### data explore

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#### Access to data files

```
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
## filter, lag
## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union
```

Add group index, merge with player information, keep only football players, delete duplicates between 3 groups, and construct group index.

```
player.info <- read.csv("/Users/mawanying/Dropbox/Luo_Jarek_YC/MRI_Injury_Description_030CT18_All_Concu</pre>
basic.info <- player.info %>% select(SUBJECTSTUDYNUM, INJURYSPORTVARSITY, CONTACTSPORTQGID, NONCONTACTS
football.info <- basic.info %>% filter(INJURYSPORTVARSITY=='Football') #football.info is 88x4
#first in second
d1 <- football.info$SUBJECTSTUDYNUM %in% football.info$CONTACTSPORTQGID
#first in third
d2 <- football.info$SUBJECTSTUDYNUM %in% football.info$NONCONTACTSPORTQGID
#second in first
d3 <- football.info$CONTACTSPORTQGID %in% football.info$SUBJECTSTUDYNUM
#second in third
d4 <- football.info$CONTACTSPORTQGID %in% football.info$NONCONTACTSPORTQGID
#third in first
d5 <- football.info$NONCONTACTSPORTQGID %in% football.info$SUBJECTSTUDYNUM
#third in second
d6 <- football.info$NONCONTACTSPORTQGID %in% football.info$CONTACTSPORTQGID
dupli <- cbind(d1, d2, d3, d4, d5, d6) #88x6
football.noDup <- football.info[rowSums(dupli)<1, ] # football.noDup is 53x4
############
            group1: SUBJECTSTUDYNUM
                                      ############
            group2: CONTACTSPORTQGID
                                      ###########
############
            group3: NONCONTACTSPORTQGID
#############
                                      ###########
```

```
group1 <- unique(as.character(football.noDup$SUBJECTSTUDYNUM))</pre>
                                                                  #SUBJECTSTUDYNUM 43x1
group2 <- unique(as.character(football.noDup$CONTACTSPORTQGID))</pre>
                                                                  #CONTACTSPORTQGID 43x1
group3 <- unique(as.character(football.noDup$NONCONTACTSPORTQGID)) #NONCONTACTSPORTQGID 43x1
# after merge, alldata_fb will have 28 players in group 1, 30players in group 2, 28 players in group 3
alldata.player <- as.character(alldata$player) #21052x1
alldata.fb.player <- alldata.player %in% c(group1, group2, group3) #indicator vector: 9280x1
groupindex <- c()</pre>
for(i in alldata.player[alldata.fb.player]){
 if(i %in% group1){
   groupindex <- c(groupindex, 1)</pre>
 if(i %in% group2){
   groupindex <- c(groupindex, 2)</pre>
 if(i %in% group3){
   groupindex <- c(groupindex, 3)</pre>
 }
}
addgroupindex <- function(data, football_index, groupindex){</pre>
 fbdata <- data[football_index, ]</pre>
 data.fb <- fbdata %>% mutate(group=groupindex)
 return(data.fb)
alldata.fb <- addgroupindex(alldata, alldata.fb.player, groupindex) #9280x204
alldata.fb_qdt <- addgroupindex(alldata_qdt, alldata.fb.player, groupindex) #9280x204
colnames(alldata.fb)[4:203] <- colnames(alldata.fb_qdt)[4:203] <- paste0("den", 1:200)
#table(alldata.fb$group)
    2
#3016 3240 3024
# there are 86 different players in total for alldata.fb
#alldata_fb will have 28 players in group 1, 30players in group 2, 28 players in group 3
```

