

# Problem Set 5 R Solutions and a Guide to Panel Data

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We will use Question 2i as our guiding example for implementing panel data in R for the purpose of this course. The short of it is that we will implement it entirely using the familiar `lm_robust` function from *estimatr*. I know I directed some people to *plm* before the strike so apologies if it led to frustration during the problem set. This is why I write my own notes and didn't share the econometrics-with-R website before; it's pretty sloppy, often inaccurate, and I usually have to spend a day figuring out the differences between R and Stata.

Just for exposition, *plm* is a good package and can even handle robust standard errors. However by default it clusters standard errors to the level of the individual fixed effects. In general, we do want to use clustered standard errors whenever we include fixed effects which is why they've made it automatic, but this problem set does ask us to consider fixed-effects models without clustering so it cannot be used. Further, *lm\_robust* is much more compatible with *linearHypothesis* when we run F-tests for a subset of covariates (such as fixed effects).

## Question 1

Let's load our data and create the log transformations we'll need:

```
guns <- read.dta13("handguns.dta") %>% mutate(lvio = log(vio),
  lrob = log(rob), lmur = log(mur))
```

Regression (i): Regress  $\ln(\text{vio})$  against shall

```
lm_robust(lvio ~ shall, data = guns, se_type = "stata")
```

```
##              Estimate Std. Error    t value    Pr(>|t|)    CI Lower
## (Intercept)  6.1349189 0.01930393  317.806773 0.000000e+00  6.0970448
## shall       -0.4429646 0.04752832  -9.320014 5.596578e-20 -0.5362148
##              CI Upper    DF
## (Intercept)  6.1727931 1171
## shall       -0.3497144 1171
```

Regression (ii): Regress  $\ln(\text{vio})$  against shall, incarc\_rate, density, avginc, pop, pb1064, pw1064, pm1029

```
lm_robust(lvio ~ shall + incarc_rate + density + avginc + pop +
  pb1064 + pw1064 + pm1029, data = guns, se_type = "stata")
```

```
##              Estimate  Std. Error    t value    Pr(>|t|)
## (Intercept)  2.981738245 0.6090197820   4.8959629 1.116039e-06
## shall       -0.368386948 0.0347879106 -10.5895106 4.419970e-25
## incarc_rate  0.001612633 0.0001806945   8.9246392 1.701409e-18
## density      0.026688475 0.0143493879   1.8599033 6.315131e-02
## avginc       0.001205122 0.0072778184   0.1655884 8.685096e-01
## pop          0.042709834 0.0031466432  13.5731416 4.578376e-39
## pb1064       0.080852602 0.0199924337   4.0441601 5.596777e-05
## pw1064       0.031200509 0.0097270734   3.2075947 1.374974e-03
## pm1029       0.008870883 0.0120603987   0.7355381 4.621600e-01
##              CI Lower    CI Upper    DF
## (Intercept)  1.786838934  4.176637556 1164
## shall       -0.436640971 -0.300132925 1164
```

```
## incarc_rate 0.001258110 0.001967156 1164
## density -0.001465083 0.054842032 1164
## avginc -0.013073987 0.015484232 1164
## pop 0.036536107 0.048883560 1164
## pb1064 0.041627365 0.120077839 1164
## pw1064 0.012115951 0.050285067 1164
## pm1029 -0.014791669 0.032533434 1164
```

**1a: Interpret the coefficient on shall in regression (ii). Is this estimate large or small in a “real-world” sense?**

The coefficient of -0.37 means that holding constant the control variables (the incarceration rate in the previous year, the population density, state income, state population, percentage of blacks aged 10–64, percentage of whites aged 10–64, and percentage of male aged 10–29), having a “shall-carry” law results in a reduction in the violent crime rate of 37%. This is a very large effect – a reduction in violent crimes of 37% is very significant in a political or real-world sense.

**1b: Does adding the control variables in regression (ii) change your conclusions about the effect of a shall-carry law, relative to regression (i)?**

Adding the control variables reduces the estimated coefficient, suggesting that the original coefficient probably was subject to some omitted variable bias. In both (i) and (ii), the effect of the shall-carry law is statistically significant at the 5% level. In (i) the estimated effect is a crime reduction of 44%, in (ii) the estimated reduction is 37%. Both estimated effects are very large. Still, in a real-world sense the difference between them is substantial also (7% of violent crimes is a lot of crime).

**1c: Suggest a variable which varies across states but plausibly varies little, or not at all, over time, and which plausibly could cause omitted variable bias in regression (ii)**

Here is one:

Severity of punishment. Laws on violent crime are almost entirely state laws and there is considerable variation across states. Severity of punishment: (i) arguably affects the crime rate and (ii) could be correlated with shall-carry laws (Texas has the death penalty, it also has a shall-carry law). If so, the OLS estimate on shall arguably overstates the effect of having a shall-carry, which is, in part, picking up the effect of tough laws.

## Question 2

**2i: Dependent variable  $\ln(\text{vio})$**

Running each regression in order

**Regression 1: no controls, no fixed effects, no clustering**

```
# 1
mod.2i.1 <- lm_robust(lvio ~ shall, data = guns, se_type = "stata")
summary(mod.2i.1)

##
## Call:
## lm_robust(formula = lvio ~ shall, data = guns, se_type = "stata")
##
```

```
## Standard error type: HC1
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF
## (Intercept)   6.135    0.01930  317.81 0.000e+00   6.0970   6.1728 1171
## shall        -0.443    0.04753   -9.32 5.597e-20  -0.5362  -0.3497 1171
##
## Multiple R-squared:  0.08664 ,    Adjusted R-squared:  0.08586
## F-statistic: 86.86 on 1 and 1171 DF,  p-value: < 2.2e-16
```

This is the same as the first regression in Question 1. No fixed effects so we're treating this panel data like any data we do OLS on.

## Regression 2: yes controls, no fixed effects, no clustering

```
mod.2i.2 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029, data = guns, se_type = "stata")
summary(mod.2i.2)
```

```
##
## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density + avginc +
##           pop + pb1064 + pw1064 + pm1029, data = guns, se_type = "stata")
##
## Standard error type: HC1
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper
## (Intercept)  2.981738  0.6090198   4.8960 1.116e-06  1.786839  4.176638
## shall       -0.368387  0.0347879 -10.5895 4.420e-25 -0.436641 -0.300133
## incarc_rate  0.001613  0.0001807   8.9246 1.701e-18  0.001258  0.001967
## density      0.026688  0.0143494   1.8599 6.315e-02 -0.001465  0.054842
## avginc       0.001205  0.0072778   0.1656 8.685e-01 -0.013074  0.015484
## pop          0.042710  0.0031466  13.5731 4.578e-39  0.036536  0.048884
## pb1064       0.080853  0.0199924   4.0442 5.597e-05  0.041627  0.120078
## pw1064       0.031201  0.0097271   3.2076 1.375e-03  0.012116  0.050285
## pm1029       0.008871  0.0120604   0.7355 4.622e-01 -0.014792  0.032533
##
##           DF
## (Intercept) 1164
## shall       1164
## incarc_rate 1164
## density     1164
## avginc      1164
## pop         1164
## pb1064      1164
## pw1064      1164
## pm1029      1164
##
## Multiple R-squared:  0.5643 ,    Adjusted R-squared:  0.5613
## F-statistic: 95.67 on 8 and 1164 DF,  p-value: < 2.2e-16
```

Again, this is the same as the second regression in Question 1. Don't forget to include the `se_type = 'stata'` argument!

