```
Out[1]: ----
```

```
In [2]: import pandas as pd
    ships = set(df["ship_id"])
    roles = set(df["role"])

def _sort_tasks(task_list):
        return sorted(task_list, key=lambda t: pd.to_datetime(t.get("start_ts")))

tasks = {}
    for ship in ships:
        tasks[ship] = {}

for _, row in df.iterrows():
        ship = row["ship_id"]
        role = row["role"]
        task_list = row["tasks"]
        tasks[ship][role] = _sort_tasks(task_list)
```

```
In [3]: import plotly.graph_objects as go

# Build prepared data per (ship, role)
def prepare_tasks_for(ship_id, role_name):
    task_list = tasks.get(ship_id, {}).get(role_name, [])
    prepared = []
```

```
for t in task list:
        start = pd.to datetime(t.get("start ts"))
        end = pd.to datetime(t.get("end ts"))
        if pd.isna(start) or pd.isna(end) or end <= start:</pre>
            continue
        prepared.append({
            "start": start,
            "end": end,
            "task id": t.get("task id") or t.get("id") or None,
            "sailing id": t.get("sailing id")
       })
   if not prepared:
        return [], [], [], [], ship id, role name
   prepared.sort(key=lambda x: x["start"])
   # Greedy lane assignment to avoid overlaps
   lanes end = []
   lane idx for task = []
   for task in prepared:
       placed = False
       for i, lane end in enumerate(lanes end):
            if task["start"] >= lane end:
                lane idx for task.append(i)
                lanes end[i] = task["end"]
                placed = True
                break
        if not placed:
            lane idx for task.append(len(lanes end))
            lanes end.append(task["end"])
   t0 = prepared[0]["start"]
   start hours = [(t["start"] - t0).total seconds() / 3600 for t in prepare
   end hours = [(t["end"] - t0).total seconds() / 3600 for t in prepared]
   dur hours = [eh - sh for sh, eh in zip(start hours, end hours)]
   y vals = [i + 1 for i in lane idx for task]
    return prepared, start hours, dur hours, y vals, t0, ship id, role name
# Collect all combinations
ship role pairs = []
for s in sorted(tasks.keys()):
   for r in sorted(tasks[s].keys()):
        ship role pairs.append((s, r))
# Precompute traces for each combination
combo traces = []
combo meta = [] # metadata for each combo: (ship, role, n traces, title, h\epsilon
for (s, r) in ship role pairs:
   prepared, start hours, dur hours, y vals, t0, ship id, role name = prepa
   traces = []
   for idx, (sh, dh, y, t) in enumerate(zip(start hours, dur hours, y vals,
        label = t["task id"] if t["task id"] is not None else f"{idx + 1}"
        sailing label = t.get("sailing id") or "N/A"
       hovertext = (
            f"Ship: {ship id}<br>Role: {role name}"
```

```
f"<br>Task ID: {label}"
            f"<br/>Sailing ID: {sailing label}"
            f"<br>Start: {t['start']}"
            f"<br/>End: {t['end']}"
            f"<br/>br>Duration (h): {dh:.2f}"
        traces.append(go.Bar(
            x=[dh],
            y=[y]
            base=[sh],
            orientation="h",
            name=f"Task {label} | Sailing {sailing label}",
            hovertext=hovertext,
            hoverinfo="text",
            marker=dict(line=dict(width=0.5, color="#777")),
            showlegend=True
        ))
    \max lane = \max(y \text{ vals}) if y vals else 1
    title = f"Tasks for Ship {ship id} - Role {role name}"
    height = max(420, 140 + 40 * max_lane)
    combo traces.append(traces)
    combo meta.append((s, r, len(traces), title, height))
# Build a single figure with all traces, only first combo visible
fig = go.Figure()
visibility = []
for ci, traces in enumerate(combo traces):
    for tr in traces:
        fig.add trace(tr)
        visibility.append(ci == 0) # only first combo visible
# Update layout for initial combo with dark theme
, , , init title, init height = combo meta[0]
fig.update layout(
   template="plotly dark",
   title=init title,
    xaxis title="Time (hours since first task start)",
    yaxis title="Overlap lane",
    bargap=0.2,
    barmode="overlay",
    height=init height,
    legend title text="Tasks (ID | sailing id)",
    paper bgcolor="#111111",
    plot bgcolor="#111111",
    font=dict(color="#e6e6e6")
fig.update yaxes(dtick=1, gridcolor="#333333")
fig.update xaxes(gridcolor="#333333")
# Build dropdown for filtering (combined Ship & Role)
buttons = []
trace offset = 0
combo offsets = []
for (_, _, ntr, _, _) in combo_meta:
    combo offsets.append((trace offset, trace offset + ntr))
```

```
trace offset += ntr
for ci, (s, r, ntr, title, height) in enumerate(combo meta):
   vis = [False] * len(visibility)
    start_idx, end_idx = combo_offsets[ci]
    for i in range(start idx, end idx):
        vis[i] = True
    buttons.append(dict(
        label=f"{s} | {r}",
        method="update",
        args=[
            {"visible": vis},
            {"title": title, "height": height}
        ],
    ))
fig.update layout(
    updatemenus=[
        dict(
            type="dropdown",
            direction="down",
            buttons=buttons,
            x=0.0,
            y=1.15,
            xanchor="left",
            yanchor="top",
            showactive=True,
