

BIOL 350: Bioinformatics

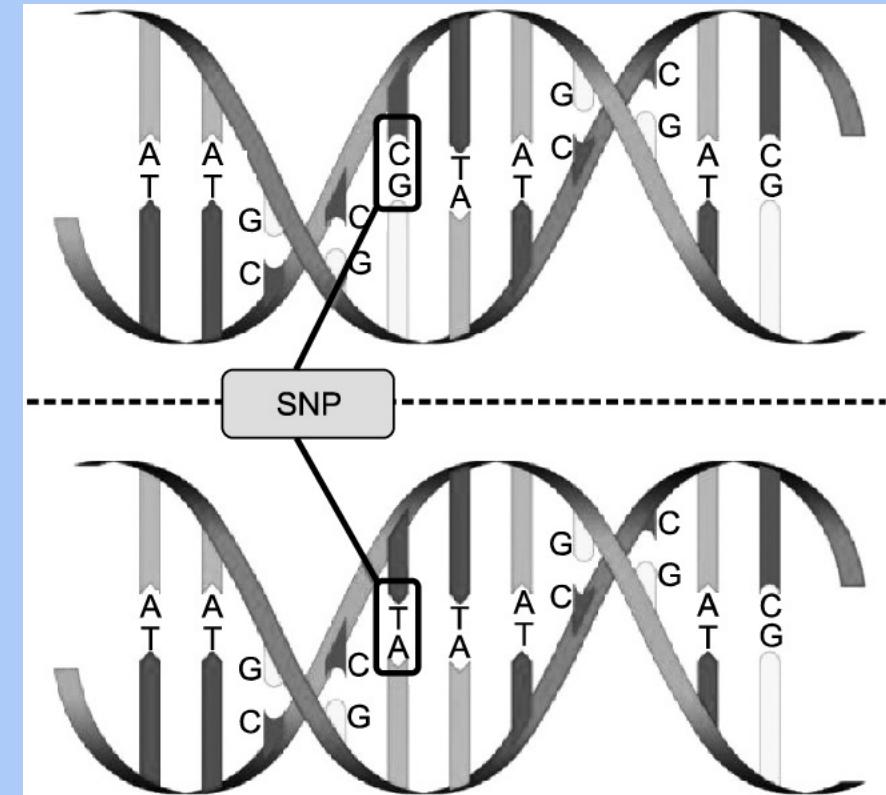
Introduction to genetic association studies

What is a SNP?

Polymorphisms and their role in genetics

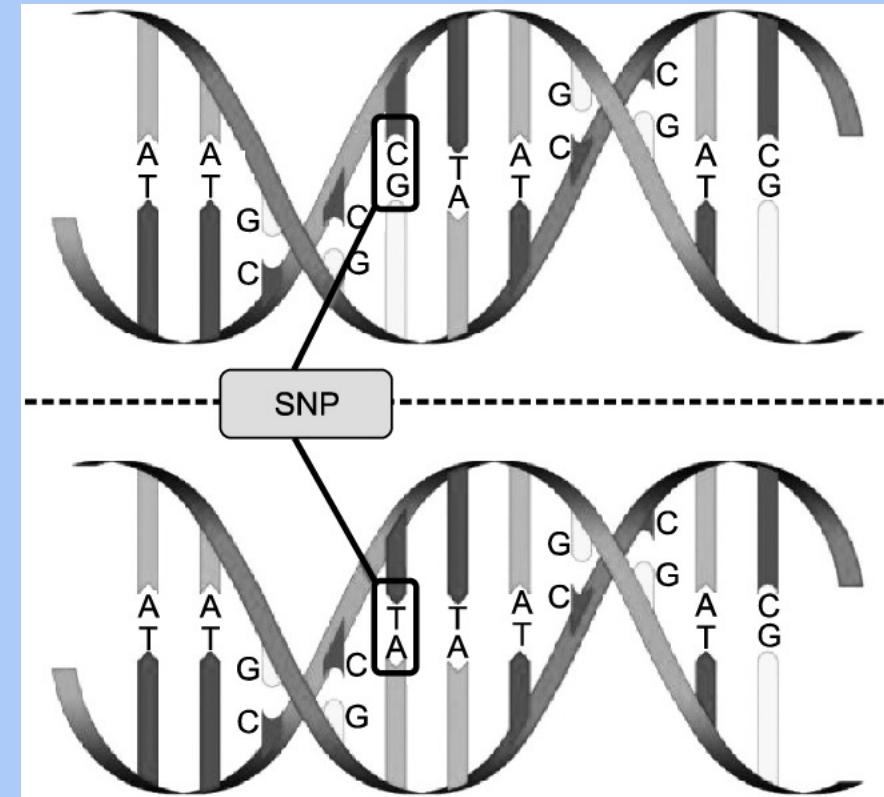
Single-nucleotide polymorphisms

- Polymorphism is the tendency of DNA to admit of different nucleotide pairs at a single locus



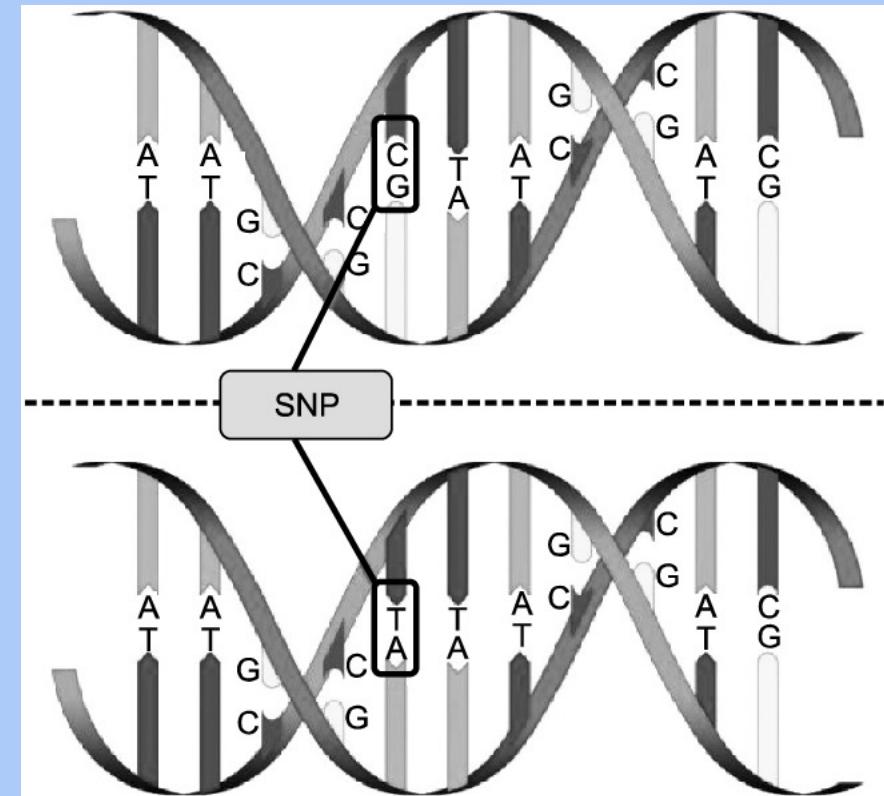
Single-nucleotide polymorphisms

- Of 3.2 billion bases, any individual is polymorphic at 4-5 million sites



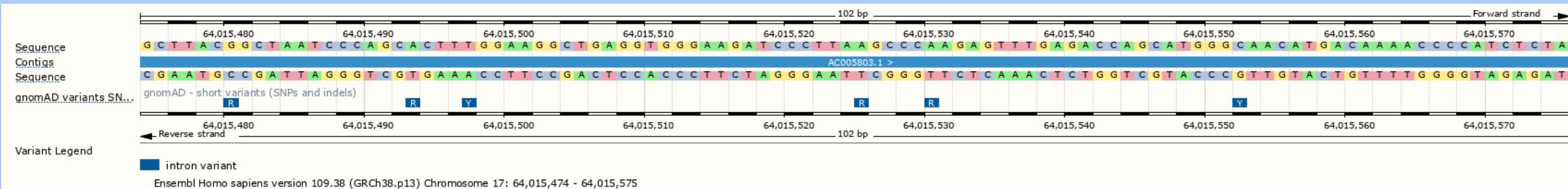
Single-nucleotide polymorphisms

- The more common allele is called the **major allele**
- The less common allele is called the **minor allele**



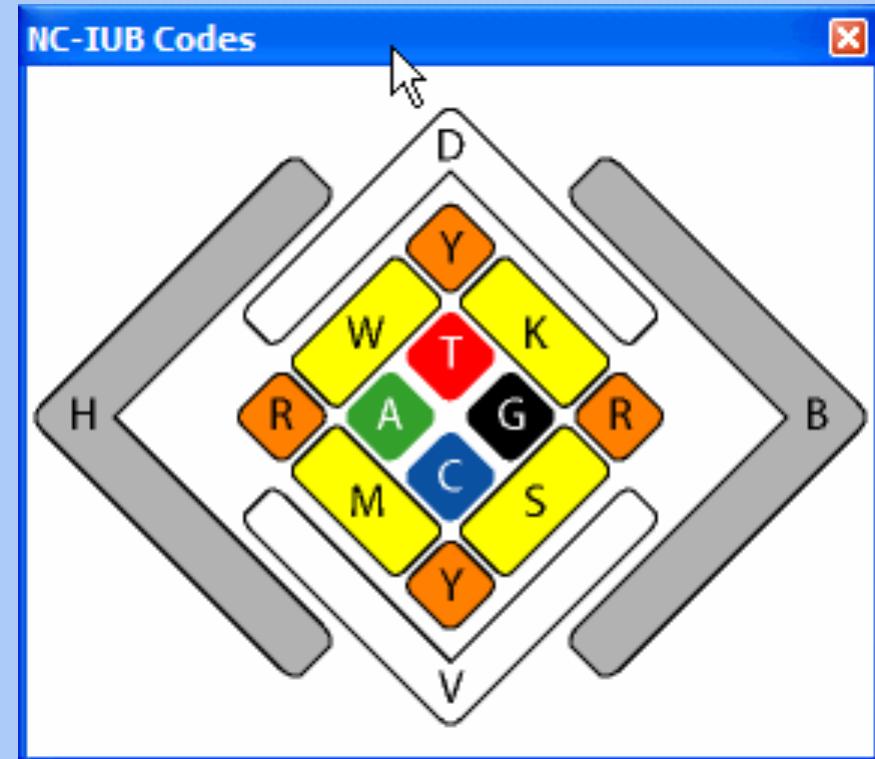
IUPAC-IUB SNP codes

- More than just A, T, G, and C?



IUPAC-IUB SNP codes

- Each polymorphism is coded by its possible alleles



[https://www.gendx.com/SBTengine/
Help_220/hs310.htm](https://www.gendx.com/SBTengine/Help_220/hs310.htm)

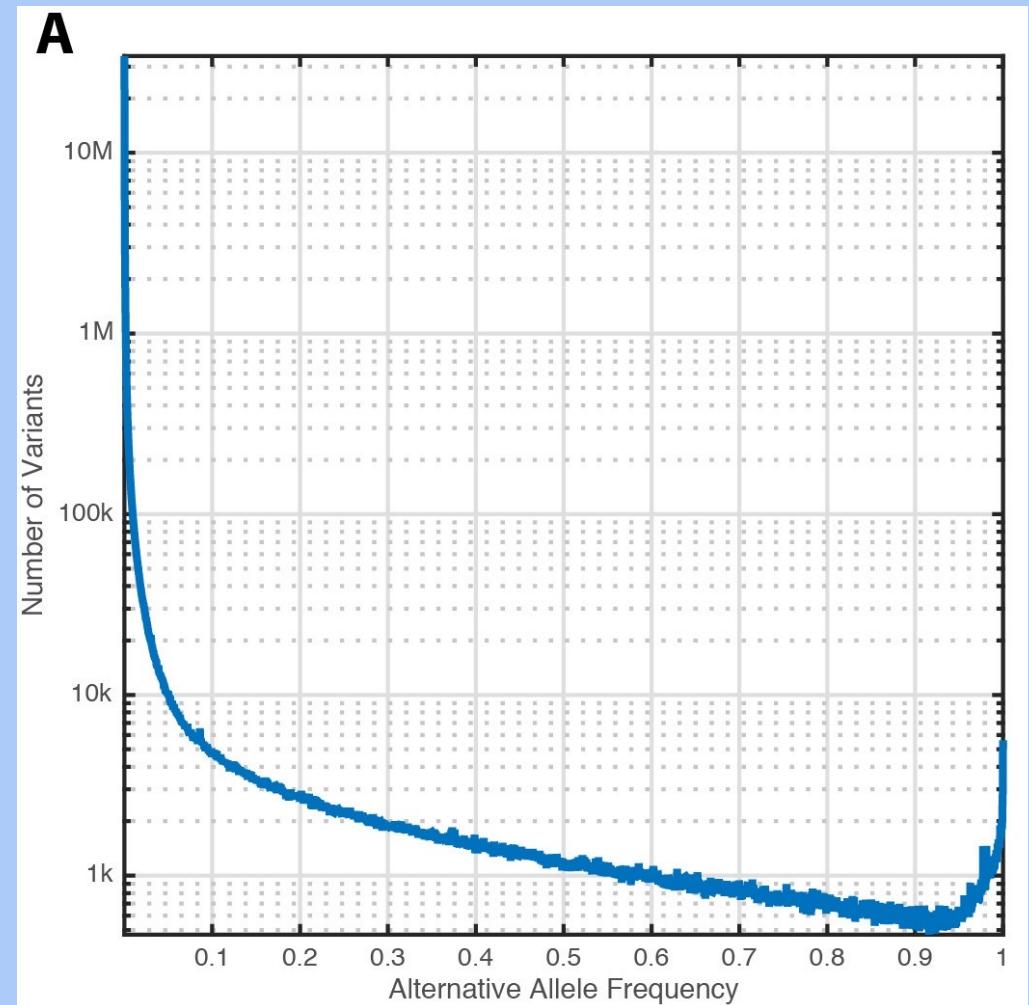
IUPAC-IUB SNP codes

- Each polymorphism is coded by its possible alleles

Code	Meaning	Explanation
R	A or G	PuRrine
Y	C or T	PYrimidine
S	G or C	Strong H-bonding
W	A or T	Weak H-bonging
K	G or T	Keto bases
M	A or C	aMino bases
B	C or G or T	not A
D	A or G or T	not C
H	A or C or T	not G
V	A or C or G	not T
N	A or C or G or T	ANy

Many rare SNPs

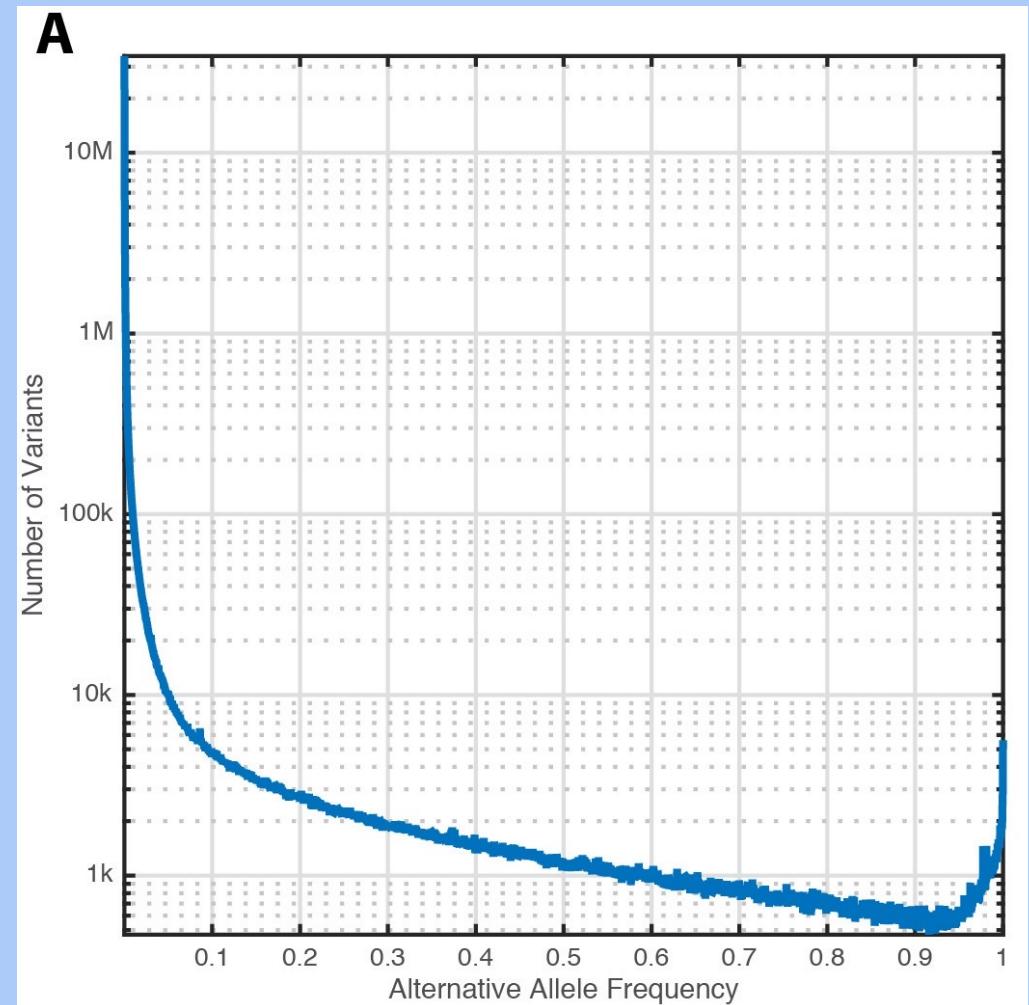
- Common SNPs have minor allele frequency (MAF) >5%



<https://www.nature.com/articles/nature15393>

Many rare SNPs

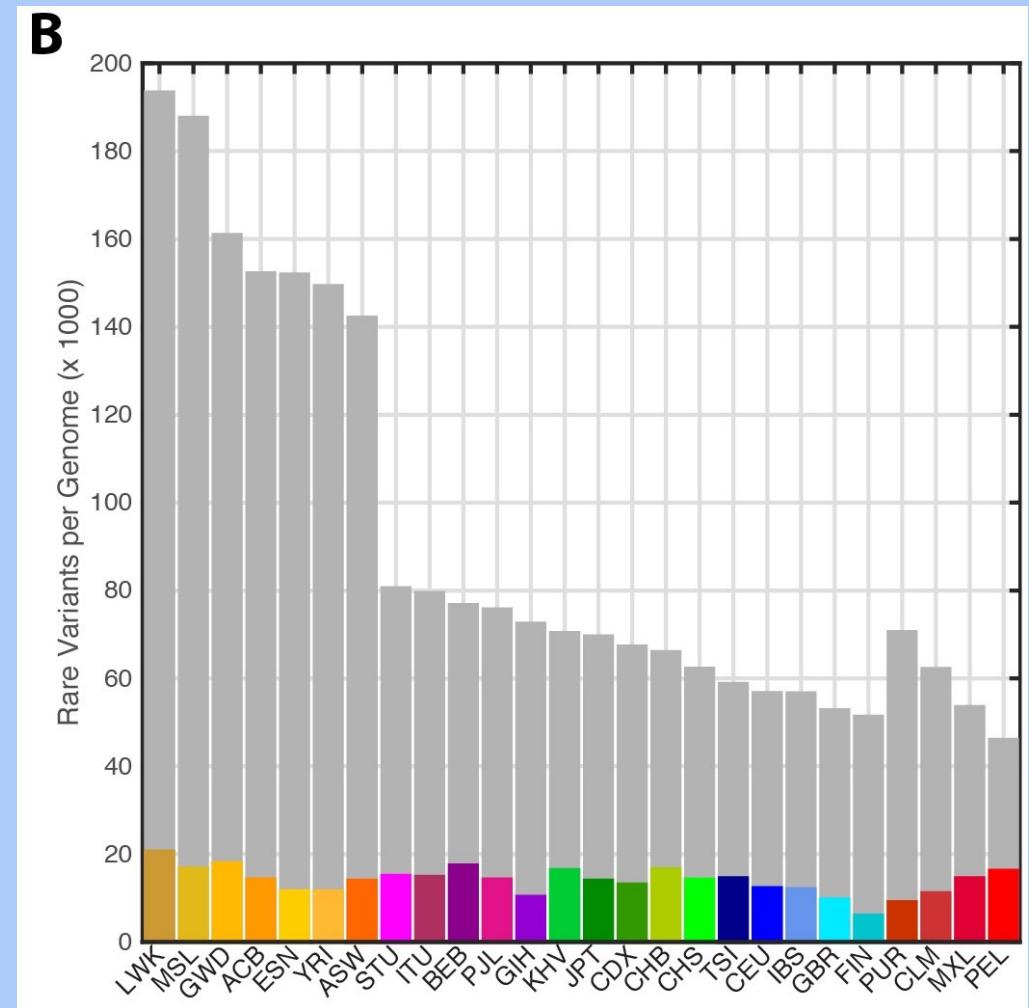
- Most SNPs of the >600 million known SNPs are very rare (frequency < 0.5%)



<https://www.nature.com/articles/nature15393>

Many rare SNPs

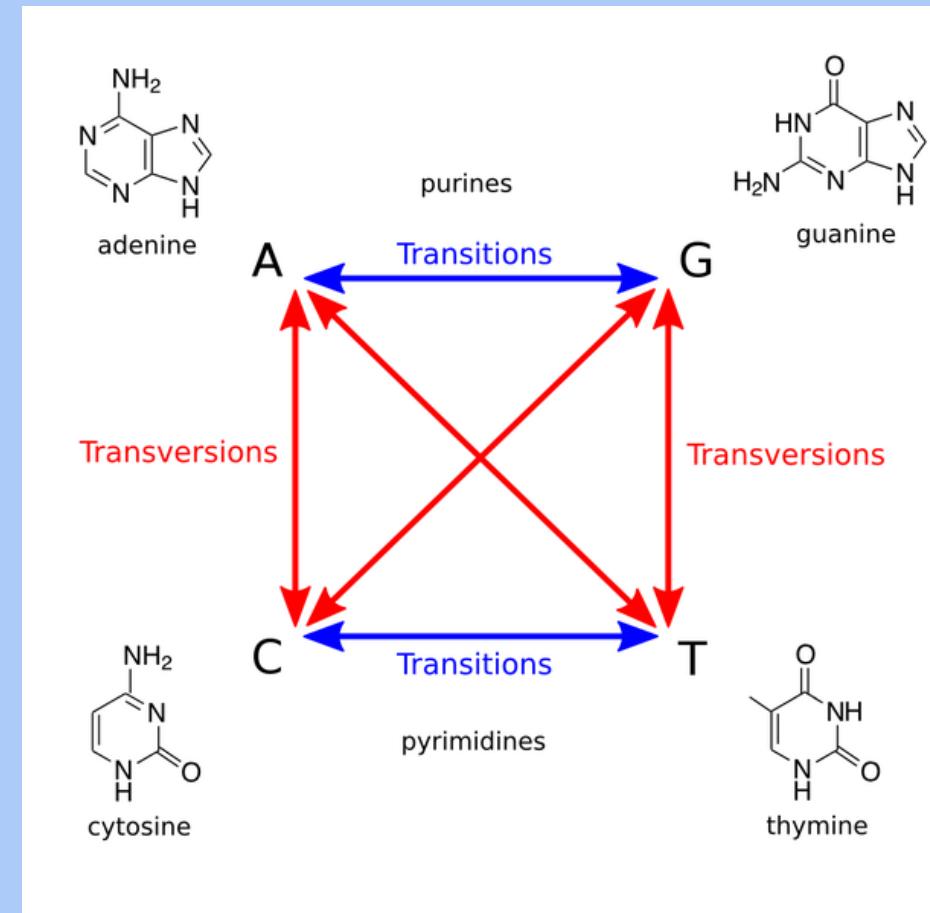
- But only <5% of an individual's genome consists of rare SNPs



<https://www.nature.com/articles/nature15393>

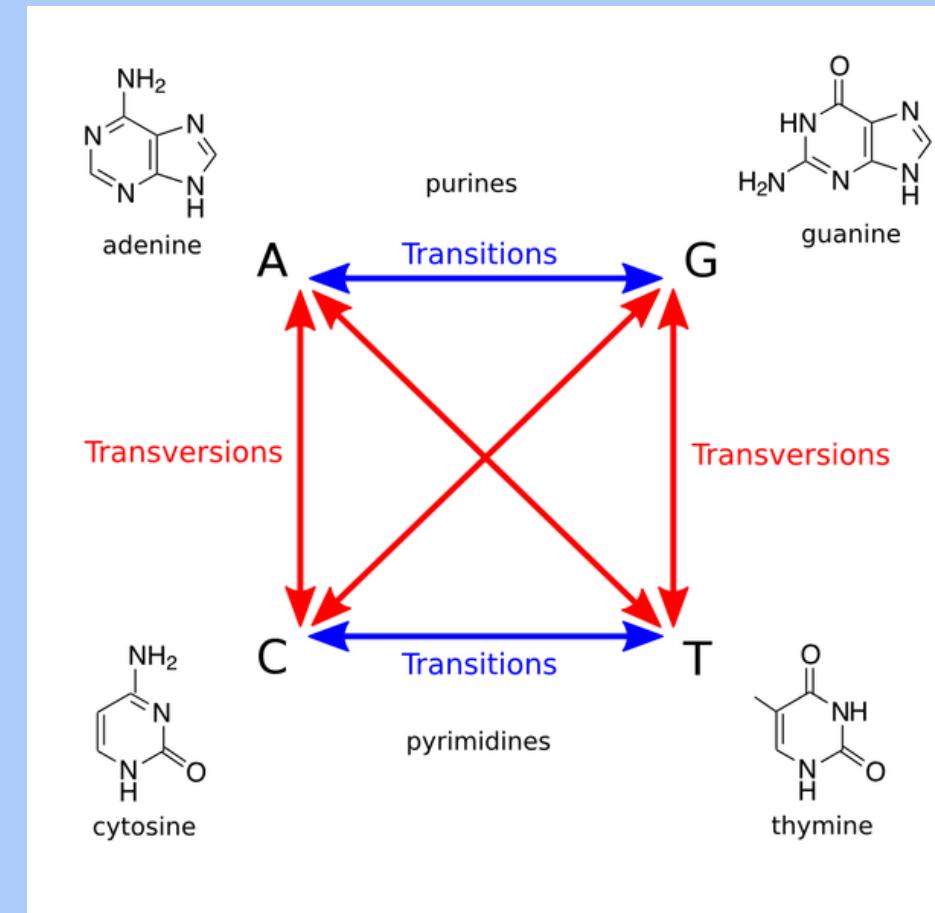
Transitions and transversions

- **Transitions** occur between nucleotides of the same type (purines or pyrimidines)
- **Transversions** occur between nucleotides of opposite type (between purines and pyrimidine)



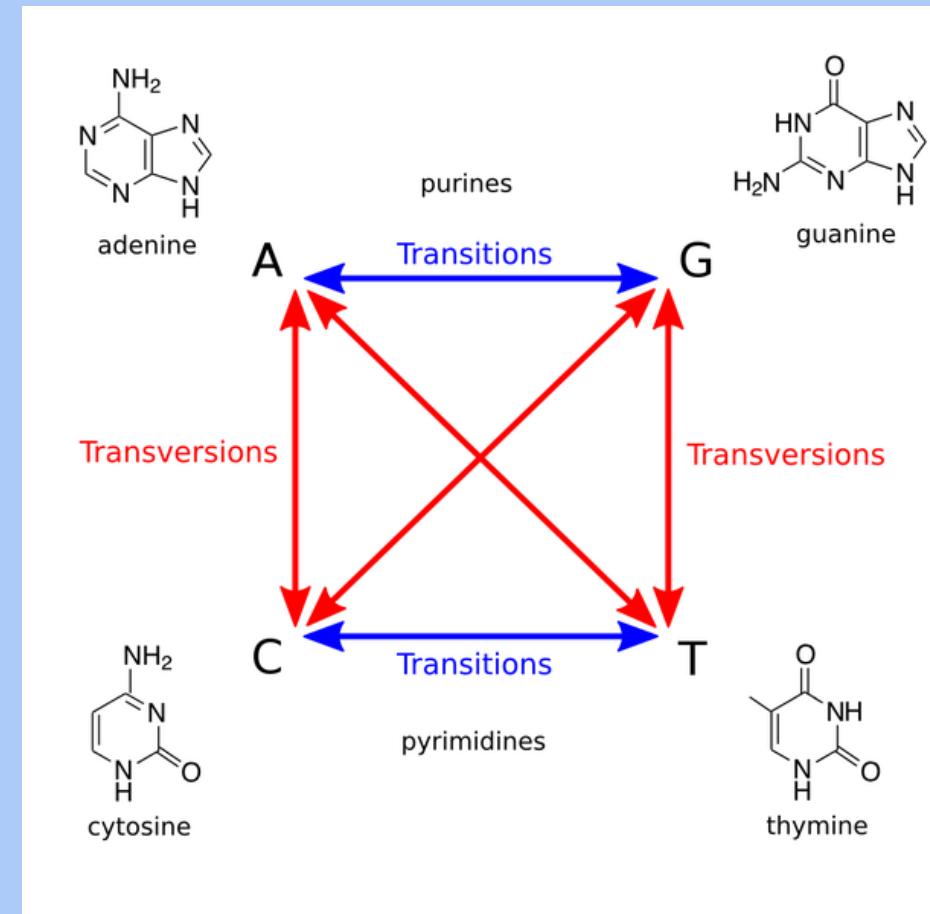
How many polymorphisms are there?