#### cluster

Using equally-spaced density (no transformation), as well as quantile-density transformation of density -log(f(Q(t)))

```
m.tract.cluster <- function(data, iter){
    # data: input dataset
    # m: measurement, in {"FA", "MD", "Da", "Dr"}

# t: tract

t <- as.character(para[iter, 1])

m <- as.character(para[iter, 2])

data.tm <- data %>% filter(tract==t, measure==m) #86x204

den.tm <- select(data.tm, den1:den200) #86x200

den.tm <- den.tm - as.vector(rep(1, dim(den.tm)[1])) %*% t(colMeans(den.tm))

den.fpca <- refund::fpca.face(data.matrix(den.tm), center = TRUE, argvals = (1:200)/200, knots = 7, p

den.score <- den.fpca$scores/sqrt(dim(den.tm)[2]) #86x5</pre>
```

```
den.cluster <- kmeans(den.score, centers = 3)</pre>
permute <- function(vec, p1, p2, p3){</pre>
  for(i in 1:length(vec)){
    if(vec[i]==1){
      vec[i] \leftarrow p1
    }else{
      if(vec[i]==2){vec[i] \leftarrow p2}else{
        vec[i] \leftarrow p3
    }
  }
  return(vec)
  perm1 <- permute(den.cluster$cluster, 1,2,3)</pre>
  perm2 <- permute(den.cluster$cluster, 1,3,2)</pre>
  perm3 <- permute(den.cluster$cluster, 2,1,3)</pre>
  perm4 <- permute(den.cluster$cluster, 2,3,1)</pre>
  perm5 <- permute(den.cluster$cluster, 3,1,2)</pre>
  perm6 <- permute(den.cluster$cluster, 3,2,1)</pre>
  misrate <- min(sum(perm1!=data.tm$group)/length(data.tm$group),</pre>
      sum(perm2!=data.tm$group)/length(data.tm$group),
      sum(perm3!=data.tm$group)/length(data.tm$group),
      sum(perm4!=data.tm$group)/length(data.tm$group),
      sum(perm5!=data.tm$group)/length(data.tm$group),
      sum(perm6!=data.tm$group)/length(data.tm$group))
  data.tm.comb = cbind(data.tm, den.score)
  return(list(misrate=misrate,
               data.tm.comb=data.tm.comb,
               den.fpca=den.fpca))
}
m.tract.cluster2 <- function(data, iter){</pre>
  # data: input dataset
  # m: measurement, in {"FA", "MD", "Da", "Dr"}
  # t: tract
  t <- as.character(para[iter, 1])
  m <- as.character(para[iter, 2])</pre>
  data.tm <- data %>% filter(tract==t, measure==m, group != 3) #86x204
  den.tm <- select(data.tm, den1:den200)</pre>
                                                #86x200
  \#den.tm \leftarrow den.tm - as.vector(rep(1, dim(den.tm)[1])) \%*\% t(colMeans(den.tm))
  den.fpca <- refund::fpca.face(data.matrix(den.tm), center = TRUE, argvals = (1:200)/200, knots = 7, p
  den.score <- den.fpca$scores/sqrt(dim(den.tm)[2]) #86x5</pre>
  den.cluster <- kmeans(den.score, centers = 2)
  permute <- function(vec, p1, p2){</pre>
    for(i in 1:length(vec)){
      if(vec[i]==1){vec[i] \leftarrow p1}else{vec[i] \leftarrow p2}
    }
    return(vec)
```