            bgcolor="#222222",
            bordercolor="#444444",
            font=dict(color="#f0f0f0", size=12)
        )
    ],
    margin=dict(t=110, r=20, l=60, b=40)
display(fig)
```

```
In [4]: # Report count of tasks by sailing_id, role, and start_hour using prepare_ta
def get_report(ship_id, role_name):
    target_ship = ship_id
    target_role = role_name

    prepared, start_hours, _, y_vals, t0, s_id, r_name = prepare_tasks_for(t

    report_rows = [
        {"sailing_id": task["sailing_id"], "role": r_name, "start_hour": tas
        "count": count}
        for task, count in zip(prepared, y_vals)
]

    report_df = pd.DataFrame(report_rows)
    return report_df
```

```
data = []
        for sh in ships:
            for rl in roles:
                data.append((sh, roles, max(get report(sh, rl)["count"])))
        pd.DataFrame(data, columns=["ship id", "role", "max count"])
Out[4]: —
In [5]: def get tasks by sailing(ship id, sailing id):
            return {role: [t for t in tks if t["sailing id"] == sailing id] for role
        selected tasks = get tasks by sailing('S1', 'S1-1')
In [6]: def get count(list of tasks):
            counts = {}
            for tup in list_of_tasks:
                counts.setdefault(tup, 0)
                counts[tup] += 1
            return counts
        selected 3days with duplicates = {role: [(x['start ts'], x['end ts']) for x
                                                  x['end ts'] < pd.to datetime('2025-
                                           selected tasks}
        selected 3days = {role: sorted(set(selected 3days with duplicates[role]), k\epsilon
                          selected 3days with duplicates}
        counts = {role: get count(selected 3days with duplicates[role]) for role in
        required personal = {role: [counts[role][x] for x in selected 3days[role]] f
In [7]: import numpy as np
        def gen columns(rl, max columns=None):
            tasks sel = selected 3days[rl]
            number of tasks = len(tasks sel)
            if number of tasks == 0:
                return np.zeros((0, 0), dtype=int)
            cols = []
            col = np.zeros(number of tasks, dtype=int)
            def dfs(i, next one allowed at, has one):
                if max columns is not None and len(cols) >= max columns:
```

```
return
    if i == number of tasks:
        if has one:
            cols.append(col.copy())
        return
    # place 0
    col[i] = 0
    dfs(i + 1, next one allowed at, has one)
    # place 1 if allowed (keep at least two zeros between ones)
    if i >= next one allowed at:
        col[i] = 1
        dfs(i + 1, i + 3, True)
        col[i] = 0 # reset
dfs(0, 0, False)
if not cols:
    return np.zeros((number of tasks, 0), dtype=int)
return np.stack(cols, axis=1)
```

```
In [8]: import gurobipy as gp
        class Solution:
            def init (self, role):
                self.role = role
                self.a matrix = gen columns(self.role)
                self.required personal = np.array(required personal[self.role])
                self.ordered_unique_tasks = selected_3days[self.role]
                self.model = qp.Model(self.role)
                self.variables = self.model.addMVar(self.a matrix.shape[1], vtype=gr
                self.solution = None
            def solve(self):
                self.model.setObjective(self.variables.sum(), gp.GRB.MINIMIZE)
                self.model.addConstr(self.a matrix @ self.variables == self.requirec
                self.model.optimize()
                self.model.write(f'{self.role}-sp.mps')
                self.model.write(f'{self.role}-sp.lp')
                return self
            def get solution(self):
                selected patterns = []
                for var in self.model.getVars():
                    var name = var.varName
                    var value = var.x
                    if var value > 0.5:
                        selected patterns.append(int(var name.split("[")[1].split("]
                        print(selected patterns)
                self.solution = {"patterns": self.a matrix[:, selected patterns]}
                schedules = {
                    f"schedule {selected patterns.index(i)}": [self.ordered unique t
                    for i in selected patterns
                self.solution["schedules"] = schedules
                return self
```

```
def run(self):
                self.solve()
                self.get solution()
                return self
In [9]: solutions = {role: Solution(role).run().solution for role in roles}
      Restricted license - for non-production use only - expires 2026-11-23
      Gurobi Optimizer version 12.0.3 build v12.0.3rc0 (linux64 - "Ubuntu 24.04.3
      LTS")
      CPU model: 12th Gen Intel(R) Core(TM) i5-12500H, instruction set [SSE2|AVX|A
      Thread count: 16 physical cores, 16 logical processors, using up to 16 threa
       Optimize a model with 11 rows, 87 columns and 208 nonzeros
      Model fingerprint: 0x4d9dd83c
      Variable types: 0 continuous, 87 integer (87 binary)
      Coefficient statistics:
                         [1e+00, 1e+00]
         Matrix range
         Objective range [1e+00, 1e+00]