- If there are n nucleotide pairs, there are n symmetric conversions:
 - A/T \rightarrow T/A transversion
 - C/G \rightarrow G/C transversion



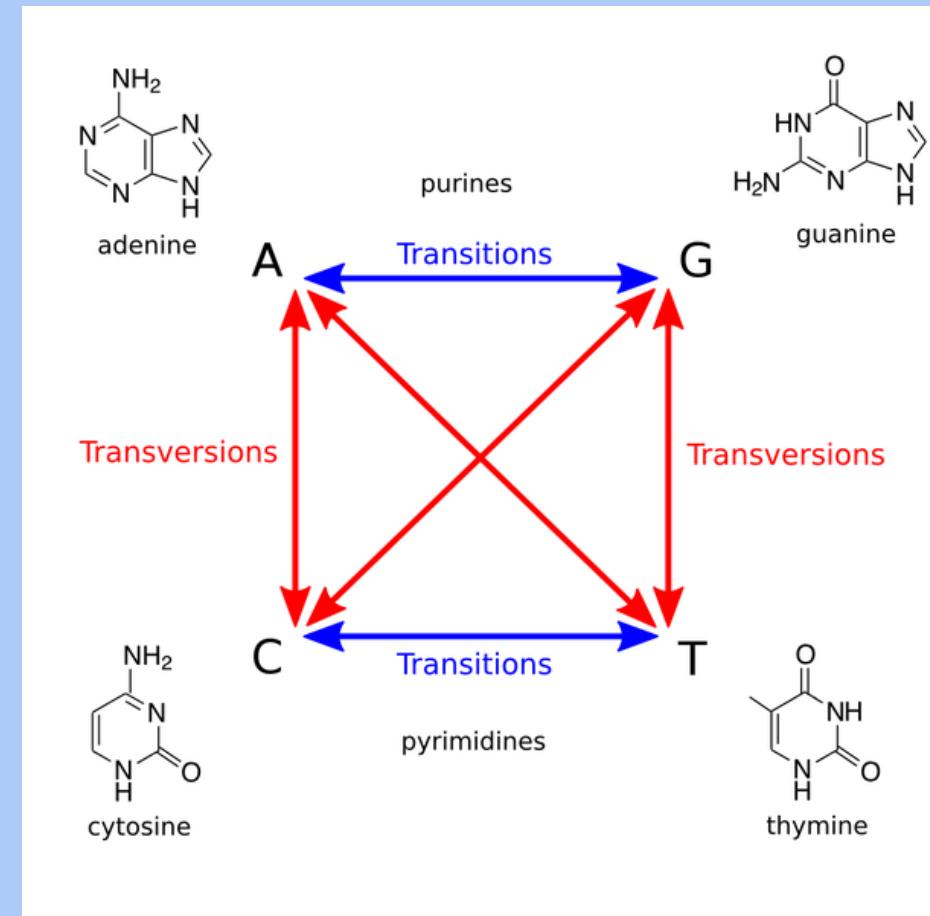
How many polymorphisms are there?

- If there are n nucleotide pairs, there are $n(n - 1)$ asymmetric conversions:
 - A/T → C/G transversion
 - A/T → G/C transition



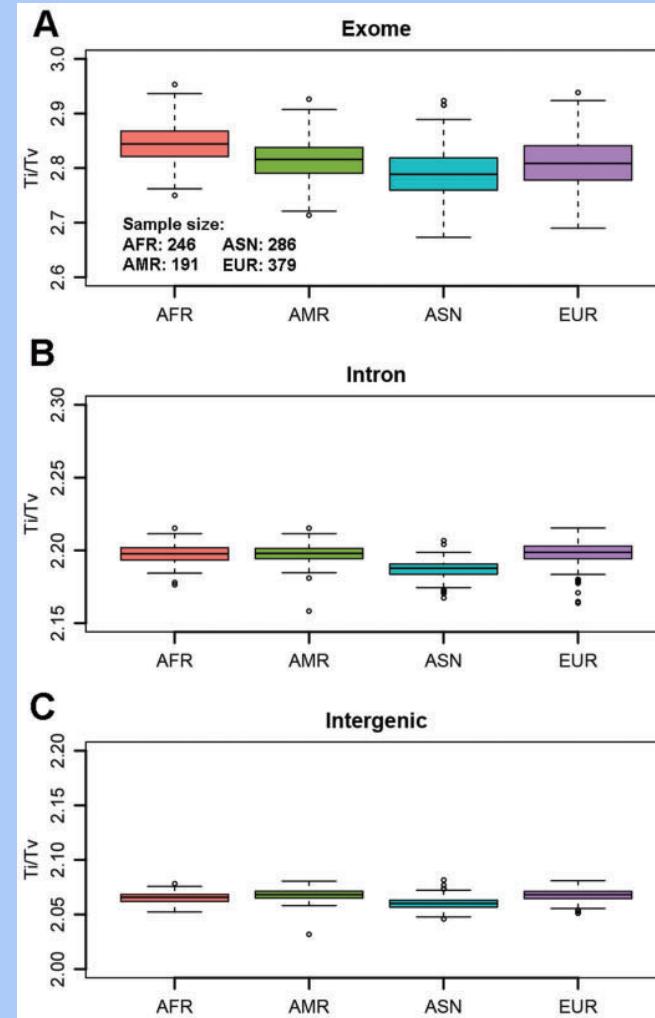
How many polymorphisms are there?

- A total of $n + n(n - 1) = n^2$ polymorphisms



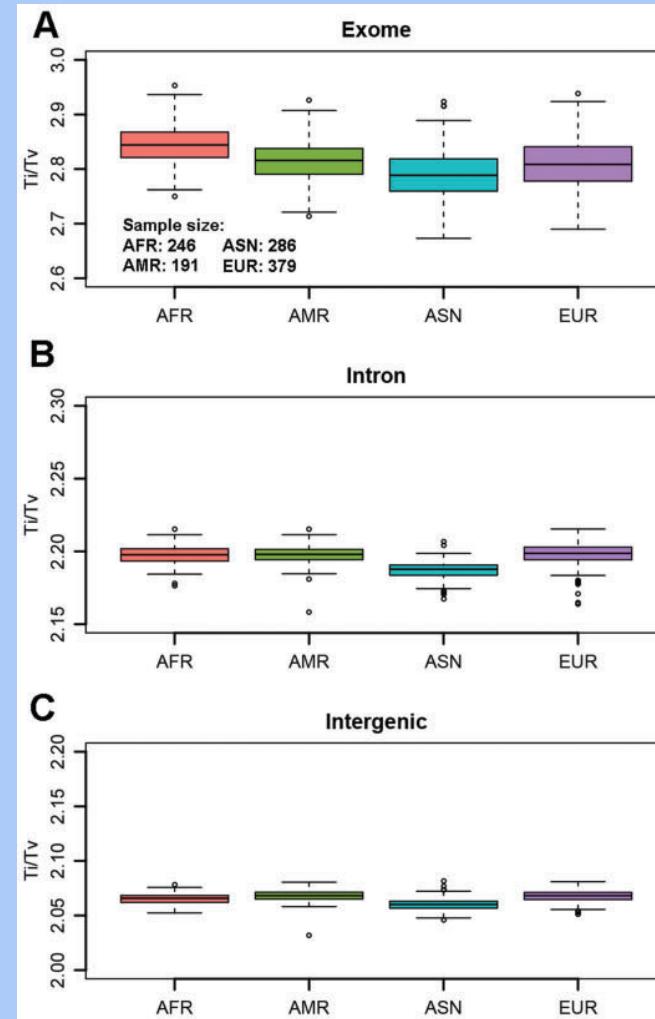
Transition-transversion ratio

- Even though there are three times as many transversions possible as transitions, in humans the ratio of transitions to transversions is approximately 2, genome-wide



Transition-transversion ratio

- In coding regions, the Ti:Tv ratio is as high as 3



Generation of sequencing data

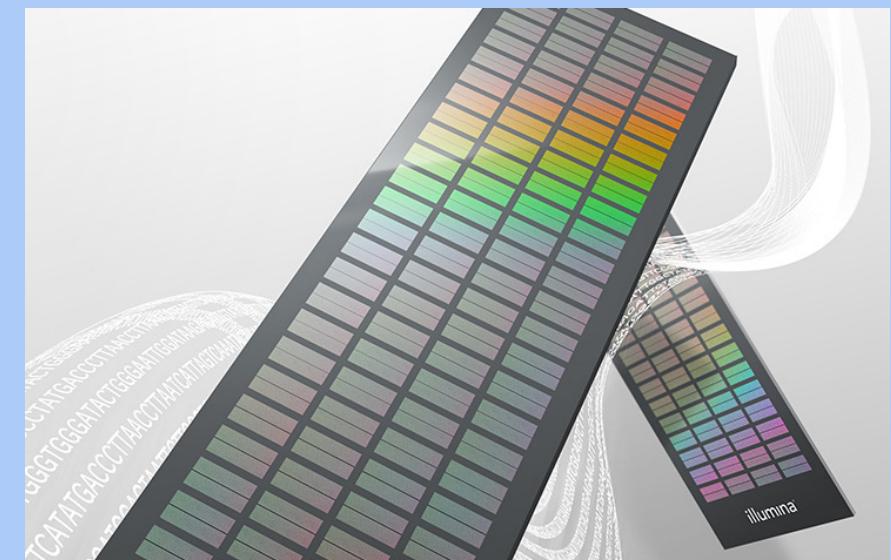
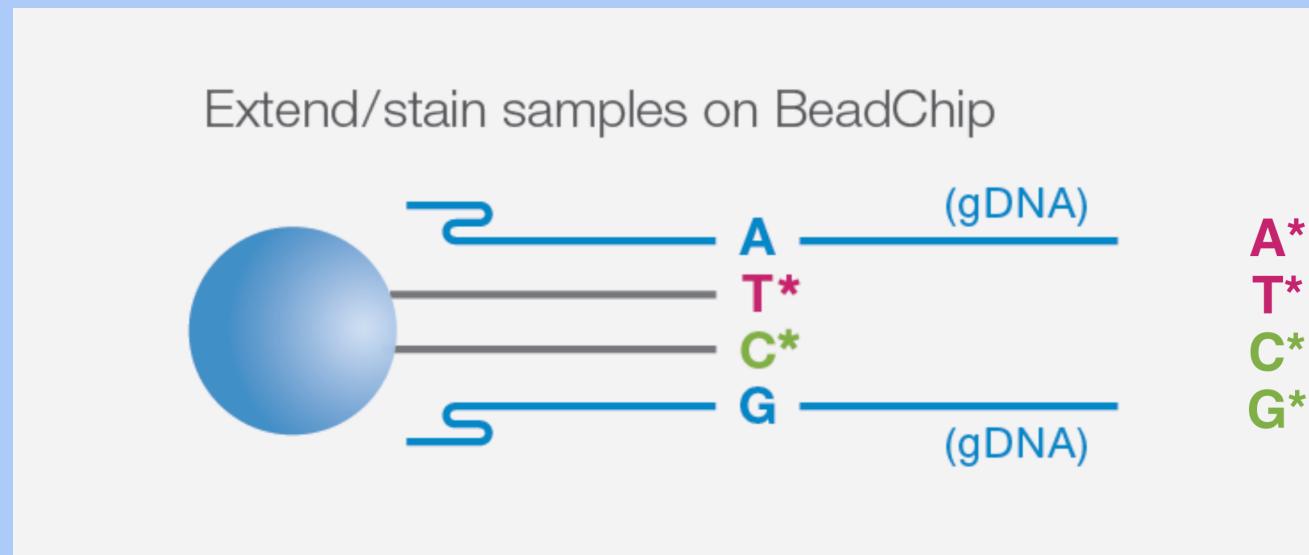
Sequencing technologies and data formats

How do we get human genotypes?

- SNP Chips
- Whole-genome sequencing

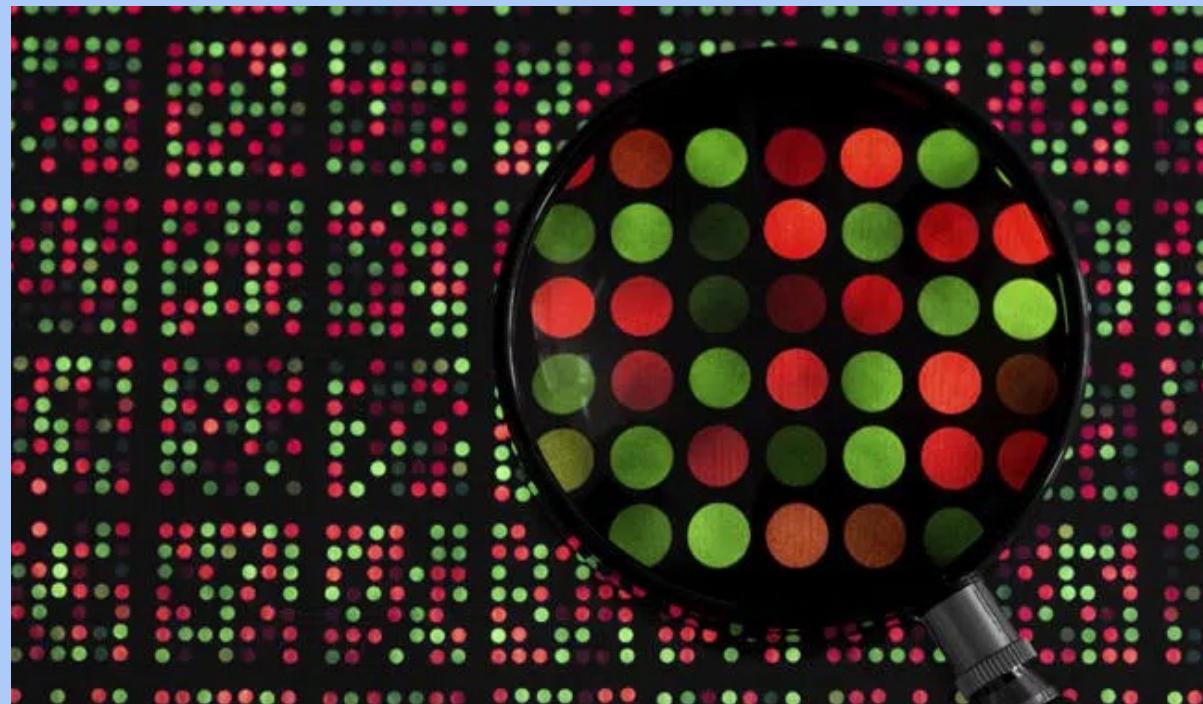
SNP Chips

- Genomic DNA binds to a complementary sequence and incorporates a fluorescently labelled nucleotide



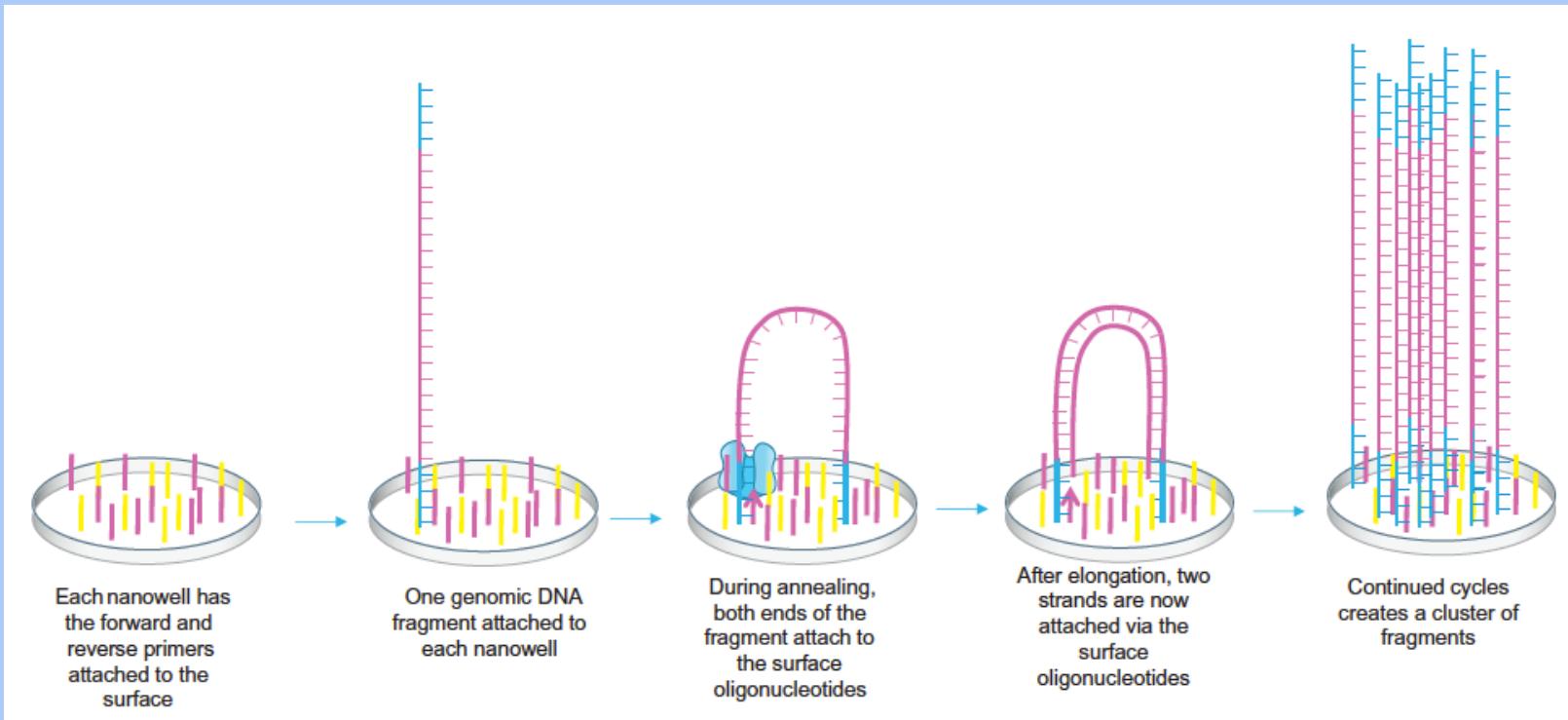
SNP Chips

- The ratio of red to green at a spot identifies the sample allele



Whole-genome sequencing (WGS)

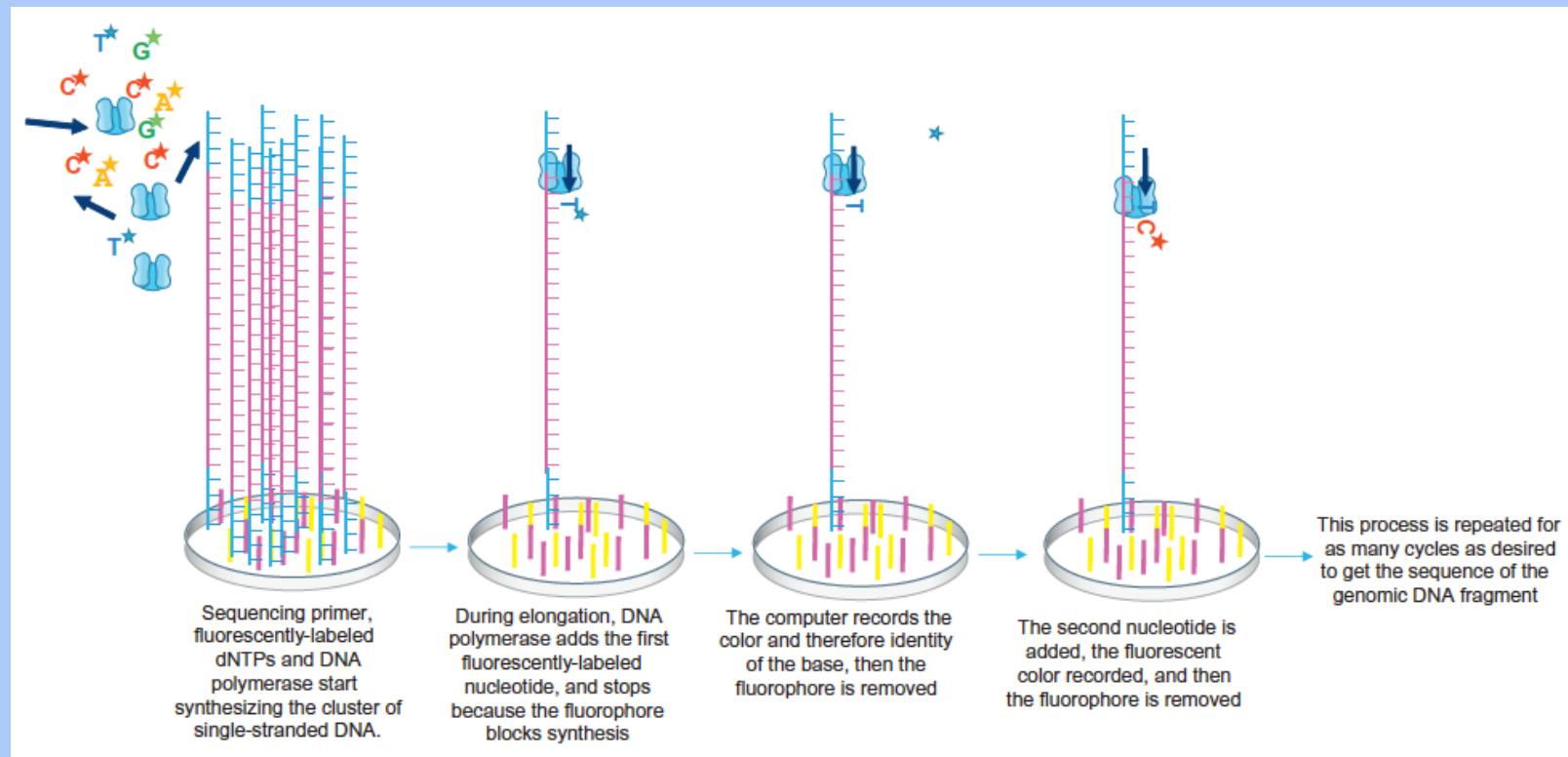
- DNA fragments from a sample are attached to a flow cell and amplified



Clark et al. *Molecular Biology (3rd Edition)*. Ch. 8: DNA Sequencing, 240-269 (2019)

Whole-genome sequencing (WGS)

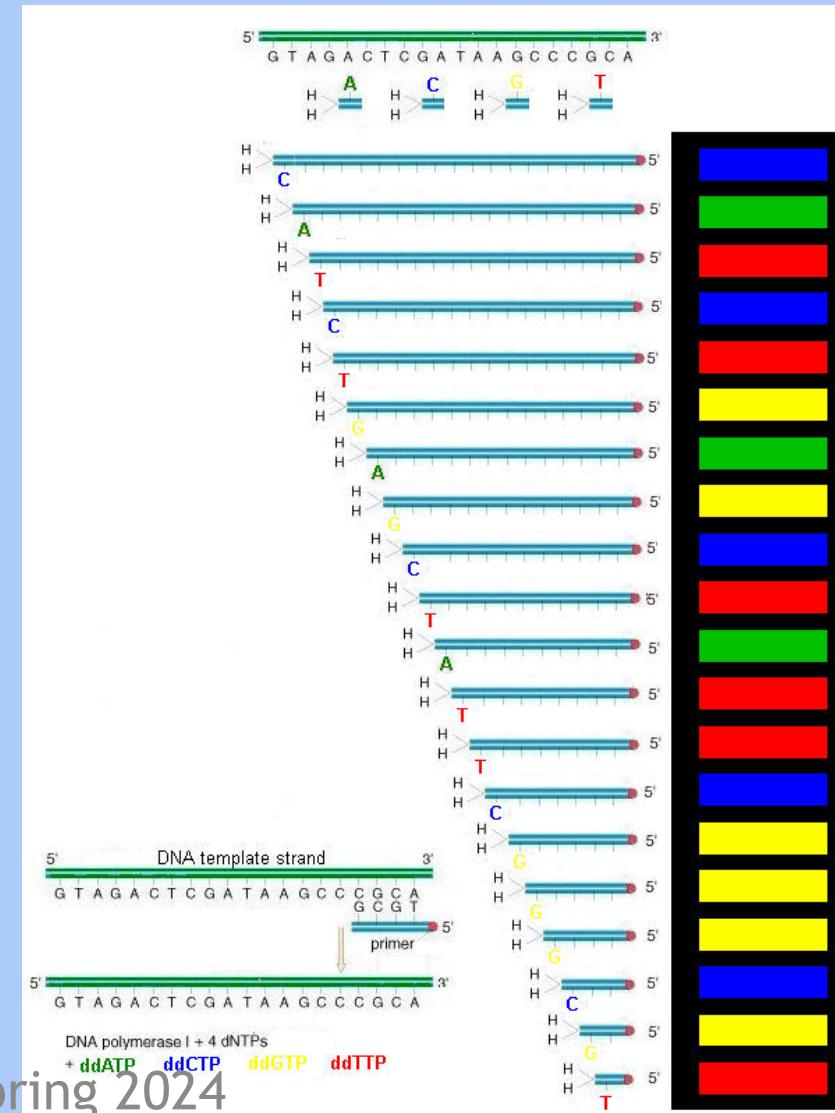
- **Sequencing by synthesis:** Short reads are produced as fluorescent nucleotides are incorporated one base at a time



Clark et al. *Molecular Biology (3rd Edition)*. Ch. 8: DNA Sequencing, 240-269 (2019)

