\mu}_{f,1} \leq \hat{\mu}_{f,3} \leq \hat{\mu}_{f,2} \text{ or } \hat{\mu}_{f,2} \leq \hat{\mu}_{f,3} \leq \hat{\mu}_{f,1} \end{cases}$$

## 4 ShrinkBayes

**ShrinkBayes** is based on the **inla** package, which applies an integrated nested Laplace approximation to fit models in empirical Bayes fashion. **ShrinkBayes** applies a zero-inflated negative binomial model with normal distributions as priors [8]. In our usage, we make the following reparameterization

$$\begin{aligned}\phi_f &= \frac{\mu_{f,1} + \mu_{f,2}}{2} && \text{(parental mean)} \\ \alpha_f &= \frac{\mu_{f,2} - \mu_{f,1}}{2} && \text{(half parental difference)} \\ \delta_f &= \mu_{f,3} - \frac{\mu_{f,1} + \mu_{f,2}}{2} && \text{(hybrid effect)}\end{aligned}$$

We use the **ShrinkSeq()** and **FitAllShrink()** functions to fit the model and use **inla.make.lincombs()**, **BFUpdatePosterior()**, and **SummaryWrap()** to calculate posterior probabilities  $P(\delta_f + \alpha_f > 0 \mid \text{data})$ ,  $P(\delta_f - \alpha_f > 0 \mid \text{data})$ ,  $P(\delta_f - \alpha_f < 0 \mid \text{data})$ , and  $P(\delta_f + \alpha_f < 0 \mid \text{data})$ , along with estimates of  $\phi_f$ ,  $\alpha_f$ , and  $\delta_f$  for  $f = 1, \dots, 25000$ . Using this information, we calculate the posterior probability that each feature  $f$  is not a heterosis feature,

$$p_{f,\text{ShrinkBayes}} = \begin{cases} 1 & |\hat{\delta}_f| < |\hat{\alpha}_f|. \text{ Otherwise,} \\ P(\delta_f + \alpha_f > 0 \mid \text{data}) & \hat{\delta}_f > -\hat{\alpha}_f \\ P(\delta_f - \alpha_f > 0 \mid \text{data}) & \hat{\delta}_f > \hat{\alpha}_f \\ P(\delta_f - \alpha_f < 0 \mid \text{data}) & \hat{\delta}_f < \hat{\alpha}_f \\ P(\delta_f + \alpha_f < 0 \mid \text{data}) & \hat{\delta}_f < -\hat{\alpha}_f \end{cases}$$

## 5 baySeq

**baySeq** uses an empirical Bayes procedure to calculate the posterior probabilities that each feature follows each of the multiple models supplied by the user [2]. In the **baySeq** framework, a user-supplied model is an assignment of libraries to treatment groups. In the case of heterosis experiments, it is appropriate to consider the following five models.

$$\begin{aligned}M_1 &: \mu_{f,1} = \mu_{f,2} = \mu_{f,3} \\ M_2 &: \mu_{f,1} = \mu_{f,2} \\ M_3 &: \mu_{f,1} = \mu_{f,3} \\ M_4 &: \mu_{f,2} = \mu_{f,3} \\ M_5 &: \text{All } \mu_{f,t} \text{'s are distinct.}\end{aligned}$$

Now, let  $p_{f,\text{baySeq}}$  be the posterior probability that feature  $f$  of a given simulated dataset is not a heterosis feature. We can calculate

$$p_{f,\text{baySeq}} = \begin{cases} 1 & \hat{\mu}_{f,1} \leq \hat{\mu}_{f,3} \leq \hat{\mu}_{f,2} \text{ or } \hat{\mu}_{f,2} \leq \hat{\mu}_{f,3} \leq \hat{\mu}_{f,1} \\ P(M_1|\text{data}) + P(M_2|\text{data}) + P(M_4|\text{data}) & \text{otherwise} \end{cases}$$

We calculate estimates  $\hat{\mu}_{f,t}$  for  $f = 1, \dots, 25000$  and  $t = 1, 2, 3$  using **edgeR** as described previously.

## 6 ROC curves

We use receiver operating characteristic (ROC) curves to compare the effectiveness of our method versus **edgeR**, **ShrinkBayes**, and **baySeq**. A ROC curve is a tool for measuring the effectiveness of a binary

classifier. It is a graph of the true positive rate (TPR) of detection against the false positive rate (FPR), so a high area under the curve (AUC) is favorable. Landau and Liu [3] describe most of the details of calculation. However, note that in this study, posterior probabilities sometimes replace p-values, and we test for heterosis, not differential expression.

## References

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