#### cluster results

```
## Misrate for 3 clusters:
## No transformation: FA
## [1] 0.5348837 0.5581395 0.5581395 0.5697674 0.5697674
## No transformation: MD
## [1] 0.5232558 0.5465116 0.5465116 0.5764706 0.5813953
## No transformation: Da
## [1] 0.5465116 0.5581395 0.5697674 0.5813953 0.5813953
## No transformation: Dr
## [1] 0.5697674 0.5813953 0.5813953 0.5813953 0.5813953
## Corresponding tracts:
## FA:
## [1] "cgc r" "ifo r" "slf l" "ar r" "cst r"
## MD:
## [1] "unc_r" "mcp"
                       "slf_1" "ml_r" "ar_1"
## Da:
## [1] "str_r" "unc_r" "ar_r" "cgc_l" "cst_l"
## Dr:
## [1] "str_r" "ar_l" "atr_l" "cgh_l" "slf_l"
## Misrate for 3 clusters:
## Quantile-density transformation: FA
## [1] 0.5116279 0.5232558 0.5465116 0.5581395 0.5697674
## Quantile-density transformation: MD
## [1] 0.5882353 0.5882353 0.5930233 0.5930233 0.5930233
## Quantile-density transformation: Da
## [1] 0.5465116 0.5813953 0.5813953 0.5813953 0.5813953
## Quantile-density transformation: Dr
## [1] 0.5348837 0.5581395 0.5581395 0.5697674 0.5697674
```

```
## Corresponding tracts:
## FA:
## [1] "ptr_l" "cgc_r" "ar_r" "slf_l" "atr_l"
## MD:
## [1] "ml_l" "ml_r" "cgh_r" "fmi"
                                       "ilf 1"
## Da:
## [1] "ar_r" "cgh_r" "fma" "ifo_l" "unc_l"
## Dr:
## [1] "ar_l" "fma"
                      "ptr_l" "ar_r" "slf_l"
only cluster first two groups
## Misrate for 2 clusters:
## No transformation: FA
## [1] 0.3448276 0.4137931 0.4137931 0.4137931 0.4137931
## No transformation: MD
## [1] 0.3965517 0.4137931 0.4137931 0.4137931 0.4310345
## No transformation: Da
## [1] 0.3793103 0.3793103 0.3965517 0.3965517 0.4137931
## No transformation: Dr
## [1] 0.3793103 0.3793103 0.3793103 0.3965517 0.4137931
## Corresponding tracts:
## FA:
## [1] "cgh_l" "ar_r" "cgc_l" "cgc_r" "ptr_l"
## MD:
## [1] "cst_l" "cst_r" "slf_l" "unc_r" "ar_r"
## Da:
## [1] "fmi" "unc_r" "atr_l" "str_r" "cgh_r"
## Dr:
## [1] "atr_l" "ptr_r" "unc_r" "ifo_r" "ar_l"
## Misrate for 2 clusters:
## FA
## [1] 0.3620690 0.3620690 0.3793103 0.3793103 0.3965517
## qd transformation: MD
## [1] 0.3793103 0.4310345 0.4310345 0.4310345 0.4310345
## qd transformation: Da
```

## [1] 0.3620690 0.3620690 0.3965517 0.4310345 0.4310345

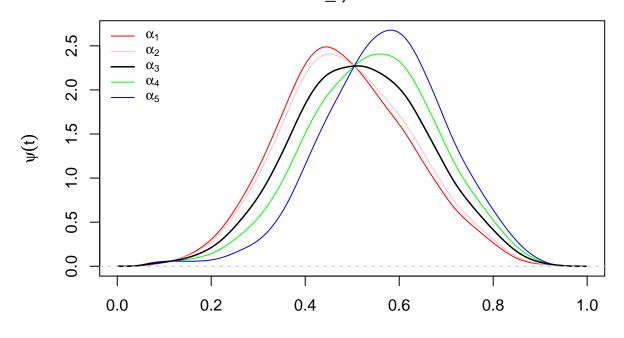
```
## qd transformation: Dr
## [1] 0.3793103 0.3965517 0.3965517 0.3965517 0.4137931
## Corresponding tracts:
## Quantile-density transformation: FA
## [1] "cst_1" "mcp" "cgh_1" "cst_r" "cgc_r"
## Quantile-density transformation: MD
## [1] "unc_r" "atr_r" "cgc_1" "cgc_r" "ifo_1"
## Quantile-density transformation: Da
## [1] "ptr_r" "unc_r" "str_1" "ifo_1" "ilf_r"
## Quantile-density transformation: Dr
## [1] "fma" "ar_1" "cgh_r" "cst_1" "slf_1"
```