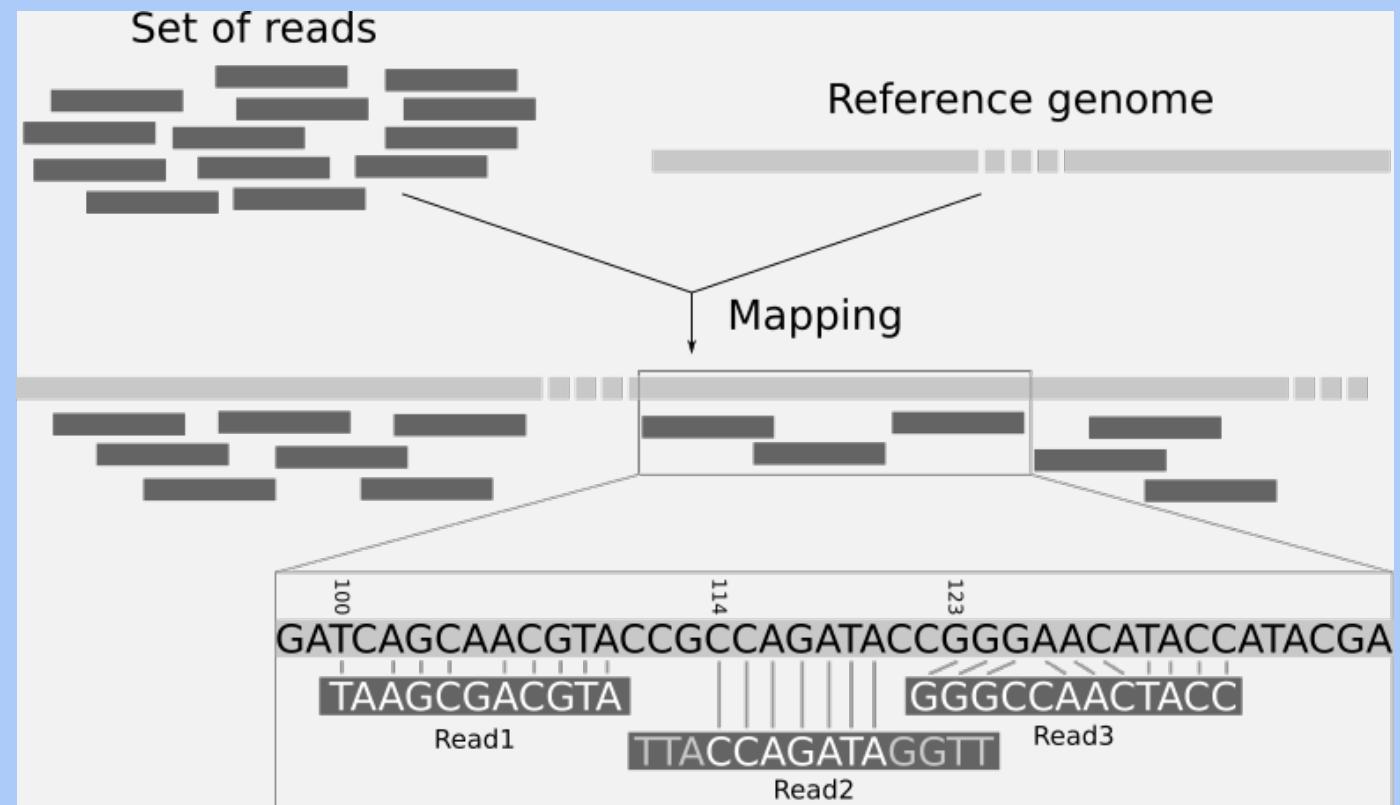
Whole-genome sequencing (WGS)

- The DNA sequence is inferred from the sequence of fluorescence images



Mapping to the reference genome

- Locate where in the genome the reads came from, and detect single-nucleotide differences from the reference sequence



Data-processing pipeline

- Generate raw reads
- Align to a reference genome
- Detect variant sites

FASTQ

- Contains raw sequence reads and their quality scores to be aligned to a reference genome (FASTA)

```
@A00178:1:HGT77DSXX:1:2171:1:17/0//:80// Z:N:0:ACAGCAAC+GTTGCTGT  
GAAGAAAAGAAGGACACAGAGGAGGGAAAGGTTGAGGAAATTGATGAAGAGAAGGAAGAGAAGAAAAGAAGACGATCAAGGAGGTTT  
+  
FFFFFFFFFFFFFFFFFFFFFFFF:FFFFFFFFFFFFFFFFFF:FFFFFFFFFFFFFFFFFF:FFFFFFFFFFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:1507:30291:23422 1:N:0:ACAGCAAC+GTTGCTGT  
ACATAGAGCTTGTGTTGCCCTCTCCTGGTGTCAAAGGGGGCCTTGGGACAAAAGGACAGCCTGAACCTCAAGCT  
+  
FFFFFFFFFFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:1507:30291:23422 2:N:0:ACAGCAAC+GTTGCTGT  
CTGGATGAGGAAGCCTGAGGAGATACCAAGGAGGTATGCTGCTTCTATAAAAGCTTGACAAATGACTGGGAAGAGCATCTGGCTGTCAAG  
+  
FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:2413:22806:35790 1:N:0:ACAGCAAC+GTTGCTGT  
GCTTGATGTTGCCCTCTCCTGGTGTCAAAGGGGGCCTTGGGACAAAAGGACAGCCTGAACCTCAAGCTGCCCTC  
+  
FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:2413:22806:35790 2:N:0:ACAGCAAC+GTTGCTGT  
GAGAAGAAAAGAACGATCAAGGAGGTTCTCATGAATGGTCCTGATCAACAAGCAGAACCTATCTGGATGAGGAAGCCTGAGGAGATCA  
+  
F:FF:FFFFFFFFFF,:FFFFFFFFFF:FFFFFFFFFF:F:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:2354:5620:8876 1:N:0:ACAGCAAC+GTTGCTGT  
ATGTTGTTGCCCTCTCCTGGTGTCAAAGGGGGCCTTGGGACAAAAGGACAGCCTGAACCTCAAGCTGCCCTCTACAG/  
+  
FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:2354:5620:8876 2:N:0:ACAGCAAC+GTTGCTGT  
AGAAGGAAGAGAAAGAGAAAAGAACGATCAAGGAGGTTCTCATGAATGGTCCTGATCAACAAGCAGAACCTATCTGGATGAGGAAC  
+  
FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF  
@A00178:71:HGT77DSXX:1:1560:6741:9815 1:N:0:ACAGCAAC+GTTGCTGT  
GCAGGATTTACCATGACTACTTTGTCATGCCAGAGAAGCTAGATTTGCCAATGATGTTATAGACCATTACGTTGCCAAGC  
+  
FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF:FFFFFFFFFF
```

SAM (BAM)

- Paired-end reads are aligned to either the forward or reverse strand of the reference genome

```
5' ACATAGACAGGGACCACCTGCAGGACACACACCGCAGGTTACTAAGGGTTACTCAACACAGTGAACAGCATATACCAGA 3'
```

```
5' ACCTGCAGGACACACACCGCAGGTTACTAAGGGTTACTCAACACAGTGA 3'
```

```
|||||||||||||||||||||||||||||||||||||||
```

```
3' TGGACGTCCCTGTGTGCGTCAAATGATTCCAAATGAGTTGTGTCACT 5'
```

<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

SAM (BAM)

- Paired-end reads are aligned to either the forward or reverse strand of the reference genome

```
Read 1: 5' ACCTGCAGGA 3'  
5' ACATAGACAGGGACCACCTGCAGGACACACACCGCAGGTTACTAAGGGTTACTCAACACAGTGAACAGCATATACAGA 3'  
forward-strand  
||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||  
reverse-strand  
3' TGTATCTGCCCTGGTGGACGTCCCTGTGTGCGTCAAATGATTCCAAATGAGTTGTGTCATTGTCGTATATGGTCT 5'  
Read 2: 3' TTGTGTCACT 5'
```

<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

SAM (BAM)

- Paired-end reads are aligned to either the forward or reverse strand of the reference genome

```
Read 2: 5' ACCTGCAGGA 3'  
5' ACATAGACAGGGACCACCTGCAGGACACACACCGCAGGTTACTAAGGGTTACTCAACACAGTGAACAGCATATACCAGA 3'  
forward-strand  
||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||||  
reverse-strand  
3' TGTATCTGTCCCTGGTGGACGTCCCTGTGTGCGTCAAATGATTCCAAATGAGTTGTGTCATTGTCGTATATGGTCT 5'  
Read 1: 3' TTGTGTCACT 5'
```

<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

SAM (BAM)

- A Sequence alignment map (SAM) or binary alignment map (BAM) file contains the alignments to the reference genome

A

Coor	10	20	30	40
ref	12345678901234	5678901234567890123456789012345		
	AGCATTTAGATAAA**GATAGCTGTGCTAGTAGGCAGTCAGCGCCAT			
+r001/1		TTAGATAAAGGATA*CTG		
+r002		aaaAGATAA*GGATA		
+r003		gcctaAGCTAA		
+r004		ATAGCT.....TCAGC		
-r003			ttagctTAGGC	
-r001/2				CAGCGGCAT

B

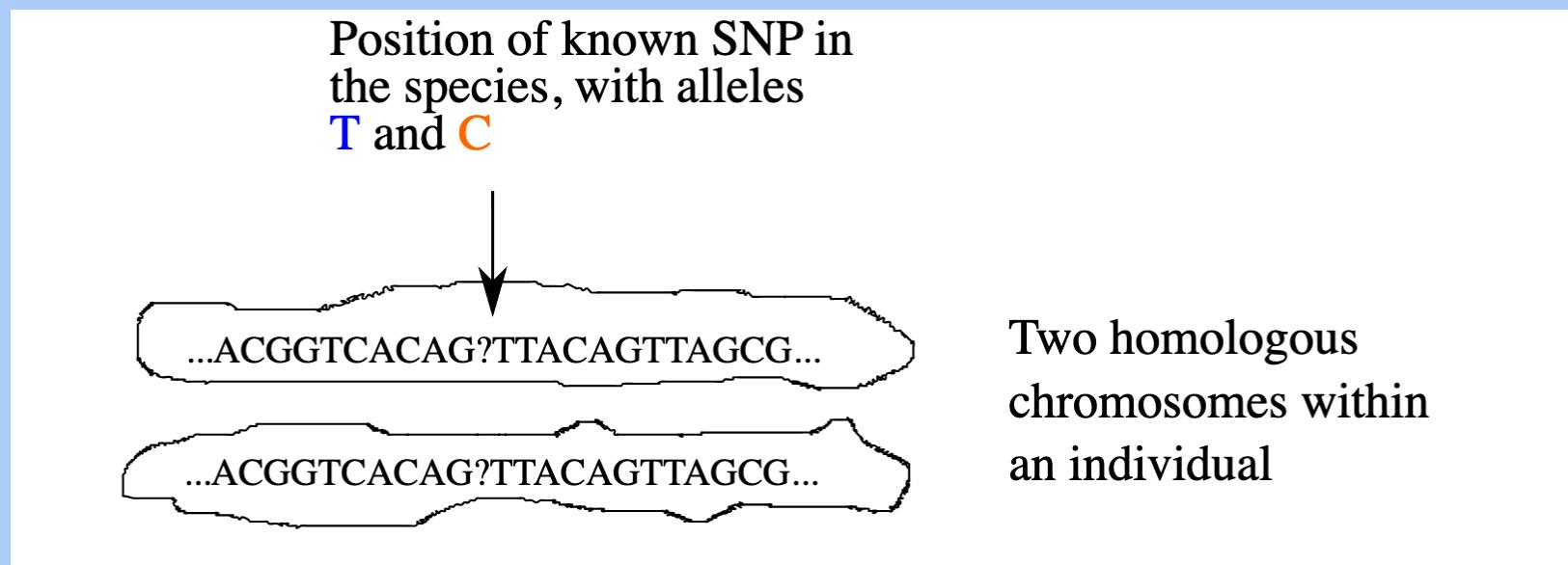
Header section		QUAL (read quality; * meaning such information is not available)	
@HD VN:1.5 SO:coordinate			
@SQ SN:ref LN:45			
r001	99 ref 7 30 8M2I4M1D3M = 37 39 TTAGATAAAGGATACTG *		
r002	0 ref 9 30 3S6M1P1I4M * 0 0 AAAAGATAAGGATA *		
r003	0 ref 9 30 5S6M * 0 0 GCCTAAGCTAA * SA:Z:ref,29,-,6H5M,17,0;		
r004	0 ref 16 30 6M14N5M * 0 0 ATAGCTTCAGC *		
r003	2064 ref 29 17 6H5M * 0 0 TAGGC * SA:Z:ref,9,+,5S6M,30,1;		
r001	147 ref 37 30 9M = 7 -39 CAGCGGCAT * NM:i:1		

Annotations below the table:

- QNAME FLAG (query template name, aka. read ID)
- RNAME (reference sequence name, e.g. chromosome /transcript id)
- POS (1-based position)
- MAPQ (mapping quality)
- CIGAR (summary of alignment, e.g. insertion, deletion)
- RNEXT (reference sequence name of the primary alignment of the NEXT read; for paired-end sequencing, NEXT read is the paired read; corresponding to the RNAME column)
- PNEXT (Position of the primary alignment of the NEXT read in the template; corresponding to the POS column)
- TLEN (the number of bases covered by the reads from the same fragment. In this particular case, it's 45 - 7 + 1 = 39 as highlighted in Panel A). Sign: plus for leftmost read, and minus for rightmost read
- SEQ (read sequence)
- Optional fields in the format of TAG:TYPE:VALUE

Variant calling (mpileup)

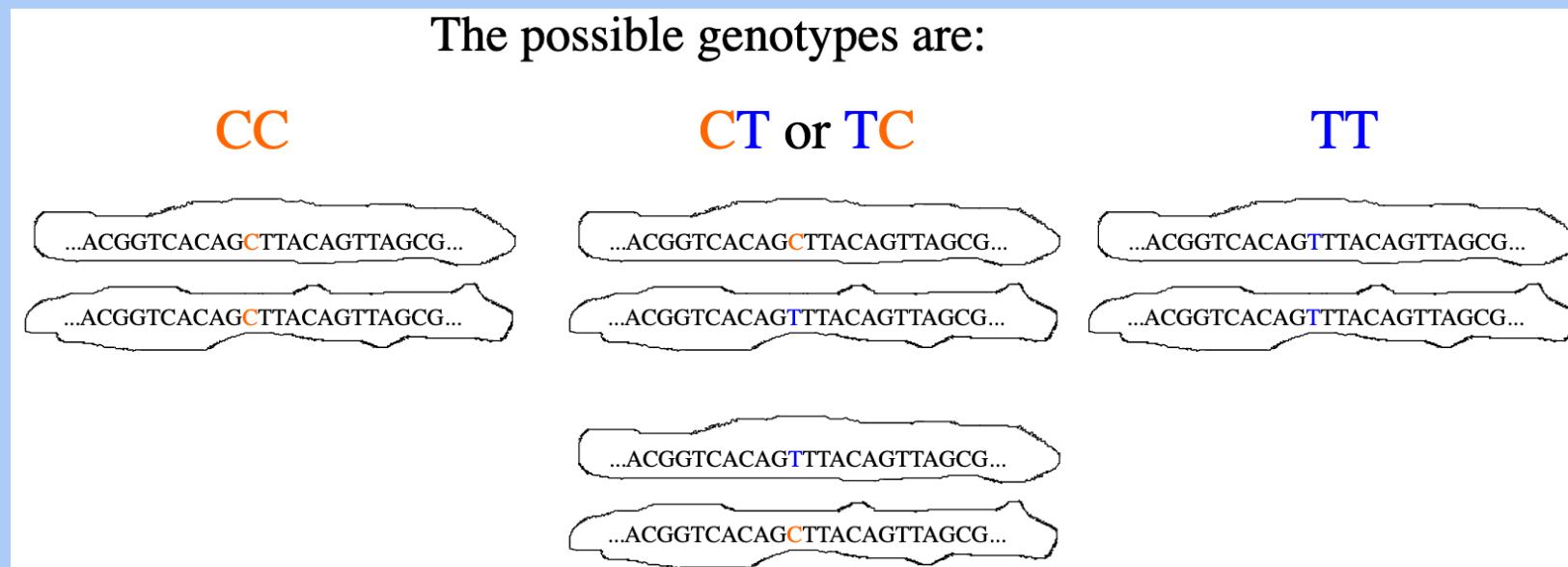
- How certain can we be of an individual's genotype?



<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

Variant calling (mpileup)

- How certain can we be of an individual's genotype?



<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

Variant calling (mpileup)

- How certain can we be of an individual's genotype?

The data are: 4 reads covering that site,
and
the associated base quality scores

<i>Read</i>			<i>Observed Base</i>	<i>PHRED-scaled base quality score</i>
#	<i>Read</i>			
1	CAG C TTACA		C	32 (A)
2	ACAG C T		C	37 (F)
3	G TTTA		T	35 (D)
4	AG C TTACAG		C	33 (B)

<https://eriqande.github.io/eca-bioinf-handbook/bioinformatic-file-formats.html#sambamfiles>

VCF

- The results of genotype-calling are stored in a variant call format (VCF) file

VCF															
#fileformat=VCFv4.2 ##contig=<ID=2,length=51304566> ##INFO=<ID=AC,Number=A,Type=Integer,Description="Allele count in genotypes"> ##INFO=<ID=AN,Number=1,Type=Integer,Description="Total number of alleles in called genotypes"> ##FORMAT=<ID=GT,Number=1,Type=String,Description="Genotype"> ##FORMAT=<ID=DP,Number=1,Type=Integer,Description="Read Depth"> ##FORMAT=<ID=GQ,Number=1,Type=Integer,Description="Genotype Quality"> #CHROM POS ID REF ALT QUAL FILTER INFO FORMAT SAMPLE1 SAMPLE2 SAMPLE3 SAMPLE4 SAMPLE5 SAMPLE6 SAMPLE7															
2	81170	.	C	T	.	.	AC=9;AN=7424	GT:DP:GQ	0/0:4:12	0/0:3:9	0/1:1:3	0/1:9:24	1/0:4:12	0/0:5:15	0/0:4:12
2	81171	.	G	A	.	.	AC=6;AN=7446	GT:DP:GQ	0/1:4:12	0/0:3:9	0/0:1:3	0/0:9:24	0/1:4:12	0/1:5:15	0/0:4:12
2	81182	.	A	G	.	.	AC=5;AN=7506	GT:DP:GQ	0/0:5:15	0/0:4:12	0/0:5:15	0/0:9:24	0/0:4:12	0/0:4:12	0/0:4:12
2	81204	.	T	G	.	.	AC=2;AN=7542	GT:DP:GQ	1/0:5:15	0/0:9:27	0/0:10:30	0/0:15:39	0/0:9:27	1/0:13:39	0/1:14:42

BCF										
2	81170	.	C	T	.	.	AC=9;AN=7424	GT:0/0:0/0:0/0:1/0:1/0:0/0:0/0:0/0	DP:4:3:1:9:4:5:4	GQ:12: 9: 3:24:12:15:12
2	81171	.	G	A	.	.	AC=6;AN=7446	GT:0/1:0/0:0/0:0/0:0/1:0/1:0/0	DP:4:3:1:9:4:5:4	GQ:12: 9: 3:24:12:15:12
2	81182	.	A	G	.	.	AC=5;AN=7506	GT:0/0:0/0:0/0:0/0:0/0:0/0:0/0	DP:5:4:5:9:4:4:4	GQ:15:12:15:24:12:12:12
2	81204	.	T	G	.	.	AC=2;AN=7542	GT:1/0:0/0:0/0:0/0:0/0:1/0:0/1	DP:5:9:10:15:9:13:14	GQ:15:27:30:39:27:39:42



VCF

- The VCF file has one row for each variant, and one column for each sequenced individual

##fileformat=VCFv4.0 ##fileDate=20110705 ##reference=1000GenomesPilot-NCBI37 ##phasing=partial ##INFO=<ID=NS,Number=1,Type=Integer,Description="Number of Samples With Data"> ##INFO=<ID=DP,Number=1,Type=Integer,Description="Total Depth"> ##INFO=<ID=AF,Number=.,Type=Float,Description="Allele Frequency"> ##INFO=<ID=AA,Number=1,Type=String,Description="Ancestral Allele"> ##INFO=<ID=DB,Number=0,Type=Flag,Description="dbSNP membership, build 129"> ##INFO=<ID=H2,Number=0,Type=Flag,Description="HapMap2 membership"> ##FILTER=<ID=q10,Description="Quality below 10"> ##FILTER=<ID=s50,Description="Less than 50% of samples have data"> ##FORMAT=<ID=GQ,Number=1,Type=Integer,Description="Genotype Quality"> ##FORMAT=<ID=GT,Number=1,Type=String,Description="Genotype"> ##FORMAT=<ID=DP,Number=1,Type=Integer,Description="Read Depth"> ##FORMAT=<ID=HQ,Number=2,Type=Integer,Description="Haplotype Quality">	FORMAT Sample1 Sample2 Sample3										
CHROM	POS	ID	REF	ALT	QUAL	FILTER	INFO	FORMAT	Sample1	Sample2	Sample3
2	4370	rs6857	G	A	29	.	NS=2;DP=13;AF=0.5;DB:H2	GT:GQ:DP:HQ	0 0:48:1:52,51	1 0:48:8:51,51	1/1:43:5:,,,
2	7330	.	T	A	3	q10	NS=5;DP=12;AF=0.017	GT:GQ:DP:HQ	0 0:46:3:58,50	0 1:3:5:65,3	0/0:41:3
2	110696	rs6855	A	G,T	67	PASS	NS=2;DP=10;AF=0.333,0.667;AA=T;DB	GT:GQ:DP:HQ	1 2:21:6:23,27	2 1:2:0:18,2	2/2:35:4
2	130237	.	T	.	47	.	NS=2;DP=16;AA=T	GT:GQ:DP:HQ	0 0:54:7:56,60	0 0:48:4:56,51	0/0:61:2
2	134567	microsat1	GTCT	G,GTACT	50	PASS	NS=2;DP=9;AA=G	GT:GQ:DP	0/1:35:4	0/2:17:2	1/1:40:3

VCF

- Codes such as GT, DP, GP give the genotype, read depth, and genotype probabilities for each individual

##fileformat=VCFv4.0							FORMAT				
##fileDate=20110705							Sample1	Sample2	Sample3		
##reference=1000GenomesPilot-NCBI37							GT:GQ:DP:HQ	0 0:48:1:52,51	1 0:48:8:51,51	1/1:43:5:,,,,	
##phasing=partial							GT:GQ:DP:HQ	0 0:46:3:58,50	0 1:3:5:65,3	0/0:41:3	
##INFO=<ID=NS,Number=1,Type=Integer,Description="Number of Samples With Data">							GT:GQ:DP:HQ	1 2:21:6:23,27	2 1:2:0:18,2	2/2:35:4	
##INFO=<ID=DP,Number=1,Type=Integer,Description="Total Depth">							GT:GQ:DP:HQ	0 0:54:7:56,60	0 0:48:4:56,51	0/0:61:2	
##INFO=<ID=AF,Number=.,Type=Float,Description="Allele Frequency">							GT:GQ:DP	0/1:35:4	0/2:17:2	1/1:40:3	
##INFO=<ID=AA,Number=1,Type=String,Description="Ancestral Allele">											
##INFO=<ID=DB,Number=0,Type=Flag,Description="dbSNP membership, build 129">											
##INFO=<ID=H2,Number=0,Type=Flag,Description="HapMap2 membership">											
##FILTER=<ID=q10,Description="Quality below 10">											
##FILTER=<ID=s50,Description="Less than 50% of samples have data">											
##FORMAT=<ID=GQ,Number=1,Type=Integer,Description="Genotype Quality">											
##FORMAT=<ID=GT,Number=1,Type=String,Description="Genotype">											
##FORMAT=<ID=DP,Number=1,Type=Integer,Description="Read Depth">											
##FORMAT=<ID=HQ,Number=2,Type=Integer,Description="Haplotype Quality">											
CHROM	POS	ID	REF	ALT	QUAL	FILTER	INFO				
2	4370	rs6857	G	A	29	.	NS=2;DP=13;AF=0.5;DB:H2	GT:GQ:DP:HQ	0 0:48:1:52,51	1 0:48:8:51,51	1/1:43:5:,,,,
2	7330	.	T	A	3	q10	NS=5;DP=12;AF=0.017	GT:GQ:DP:HQ	0 0:46:3:58,50	0 1:3:5:65,3	0/0:41:3
2	110696	rs6855	A	G,T	67	PASS	NS=2;DP=10;AF=0.333,0.667;AA=T;DB	GT:GQ:DP:HQ	1 2:21:6:23,27	2 1:2:0:18,2	2/2:35:4
2	130237	.	T	.	47	.	NS=2;DP=16;AA=T	GT:GQ:DP:HQ	0 0:54:7:56,60	0 0:48:4:56,51	0/0:61:2
2	134567	microsat1	GTCT	G,GTACT	50	PASS	NS=2;DP=9;AA=G	GT:GQ:DP	0/1:35:4	0/2:17:2	1/1:40:3

Principal components analysis

The concept of genetic ancestry

The HapMap Project

- International genotyping consortium launched in 2002 to find common polymorphisms linked to rare disease loci



<https://pubmed.ncbi.nlm.nih.gov/16255080/>

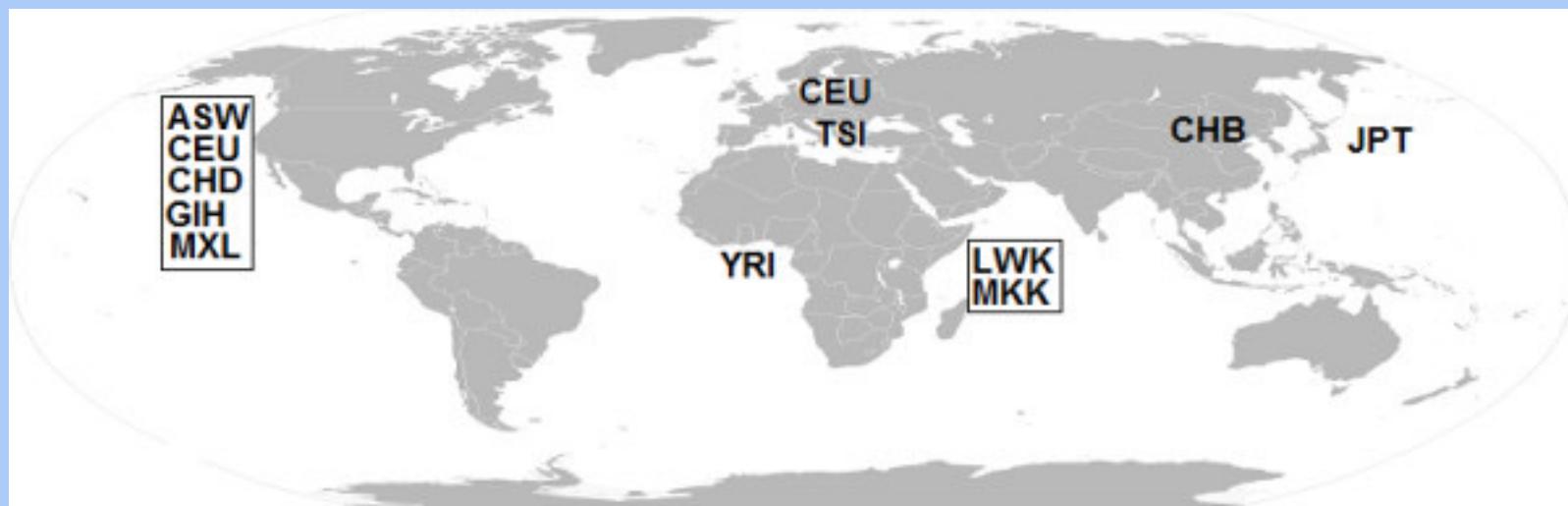
The HapMap Project

- Variants occur together on a small number of haplotypes



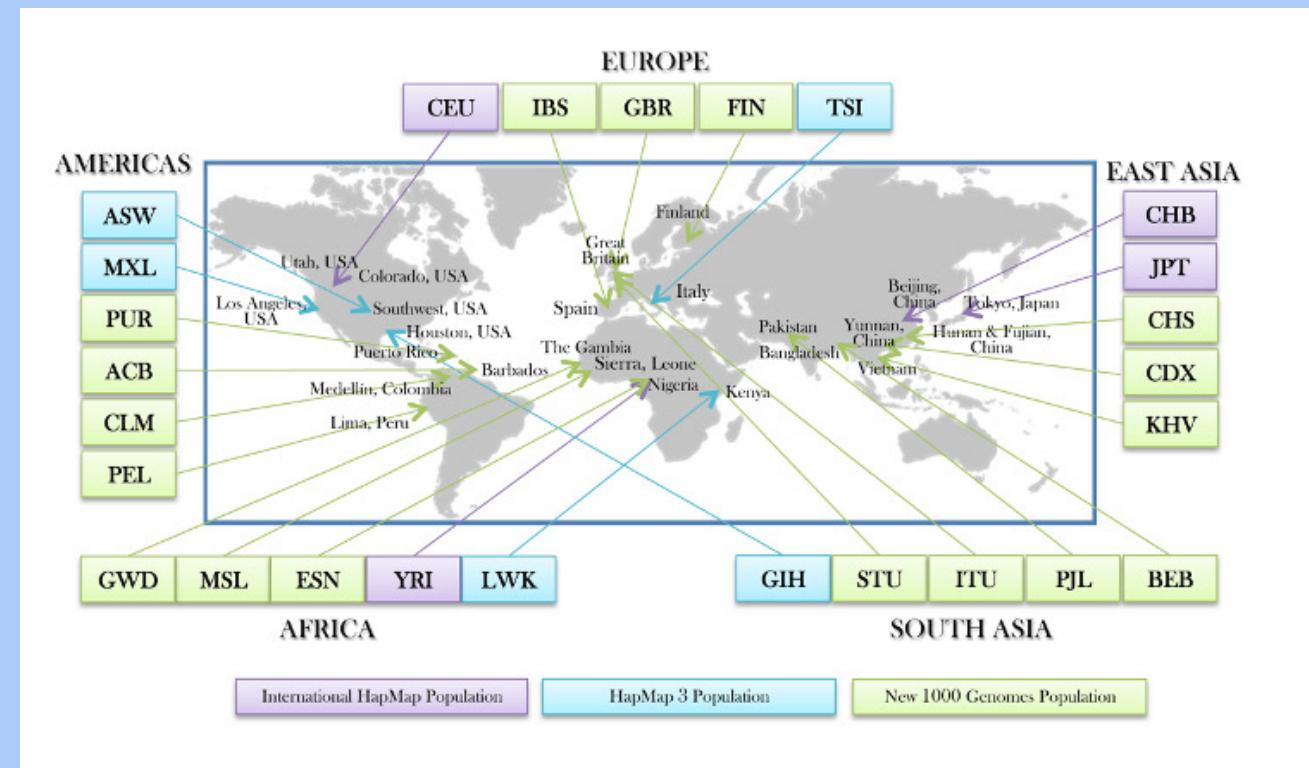
The HapMap Project

- Phase 3 (2010): genotyping and PCR resequencing of 1.6 million SNPs from 1,184 human samples from different parts of the world