### Regression 3: yes controls, state fixed effects, no clustering

Now we're exploiting the panel structure of the data by including fixed effects. `lm_robust` already includes a `fixed_effects` argument that handles these:

```
mod.2i.3 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029, fixed_effects = ~state,
  se_type = "stata", data = guns)
summary(mod.2i.3)
```

```
##
## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density + avginc +
##      pop + pb1064 + pw1064 + pm1029, data = guns, fixed_effects = ~state,
##      se_type = "stata")
##
## Standard error type:  HC1
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)    CI Lower    CI Upper
## shall          -4.614e-02  1.994e-02 -2.3136 2.087e-02 -0.0852721 -0.0070109
## incarc_rate    -7.101e-05  9.731e-05 -0.7297 4.657e-01 -0.0002619  0.0001199
## density       -1.723e-01  1.049e-01 -1.6428 1.007e-01 -0.3780724  0.0334925
## avginc        -9.204e-03  6.733e-03 -1.3669 1.719e-01 -0.0224155  0.0040080
## pop           1.152e-02  9.704e-03  1.1876 2.353e-01 -0.0075162  0.0305655
## pb1064         1.043e-01  1.656e-02  6.2990 4.305e-10  0.0717976  0.1367633
## pw1064         4.086e-02  5.386e-03  7.5867 6.903e-14  0.0302935  0.0514287
## pm1029        -5.027e-02  7.791e-03 -6.4528 1.634e-10 -0.0655588 -0.0349863
##              DF
## shall          1114
## incarc_rate    1114
## density        1114
## avginc         1114
## pop            1114
## pb1064         1114
## pw1064         1114
## pm1029         1114
##
## Multiple R-squared:  0.9411 ,    Adjusted R-squared:  0.938
## Multiple R-squared (proj. model):  0.2178 ,    Adjusted R-squared (proj. model):  0.1771
## F-statistic (proj. model):  28.1 on 8 and 1114 DF,  p-value: < 2.2e-16
```

These give us exactly the same estimates and standard errors as Stata. I'll just flag here that when we read this regression output, make sure you get the decimal points correct. The coefficient on *shall* here is -4.614e-02, which means -0.04614 (move the decimal point to the left twice). I don't want you guys to lose points for something as silly as decimal places.

So the only downside here is that it omits the estimates on the fixed effects regressors, which makes it (as far as I know) impossible to do the F-test we want to do. So for that reason, we'll want to run this same model slightly differently by explicitly including the fixed effects in the right-hand side of the formula: "+ factor(state)". "factor" here just creates dummy variables for each state. If we did not use "factor" then it would treat *state* as one continuous variable taking on values from 1-50, which is not an implementation of fixed effects.

```
mod.2i.3 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state),
```

```
se_type = "stata", data = guns)
summary(mod.2i.3)
```

```
##
## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density + avginc +
##      pop + pb1064 + pw1064 + pm1029 + factor(state), data = guns,
##      se_type = "stata")
##
## Standard error type:  HC1
##
## Coefficients:
##              Estimate Std. Error  t value
## (Intercept)      4.037e+00  3.846e-01  10.49648
## shall           -4.614e-02  1.994e-02  -2.31364
## incarc_rate      -7.101e-05  9.731e-05  -0.72971
## density          -1.723e-01  1.049e-01  -1.64275
## avginc           -9.204e-03  6.733e-03  -1.36686
## pop              1.152e-02  9.704e-03   1.18758
## pb1064            1.043e-01  1.656e-02   6.29896
## pw1064            4.086e-02  5.386e-03   7.58672
## pm1029           -5.027e-02  7.791e-03  -6.45284
## factor(state)Alaska      5.596e-02  7.884e-02   0.70988
## factor(state)Arizona      2.404e-01  8.723e-02   2.75595
## factor(state)Arkansas    -1.273e-01  7.145e-02  -1.78133
## factor(state)California    2.442e-01  2.377e-01   1.02739
## factor(state)Colorado    -1.051e-01  1.180e-01  -0.89052
## factor(state)Connecticut  -9.557e-02  1.412e-01  -0.67658
## factor(state)Delaware      9.760e-02  8.245e-02   1.18377
## factor(state)District of Columbia  2.759e+00  1.005e+00   2.74624
## factor(state)Florida       6.771e-01  1.201e-01   5.63622
## factor(state)Georgia       2.253e-02  5.466e-02   0.41225
## factor(state)Hawaii       -1.128e+00  2.586e-01  -4.36118
## factor(state)Idaho         -5.030e-01  1.236e-01  -4.07041
## factor(state)Illinois      4.086e-01  1.128e-01   3.62044
## factor(state)Indiana       -2.057e-01  1.160e-01  -1.77303
## factor(state)Iowa          -6.291e-01  1.317e-01  -4.77677
## factor(state)Kansas        -1.808e-01  1.010e-01  -1.79093
## factor(state)Kentucky      -4.256e-01  1.091e-01  -3.90056
## factor(state)Louisiana      3.685e-01  5.736e-02   6.42495
## factor(state)Maine         -1.132e+00  1.508e-01  -7.50545
## factor(state)Maryland       3.961e-01  6.342e-02   6.24620
## factor(state)Massachusetts  2.869e-01  1.571e-01   1.82596
## factor(state)Michigan       2.449e-01  1.051e-01   2.33142
## factor(state)Minnesota     -5.760e-01  1.290e-01  -4.46351
## factor(state)Mississippi    -3.930e-01  7.799e-02  -5.03909
## factor(state)Missouri       1.455e-01  9.317e-02   1.56196
## factor(state)Montana       -9.910e-01  1.228e-01  -8.07170
## factor(state)Nebraska       -4.432e-01  1.204e-01  -3.68281
## factor(state)Nevada         3.226e-01  9.154e-02   3.52438
## factor(state)New Hampshire -1.277e+00  1.466e-01  -8.71041
## factor(state)New Jersey     1.222e-01  1.427e-01   0.85633
## factor(state)New Mexico     3.818e-01  7.856e-02   4.85967
## factor(state)New York       4.354e-01  1.728e-01   2.51994
```