#### Visualized variation modes

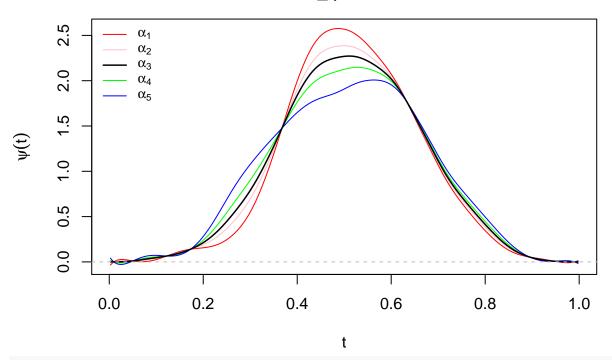
```
\#fb\_score \leftarrow lapply(1:dim(para)[1], function(x) m.tract.cluster2(alldata.fb, x)$data.tm.comb)
#fb score <- do.call(rbind, fb score) #9280x209
\#fb\_scorefpca \leftarrow lapply(1:dim(para)[1], function(x) m.tract.cluster2(alldata.fb, x)$den.fpca)
var_mode <- function(data, m, t, title, qd){</pre>
loc_m <- which(para[,2]==m)</pre>
loc <- loc_m[which(para[loc_m,1]==t)] #loc in the para that is tract=='unc_r', measure=='Da'
fb_scorefpca <- lapply(loc, function(x) m.tract.cluster2(data, x)$den.fpca)</pre>
eigenf <- fb_scorefpca[[1]]$efunctions*sqrt(200)</pre>
eigens <- fb_scorefpca[[1]]$scores/sqrt(200)</pre>
mean <- fb_scorefpca[[1]]$mu</pre>
pc1_score_q <- quantile(eigens[,1], c(0.1, 0.25, 0.75, 0.95))
modes1 <- cbind(t(as.vector(pc1_score_q)%*% t(eigenf[,1])) + mean, mean) #200x5
pc2_score_q <- quantile(eigens[,2], c(0.1, 0.25, 0.75, 0.95))
modes2 <- cbind(t(as.vector(pc2_score_q)%*% t(eigenf[,2])) + mean, mean) #200x5
tran_back <- function(den.tran.y, den.quantiles){</pre>
  thetax <- sum((head(exp(den.tran.y), -1)+tail(exp(den.tran.y), -1))/2*(diff(den.quantiles/100)[1]))
  tranback_x <- sapply(1:200, function(x){</pre>
    sum((head(exp(den.tran.y)[1:x], -1)+tail(exp(den.tran.y)[1:x], -1))/2*(diff(den.quantiles/100)[1]))/
  })
  tranback_y <- exp(-den.tran.y)*thetax</pre>
  return(list(tranback_x= tranback_x,
              tranback_y=tranback_y,
              thetax=thetax))
}
if(qd==0){
matplot(den.quantiles/100, modes1, main=paste0("1st PC modes, ",title, "\n tract:", t, ", measure:", m)
        xlab="t", ylab=expression(psi(t)),
        col=c("red","pink","green","blue", "black"), type="l",
        lty=c(1,1,1,1,1), lwd=c(1,1,1,1,1.5))
```

```
abline(h=0, col="grey", lwd=1, lty=2)
legend("topleft", c(expression(alpha[1]), expression(alpha[2]), expression(alpha[3]), expression(alpha[4])
matplot(den.quantiles/100, modes2, main=paste0("1st PC modes, ",title, "\n tract:", t, ", measure:", m)
        xlab="t", ylab=expression(psi(t)),
        col=c("red","pink","green","blue", "black"), type="l",
        lty=c(1,1,1,1,1), lwd=c(1,1,1,1,1.5))
abline(h=0, col="grey", lwd=1, lty=2)
legend("topleft", c(expression(alpha[1]), expression(alpha[2]), expression(alpha[3]), expression(alpha[4])
}
if(qd==1){
tran_den <- lapply(data.frame(modes1), function(x){tran_back(x, den.quantiles)})</pre>
plot(tran_den[[1]] $tranback_x, tran_den[[1]] $tranback_y, type="l",main=paste0("1st PC modes, ",title, "