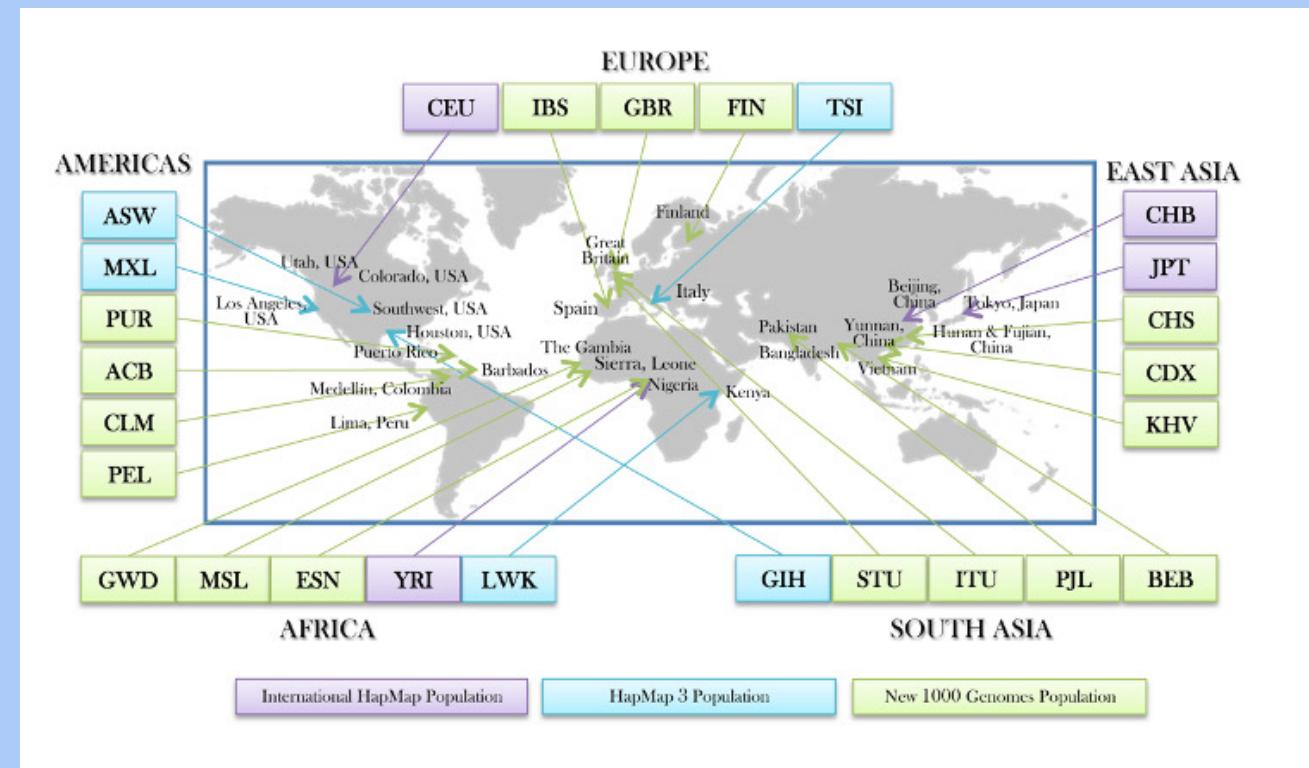
The 1000 Genomes Project

- An international consortium launched in 2008 to catalog rare variants (frequency < 1%) taking advantage of new sequencing technologies

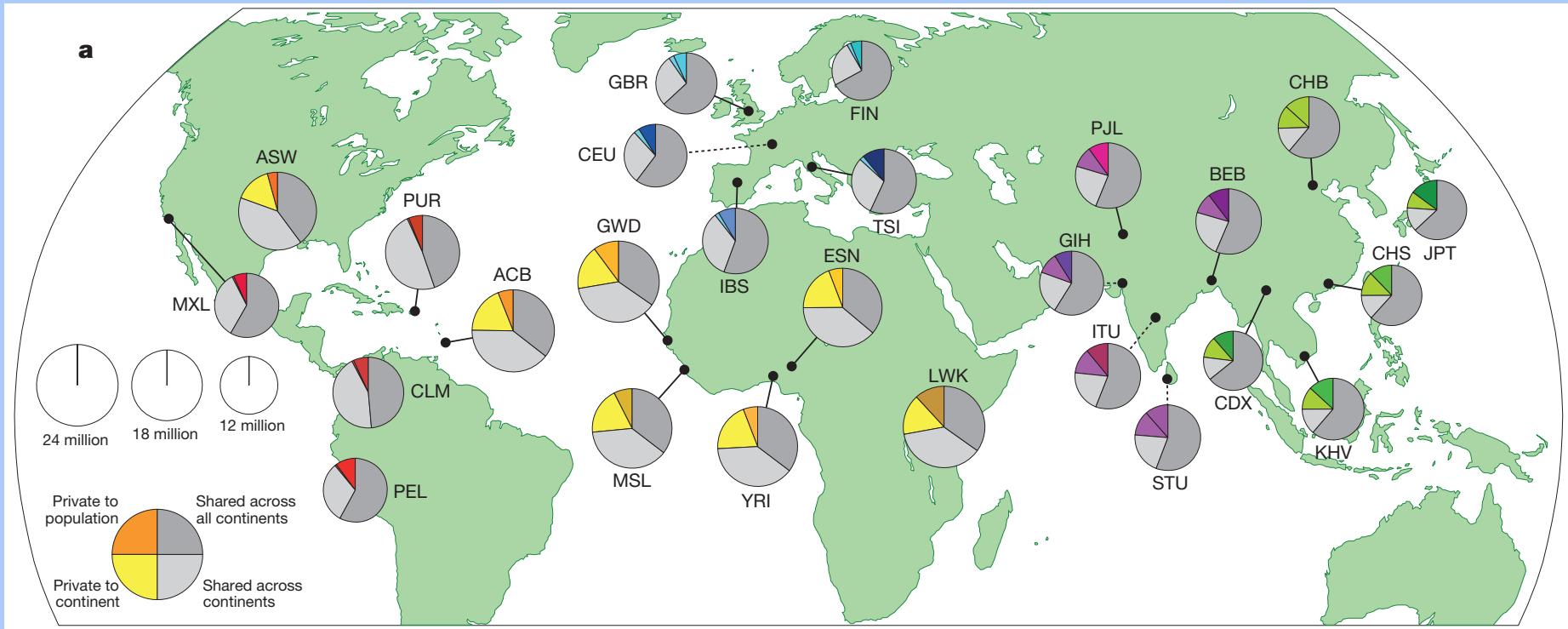


The 1000 Genomes Project

- Phase 3 release (2015) contained data from 2,504 individuals representing 26 populations across the globe, and identified 85 million new SNPs



Global genetic variation



- Most SNPs are shared across continents, and the majority of variation (~85%) is within rather than between populations

The same yet different?

- Most variation is within-populations rather than between-populations
- Yet regional differences in allele frequencies lead to noticeable differences in phenotypes



Statistical variation of an allele

- Variation of the counts x_i of an allele about the group mean \bar{x}_j and the population mean \bar{x}

$$\sum_i (x_i - \bar{x})^2 = \sum_i (x_i - \bar{x}_{j(i)})^2 + \sum_i (\bar{x}_{j(i)} - \bar{x})^2$$

Total variation Within-population variation Between-population variation

- Most SNPs are shared across continents, and the majority of variation (~85%) is within rather than between populations

Example: lactase nonpersistence (lactose intolerance)

- The T allele of rs182549 is completely associated with the ability to digest lactose in Europeans

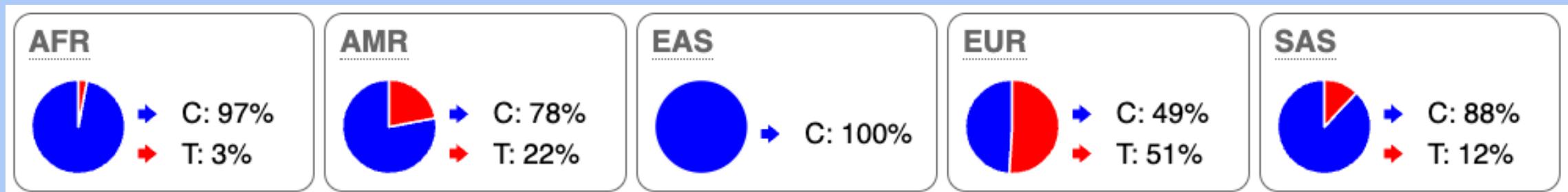
	CC	CT	TT
Non-persistence	59	0	0
Persistence	0	63	74

<https://pubmed.ncbi.nlm.nih.gov/11788828/>

Example: lactase nonpersistence (lactose intolerance)

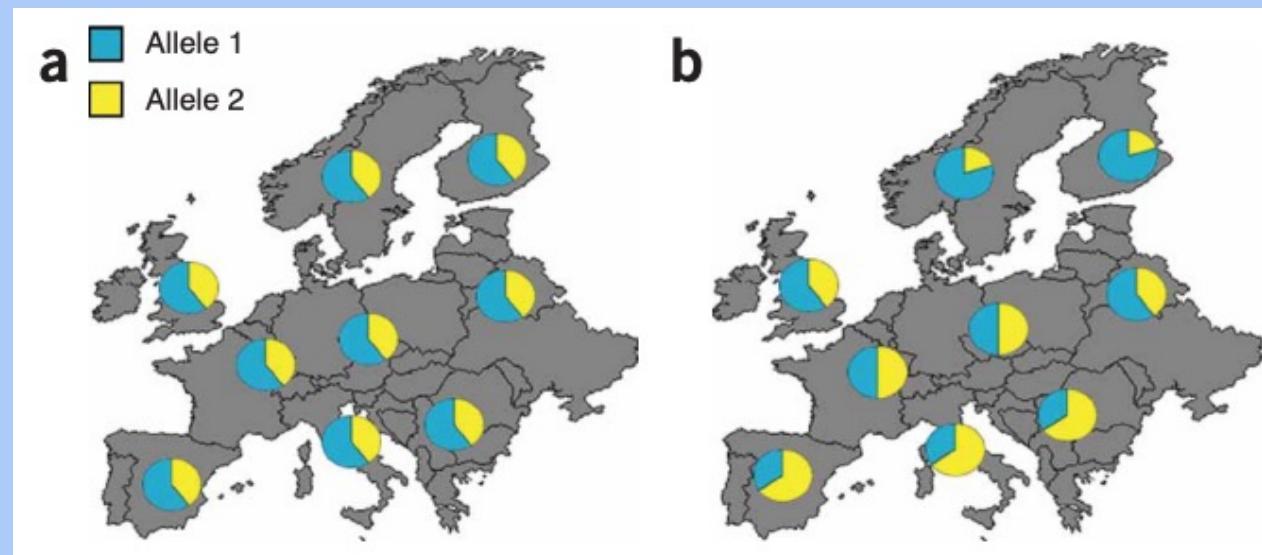
- Yet the polymorphism is almost absent in the African population, despite the presence of lactase persistence

<https://pubmed.ncbi.nlm.nih.gov/15106124/>



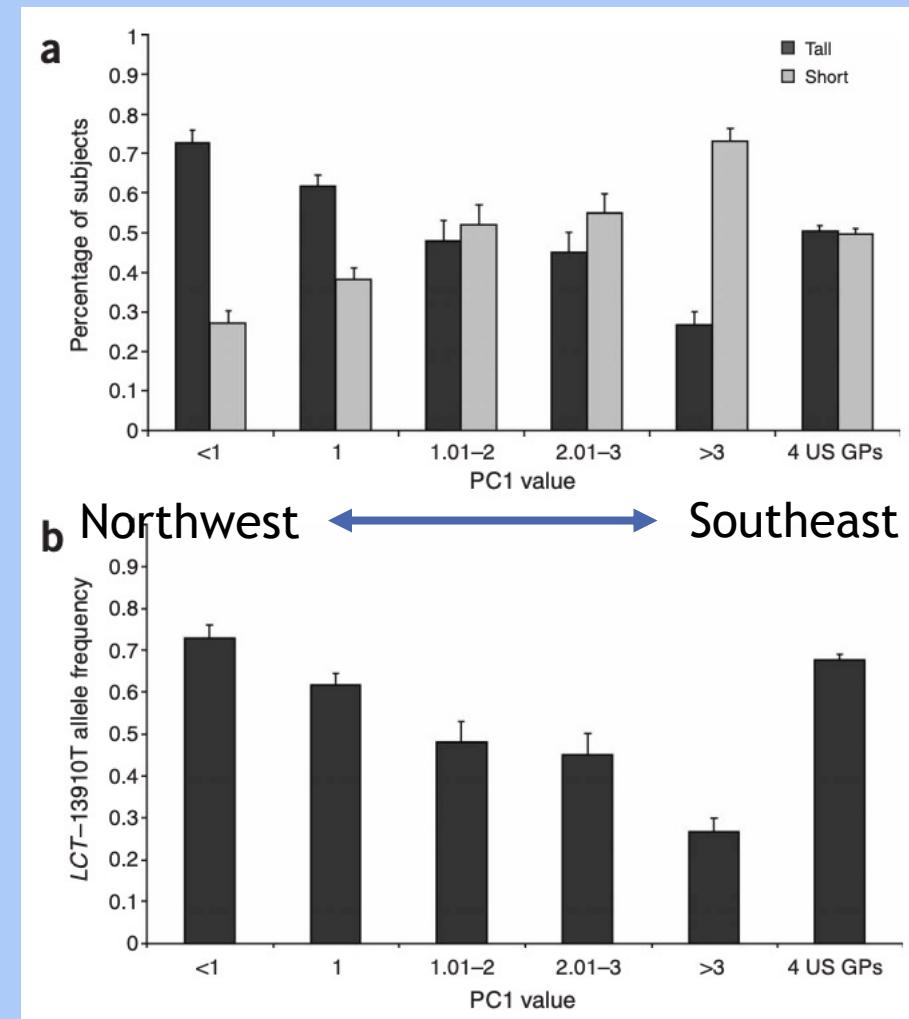
Population stratification

- An allele may appear associated with a phenotype when in fact it is associated with geographic origin (genetic ancestry)



Spurious association

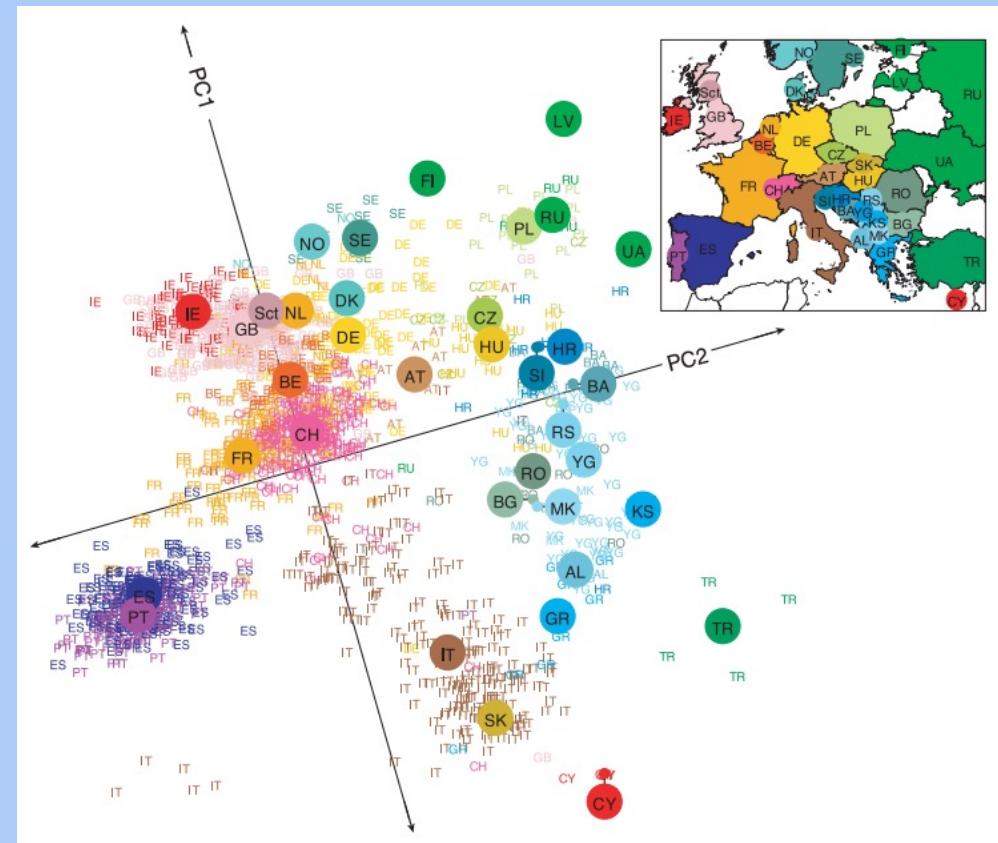
- An allele of the lactase-persistence SNP is spuriously associated with height, as its frequency is higher in individuals with Northern European ancestry vs. Southern



<https://pubmed.ncbi.nlm.nih.gov/16041375/>

Principal components analysis

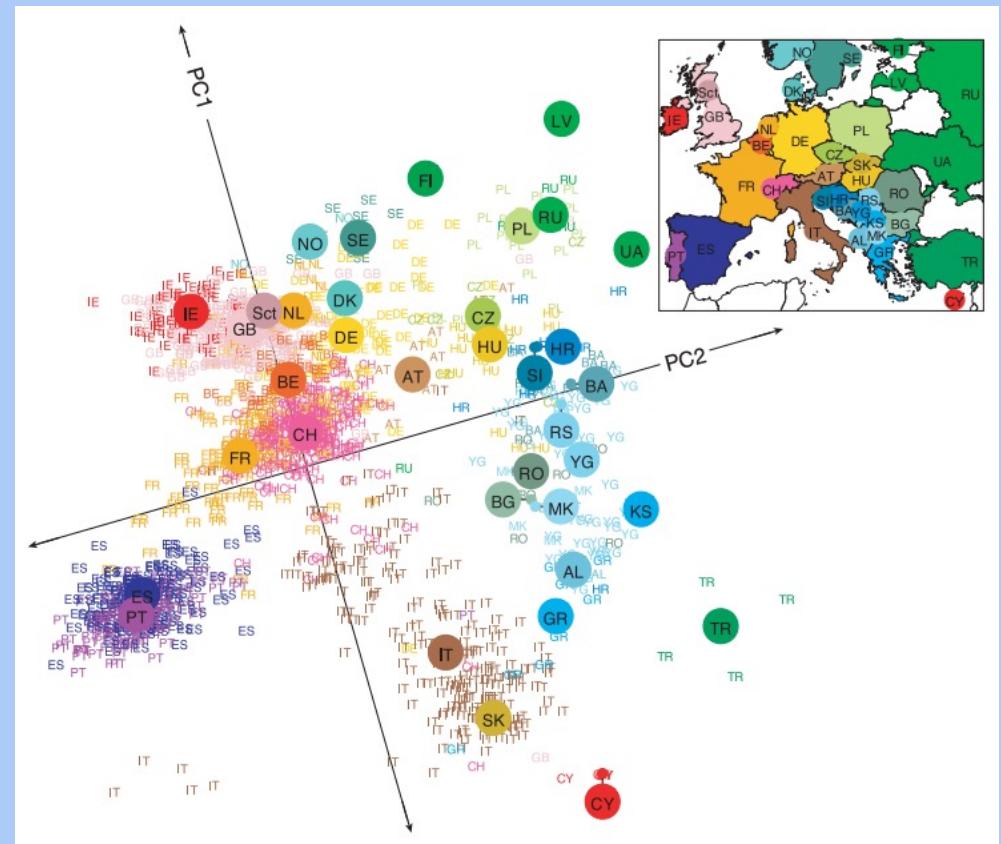
- Genotypes can distinguish population groups



<https://pubmed.ncbi.nlm.nih.gov/18758442/>

Principal components analysis

- Looking at which variants segregate together can tell us about an individual's likely genetic ancestry



<https://pubmed.ncbi.nlm.nih.gov/18758442/>

Genotype matrix

- n individuals are genotyped at m SNPs

$$\mathbf{X} = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix}$$

Genotype matrix

- The number of alternate alleles is 0, 1, or 2

$$\mathbf{X} = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix}$$

Genotype matrix

- “Standardize” each genotype by subtracting the mean allele (column) frequency and dividing by its standard error

$$\mathbf{X} = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix}$$

“Idealized” individuals

- An “idealized” subject of a particular genetic ancestry has genotypes v at m SNPs

$$\mathbf{X}\mathbf{V}^T = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix} \begin{pmatrix} v_{11} & v_{21} & v_{31} \\ \vdots & \vdots & \vdots \\ v_{1m} & v_{2m} & v_{3m} \end{pmatrix}$$

“Idealized” individuals

- The position of individual 1 on PC1 is the “amount” of idealized person 1 in individual 1

$$\mathbf{X}\mathbf{V}^T = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix} \begin{pmatrix} v_{11} & v_{21} & v_{31} \\ \vdots & \vdots & \vdots \\ v_{1m} & v_{2m} & v_{3m} \end{pmatrix}$$

“Idealized” individuals

- The idea of PCA is to find the amount of each idealized individual in each actual individual

$$\mathbf{X}\mathbf{V}^T = \begin{pmatrix} x_{11} & \cdots & x_{1m} \\ x_{21} & \cdots & x_{2m} \\ \vdots & & \vdots \\ x_{n1} & \cdots & x_{nm} \end{pmatrix} \begin{pmatrix} v_{11} & v_{21} & v_{31} \\ \vdots & \vdots & \vdots \\ v_{1m} & v_{2m} & v_{3m} \end{pmatrix}$$

Genomic relationship matrix (GRM)

- The GRM is computed by comparing how similar any subject is to any other

$$\mathbf{X}\mathbf{X}^T = \begin{pmatrix} \mathbf{x}_1 \cdot \mathbf{x}_1 & \cdots & \mathbf{x}_1 \cdot \mathbf{x}_n \\ \mathbf{x}_2 \cdot \mathbf{x}_1 & \cdots & \mathbf{x}_2 \cdot \mathbf{x}_n \\ \vdots & & \vdots \\ \mathbf{x}_n \cdot \mathbf{x}_1 & \cdots & \mathbf{x}_n \cdot \mathbf{x}_n \end{pmatrix}$$

Genomic relationship matrix (GRM)

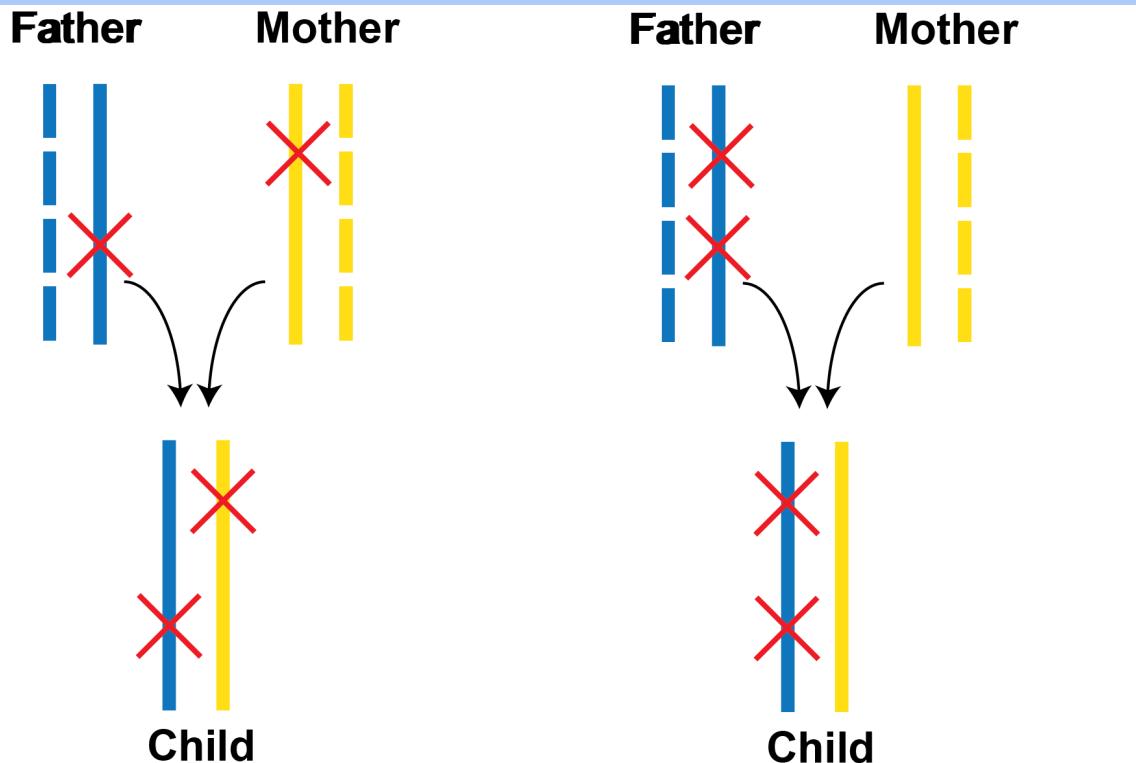
- The **eigenvectors** (columns of \mathbf{U}) of the GRM contain the ancestry components

$$\mathbf{X}\mathbf{X}^T \mathbf{U} = \mathbf{U}\boldsymbol{\Sigma}^2$$

Linkage disequilibrium

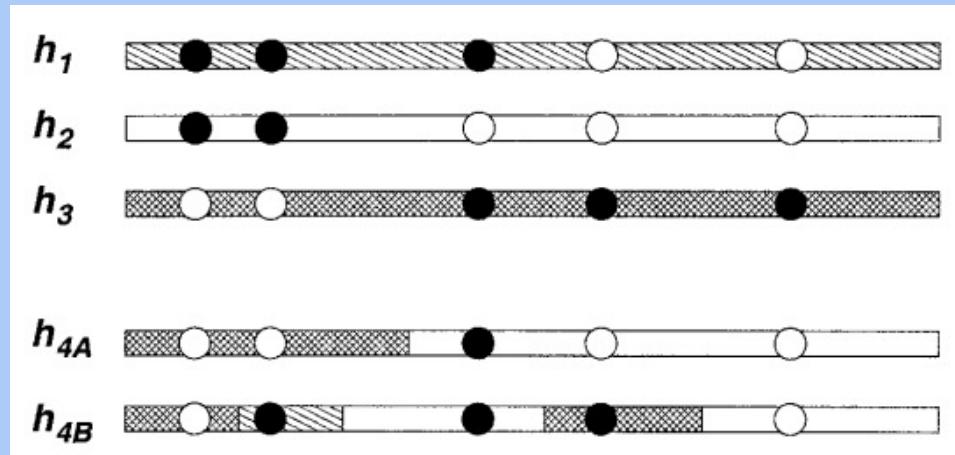
Determining a set of independent SNPs

SNPs can occur on either of two chromosomes



- Genotype data do not tell us which chromosomes carry the polymorphism
- When at least one parent is homozygous at each SNP, **haplotype phase** can be unambiguously assigned