## factor(state)North Carolina	-9.656e-02	5.689e-02	-1.69737	
## factor(state)North Dakota	-1.843e+00	1.136e-01	-16.22255	
## factor(state)Ohio	-1.885e-01	1.339e-01	-1.40800	
## factor(state)Oklahoma	-4.115e-02	6.814e-02	-0.60389	
## factor(state)Oregon	4.947e-03	1.194e-01	0.04144	
## factor(state)Pennsylvania	-3.250e-01	1.439e-01	-2.25800	
## factor(state)Rhode Island	-1.004e-01	1.670e-01	-0.60090	
## factor(state)South Carolina	3.341e-01	5.764e-02	5.79513	
## factor(state)South Dakota	-1.025e+00	1.041e-01	-9.84327	
## factor(state)Tennessee	4.468e-02	8.020e-02	0.55709	
## factor(state)Texas	5.265e-02	1.592e-01	0.33067	
## factor(state)Utah	-3.039e-01	1.120e-01	-2.71439	
## factor(state)Vermont	-1.255e+00	1.498e-01	-8.37706	
## factor(state)Virginia	-6.018e-01	6.013e-02	-10.00759	
## factor(state)Washington	-1.322e-01	1.077e-01	-1.22768	
## factor(state)West Virginia	-9.691e-01	1.273e-01	-7.61364	
## factor(state)Wisconsin	-7.812e-01	1.201e-01	-6.50498	
## factor(state)Wyoming	-4.804e-01	1.293e-01	-3.71510	
##	Pr(> t )	CI Lower	CI Upper	DF
## (Intercept)	1.212e-24	3.2821852	4.7913662	1114
## shall	2.087e-02	-0.0852721	-0.0070109	1114
## incarc_rate	4.657e-01	-0.0002619	0.0001199	1114
## density	1.007e-01	-0.3780724	0.0334925	1114
## avginc	1.719e-01	-0.0224155	0.0040080	1114
## pop	2.353e-01	-0.0075162	0.0305655	1114
## pb1064	4.305e-10	0.0717976	0.1367633	1114
## pw1064	6.903e-14	0.0302935	0.0514287	1114
## pm1029	1.634e-10	-0.0655588	-0.0349863	1114
## factor(state)Alaska	4.779e-01	-0.0987211	0.2106508	1114
## factor(state)Arizona	5.948e-03	0.0692506	0.4115726	1114
## factor(state)Arkansas	7.513e-02	-0.2674677	0.0129161	1114
## factor(state)California	3.045e-01	-0.2222089	0.7106903	1114
## factor(state)Colorado	3.734e-01	-0.3366259	0.1264526	1114
## factor(state)Connecticut	4.988e-01	-0.3727071	0.1815767	1114
## factor(state)Delaware	2.368e-01	-0.0641709	0.2593666	1114
## factor(state)District of Columbia	6.125e-03	0.7879023	4.7309053	1114
## factor(state)Florida	2.201e-08	0.4414163	0.9128763	1114
## factor(state)Georgia	6.802e-01	-0.0847081	0.1297720	1114
## factor(state)Hawaii	1.413e-05	-1.6354309	-0.6204919	1114
## factor(state)Idaho	5.024e-05	-0.7454639	-0.2605340	1114
## factor(state)Illinois	3.073e-04	0.1871443	0.6299893	1114
## factor(state)Indiana	7.650e-02	-0.4332429	0.0219301	1114
## factor(state)Iowa	2.019e-06	-0.8875645	-0.3707156	1114
## factor(state)Kansas	7.358e-02	-0.3789507	0.0172826	1114
## factor(state)Kentucky	1.017e-04	-0.6396215	-0.2114882	1114
## factor(state)Louisiana	1.951e-10	0.2559922	0.4810864	1114
## factor(state>Maine	1.250e-13	-1.4279067	-0.8360551	1114
## factor(state)Maryland	5.973e-10	0.2716935	0.5205617	1114
## factor(state)Massachusetts	6.812e-02	-0.0213909	0.5952020	1114
## factor(state)Michigan	1.991e-02	0.0387974	0.4510353	1114
## factor(state)Minnesota	8.882e-06	-0.8292149	-0.3228040	1114
## factor(state)Mississippi	5.454e-07	-0.5460035	-0.2399664	1114
## factor(state)Missouri	1.186e-01	-0.0372820	0.3283517	1114
## factor(state)Montana	1.784e-15	-1.2319122	-0.7501145	1114

```
## factor(state)Nebraska      2.417e-04 -0.6793814 -0.2070935 1114
## factor(state)Nevada        4.417e-04  0.1430070  0.5022155 1114
## factor(state)New Hampshire 1.077e-17 -1.5647192 -0.9893848 1114
## factor(state)New Jersey    3.920e-01 -0.1578117  0.4022392 1114
## factor(state)New Mexico    1.344e-06  0.2276388  0.5359302 1114
## factor(state)New York      1.188e-02  0.0963949  0.7744876 1114
## factor(state)North Carolina 8.991e-02 -0.2081738  0.0150594 1114
## factor(state)North Dakota  2.722e-53 -2.0662922 -1.6203927 1114
## factor(state)Ohio          1.594e-01 -0.4511528  0.0741758 1114
## factor(state)Oklahoma      5.460e-01 -0.1748345  0.0925422 1114
## factor(state)Oregon        9.670e-01 -0.2292791  0.2391732 1114
## factor(state)Pennsylvania  2.414e-02 -0.6073424 -0.0425854 1114
## factor(state)Rhode Island  5.480e-01 -0.4281338  0.2273812 1114
## factor(state)South Carolina 8.879e-09  0.2209491  0.4471531 1114
## factor(state)South Dakota  5.600e-22 -1.2288430 -0.8203665 1114
## factor(state)Tennessee     5.776e-01 -0.1126851  0.2020461 1114
## factor(state)Texas         7.410e-01 -0.2597820  0.3650913 1114
## factor(state)Utah          6.742e-03 -0.5235926 -0.0842291 1114
## factor(state)Vermont       1.616e-16 -1.5483595 -0.9606847 1114
## factor(state)Virginia      1.233e-22 -0.7197493 -0.4837837 1114
## factor(state)Washington    2.198e-01 -0.3434125  0.0790674 1114
## factor(state)West Virginia 5.664e-14 -1.2189054 -0.7193911 1114
## factor(state)Wisconsin     1.171e-10 -1.0168624 -0.5455824 1114
## factor(state)Wyoming       2.132e-04 -0.7341196 -0.2266814 1114
##
## Multiple R-squared:  0.9411 ,    Adjusted R-squared:  0.938
## F-statistic: 364.9 on 58 and 1114 DF,  p-value: < 2.2e-16
```

The output is now much longer since we're including 50 fixed effects. But scroll up to the top and you'll find the estimates and standard errors on the main regressors are exactly the same.

Now let's do hypothesis testing on the fixed effects. We'll want to refer to the fixed effects by name so that we can use our familiar *linearHypothesis* function from the *car* package. But there are 50 of them, too many to type out manually. So let's first pull the vector of coefficients:

```
mod.2i.3$coefficients
```

```
##              (Intercept)                shall
##          4.036775691                -0.046141523
##          incarc_rate                density
##        -0.000071008                -0.172289988
##          avginc                pop
##        -0.009203729                0.011524661
##          pb1064                pw1064
##          0.104280401                0.040861070
##          pm1029                factor(state)Alaska
##        -0.050272536                0.055964866
##          factor(state)Arizona                factor(state)Arkansas
##          0.240411594                -0.127275803
##          factor(state)California                factor(state)Colorado
##          0.244240711                -0.105086645
##          factor(state)Connecticut                factor(state)Delaware
##        -0.095565202                0.097597850
## factor(state)District of Columbia                factor(state)Florida
##          2.759403816                0.677146315
##          factor(state)Georgia                factor(state)Hawaii
```

```
##          0.022531955          -1.127961420
##          factor(state)Idaho          factor(state)Illinois
##          -0.502998956          0.408566818
##          factor(state)Indiana          factor(state)Iowa
##          -0.205656410          -0.629140037
##          factor(state)Kansas          factor(state)Kentucky
##          -0.180834078          -0.425554844
##          factor(state)Louisiana          factor(state)Maine
##          0.368539270          -1.131980906
##          factor(state)Maryland          factor(state)Massachusetts
##          0.396127607          0.286905573
##          factor(state)Michigan          factor(state)Minnesota
##          0.244916361          -0.576009440
##          factor(state)Mississippi          factor(state)Missouri
##          -0.392984941          0.145534836
##          factor(state)Montana          factor(state)Nebraska
##          -0.991013338          -0.443237440
##          factor(state)Nevada          factor(state)New Hampshire
##          0.322611270          -1.277051983
##          factor(state)New Jersey          factor(state)New Mexico
##          0.122213752          0.381784511
##          factor(state)New York          factor(state)North Carolina
##          0.435441260          -0.096557172
##          factor(state)North Dakota          factor(state)Ohio
##          -1.843342441          -0.188488494
##          factor(state)Oklahoma          factor(state)Oregon
##          -0.041146116          0.004947080
##          factor(state)Pennsylvania          factor(state)Rhode Island
##          -0.324963870          -0.100376301
##          factor(state)South Carolina          factor(state)South Dakota
##          0.334051082          -1.024604778
##          factor(state)Tennessee          factor(state)Texas
##          0.044680502          0.052654625
##          factor(state)Utah          factor(state)Vermont
##          -0.303910876          -1.254522082
##          factor(state)Virginia          factor(state)Washington
##          -0.601766471          -0.132172552
##          factor(state)West Virginia          factor(state)Wisconsin
##          -0.969148238          -0.781222394
##          factor(state)Wyoming
##          -0.480400511
```