         Bounds range
                         [1e+00, 1e+00]
         RHS range
                         [1e+00, 1e+00]
       Found heuristic solution: objective 11.0000000
       Presolve time: 0.00s
      Presolved: 11 rows, 87 columns, 208 nonzeros
      Variable types: 0 continuous, 87 integer (87 binary)
      Root relaxation: objective 3.000000e+00, 23 iterations, 0.00 seconds (0.00 w
       ork units)
                        Current Node
                                              Objective Bounds
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       Expl Unexpl | Obj Depth IntInf | Incumbent
                                                       BestBd
                                                                Gap | It/Node Time
                                 0
                                         3.0000000
                                                      3.00000 0.00%
       Explored 1 nodes (23 simplex iterations) in 0.03 seconds (0.00 work units)
      Thread count was 16 (of 16 available processors)
       Solution count 2: 3 11
       Optimal solution found (tolerance 1.00e-04)
       Best objective 3.000000000000e+00, best bound 3.0000000000e+00, gap 0.000
      0%
       [39]
       [39, 58]
       [39, 58, 86]
       Gurobi Optimizer version 12.0.3 build v12.0.3rc0 (linux64 - "Ubuntu 24.04.3
      LTS")
       CPU model: 12th Gen Intel(R) Core(TM) i5-12500H, instruction set [SSE2|AVX|A
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      Thread count: 16 physical cores, 16 logical processors, using up to 16 threa
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      Model fingerprint: 0x4d9dd83c
      Variable types: 0 continuous, 87 integer (87 binary)
      Coefficient statistics:
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         Objective range [1e+00, 1e+00]
         Bounds range [1e+00, 1e+00]
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       Found heuristic solution: objective 11.0000000
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```

```
Presolved: 11 rows, 87 columns, 208 nonzeros
Variable types: 0 continuous, 87 integer (87 binary)
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Explored 1 nodes (23 simplex iterations) in 0.02 seconds (0.00 work units)
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```

```
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  Matrix range
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 Expl Unexpl | Obj Depth IntInf | Incumbent
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                         0
                                               3.00000 0.00%
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0%
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CPU model: 12th Gen Intel(R) Core(TM) i5-12500H, instruction set [SSE2|AVX|A
VX21
Thread count: 16 physical cores, 16 logical processors, using up to 16 threa
Optimize a model with 11 rows, 87 columns and 208 nonzeros
Model fingerprint: 0x4d9dd83c
Variable types: 0 continuous, 87 integer (87 binary)
Coefficient statistics:
  Matrix range [1e+00, 1e+00]
  Objective range [1e+00, 1e+00]
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Root relaxation: objective 3.000000e+00, 23 iterations, 0.00 seconds (0.00 w
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0%
[39]
[39, 58]
[39, 58, 86]
```

```
In [10]: import pandas as pd
         import plotly.express as px
         # --- Flatten your solutions dict into a DataFrame ---
         records = []
         for role, data in solutions.items():
             for schedule name, intervals in data["schedules"].items():
                 for start, end in intervals:
                      records.append({
                         "role": role,
                         "schedule": schedule name,
                         "start": start,
                         "end": end
                     })
         df = pd.DataFrame(records)
         df = df.sort values(by=["role", "schedule", "start"])
         # --- Convert datetimes to hours since first start (relative time axis) ---
         t0 = df["start"].min()
         df["start hours"] = (df["start"] - t0).dt.total seconds() / 3600
         df["duration hours"] = (df["end"] - df["start"]).dt.total seconds() / 3600
         # --- Generate one plot per role ---
         figs = \{\}
         for role in df["role"].unique():
             role_df = df[df["role"] == role]
             fig = px.bar(
                 role df,
                 x="duration_hours",
                 y="schedule",
                 base="start hours", # start of bar
                 color="schedule",
                 orientation="h",
                 title=f"Schedules for Role: {role} (Hours since first start)"
             fig.update layout(
                 xaxis title="Time (hours)",
                 yaxis title="Schedules",
                 bargap=0.3,
                 height=500
             fig.update_yaxes(autorange="reversed") # keep first schedule on top
             figs[role] = fig
         # --- Show one of them (for example, first role) ---
         for rl in list(figs.keys()):
             display(figs[rl])
```