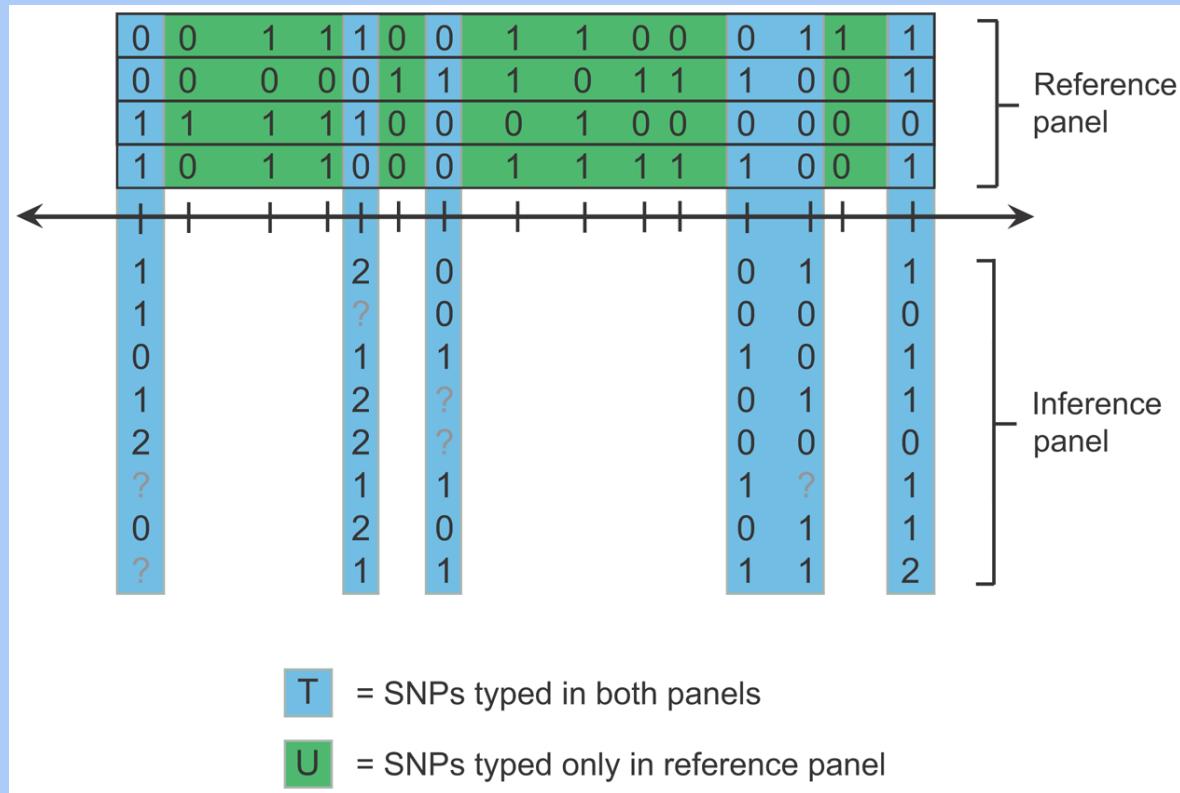
Statistical phasing and imputation



<https://pubmed.ncbi.nlm.nih.gov/14704198/>

- Genotyped individuals can be computationally phased by modelling each chromosome as an imperfect mosaic of chromosomes from a reference panel

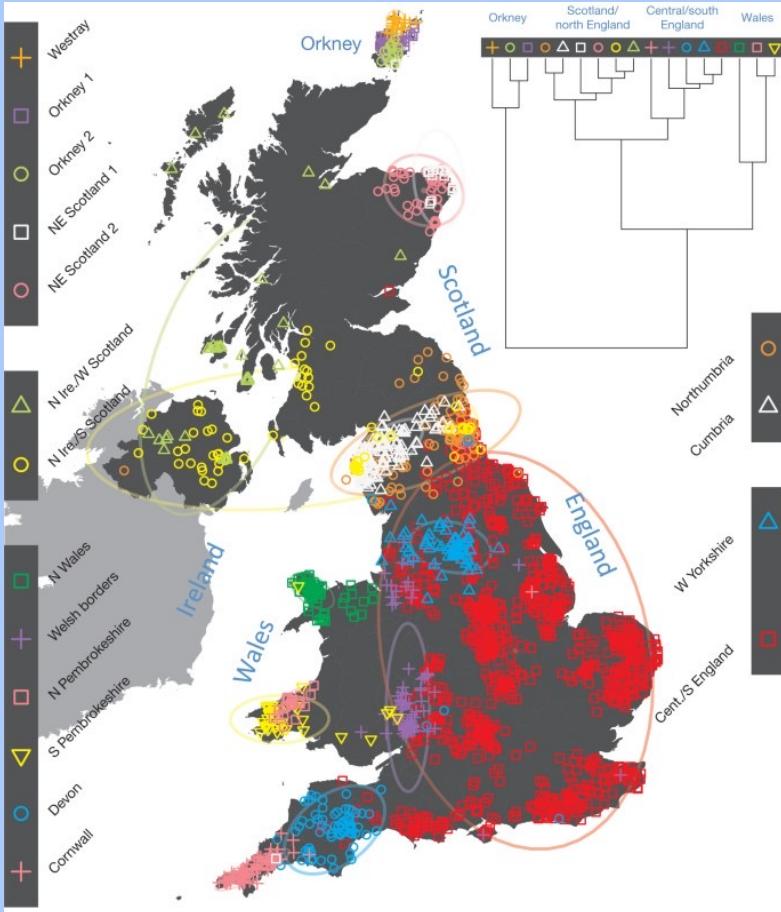
Statistical phasing and imputation



- Variants that have not been typed can be **imputed** into the inference sample
- Imputation accuracy depends on the inference and reference samples being of similar genetic ancestry

<https://pubmed.ncbi.nlm.nih.gov/19543373/>

Different haplotypes distinguish different populations



- Individuals can be grouped into populations with which they have the most haplotype-sharing

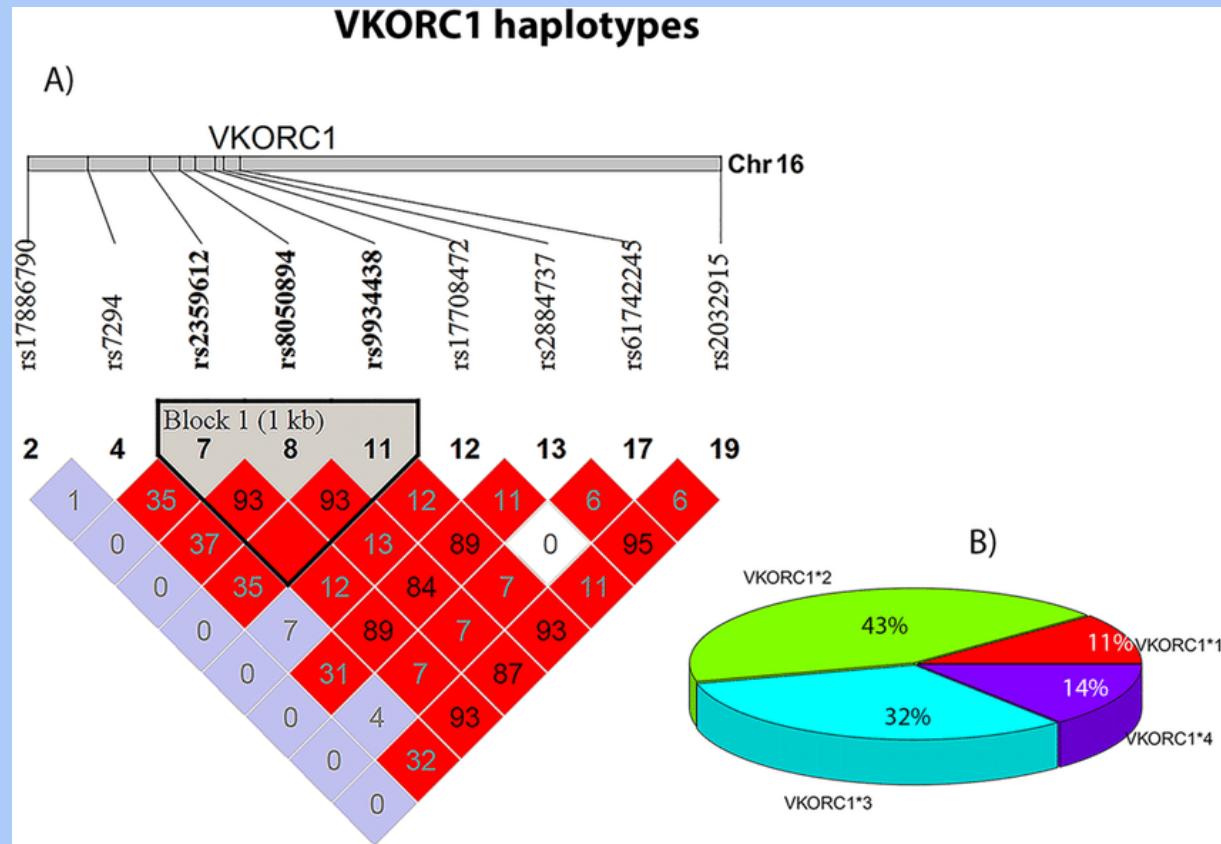
<https://pubmed.ncbi.nlm.nih.gov/25788095/>

Linkage disequilibrium

- Linkage disequilibrium is the population tendency of alleles to be inherited on a single chromosome and is measured using a correlation coefficient between the alleles of different SNPs

$$r_{A,B} = \frac{p_{A,B} - p_A p_B}{\sqrt{p_A (1 - p_A) p_B (1 - p_B)}}$$

LD blocks and haplotype structure



<https://pubmed.ncbi.nlm.nih.gov/32221414/>

- Plots of pairwise r^2 values show which SNPs are inherited together in the population as common haplotypes

Haplotype simulation using LD

- Simulate a haplotype by ensuring that the frequencies and LD between any two alleles match the reference data
- No assumptions about phylogenies or knowledge of evolutionary theory is required

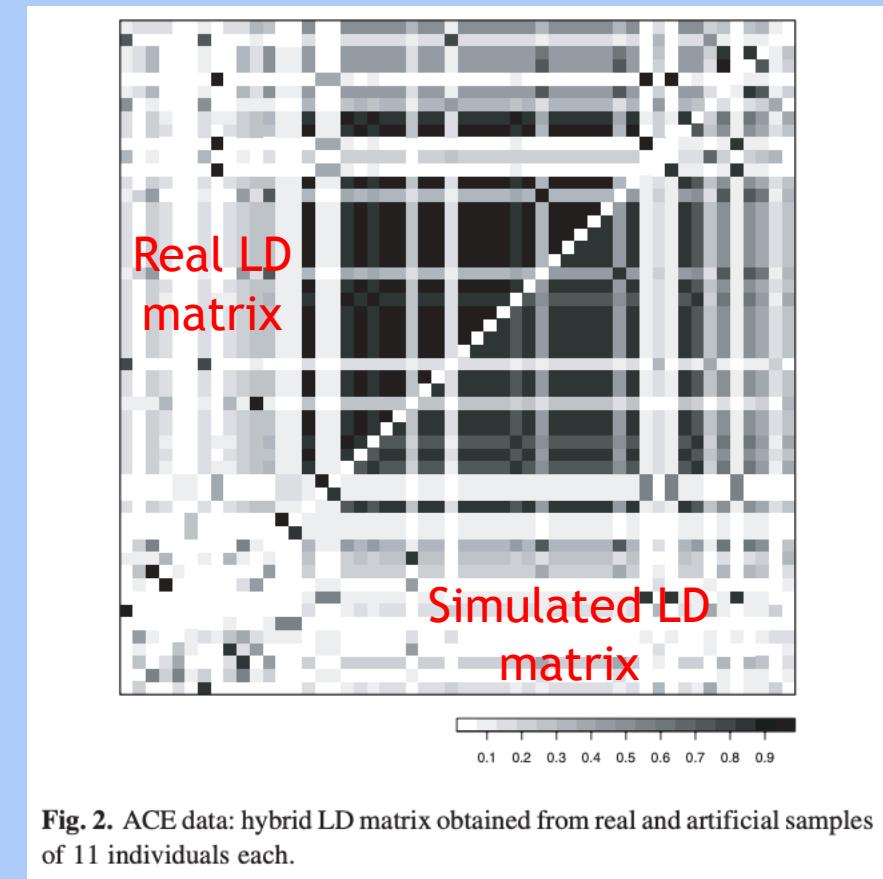
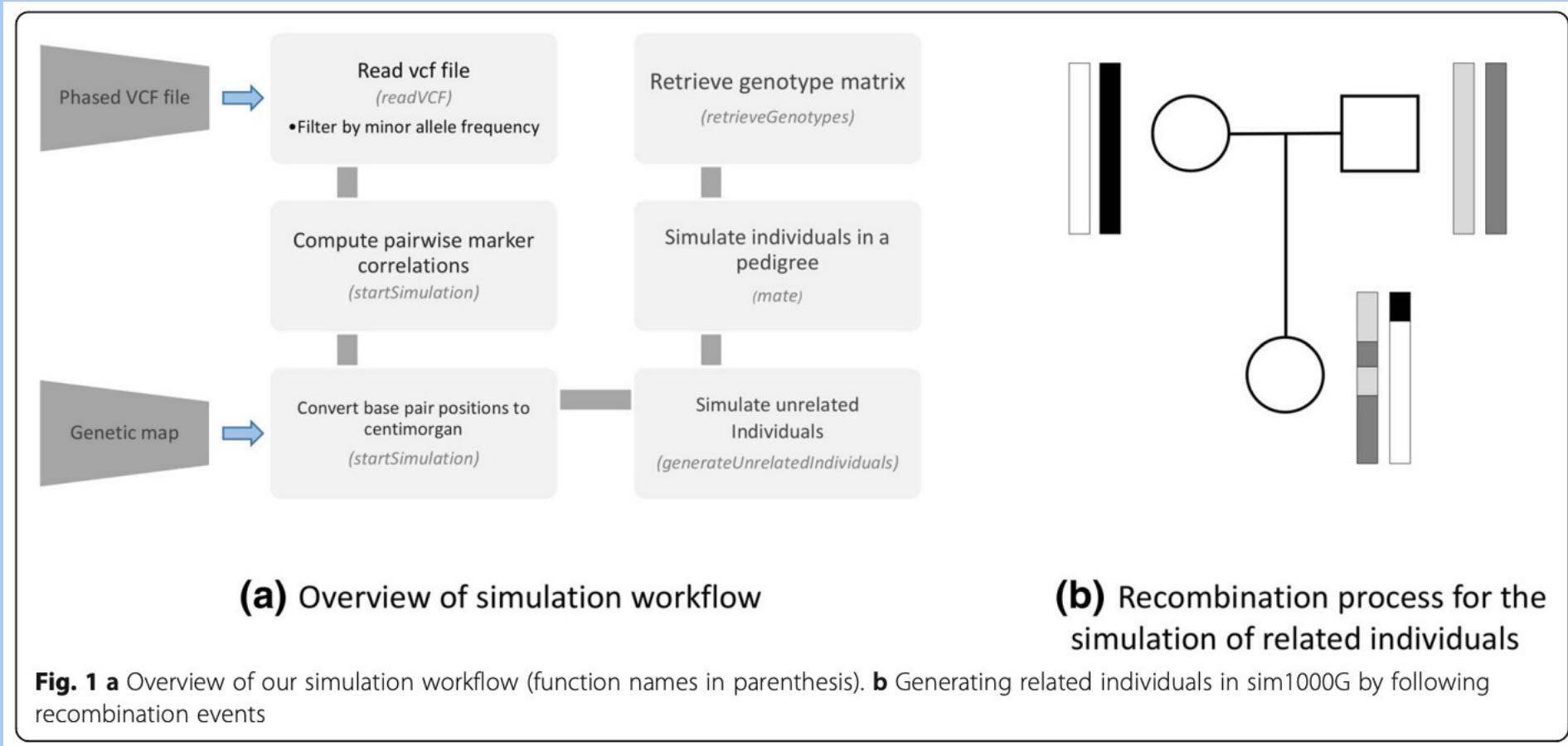


Fig. 2. ACE data: hybrid LD matrix obtained from real and artificial samples of 11 individuals each.

<https://pubmed.ncbi.nlm.nih.gov/16188927/>

sim1000G: simulate haplotypes from an input vcf

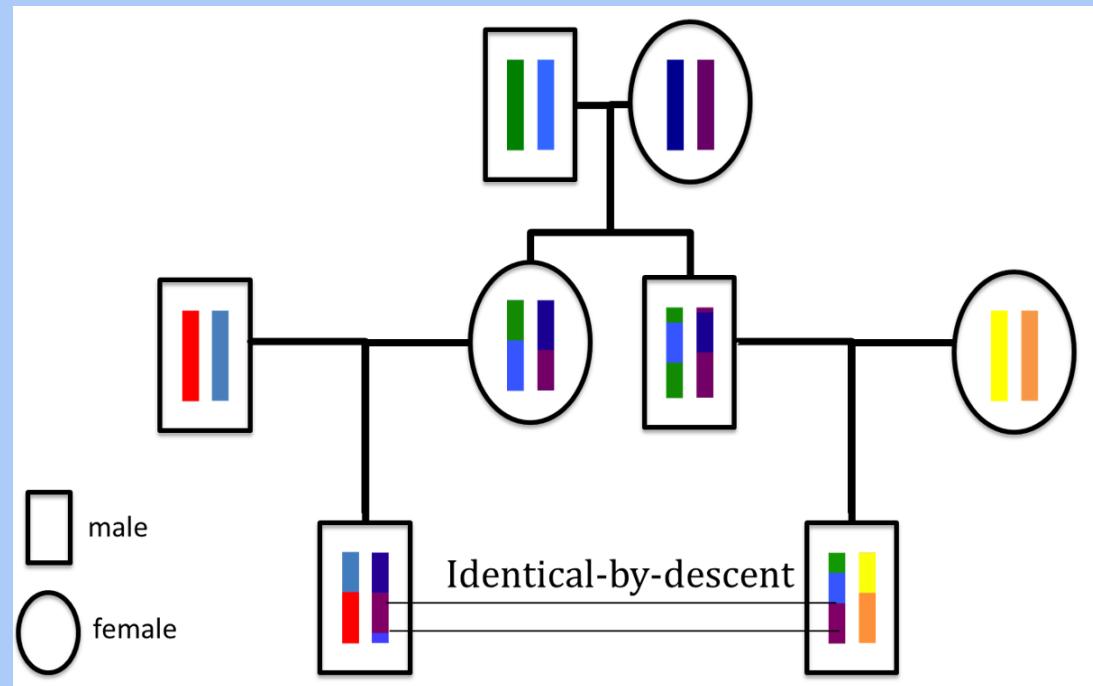


<https://pubmed.ncbi.nlm.nih.gov/30646839/>

Kinship analysis

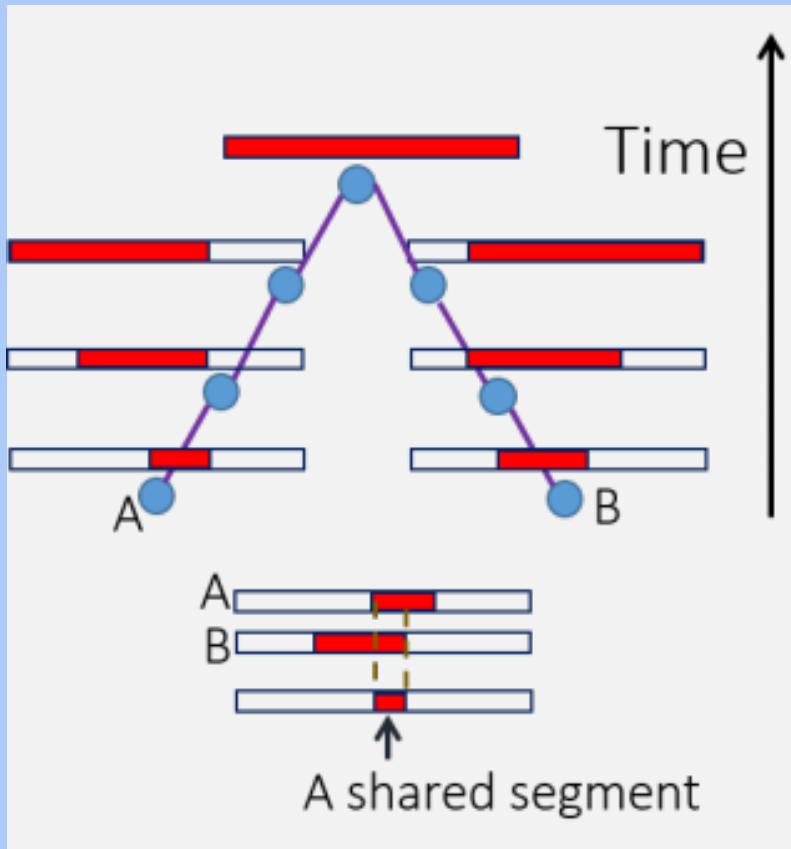
The concept of genetic relatedness

Relatives share haplotypes IBD



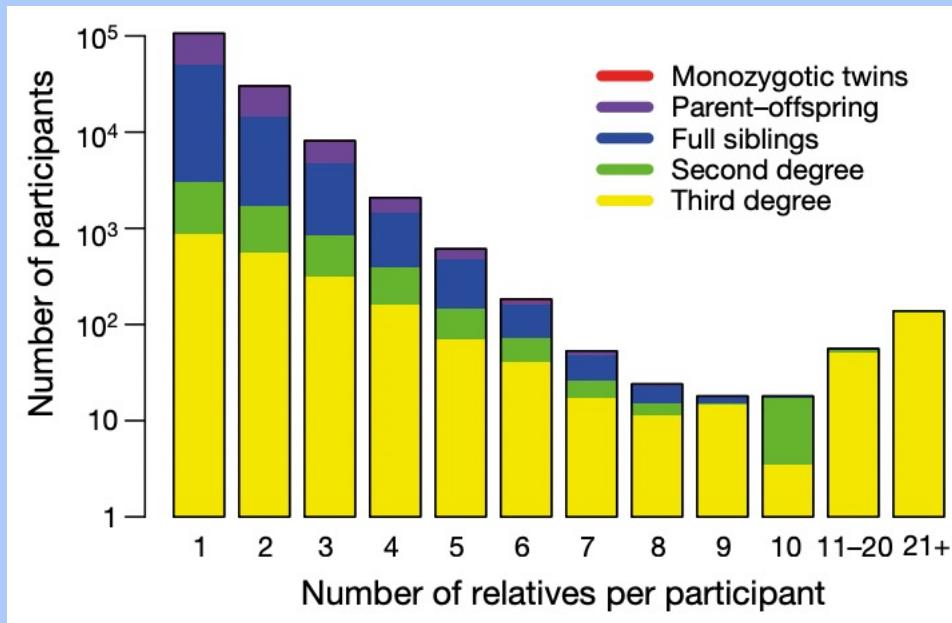
- Segments of DNA inherited from a common ancestor are said to be **identical by descent**
- DNA that just happens to be the same is **identical by state**

Haplotype sharing decays over time



- The longer the IBD segment, the more closely related are the two individuals

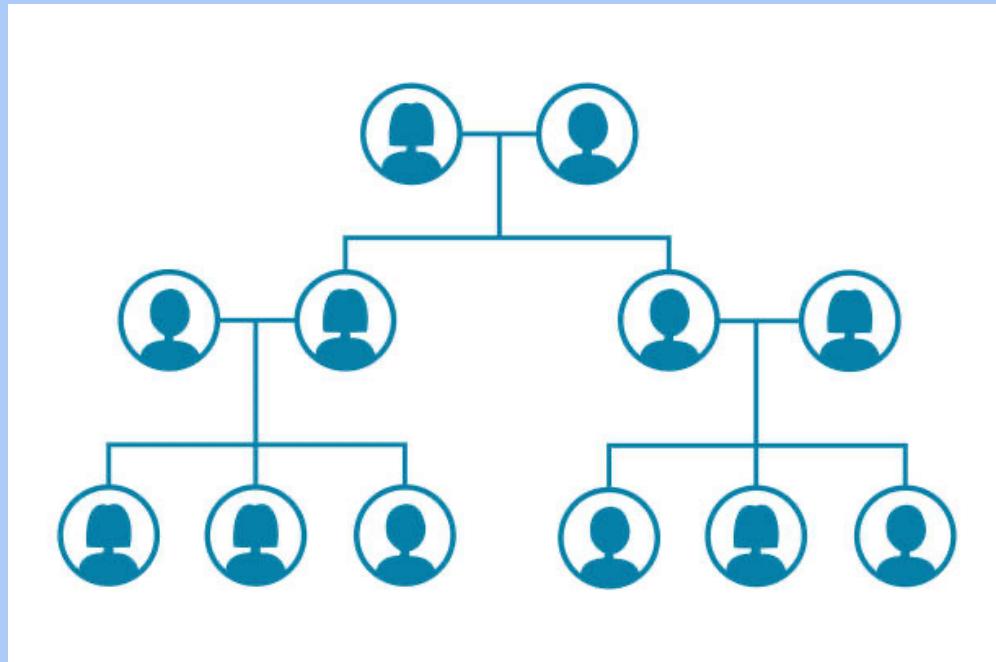
Kinship in genetic association studies



<https://pubmed.ncbi.nlm.nih.gov/30305743/>

- Genomic datasets, such as the UK Biobank, contain related individuals
- Sometimes there is even “cryptic” relatedness
- Because of IBD sharing, not all the observations are independent, and genotype-phenotype associations may be confounded

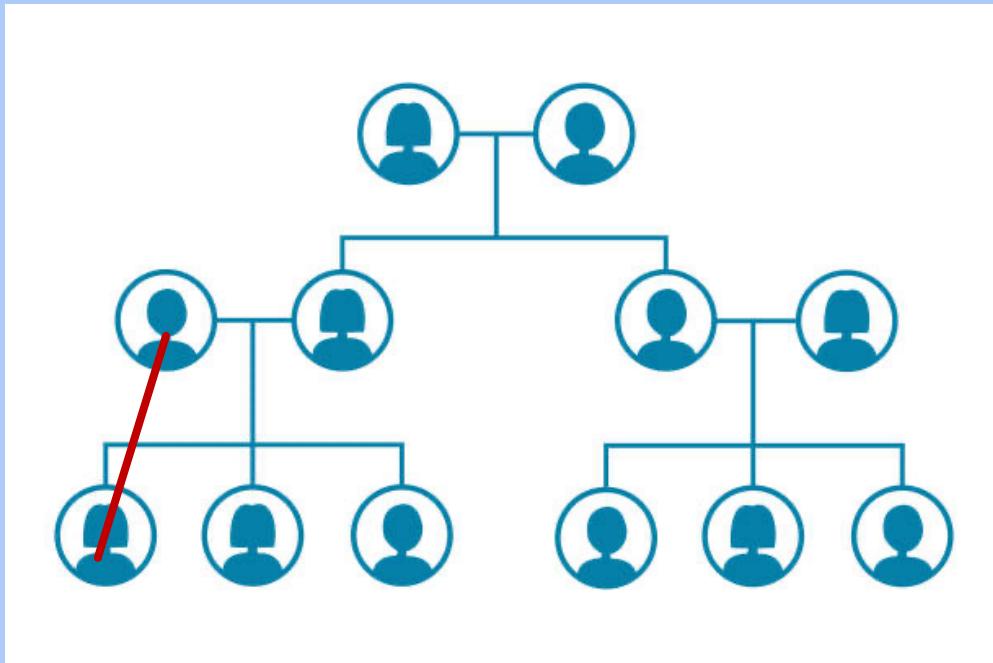
Degree of relatedness



- R is the effective number of meioses separating two individuals through their two parents 1 and 2
- $R \rightarrow \infty$ for unrelated individuals