We only need their names rather than the actual estimates:

```
coef.names <- names(mod.2i.3$coefficients)
coef.names
```

```
## [1] "(Intercept)"
## [2] "shall"
## [3] "incarc_rate"
## [4] "density"
## [5] "avginc"
## [6] "pop"
## [7] "pb1064"
## [8] "pw1064"
```



```

## [9] "pm1029"
## [10] "factor(state)Alaska"
## [11] "factor(state)Arizona"
## [12] "factor(state)Arkansas"
## [13] "factor(state)California"
## [14] "factor(state)Colorado"
## [15] "factor(state)Connecticut"
## [16] "factor(state)Delaware"
## [17] "factor(state)District of Columbia"
## [18] "factor(state)Florida"
## [19] "factor(state)Georgia"
## [20] "factor(state)Hawaii"
## [21] "factor(state)Idaho"
## [22] "factor(state)Illinois"
## [23] "factor(state)Indiana"
## [24] "factor(state)Iowa"
## [25] "factor(state)Kansas"
## [26] "factor(state)Kentucky"
## [27] "factor(state)Louisiana"
## [28] "factor(state>Maine"
## [29] "factor(state)Maryland"
## [30] "factor(state)Massachusetts"
## [31] "factor(state)Michigan"
## [32] "factor(state)Minnesota"
## [33] "factor(state)Mississippi"
## [34] "factor(state)Missouri"
## [35] "factor(state)Montana"
## [36] "factor(state)Nebraska"
## [37] "factor(state)Nevada"
## [38] "factor(state)New Hampshire"
## [39] "factor(state)New Jersey"
## [40] "factor(state)New Mexico"
## [41] "factor(state)New York"
## [42] "factor(state)North Carolina"
## [43] "factor(state)North Dakota"
## [44] "factor(state)Ohio"
## [45] "factor(state)Oklahoma"
## [46] "factor(state)Oregon"
## [47] "factor(state)Pennsylvania"
## [48] "factor(state)Rhode Island"
## [49] "factor(state)South Carolina"
## [50] "factor(state)South Dakota"
## [51] "factor(state)Tennessee"
## [52] "factor(state)Texas"
## [53] "factor(state)Utah"
## [54] "factor(state)Vermont"
## [55] "factor(state)Virginia"
## [56] "factor(state)Washington"
## [57] "factor(state)West Virginia"
## [58] "factor(state)Wisconsin"
## [59] "factor(state)Wyoming"

```

Clearly, we only want the names that begin with “factor(state)” since those are the fixed effects. We can do this by observing that the fixed effects begin with variable 10 (“factor(state)Alaska”) and go on to variable

59 ("factor(state)Wyoming") so that we can manually define state coefficients as follows:

```
state.coefficients <- coef.names[10:59]
state.coefficients
```

```
## [1] "factor(state)Alaska"
## [2] "factor(state)Arizona"
## [3] "factor(state)Arkansas"
## [4] "factor(state)California"
## [5] "factor(state)Colorado"
## [6] "factor(state)Connecticut"
## [7] "factor(state)Delaware"
## [8] "factor(state)District of Columbia"
## [9] "factor(state)Florida"
## [10] "factor(state)Georgia"
## [11] "factor(state)Hawaii"
## [12] "factor(state)Idaho"
## [13] "factor(state)Illinois"
## [14] "factor(state)Indiana"
## [15] "factor(state)Iowa"
## [16] "factor(state)Kansas"
## [17] "factor(state)Kentucky"
## [18] "factor(state)Louisiana"
## [19] "factor(state>Maine"
## [20] "factor(state)Maryland"
## [21] "factor(state)Massachusetts"
## [22] "factor(state)Michigan"
## [23] "factor(state)Minnesota"
## [24] "factor(state)Mississippi"
## [25] "factor(state)Missouri"
## [26] "factor(state)Montana"
## [27] "factor(state)Nebraska"
## [28] "factor(state)Nevada"
## [29] "factor(state)New Hampshire"
## [30] "factor(state)New Jersey"
## [31] "factor(state)New Mexico"
## [32] "factor(state)New York"
## [33] "factor(state)North Carolina"
## [34] "factor(state)North Dakota"
## [35] "factor(state)Ohio"
## [36] "factor(state)Oklahoma"
## [37] "factor(state)Oregon"
## [38] "factor(state)Pennsylvania"
## [39] "factor(state)Rhode Island"
## [40] "factor(state)South Carolina"
## [41] "factor(state)South Dakota"
## [42] "factor(state)Tennessee"
## [43] "factor(state)Texas"
## [44] "factor(state)Utah"
## [45] "factor(state)Vermont"
## [46] "factor(state)Virginia"
## [47] "factor(state)Washington"
## [48] "factor(state)West Virginia"
## [49] "factor(state)Wisconsin"
## [50] "factor(state)Wyoming"
```

Alternatively, let's use a new function (no new packages needed; it's standard in R) intuitively called *startsWith*. `startsWith` takes in a vector of strings/words as its first argument and a string of interest as its second argument. Then it outputs a vector that (obviously) outputs TRUE if it does begin with that string of interest and FALSE otherwise:

```
startsWith(coef.names, "factor(state)")
```

```
## [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE TRUE TRUE
## [12] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [23] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [34] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [45] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [56] TRUE TRUE TRUE TRUE
```

We use this as an index to select the coefficient names for which this is true:

```
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
state.coefficients
```

```
## [1] "factor(state)Alaska"
## [2] "factor(state)Arizona"
## [3] "factor(state)Arkansas"
## [4] "factor(state)California"
## [5] "factor(state)Colorado"
## [6] "factor(state)Connecticut"
## [7] "factor(state)Delaware"
## [8] "factor(state)District of Columbia"
## [9] "factor(state)Florida"
## [10] "factor(state)Georgia"
## [11] "factor(state)Hawaii"
## [12] "factor(state)Idaho"
## [13] "factor(state)Illinois"
## [14] "factor(state)Indiana"
## [15] "factor(state)Iowa"
## [16] "factor(state)Kansas"
## [17] "factor(state)Kentucky"
## [18] "factor(state)Louisiana"
## [19] "factor(state>Maine"
## [20] "factor(state)Maryland"
## [21] "factor(state)Massachusetts"
## [22] "factor(state)Michigan"
## [23] "factor(state)Minnesota"
## [24] "factor(state)Mississippi"
## [25] "factor(state)Missouri"
## [26] "factor(state)Montana"
## [27] "factor(state)Nebraska"
## [28] "factor(state)Nevada"
## [29] "factor(state)New Hampshire"
## [30] "factor(state)New Jersey"
## [31] "factor(state)New Mexico"
## [32] "factor(state)New York"
## [33] "factor(state)North Carolina"
## [34] "factor(state)North Dakota"
## [35] "factor(state)Ohio"
## [36] "factor(state)Oklahoma"
## [37] "factor(state)Oregon"
```

```
## [38] "factor(state)Pennsylvania"
## [39] "factor(state)Rhode Island"
## [40] "factor(state)South Carolina"
## [41] "factor(state)South Dakota"
## [42] "factor(state)Tennessee"
## [43] "factor(state)Texas"
## [44] "factor(state)Utah"
## [45] "factor(state)Vermont"
## [46] "factor(state)Virginia"
## [47] "factor(state)Washington"
## [48] "factor(state)West Virginia"
## [49] "factor(state)Wisconsin"
## [50] "factor(state)Wyoming"
```

Exactly what we wanted. Now we just use this vector of variable names as the hypothesis argument in `linearHypothesis`. By default, this will jointly test the hypotheses that all these variables are equal to zero:

```
linearHypothesis(mod.2i.3, state.coefficients, test = "F")
```

```
## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0
## factor(state)Florida = 0
## factor(state)Georgia = 0
## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state>Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
```

```

## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0
## factor(state)Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lvio ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##      pw1064 + pm1029 + factor(state)
##
##      Res.Df Df      F    Pr(>F)
## 1      1164
## 2      1114 50 210.38 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Conveniently as usual, the output begins with the set of hypotheses we want to test so we know we're running the right test. The F-statistic is 210.38, exactly as Stata has it.

#### Regression 4: yes controls, state and year fixed effects, no clustering

Again, we have the option to use the *fixed\_effects* argument in *lm\_robust* for the case with multiple fixed effects:

```

mod.2i.4 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029, fixed_effects = ~state +
  year, se_type = "stata", data = guns)
summary(mod.2i.4)

```

```

##
## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density +
##      pop + pb1064 + pw1064 + pm1029, data = guns, fixed_effects = ~state +
##      year, se_type = "stata")
##
## Standard error type:  HC1
##
## Coefficients:
##      Estimate Std. Error t value Pr(>|t|)    CI Lower  CI Upper
## shall      -2.799e-02  1.937e-02 -1.4450 1.488e-01 -6.601e-02  0.0100196
## incarc_rate  7.599e-05  8.292e-05  0.9165 3.596e-01 -8.671e-05  0.0002387
## density     -9.155e-02  6.487e-02 -1.4114 1.584e-01 -2.188e-01  0.0357256
## avginc       9.586e-04  7.197e-03  0.1332 8.941e-01 -1.316e-02  0.0150800

```

```
## pop          -4.754e-03  6.703e-03 -0.7093 4.783e-01 -1.791e-02 0.0083976
## pb1064        2.919e-02  2.104e-02  1.3874 1.656e-01 -1.209e-02 0.0704637
## pw1064        9.250e-03  8.518e-03  1.0859 2.777e-01 -7.464e-03 0.0259639
## pm1029        7.333e-02  1.878e-02  3.9052 9.992e-05  3.648e-02 0.1101670
##              DF
## shall         1092
## incarc_rate   1092
## density       1092
## avginc        1092
## pop           1092
## pb1064        1092
## pw1064        1092
## pm1029        1092
##
## Multiple R-squared:  0.9562 ,    Adjusted R-squared:  0.953
## Multiple R-squared (proj. model):  0.05635 , Adjusted R-squared (proj. model):  -0.01278
## F-statistic (proj. model): 7.823 on 8 and 1092 DF,  p-value: 2.935e-10
```

Note that once again, it's important to have the “~” to begin the “fixed\_effects” argument (not sure why) and to separate the fixed effects dimensions with a “+” (with the individual fixed effects going first). Again, exactly the estimates and standard errors we wanted. Since we'll again be testing the fixed effects jointly for significance, we'll need to include the fixed effects as regressors explicitly:

```
# 4
mod.2i.4 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), se_type = "stata", data = guns)
summary(mod.2i.4)