                                tran_den[[3]]$tranback_y, tran_den[[4]]$tranback_y,
                                tran_den[[5]]$tranback_y))),
     xlab="x", ylab='f(x)')
abline(h=0, col="grey", lwd=1, lty=2)
lines(tran_den[[2]]$tranback_x, tran_den[[2]]$tranback_y, type="1", col="pink")
lines(tran_den[[3]]$tranback_x, tran_den[[3]]$tranback_y, type="1", col="green")
lines(tran_den[[4]]$tranback_x, tran_den[[4]]$tranback_y, type="1", col="blue")
lines(tran_den[[5]]$tranback_x, tran_den[[5]]$tranback_y,col="black", lwd=1.5)
legend("topleft", c(expression(alpha[1]), expression(alpha[2]), expression(alpha[3]), expression(alpha[4])
tran_den2 <- lapply(data.frame(modes2), function(x){tran_back(x, den.quantiles)})</pre>
plot(tran_den2[[1]]$tranback_x, tran_den2[[1]]$tranback_y, type="l",main=paste0("2nd PC modes, ",title,
     xlab="x", ylab=expression(psi^{-1}(x)),
     col="red", ylim=c(0, max(c(tran_den2[[1]]$tranback_y, tran_den2[[2]]$tranback_y,
                                tran_den2[[3]]$tranback_y, tran_den2[[4]]$tranback_y,
                                tran_den2[[5]]$tranback_y))))
abline(h=0, col="grey", lwd=1, lty=2)
lines(tran_den2[[2]]$tranback_x, tran_den2[[2]]$tranback_y, type="1", col="pink")
lines(tran_den2[[3]]$tranback_x, tran_den2[[3]]$tranback_y, type="1", col="green")
lines(tran_den2[[4]]$tranback_x, tran_den2[[4]]$tranback_y, type="1", col="blue")
lines(tran_den2[[5]]$tranback_x, tran_den2[[5]]$tranback_y, col="black", lwd=1.5)
legend("topleft", c(expression(alpha[1]), expression(alpha[2]), expression(alpha[3]), expression(alpha[4])
}
}
locM <- which.min(c(min(misrate_FA_qdt2), min(misrate_MD_qdt2), min(misrate_Da_qdt2), min(misrate_Dr_qd</pre>
minM <- c('FA', 'MD', 'Da', 'Dr')[locM]
minT <- c(as.character(tractnames)[order(misrate_FA_qdt2)[1]],</pre>
          as.character(tractnames)[order(misrate_MD_qdt2)[1]],
          as.character(tractnames)[order(misrate_Da_qdt2)[1]],
          as.character(tractnames)[order(misrate_Dr_qdt2)[1]])[locM]
var_mode(alldata.fb, m=minM, t=minT, title='Ordinary FPCA', qd=0)
```

# 1st PC modes, Ordinary FPCA tract:cst\_I, measure:FA

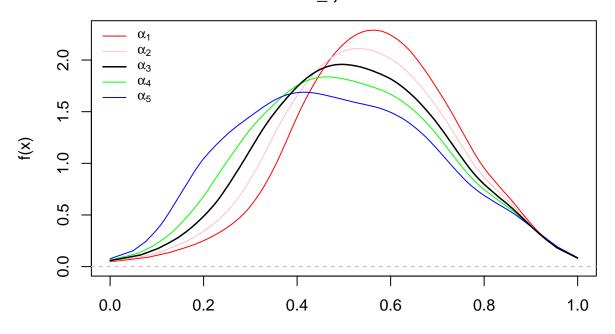


1st PC modes, Ordinary FPCA tract:cst\_I, measure:FA



var\_mode(alldata.fb\_qdt, m=minM, t=minT, title='log quantile-density transformation', qd=1)

## 1st PC modes, log quantile-density transformation tract:cst\_l, measure:FA



2nd PC modes, log quantile-density transformation tract:cst\_I, measure:FA