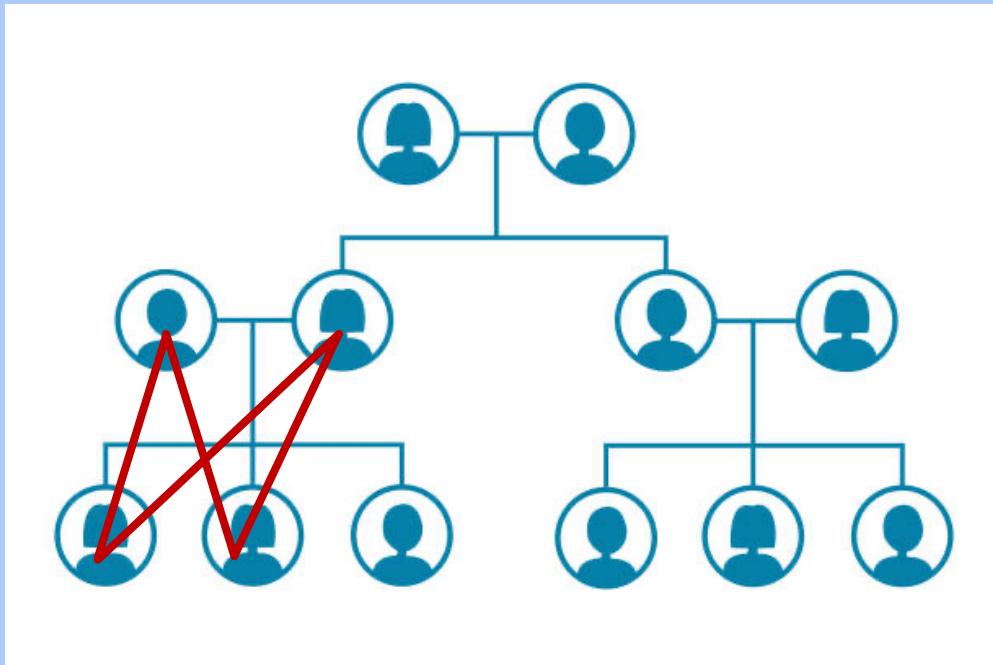
$$\frac{1}{2^R} = \frac{1}{2^{R_1}} + \frac{1}{2^{R_2}}$$

Degree of relatedness



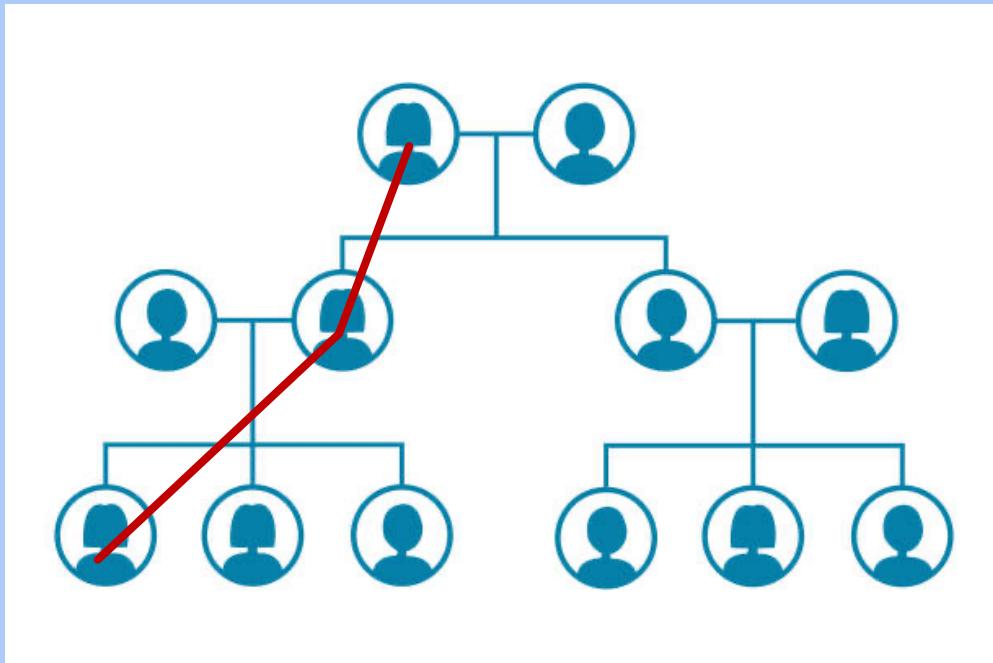
- Parent-child: $R = 1$
meiosis

Degree of relatedness



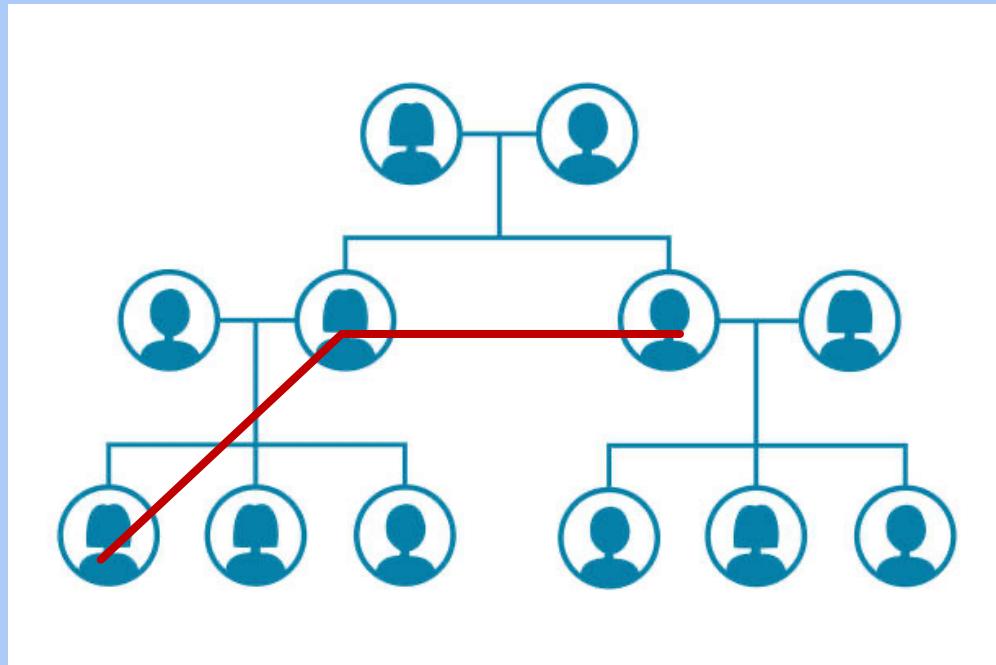
- Siblings: $R = 1 / 2^1 = 1 / 2^2 + 1 / 2^2$ “effective” meiosis:

Degree of relatedness



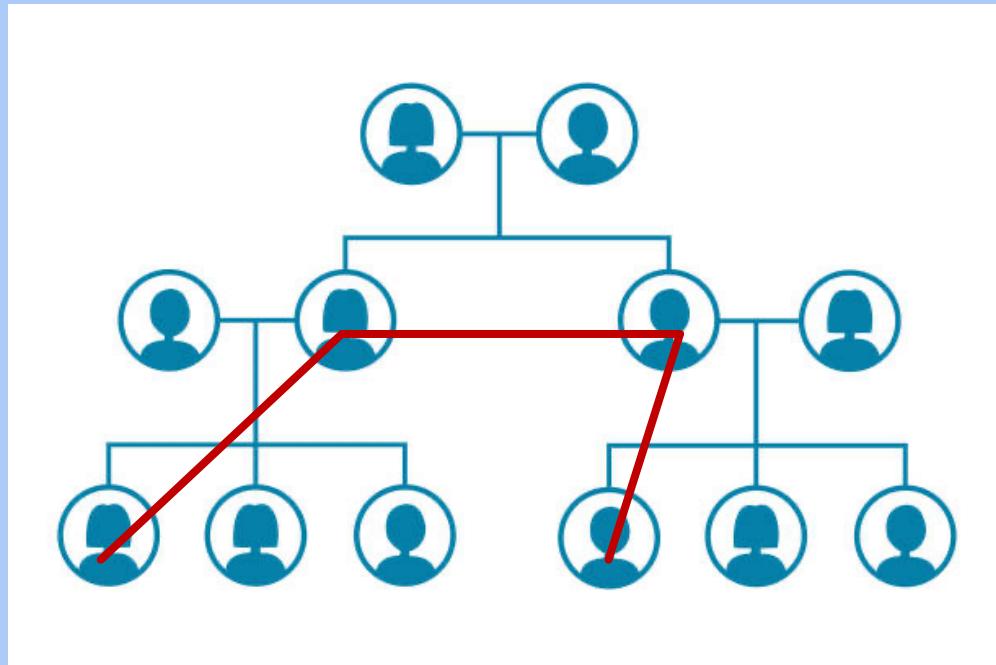
- Grandparent-grandchild:
 $R = 2$ meioses

Degree of relatedness



- Avuncular: $R = 2$ meioses

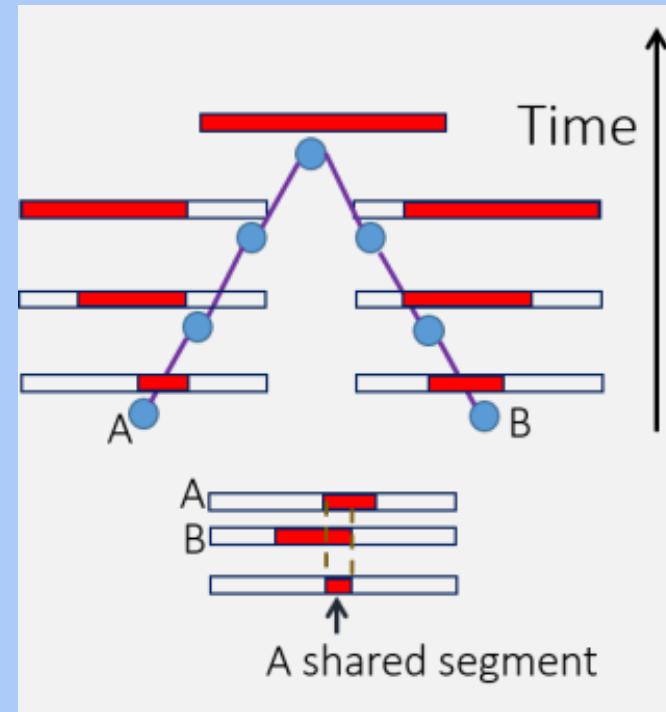
Degree of relatedness



- Cousins: $R = 3$ meioses

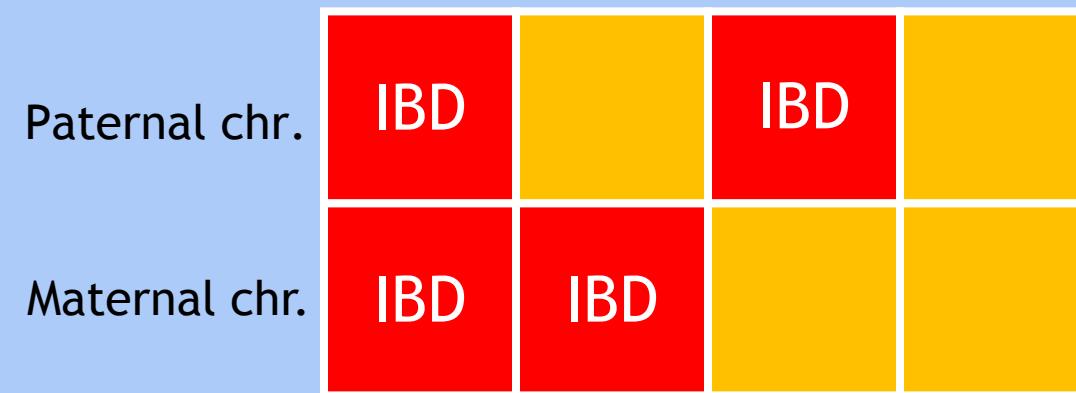
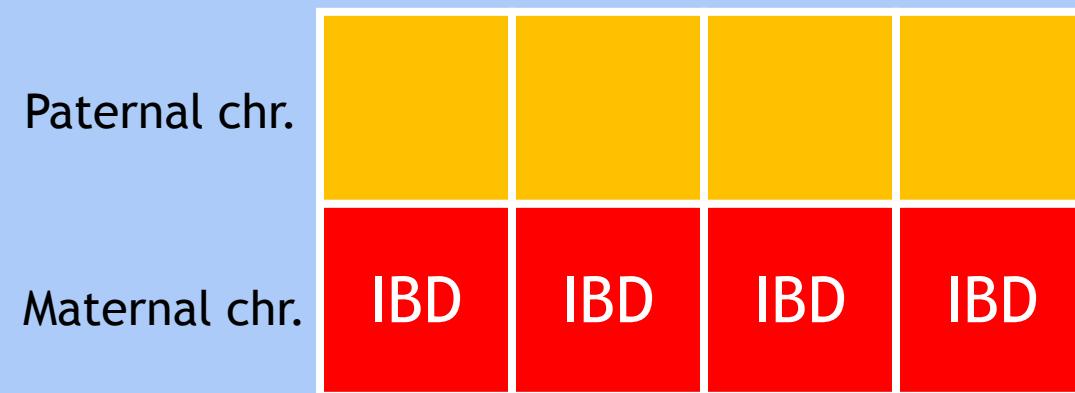
Degree of relatedness and the fraction of the genome shared IBD

- $r = 1 / 2^R$ is the fraction of the genome shared IBD, because there is a $1/2$ probability that the gene is passed on in each of R meioses



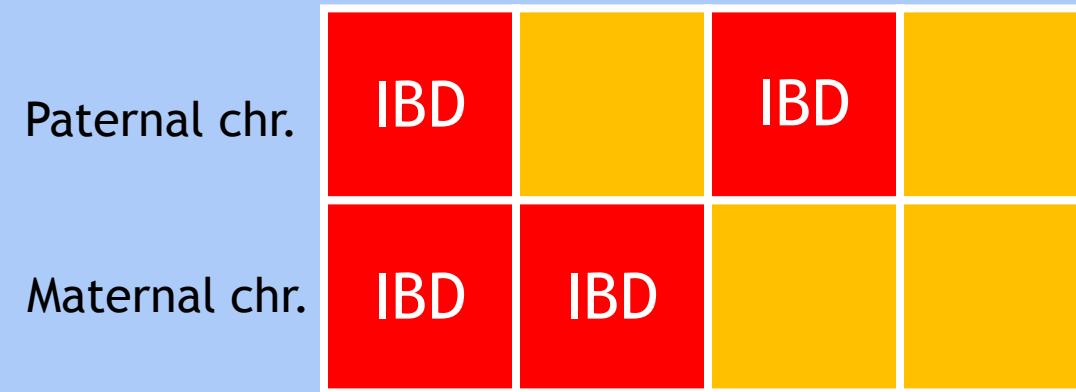
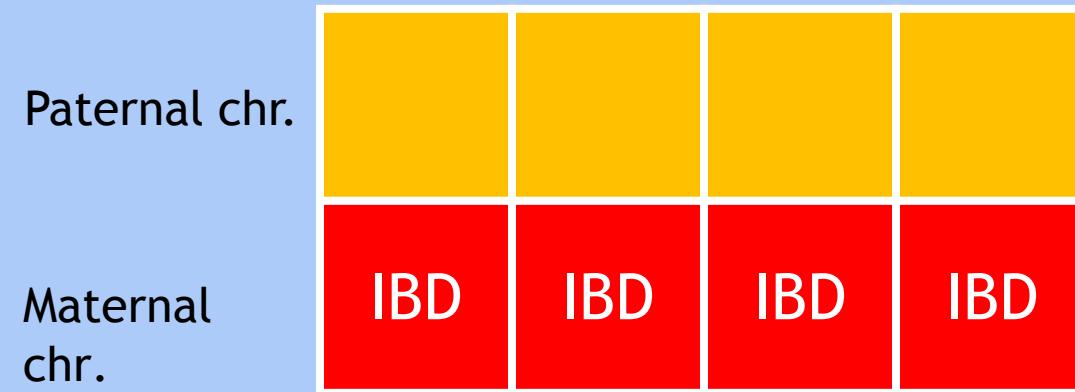
Degree of relatedness and the fraction of the genome shared IBD

- A child shares **half** of its DNA with its parent
- A child shares (a different) **half** its DNA with its full sib



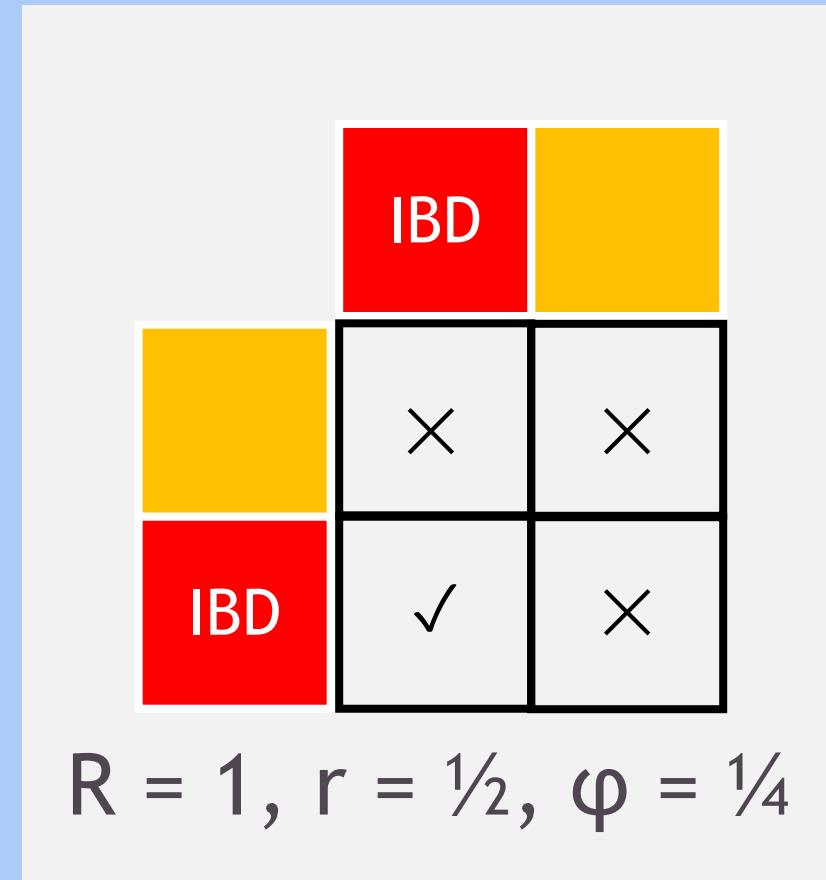
Degree of relatedness and the fraction of the genome shared IBD

- A child has 0 probability of IBD = 0 with its parent
- A child has 0.25 probability of IBD = 0 with its sib



The coefficient of relatedness φ

- φ is the probability that any two alleles at a single locus chosen from two individuals are shared IBD
- φ is equal to half of $r = 1 / 2^R$



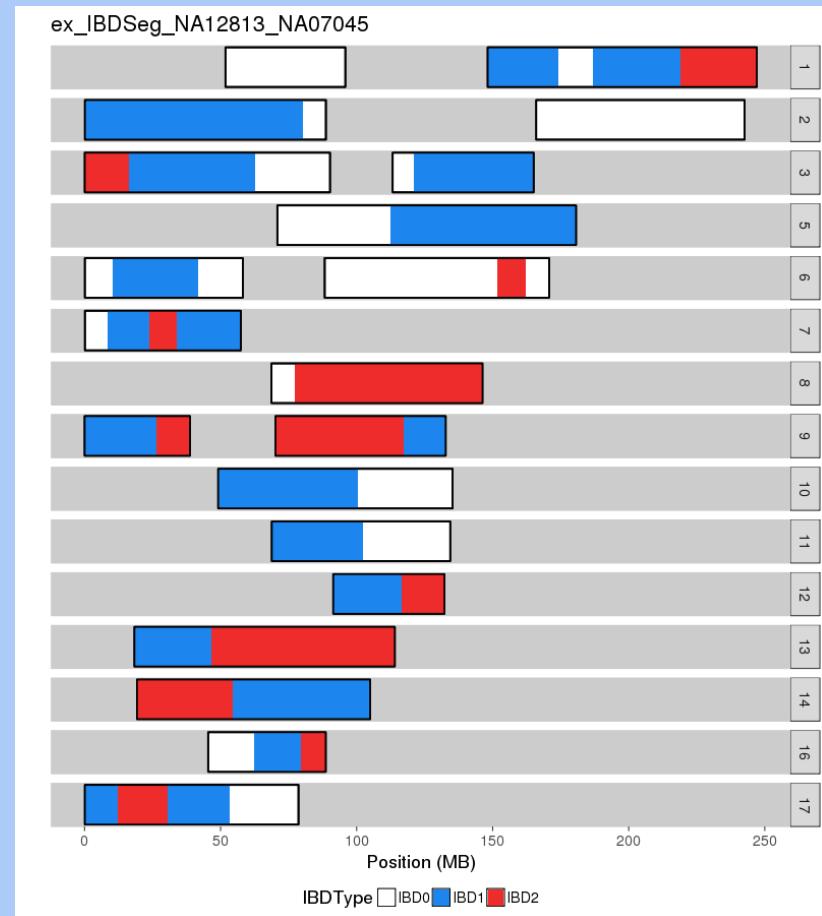
Coefficient of relatedness and IBD = 0

- φ decreases as the probability that a pair of individuals should be IBD = 0 increases

Relationship	R	φ	IBD = 0
Monozygotic twins	0	0.5	0
Parent-child	1	0.25	0
Full sibs	1	0.25	0.25
2 nd degree	2	0.125	0.5
3 rd degree	3	0.0625	0.75
Unrelated	∞	0	1

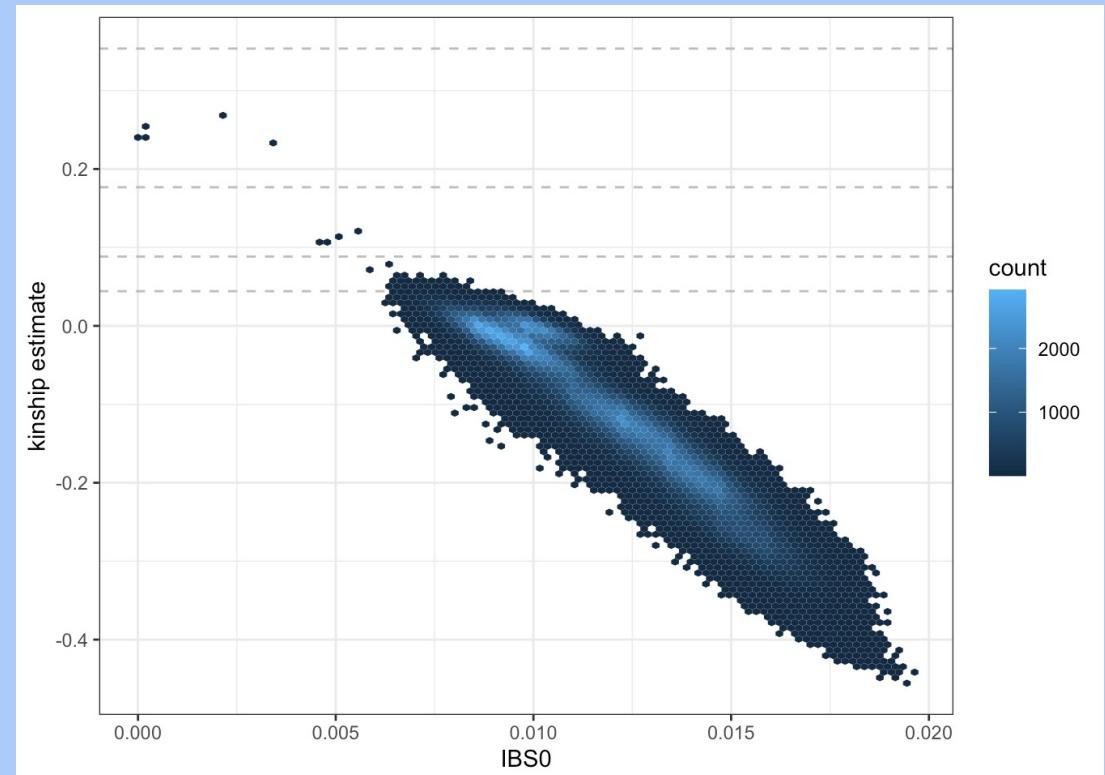
Kinship-based Inference for GWAS (KING)

- Estimate φ and IBD sharing from the number of sites at which two individuals are both heterozygotes (Aa, Aa) or opposite homozygotes (AA, aa)
- Avoids estimating population allele fractions, just focuses on pairs



Kinship-based Inference for GWAS (KING)