##
## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density + avginc +
##      pop + pb1064 + pw1064 + pm1029 + factor(state) + factor(year),
##      data = guns, se_type = "stata")
##
## Standard error type:  HC1
##
## Coefficients:
##              Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)    3.972e+00  4.490e-01   8.8463 3.571e-18
## shall         -2.799e-02  1.937e-02  -1.4450 1.488e-01
## incarc_rate     7.599e-05  8.292e-05   0.9165 3.596e-01
## density       -9.155e-02  6.487e-02  -1.4114 1.584e-01
## avginc         9.586e-04  7.197e-03   0.1332 8.941e-01
## pop           -4.754e-03  6.703e-03  -0.7093 4.783e-01
## pb1064         2.919e-02  2.104e-02   1.3874 1.656e-01
## pw1064         9.250e-03  8.518e-03   1.0859 2.777e-01
## pm1029         7.333e-02  1.878e-02   3.9052 9.992e-05
## factor(state)Alaska  -1.474e-01  6.964e-02  -2.1166 3.452e-02
## factor(state)Arizona   1.394e-01  7.168e-02   1.9441 5.214e-02
## factor(state)Arkansas  -1.565e-01  5.377e-02  -2.9105 3.682e-03
## factor(state)California  5.385e-01  1.820e-01   2.9595 3.148e-03
## factor(state)Colorado  -1.261e-01  1.008e-01  -1.2508 2.113e-01
## factor(state)Connecticut -1.074e-01  1.213e-01  -0.8853 3.762e-01
## factor(state)Delaware   3.334e-02  7.009e-02   0.4758 6.343e-01
```

## factor(state)District of Columbia	1.988e+00	6.311e-01	3.1506	1.674e-03
## factor(state)Florida	8.598e-01	9.898e-02	8.6867	1.341e-17
## factor(state)Georgia	3.073e-02	4.099e-02	0.7498	4.535e-01
## factor(state)Hawaii	-1.010e+00	2.207e-01	-4.5769	5.259e-06
## factor(state)Idaho	-6.831e-01	1.078e-01	-6.3389	3.380e-10
## factor(state)Illinois	4.953e-01	9.159e-02	5.4078	7.834e-08
## factor(state)Indiana	-2.361e-01	9.855e-02	-2.3957	1.676e-02
## factor(state)Iowa	-7.003e-01	1.122e-01	-6.2410	6.210e-10
## factor(state)Kansas	-2.824e-01	8.373e-02	-3.3733	7.689e-04
## factor(state)Kentucky	-4.660e-01	9.120e-02	-5.1094	3.812e-07
## factor(state)Louisiana	2.727e-01	4.284e-02	6.3651	2.867e-10
## factor(state>Maine	-1.142e+00	1.322e-01	-8.6334	2.077e-17
## factor(state)Maryland	4.707e-01	6.454e-02	7.2929	5.816e-13
## factor(state)Massachusetts	2.664e-01	1.291e-01	2.0642	3.923e-02
## factor(state)Michigan	2.886e-01	8.751e-02	3.2979	1.005e-03
## factor(state)Minnesota	-6.150e-01	1.106e-01	-5.5605	3.381e-08
## factor(state)Mississippi	-5.105e-01	6.878e-02	-7.4220	2.316e-13
## factor(state)Missouri	1.584e-01	7.516e-02	2.1071	3.534e-02
## factor(state)Montana	-1.027e+00	1.052e-01	-9.7619	1.221e-21
## factor(state)Nebraska	-5.439e-01	1.021e-01	-5.3275	1.209e-07
## factor(state)Nevada	3.236e-01	8.258e-02	3.9191	9.442e-05
## factor(state)New Hampshire	-1.309e+00	1.263e-01	-10.3629	4.573e-24
## factor(state)New Jersey	2.104e-01	1.206e-01	1.7449	8.129e-02
## factor(state)New Mexico	2.877e-01	6.740e-02	4.2680	2.144e-05
## factor(state)New York	6.948e-01	1.437e-01	4.8360	1.515e-06
## factor(state)North Carolina	-7.169e-02	4.582e-02	-1.5647	1.180e-01
## factor(state)North Dakota	-2.073e+00	1.038e-01	-19.9742	6.667e-76
## factor(state)Ohio	-8.862e-02	1.097e-01	-0.8081	4.192e-01
## factor(state)Oklahoma	-9.372e-02	5.191e-02	-1.8054	7.128e-02
## factor(state)Oregon	3.654e-02	1.024e-01	0.3567	7.214e-01
## factor(state)Pennsylvania	-1.519e-01	1.208e-01	-1.2567	2.091e-01
## factor(state)Rhode Island	-2.263e-01	1.258e-01	-1.7989	7.232e-02
## factor(state)South Carolina	2.759e-01	4.844e-02	5.6961	1.575e-08
## factor(state)South Dakota	-1.192e+00	9.250e-02	-12.8901	1.717e-35
## factor(state)Tennessee	9.298e-02	6.804e-02	1.3666	1.720e-01
## factor(state)Texas	1.200e-01	1.206e-01	0.9956	3.197e-01
## factor(state)Utah	-7.211e-01	1.210e-01	-5.9581	3.438e-09
## factor(state)Vermont	-1.326e+00	1.291e-01	-10.2764	1.038e-23
## factor(state)Virginia	-5.622e-01	5.714e-02	-9.8381	6.103e-22
## factor(state)Washington	-1.219e-01	9.470e-02	-1.2876	1.982e-01
## factor(state)West Virginia	-9.411e-01	1.031e-01	-9.1282	3.281e-19
## factor(state)Wisconsin	-8.292e-01	1.025e-01	-8.0904	1.572e-15
## factor(state)Wyoming	-6.536e-01	1.071e-01	-6.1012	1.460e-09
## factor(year)78	5.853e-02	3.441e-02	1.7007	8.929e-02
## factor(year)79	1.639e-01	3.259e-02	5.0312	5.695e-07
## factor(year)80	2.171e-01	3.497e-02	6.2066	7.675e-10
## factor(year)81	2.173e-01	3.560e-02	6.1028	1.445e-09
## factor(year)82	1.946e-01	3.350e-02	5.8099	8.192e-09
## factor(year)83	1.586e-01	3.555e-02	4.4621	8.958e-06
## factor(year)84	1.930e-01	3.908e-02	4.9380	9.124e-07
## factor(year)85	2.445e-01	4.293e-02	5.6949	1.586e-08
## factor(year)86	3.241e-01	4.758e-02	6.8115	1.592e-11
## factor(year)87	3.244e-01	5.172e-02	6.2720	5.126e-10
## factor(year)88	3.867e-01	5.670e-02	6.8210	1.495e-11

## factor(year)89	4.422e-01	6.139e-02	7.2028	1.097e-12
## factor(year)90	5.430e-01	7.697e-02	7.0551	3.057e-12
## factor(year)91	5.959e-01	8.060e-02	7.3939	2.834e-13
## factor(year)92	6.275e-01	8.513e-02	7.3709	3.339e-13
## factor(year)93	6.497e-01	8.836e-02	7.3530	3.793e-13
## factor(year)94	6.354e-01	9.264e-02	6.8590	1.159e-11
## factor(year)95	6.277e-01	9.658e-02	6.4994	1.224e-10
## factor(year)96	5.713e-01	1.011e-01	5.6524	2.019e-08
## factor(year)97	5.501e-01	1.050e-01	5.2374	1.953e-07
## factor(year)98	4.933e-01	1.105e-01	4.4649	8.841e-06
## factor(year)99	4.329e-01	1.160e-01	3.7309	2.006e-04
##	CI Lower	CI Upper	DF	
## (Intercept)	3.091e+00	4.8530018	1092	
## shall	-6.601e-02	0.0100196	1092	
## incarc_rate	-8.671e-05	0.0002387	1092	
## density	-2.188e-01	0.0357256	1092	
## avginc	-1.316e-02	0.0150800	1092	
## pop	-1.791e-02	0.0083976	1092	
## pb1064	-1.209e-02	0.0704637	1092	
## pw1064	-7.464e-03	0.0259639	1092	
## pm1029	3.648e-02	0.1101670	1092	
## factor(state)Alaska	-2.840e-01	-0.0107541	1092	
## factor(state)Arizona	-1.292e-03	0.2800054	1092	
## factor(state)Arkansas	-2.620e-01	-0.0509951	1092	
## factor(state)California	1.815e-01	0.8955929	1092	
## factor(state)Colorado	-3.238e-01	0.0716814	1092	
## factor(state)Connecticut	-3.453e-01	0.1306034	1092	
## factor(state)Delaware	-1.042e-01	0.1708617	1092	
## factor(state)District of Columbia	7.500e-01	3.2266616	1092	
## factor(state)Florida	6.656e-01	1.0540259	1092	
## factor(state)Georgia	-4.969e-02	0.1111637	1092	
## factor(state)Hawaii	-1.443e+00	-0.5770525	1092	
## factor(state)Idaho	-8.945e-01	-0.4716518	1092	
## factor(state)Illinois	3.156e-01	0.6749862	1092	
## factor(state)Indiana	-4.295e-01	-0.0427243	1092	
## factor(state)Iowa	-9.205e-01	-0.4801470	1092	
## factor(state)Kansas	-4.467e-01	-0.1181500	1092	
## factor(state)Kentucky	-6.449e-01	-0.2870351	1092	
## factor(state)Louisiana	1.886e-01	0.3567818	1092	
## factor(state)Maine	-1.401e+00	-0.8822160	1092	
## factor(state)Maryland	3.440e-01	0.5973223	1092	
## factor(state)Massachusetts	1.318e-02	0.5196924	1092	
## factor(state)Michigan	1.169e-01	0.4603109	1092	
## factor(state)Minnesota	-8.320e-01	-0.3979957	1092	
## factor(state)Mississippi	-6.455e-01	-0.3755413	1092	
## factor(state)Missouri	1.089e-02	0.3058613	1092	
## factor(state)Montana	-1.233e+00	-0.8202736	1092	
## factor(state)Nebraska	-7.442e-01	-0.3435620	1092	
## factor(state)Nevada	1.616e-01	0.4856771	1092	
## factor(state)New Hampshire	-1.557e+00	-1.0609113	1092	
## factor(state)New Jersey	-2.620e-02	0.4470395	1092	
## factor(state)New Mexico	1.554e-01	0.4199063	1092	
## factor(state)New York	4.129e-01	0.9767127	1092	
## factor(state)North Carolina	-1.616e-01	0.0182109	1092	



```
## factor(state)North Dakota      -2.276e+00 -1.8690888 1092
## factor(state)Ohio               -3.038e-01  0.1265583 1092
## factor(state)Oklahoma           -1.956e-01  0.0081342 1092
## factor(state)Oregon             -1.644e-01  0.2374939 1092
## factor(state)Pennsylvania       -3.889e-01  0.0852368 1092
## factor(state)Rhode Island       -4.731e-01  0.0205370 1092
## factor(state)South Carolina     1.809e-01  0.3709622 1092
## factor(state)South Dakota       -1.374e+00 -1.0108516 1092
## factor(state)Tennessee          -4.052e-02  0.2264865 1092
## factor(state)Texas              -1.165e-01  0.3565820 1092
## factor(state)Utah               -9.586e-01 -0.4836416 1092
## factor(state)Vermont            -1.579e+00 -1.0729863 1092
## factor(state)Virginia           -6.743e-01 -0.4500362 1092
## factor(state)Washington         -3.078e-01  0.0638812 1092
## factor(state)West Virginia      -1.143e+00 -0.7387812 1092
## factor(state)Wisconsin          -1.030e+00 -0.6280844 1092
## factor(state)Wyoming            -8.638e-01 -0.4434093 1092
## factor(year)78                  -8.998e-03  0.1260507 1092
## factor(year)79                  1.000e-01  0.2278873 1092
## factor(year)80                  1.485e-01  0.2857014 1092
## factor(year)81                  1.474e-01  0.2871053 1092
## factor(year)82                  1.289e-01  0.2603645 1092
## factor(year)83                  8.888e-02  0.2284073 1092
## factor(year)84                  1.163e-01  0.2696730 1092
## factor(year)85                  1.602e-01  0.3287086 1092
## factor(year)86                  2.307e-01  0.4174481 1092
## factor(year)87                  2.229e-01  0.4258390 1092
## factor(year)88                  2.755e-01  0.4979918 1092
## factor(year)89                  3.217e-01  0.5626788 1092
## factor(year)90                  3.920e-01  0.6940776 1092
## factor(year)91                  4.378e-01  0.7540942 1092
## factor(year)92                  4.605e-01  0.7945618 1092
## factor(year)93                  4.764e-01  0.8231231 1092
## factor(year)94                  4.536e-01  0.8171923 1092
## factor(year)95                  4.382e-01  0.8171777 1092
## factor(year)96                  3.730e-01  0.7696754 1092
## factor(year)97                  3.440e-01  0.7562098 1092
## factor(year)98                  2.765e-01  0.7100695 1092
## factor(year)99                  2.052e-01  0.6605369 1092
##
## Multiple R-squared:  0.9562 ,    Adjusted R-squared:  0.953
## F-statistic: 479.8 on 80 and 1092 DF,  p-value: < 2.2e-16
```

Now we want to test the state FEs separately from the