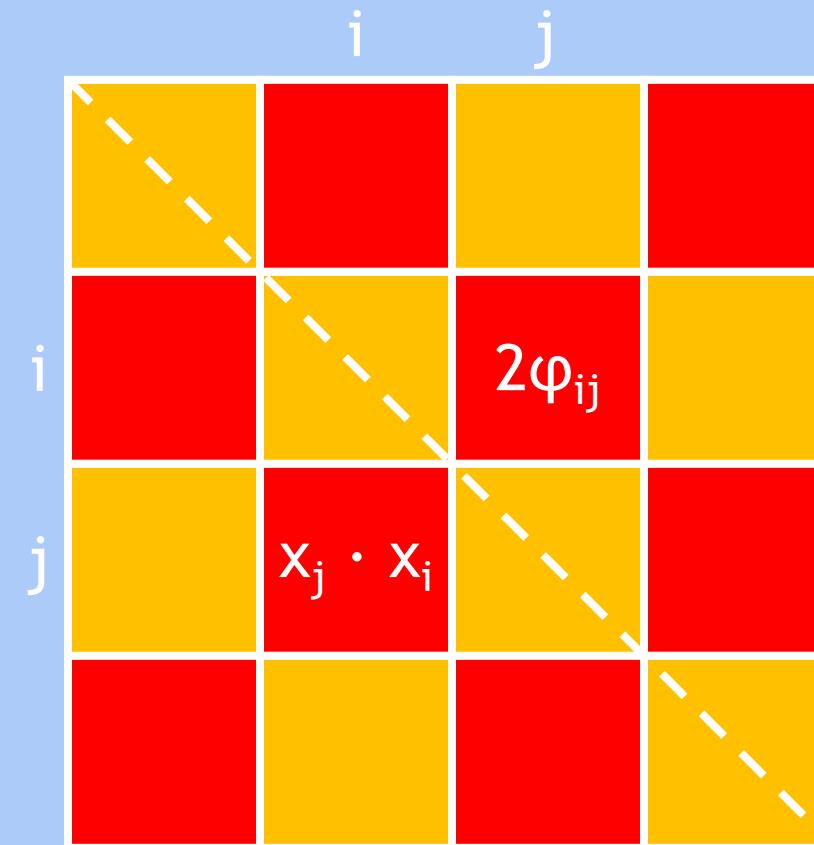
- φ is plotted vs. the fraction of IBS = 0 sites (AA,aa)
- Negative estimates indicate unrelated individuals from different populations



https://uw-gac.github.io/SISG_2021/ancestry-and-relatedness-inference.html

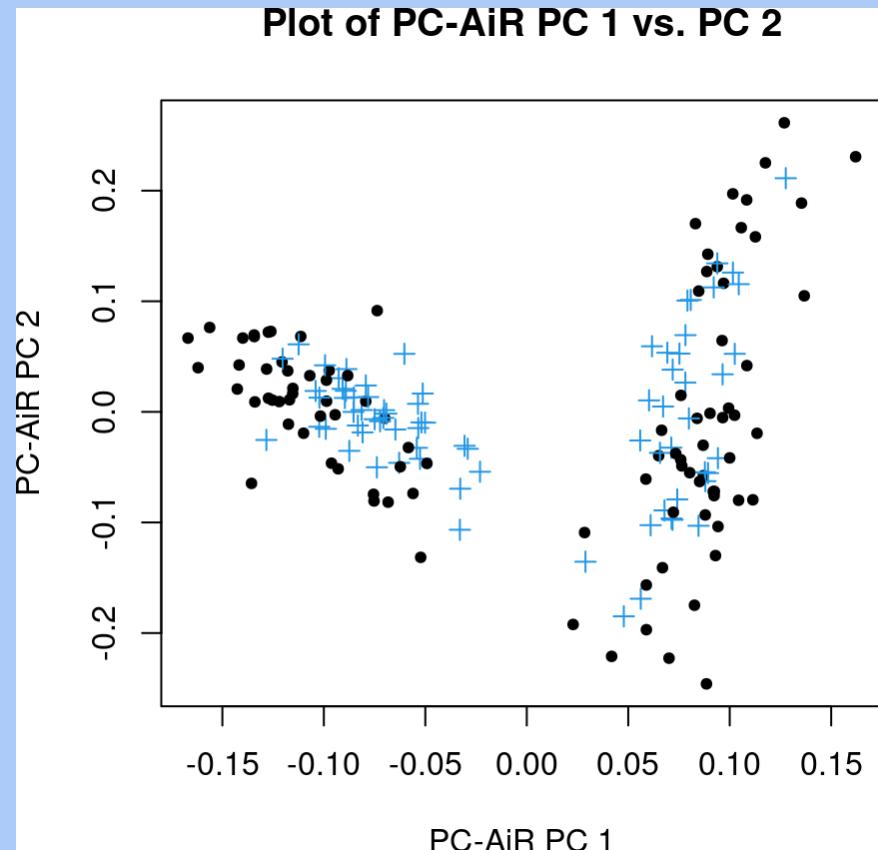
Updating the GRM

- The KING kinship coefficients 2φ are approximately equal to the GRM, but the estimate may be biased by population structure



PC-AiR: PCA in Related Samples

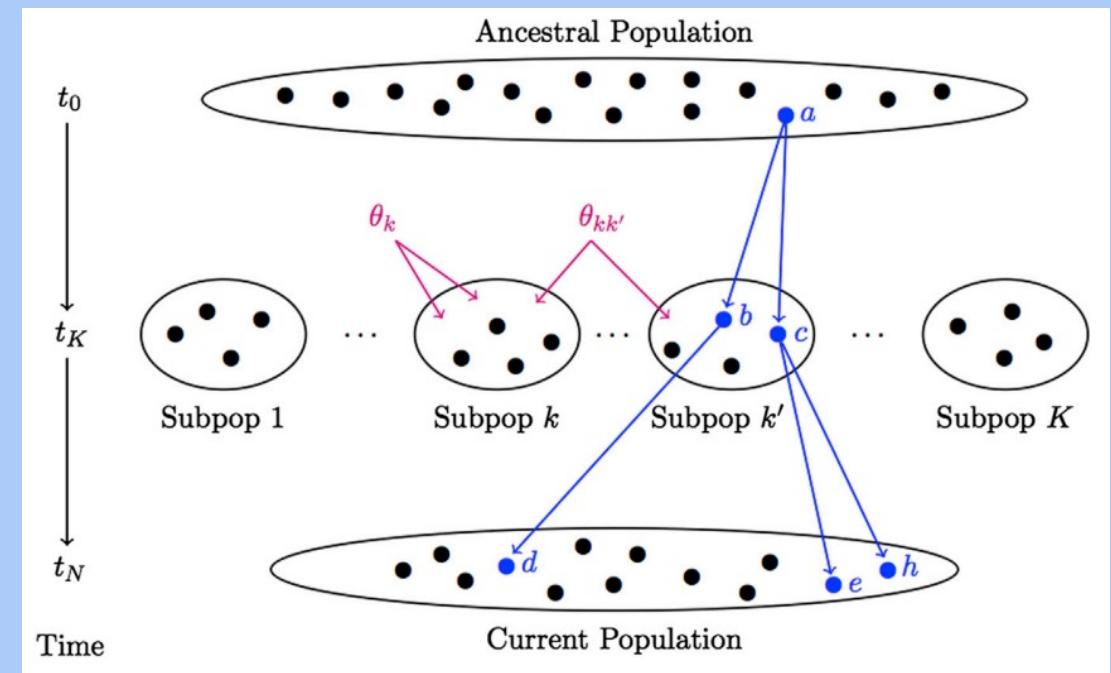
- Based on the KING estimates, PC-AiR computes PCs for a set of unrelated individuals (black)
- PCs for the remaining samples (blue) are estimated from their similarity to the unrelated subset



<https://bioconductor.org/packages/devel/bioc/vignettes/GENESIS/inst/doc/pcair.html>

PC-Relate

- PC-Relate uses the updated PCs to correct the GRM for population structure
- The updated GRM reflects recent kinship only



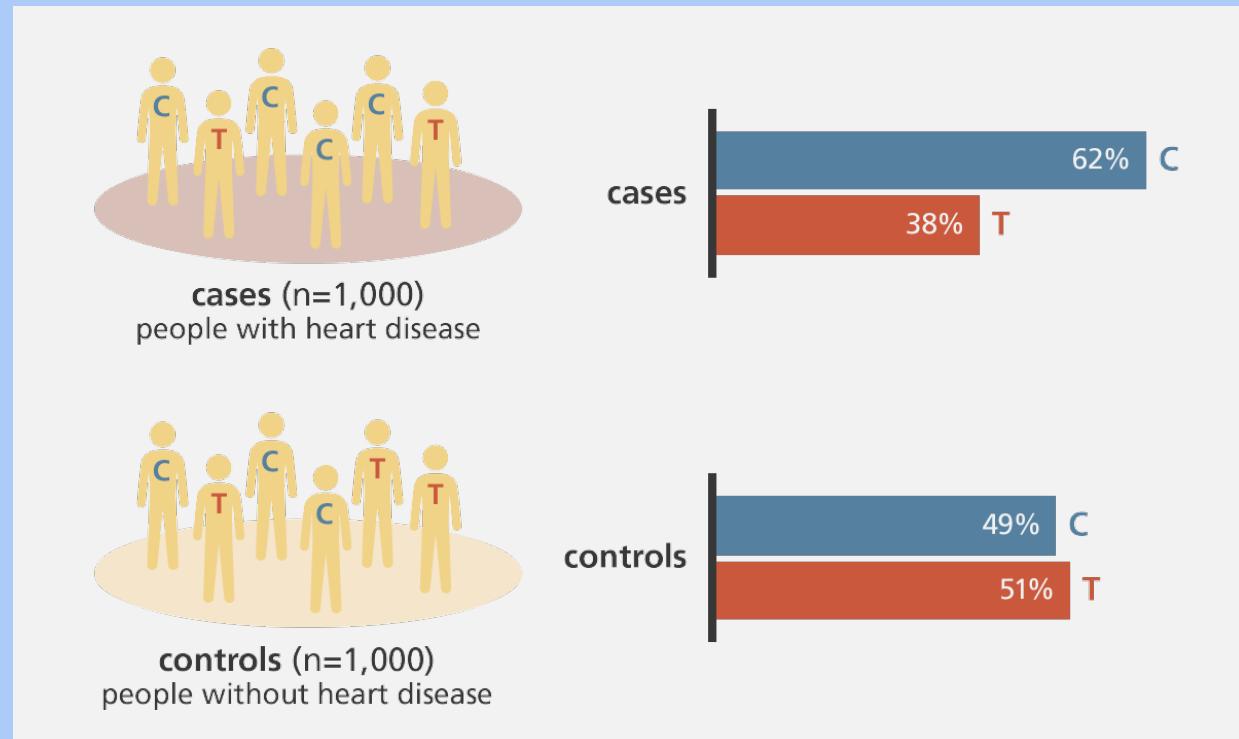
<https://pubmed.ncbi.nlm.nih.gov/26748516/>

Association testing

Logistic regression and linear mixed models

Case-control studies

- Is a genetic variant associated with disease?
- Is a genetic variant enriched in people with disease compared to people without?
- To find out, collect many people with disease (Cases) and many healthy individuals (Controls) from the same population



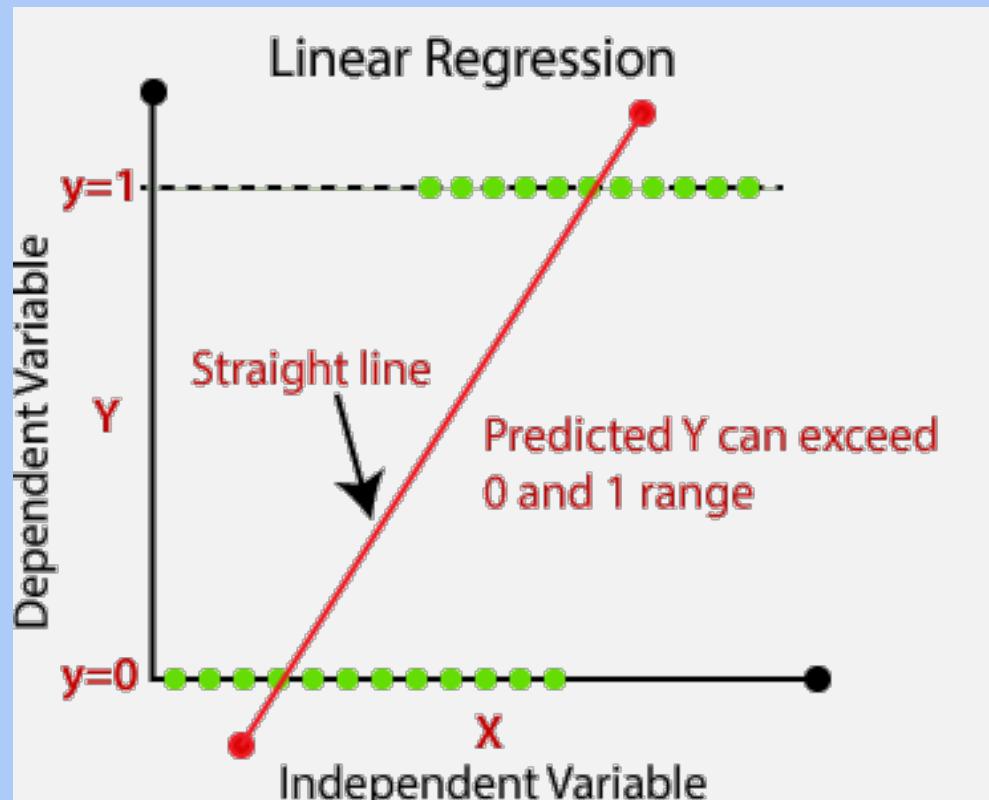
The odds ratio

- The OR is the ratio of the odds that Cases have the risk allele ($620 / 380$) to the odds that Controls have the risk allele ($490 / 510$)
- The OR is a **crude** measure of association that is not **adjusted** for other covariates (age, sex, ethnicity, etc.) that may also be associated with disease

	Cases	Controls
C	620	490
T	380	510

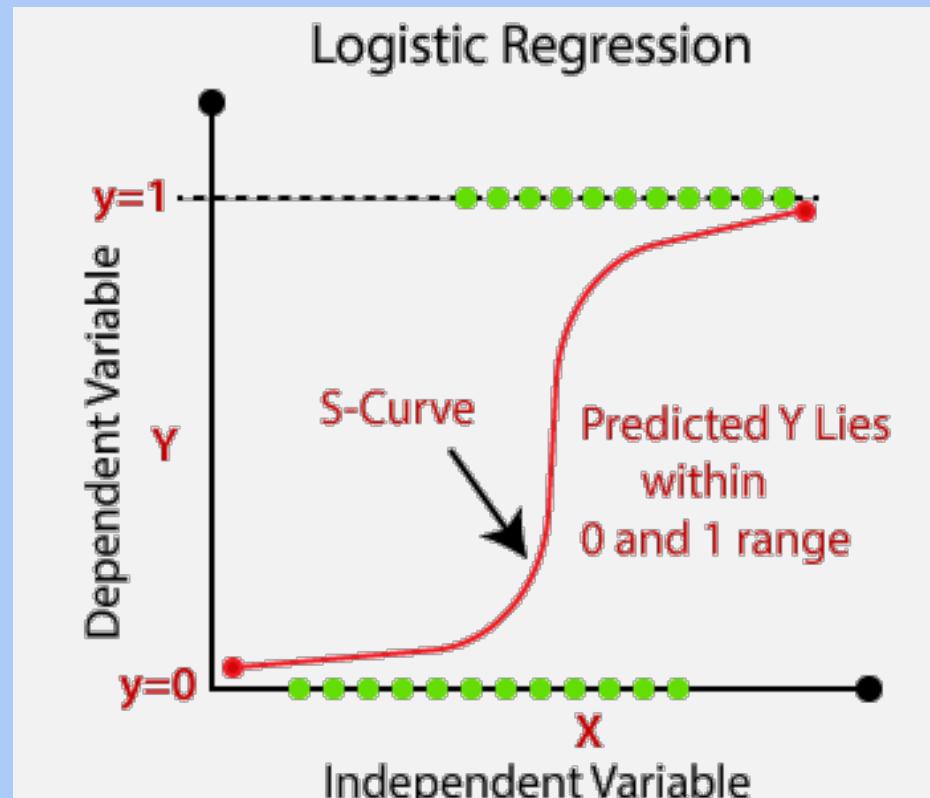
$$OR = (620 \times 510) / (490 \times 380) = 1.70$$

Linear vs. logistic regression



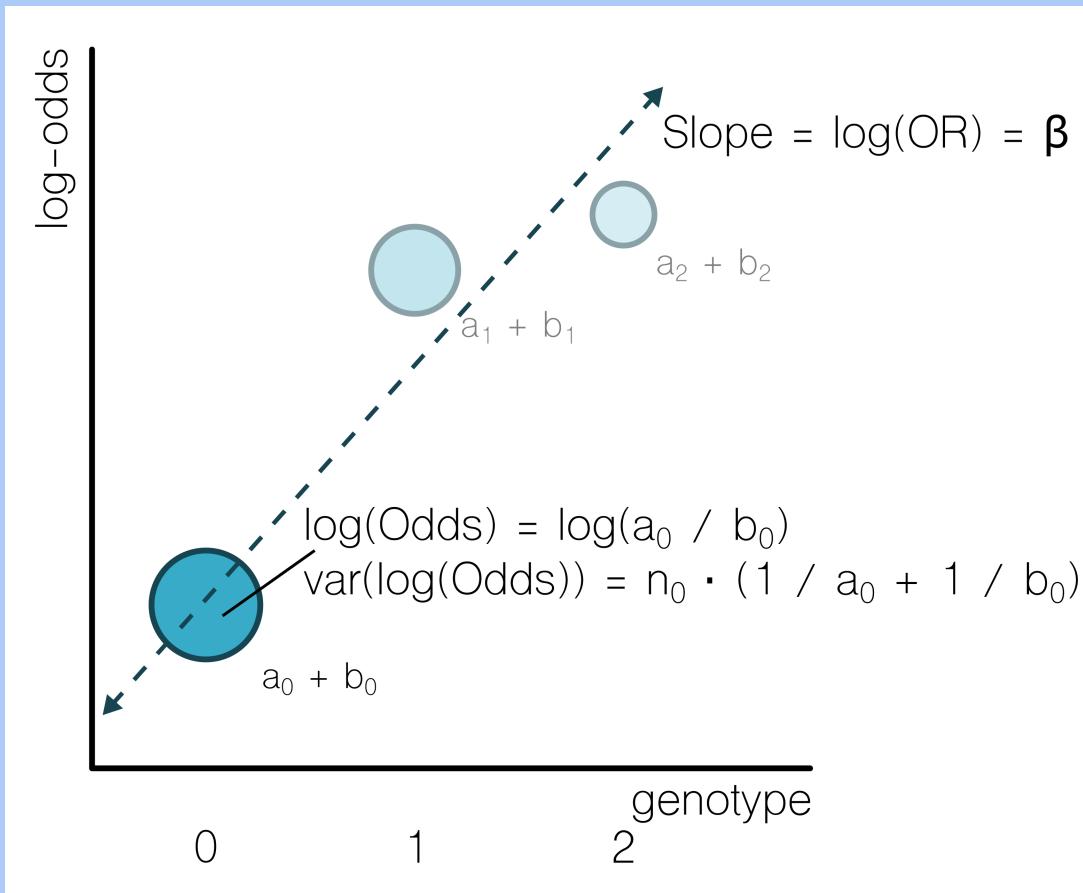
- In linear regression, we can find the association of a **continuous variate Y** with a predictor X_1 and other covariates X_2, X_3 , etc.

Linear vs. logistic regression



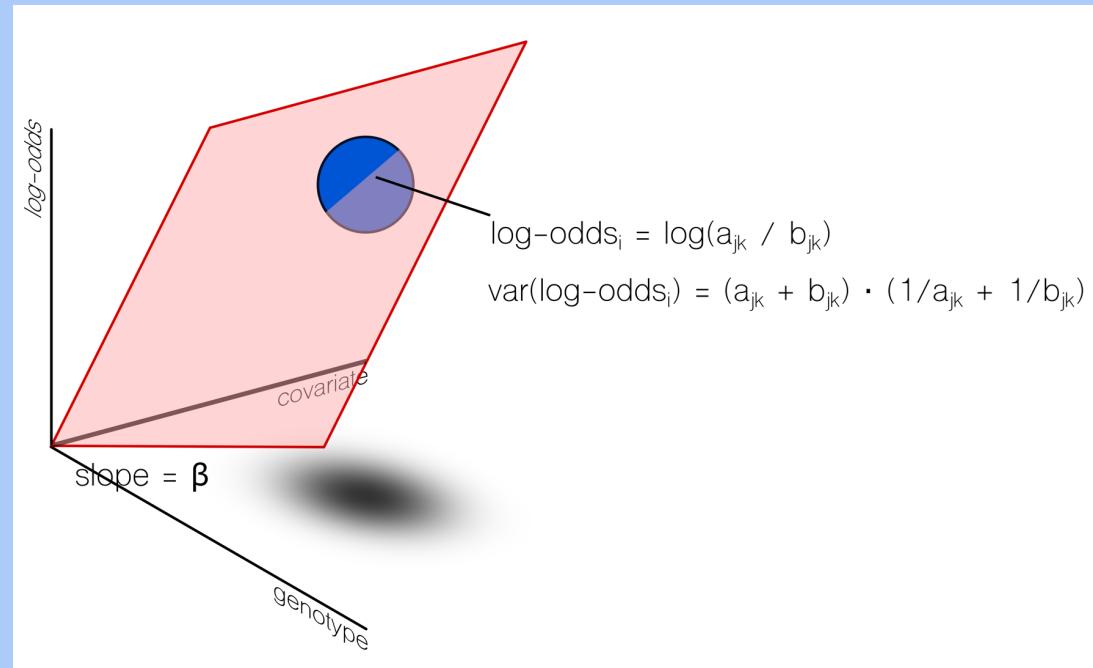
- In logistic regression, we can find the association of a **binary variate** Y with a predictor X_1 and other covariates X_2, X_3 , etc.
- The sigmoid curve is an individual's probability of developing disease

Linear vs. logistic regression



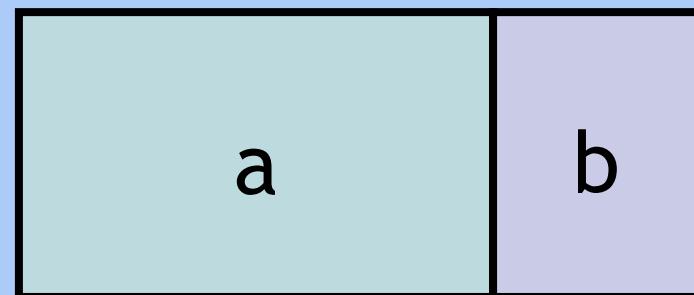
- Logistic regression can be thought of like linear regression is we transform the OR into the $\log(\text{OR})$ and regress vs. SNP genotype

Linear vs. logistic regression



- Other covariates can be accounted for as additional independent variables
- The model is actually fit using the principle of **maximum-likelihood**

Simulating a binary phenotype

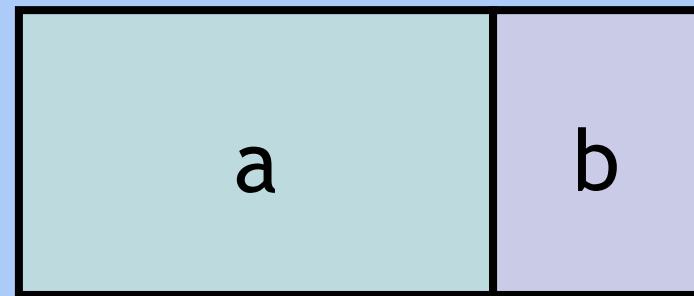


- If odds = a / b , then prob = $a / (a + b) = \text{odds} / (1 + \text{odds})$

Simulating a binary phenotype

$$\log(\text{odds}) = \beta_0 + X_1\beta_1$$

- β_0 is the baseline odds
- β_1 is the log-OR
- X_1 is the SNP genotype

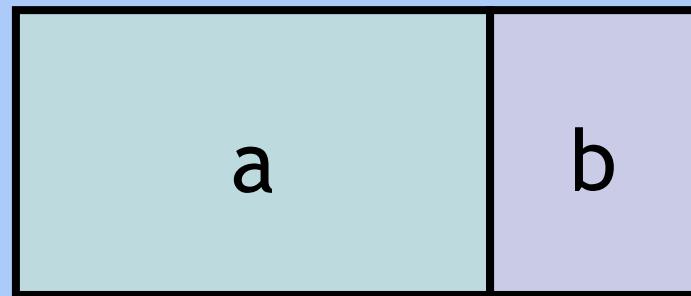


- If odds = a / b , then prob = $a / (a + b) = \text{odds} / (1 + \text{odds})$

Simulating a binary phenotype

$$\text{prob} = \frac{e^{\beta_0 + X_1 \beta_1}}{1 + e^{\beta_0 + X_1 \beta_1}}$$

- prob is the probability of developing disease (being a Case in the study)

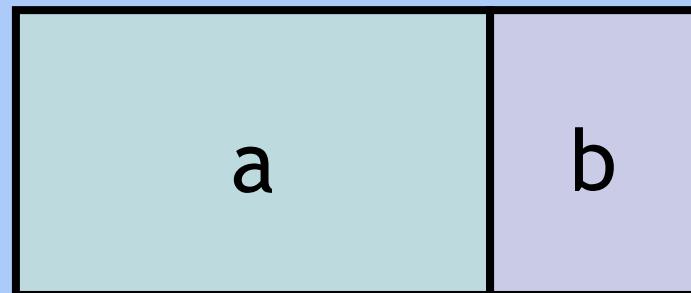


- If odds = a / b, then prob = a / (a + b) = odds / (1 + odds)

Simulating a binary phenotype

$$\text{prob} = \frac{e^{(X_1 - \bar{X}_1)\beta_1}}{1 + e^{(X_1 - \bar{X}_1)\beta_1}}$$

- β_0 becomes the mean log-odds so that the mean odds of disease is 1 (50% Cases, 50% Controls)

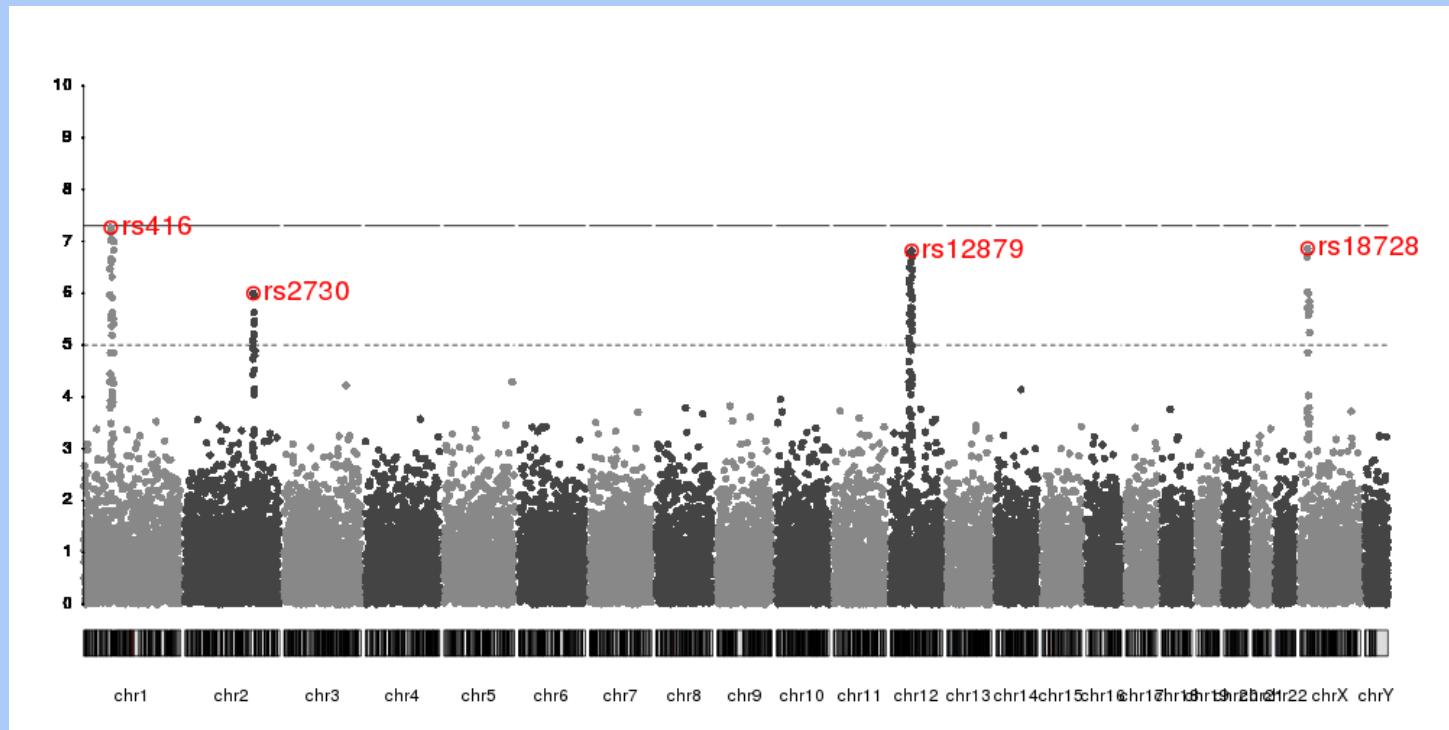


- If odds = a / b, then prob = a / (a + b) = odds / (1 + odds)

Estimating the SNP effect

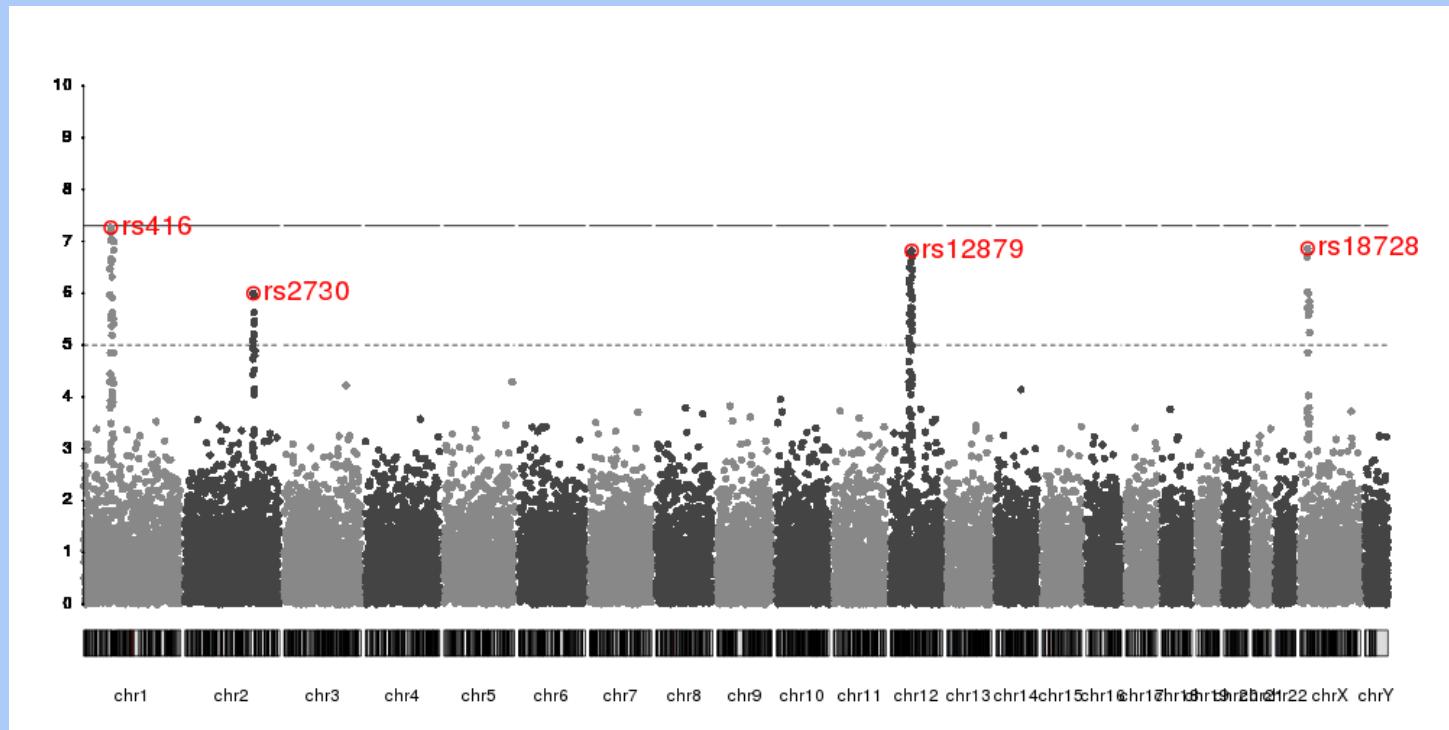
- We want to be able to **detect** the association of one SNP with disease by fitting the model $Y = \beta_0 + \beta_1 X_1 + \dots$ and finding a slope β_1 significantly different from 0

Estimating the SNP effect



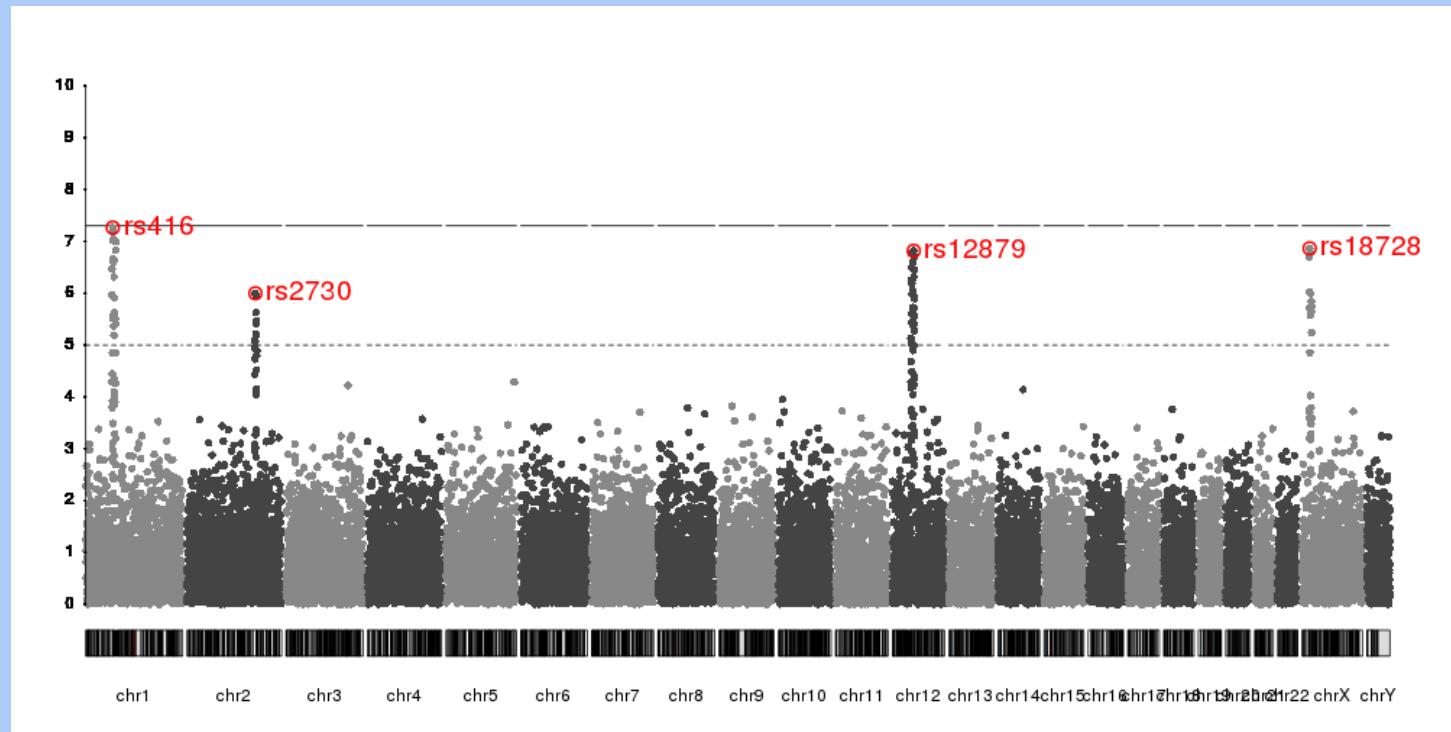
- A **Manhattan plot** gives the p-value of the log-OR estimate for each SNP

Estimating the SNP effect



- Because there are more SNPs than subjects, we cannot fit all SNPs at once

Estimating the SNP effect

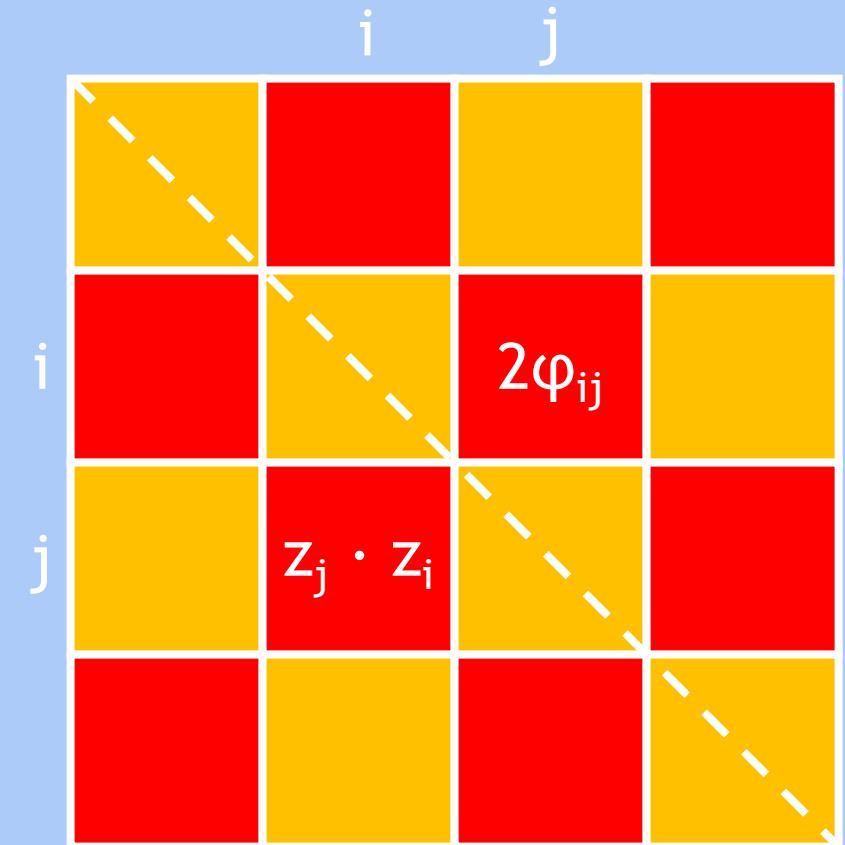


- But we can fit one SNP plus the “average” effect of all the remaining SNPs

Linear mixed models

- The solution for the **best estimate** of the SNP effect β_1 in the presence of all the remaining SNPs involves the GRM ZZ^T

$$\mathbf{X}^T (\mathbf{I} + \mathbf{Z}\mathbf{Z}^T)^{-1} \hat{\beta} = \mathbf{X}^T (\mathbf{I} + \mathbf{Z}\mathbf{Z}^T)^{-1} \mathbf{Y}$$



Linear mixed models

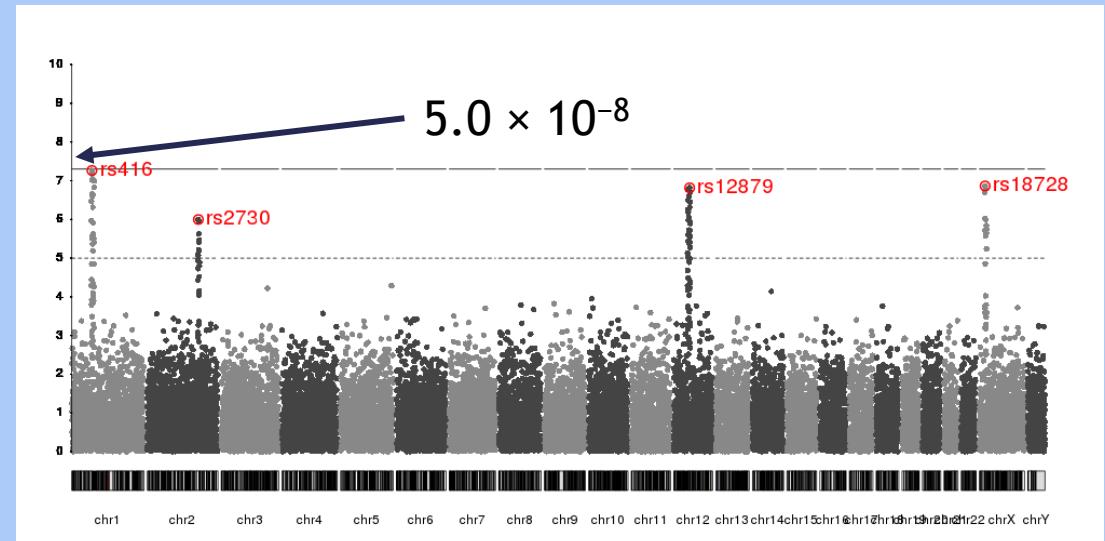
- Other covariates commonly included in the model are age, sex, and the first few genotype principal components (from PC-AiR)

Linear mixed models

- If the model including the SNP represents a significant improvement over the **null model** (the model without the SNP), we can reject the null hypothesis that the OR = 1

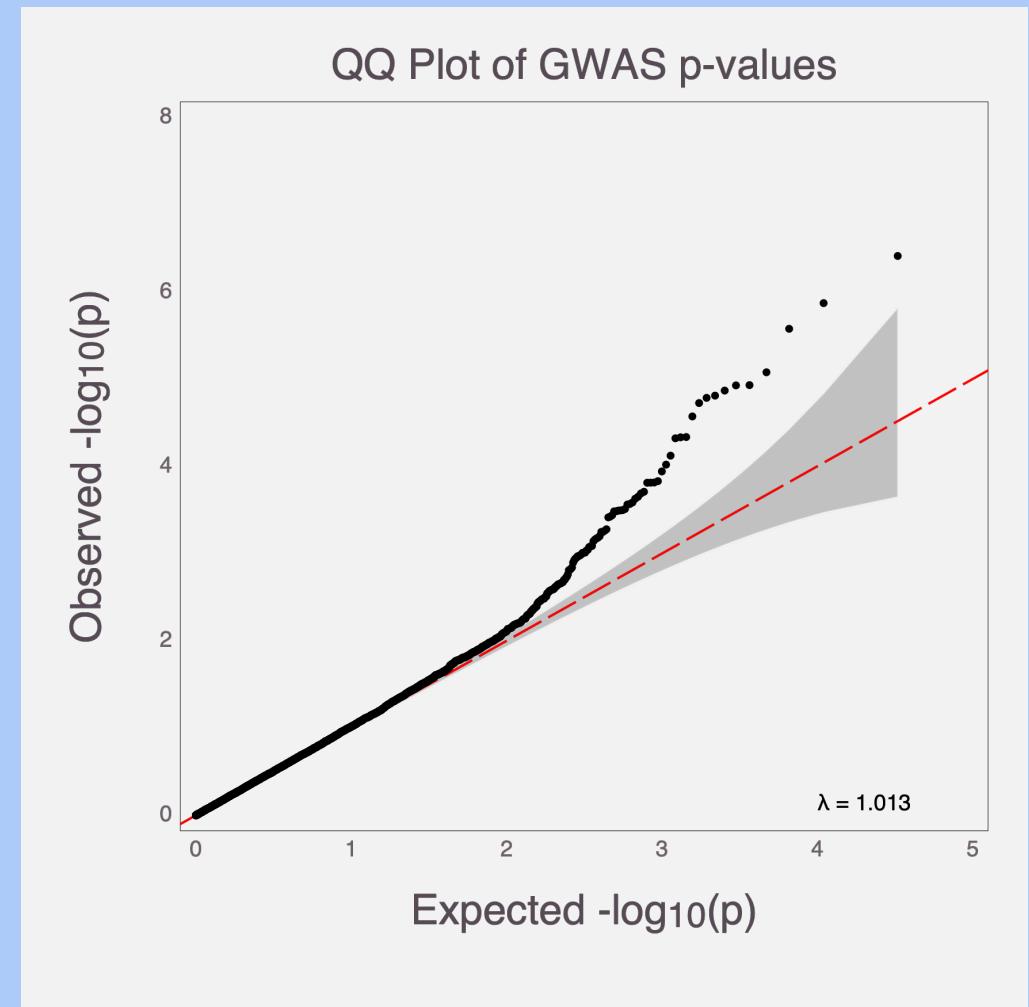
Linear mixed models

- But because of **multiple-testing**, our p-value threshold is $0.05 / 10^6$ (i.e., you perform the same test 10^6 times)
- SNPs with $p < 5.0 \times 10^{-8}$ are said to achieve **genome-wide significance**



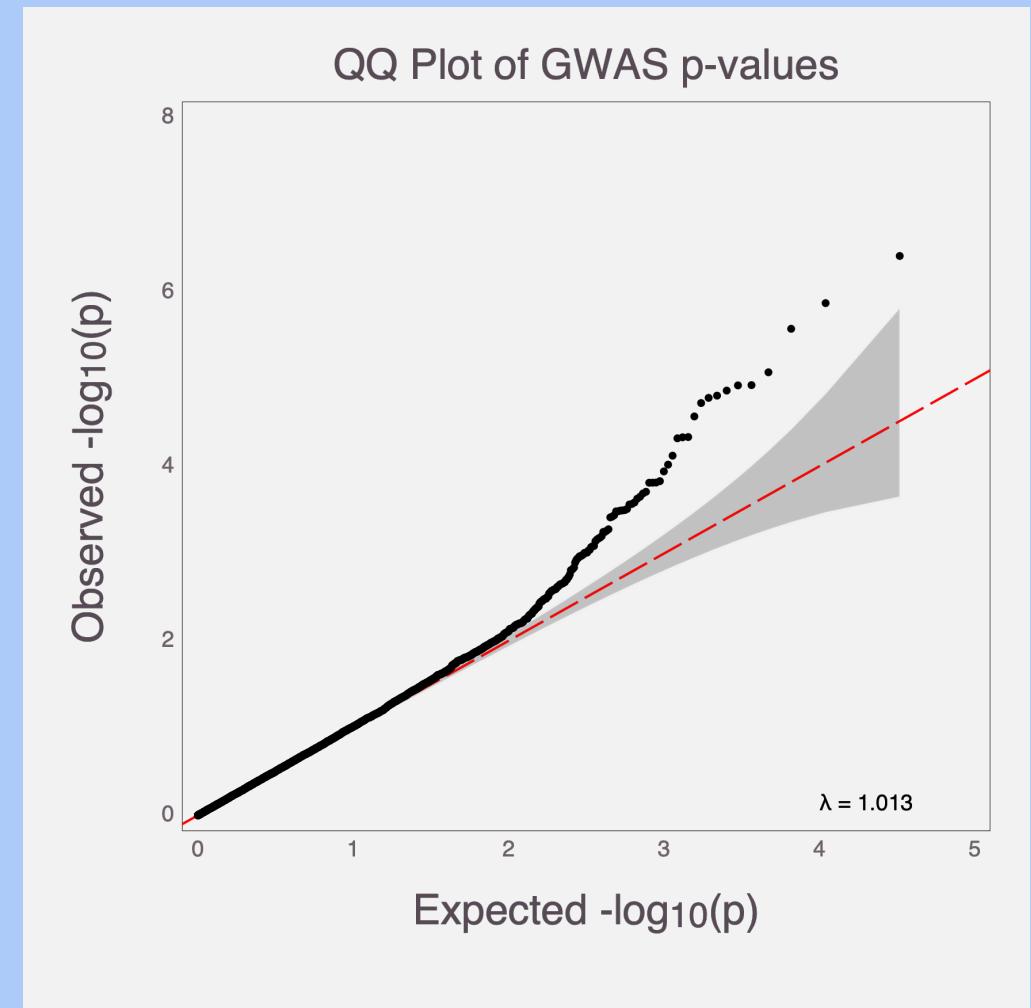
QQ plots

- To assess if the distribution of SNP effects is significantly different from that expected by chance, we make a quantile or QQ plot



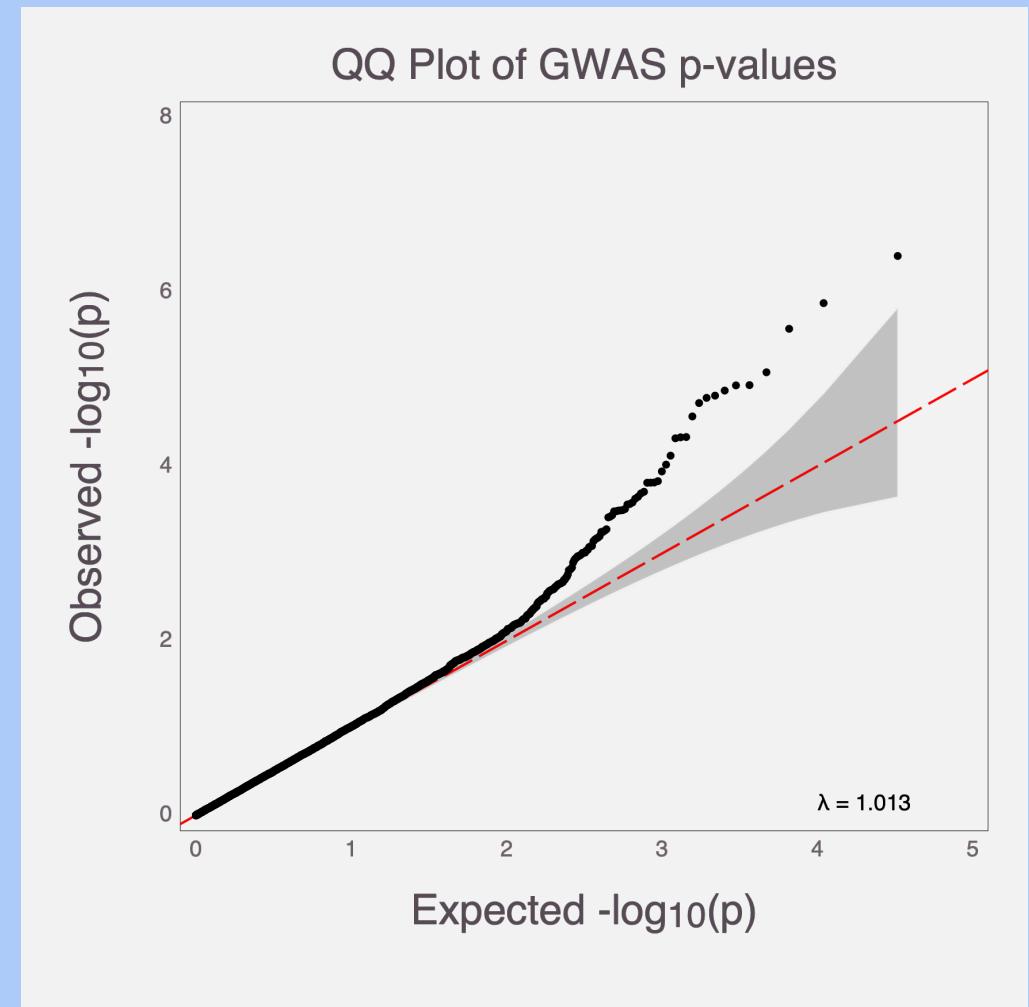
QQ plots

- Put the **observed** p-value (negative log-10) in order from smallest to biggest



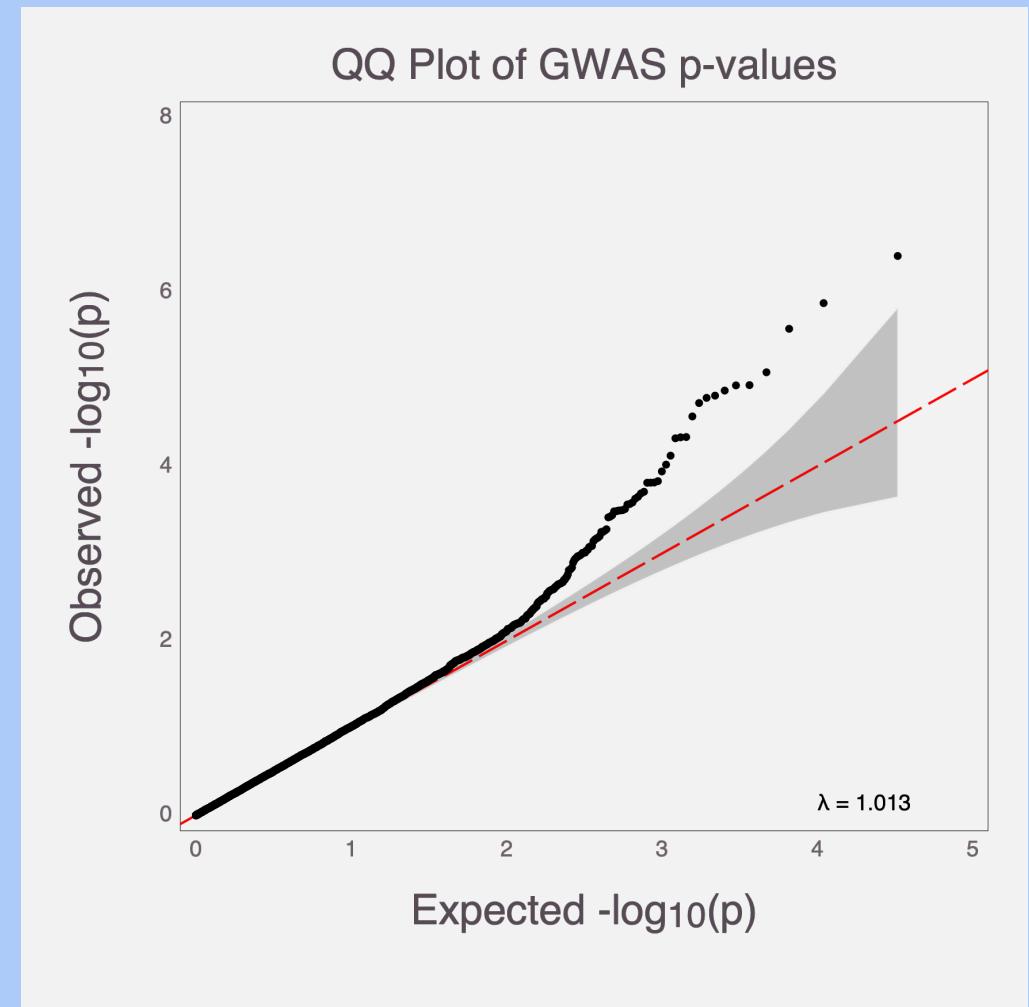
QQ plots

- The **expected** p-values for the quantiles of m SNPs, are $1/m, 2/m, \dots, 1$
- Take the negative log-10 and put in order from smallest to biggest



QQ plots

- SNPs falling above the line of identity indicate an excess of quantiles (β 's) with small p-values



Common data formats

How genotype data are stored

MAP

- PLINK file containing the locations and names of SNPs

1	rs12562034	0	758311	A	G
1	rs12124819	0	766409	G	A
1	rs4475691	0	836671	T	C
1	rs3748597	0	878522	T	C
1	rs28705211	0	890368	C	G
1	rs13303118	0	908247	G	T
1	rs9777703	0	918699	C	T
1	rs3121567	0	933331	A	G
1	rs3934834	0	995669	T	C
1	rs9442372	0	1008567	A	G
1	rs3737728	0	1011278	T	C
1	rs6687776	0	1020428	T	C
1	rs9651273	0	1021403	A	G
1	rs4970405	0	1038818	G	A

PED

- PLINK file containing genotypes and phenotypes of individuals in different families

FID	IID	FATID	MATID	SEX	PHENO	rs1	rs2	rs3	rs4	rs5
FAM1	1	0	0	1	1	G G	A A	A A	C C	G G
FAM1	2	0	0	1	2	G G	A A	A A	C C	G G
FAM1	3	0	0	1	2	G G	A A	A A	C C	G G
FAM2	1	0	0	1	2	G G	A A	A A	C C	G G
FAM2	2	0	0	1	2	G G	A A	A A	C C	G G
FAM2	3	0	0	1	2	G G	A A	A A	C C	G G
FAM3	1	0	0	1	2	G G	A A	A A	C C	G G
FAM3	2	0	0	1	2	G G	A A	A A	C C	G G
FAM3	3	0	0	1	2	A A	G G	G G	C C	G G

GDS

- Genomic data structure used for conducting GWAS in R

```
# Open a GDS file
(genofile <- snpgdsOpen(snpgdsExampleFileName()))

## File: /tmp/RtmpfdOhhS/Rinst4d3a91a981738/SNPRelate/extdata/hapmap_genotype.gds (709.6K)
## +   [ ] *
## |--+ sample.id    { VStr8 279 ZIP(29.9%), 679B }
## |--+ snp.id      { Int32 9088 ZIP(34.8%), 12.3K }
## |--+ snp.rs.id   { VStr8 9088 ZIP(40.1%), 36.2K }
## |--+ snp.position { Int32 9088 ZIP(94.7%), 33.6K }
## |--+ snp.chromosome { UInt8 9088 ZIP(0.94%), 85B } *
## |--+ snp.allele   { VStr8 9088 ZIP(11.3%), 4.0K }
## |--+ genotype    { Bit2 279x9088, 619.0K } *
## \--+ sample.annot [ data.frame ] *
##     |--+ family.id   { VStr8 279 ZIP(34.4%), 514B }
##     |--+ father.id   { VStr8 279 ZIP(31.5%), 220B }
##     |--+ mother.id   { VStr8 279 ZIP(30.9%), 214B }
##     |--+ sex         { VStr8 279 ZIP(17.0%), 95B }
##     \--+ pop.group   { VStr8 279 ZIP(6.18%), 69B }
```