```
## F-statistic:
coef.names <- mod.2i.4$coefficients %>% names
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2i.4, state.coefficients, test = "F")
```

```
## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
```

```

## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0
## factor(state)Florida = 0
## factor(state)Georgia = 0
## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state)Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0
## factor(state)Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lvio ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##           pw1064 + pm1029 + factor(state) + factor(year)
##

```

```
##   Res.Df Df      F    Pr(>F)
## 1    1142
## 2    1092 50 309.29 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

linearHypothesis(mod.2i.4, year.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0
## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lvio ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state) + factor(year)
##
##   Res.Df Df      F    Pr(>F)
## 1    1114
## 2    1092 22  13.9 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

### Regression 5: yes controls, state and year fixed effects, yes clustering

*lm\_robust* includes a “clusters” argument. Always choose the individual dimension for clustering. And once again, do not forget the “se\_type = ‘stata’” argument:

```
# 5
mod.2i.5 <- lm_robust(lvio ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), clusters = state, se_type = "stata", data = guns)
summary(mod.2i.5)

##
```

```

## Call:
## lm_robust(formula = lvio ~ shall + incarc_rate + density + avginc +
##      pop + pb1064 + pw1064 + pm1029 + factor(state) + factor(year),
##      data = guns, clusters = state, se_type = "stata")
##
## Standard error type:  stata
##
## Coefficients:
##
##      Estimate Std. Error  t value  Pr(>|t|)
## (Intercept)      3.972e+00  1.1097648   3.57913  7.778e-04
## shall            -2.799e-02  0.0416385  -0.67230  5.045e-01
## incarc_rate       7.599e-05  0.0002126   0.35746  7.222e-01
## density          -9.155e-02  0.1266662  -0.72280  4.732e-01
## avginc           9.586e-04  0.0168665   0.05684  9.549e-01
## pop             -4.754e-03  0.0155742  -0.30528  7.614e-01
## pb1064           2.919e-02  0.0506622   0.57609  5.671e-01
## pw1064           9.250e-03  0.0242941   0.38076  7.050e-01
## pm1029           7.333e-02  0.0536612   1.36645  1.779e-01
## factor(state)Alaska      -1.474e-01  0.1280179  -1.15139  2.550e-01
## factor(state)Arizona      1.394e-01  0.1626619   0.85673  3.957e-01
## factor(state)Arkansas     -1.565e-01  0.0916509  -1.70763  9.391e-02
## factor(state)California    5.385e-01  0.4638773   1.16095  2.512e-01
## factor(state)Colorado     -1.261e-01  0.2620806  -0.48097  6.326e-01
## factor(state)Connecticut  -1.074e-01  0.2988469  -0.35927  7.209e-01
## factor(state)Delaware      3.334e-02  0.1198122   0.27830  7.819e-01
## factor(state)District of Columbia  1.988e+00  1.2841751   1.54834  1.278e-01
## factor(state)Florida      8.598e-01  0.2471365   3.47910  1.052e-03
## factor(state)Georgia       3.073e-02  0.0549982   0.55883  5.788e-01
## factor(state)Hawaii       -1.010e+00  0.5318146  -1.89929  6.330e-02
## factor(state)Idaho        -6.831e-01  0.2410346  -2.83403  6.613e-03
## factor(state)Illinois      4.953e-01  0.2358775   2.09974  4.082e-02
## factor(state)Indiana      -2.361e-01  0.2436553  -0.96895  3.372e-01
## factor(state)Iowa         -7.003e-01  0.2618793  -2.67423  1.009e-02
## factor(state)Kansas       -2.824e-01  0.1962850  -1.43890  1.564e-01
## factor(state)Kentucky     -4.660e-01  0.2167101  -2.15027  3.639e-02
## factor(state)Louisiana     2.727e-01  0.0840986   3.24279  2.111e-03
## factor(state)Maine        -1.142e+00  0.2883486  -3.95941  2.381e-04
## factor(state)Maryland      4.707e-01  0.1408361   3.34208  1.580e-03
## factor(state)Massachusetts  2.664e-01  0.3224811   0.82620  4.126e-01
## factor(state)Michigan      2.886e-01  0.2151058   1.34168  1.858e-01
## factor(state)Minnesota    -6.150e-01  0.2797847  -2.19818  3.259e-02
## factor(state)Mississippi   -5.105e-01  0.1683598  -3.03221  3.841e-03
## factor(state)Missouri      1.584e-01  0.1845778   0.85805  3.950e-01
## factor(state)Montana      -1.027e+00  0.2074646  -4.94843  8.880e-06
## factor(state)Nebraska     -5.439e-01  0.2245000  -2.42260  1.908e-02
## factor(state)Nevada        3.236e-01  0.1887725   1.71445  9.264e-02
## factor(state)New Hampshire -1.309e+00  0.3161359  -4.13970  1.334e-04
## factor(state)New Jersey    2.104e-01  0.2901715   0.72515  4.717e-01
## factor(state)New Mexico    2.877e-01  0.1363345   2.10995  3.989e-02
## factor(state)New York      6.948e-01  0.3355115   2.07088  4.355e-02
## factor(state)North Carolina -7.169e-02  0.0749761  -0.95613  3.436e-01
## factor(state)North Dakota  -2.073e+00  0.2262214  -9.16225  2.804e-12
## factor(state)Ohio         -8.862e-02  0.2822928  -0.31393  7.549e-01
## factor(state)Oklahoma     -9.372e-02  0.1048261  -0.89406  3.756e-01

```

## factor(state)Oregon	3.654e-02	0.2537003	0.14401	8.861e-01
## factor(state)Pennsylvania	-1.519e-01	0.3235810	-0.46929	6.409e-01
## factor(state)Rhode Island	-2.263e-01	0.2767852	-0.81749	4.175e-01
## factor(state)South Carolina	2.759e-01	0.0743856	3.70928	5.219e-04
## factor(state)South Dakota	-1.192e+00	0.1791106	-6.65707	2.065e-08
## factor(state)Tennessee	9.298e-02	0.1433209	0.64878	5.195e-01
## factor(state)Texas	1.200e-01	0.2922980	0.41064	6.831e-01
## factor(state)Utah	-7.211e-01	0.2614627	-2.75803	8.100e-03
## factor(state)Vermont	-1.326e+00	0.2916528	-4.54721	3.476e-05
## factor(state)Virginia	-5.622e-01	0.1355022	-4.14867	1.296e-04
## factor(state)Washington	-1.219e-01	0.2486475	-0.49040	6.260e-01
## factor(state)West Virginia	-9.411e-01	0.2600945	-3.61818	6.906e-04
## factor(state)Wisconsin	-8.292e-01	0.2514955	-3.29701	1.803e-03
## factor(state)Wyoming	-6.536e-01	0.2461306	-2.65554	1.059e-02
## factor(year)78	5.853e-02	0.0165213	3.54247	8.693e-04
## factor(year)79	1.639e-01	0.0250116	6.55490	2.983e-08
## factor(year)80	2.171e-01	0.0341749	6.35191	6.194e-08
## factor(year)81	2.173e-01	0.0400829	5.42014	1.716e-06
## factor(year)82	1.946e-01	0.0476286	4.08647	1.585e-04
## factor(year)83	1.586e-01	0.0607288	2.61235	1.184e-02
## factor(year)84	1.930e-01	0.0787452	2.45079	1.779e-02
## factor(year)85	2.445e-01	0.0943093	2.59228	1.247e-02
## factor(year)86	3.241e-01	0.1113838	2.90967	5.388e-03
## factor(year)87	3.244e-01	0.1278176	2.53772	1.432e-02
## factor(year)88	3.867e-01	0.1428701	2.70694	9.267e-03
## factor(year)89	4.422e-01	0.1570114	2.81645	6.933e-03
## factor(year)90	5.430e-01	0.2005249	2.70813	9.238e-03
## factor(year)91	5.959e-01	0.2086882	2.85568	6.238e-03
## factor(year)92	6.275e-01	0.2219437	2.82737	6.733e-03
## factor(year)93	6.497e-01	0.2297025	2.82862	6.710e-03
## factor(year)94	6.354e-01	0.2385238	2.66396	1.037e-02
## factor(year)95	6.277e-01	0.2478471	2.53254	1.451e-02
## factor(year)96	5.713e-01	0.2591432	2.20474	3.210e-02
## factor(year)97	5.501e-01	0.2672680	2.05829	4.479e-02
## factor(year)98	4.933e-01	0.2808721	1.75628	8.516e-02
## factor(year)99	4.329e-01	0.2926991	1.47892	1.454e-01
##	CI Lower	CI Upper	DF	
## (Intercept)	1.742969	6.201025	50	
## shall	-0.111627	0.055640	50	
## incarc_rate	-0.000351	0.000503	50	
## density	-0.345971	0.162862	50	
## avginc	-0.032919	0.034836	50	
## pop	-0.036036	0.026527	50	
## pb1064	-0.072572	0.130944	50	
## pw1064	-0.039546	0.058046	50	
## pm1029	-0.034456	0.181107	50	
## factor(state)Alaska	-0.404530	0.109733	50	
## factor(state)Arizona	-0.187359	0.466073	50	
## factor(state)Arkansas	-0.340592	0.027580	50	
## factor(state)California	-0.393187	1.470263	50	
## factor(state)Colorado	-0.652458	0.400351	50	
## factor(state)Connecticut	-0.707617	0.492886	50	
## factor(state)Delaware	-0.207306	0.273994	50	
## factor(state)District of Columbia	-0.590998	4.567685	50	

## factor(state)Florida	0.363425	1.356201	50
## factor(state)Georgia	-0.079732	0.141202	50
## factor(state)Hawaii	-2.078254	0.058108	50
## factor(state)Idaho	-1.167231	-0.198967	50
## factor(state)Illinois	0.021508	0.969056	50
## factor(state)Indiana	-0.725485	0.253307	50
## factor(state>Iowa	-1.226325	-0.174325	50
## factor(state)Kansas	-0.676685	0.111815	50
## factor(state)Kentucky	-0.901260	-0.030710	50
## factor(state)Louisiana	0.103797	0.441631	50
## factor(state>Maine	-1.720856	-0.562525	50
## factor(state)Maryland	0.187808	0.753563	50
## factor(state)Massachusetts	-0.381287	0.914157	50
## factor(state)Michigan	-0.143449	0.720656	50
## factor(state)Minnesota	-1.176981	-0.053053	50
## factor(state)Mississippi	-0.848663	-0.172342	50
## factor(state)Missouri	-0.212358	0.529113	50
## factor(state)Montana	-1.443329	-0.609919	50
## factor(state)Nebraska	-0.994794	-0.092951	50
## factor(state)Nevada	-0.055520	0.702802	50
## factor(state)New Hampshire	-1.943684	-0.673729	50
## factor(state)New Jersey	-0.372408	0.793245	50
## factor(state)New Mexico	0.013824	0.561495	50
## factor(state)New York	0.020911	1.368700	50
## factor(state)North Carolina	-0.222281	0.078907	50
## factor(state)North Dakota	-2.527077	-1.618319	50
## factor(state)Ohio	-0.655622	0.478381	50
## factor(state)Oklahoma	-0.304270	0.116829	50
## factor(state)Oregon	-0.473036	0.546108	50
## factor(state)Pennsylvania	-0.801783	0.498080	50
## factor(state)Rhode Island	-0.782208	0.329671	50
## factor(state)South Carolina	0.126509	0.425325	50
## factor(state)South Dakota	-1.552107	-0.832598	50
## factor(state)Tennessee	-0.194885	0.380852	50
## factor(state)Texas	-0.467069	0.707126	50
## factor(state)Utah	-1.246286	-0.195959	50
## factor(state)Vermont	-1.912009	-0.740405	50
## factor(state)Virginia	-0.834318	-0.289990	50
## factor(state)Washington	-0.621359	0.377487	50
## factor(state)West Virginia	-1.463483	-0.418653	50
## factor(state)Wisconsin	-1.334327	-0.324039	50
## factor(state)Wyoming	-1.147978	-0.159242	50
## factor(year)78	0.025342	0.091710	50
## factor(year)79	0.113711	0.214186	50
## factor(year)80	0.148434	0.285718	50
## factor(year)81	0.136746	0.297764	50
## factor(year)82	0.098968	0.290298	50
## factor(year)83	0.036667	0.280622	50
## factor(year)84	0.034824	0.351153	50
## factor(year)85	0.055051	0.433902	50
## factor(year)86	0.100369	0.547811	50
## factor(year)87	0.067636	0.581094	50
## factor(year)88	0.099778	0.673704	50
## factor(year)89	0.126847	0.757581	50

```
## factor(year)90          0.140282  0.945814 50
## factor(year)91          0.176783  1.015108 50
## factor(year)92          0.181730  1.073304 50
## factor(year)93          0.188370  1.111113 50
## factor(year)94          0.156330  1.114508 50
## factor(year)95          0.129867  1.125499 50
## factor(year)96          0.050838  1.091847 50
## factor(year)97          0.013292  1.086939 50
## factor(year)98         -0.070858  1.057439 50
## factor(year)99         -0.155026  1.020781 50
##
## Multiple R-squared:  0.9562 ,    Adjusted R-squared:  0.953
## F-statistic:      NA on 80 and 50 DF,  p-value: NA
```

This time, we only want to test the year fixed effects:

```
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2i.5, year.coefficients, test = "F")
```

```
## Linear hypothesis test
##
## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0
## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lvio ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state) + factor(year)
##
##   Res.Df Df       F    Pr(>F)
## 1    1114
## 2    1092 22 20.675 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

## 2ii: Dependent variable $\ln(\text{rob})$

I'll suppress the regression output so that we don't just produce a massive document full of fixed effects estimates, but the results do indeed match up exactly with the Stata solutions:

```
# 1
mod.2ii.1 <- lm_robust(lrob ~ shall, data = guns, se_type = "stata")
# summary(mod.2ii.1)

# 2
mod.2ii.2 <- lm_robust(lrob ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029, data = guns, se_type = "stata")
# summary(mod.2ii.2)

# 3
mod.2ii.3 <- lm_robust(lrob ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state),
  se_type = "stata", data = guns)
# summary(mod.2ii.3) F-statistic:
coef.names <- names(mod.2ii.3$coefficients)
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
linearHypothesis(mod.2ii.3, state.coefficients, test = "F")
```

```
## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0
## factor(state)Florida = 0
## factor(state)Georgia = 0
## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state)Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
```



```

## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0
## factor(state)Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lrob ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state)
##
##   Res.Df Df      F    Pr(>F)
## 1    1164
## 2    1114 50 190.47 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# 4
mod.2ii.4 <- lm_robust(lrob ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), se_type = "stata", data = guns)
# summary(mod.2ii.4) F-statistic:
coef.names <- mod.2ii.4$coefficients %>% names
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2ii.4, state.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0
## factor(state)Florida = 0
## factor(state)Georgia = 0

```

```

## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state)Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0
## factor(state)Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lrob ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state) + factor(year)
##
##   Res.Df Df      F    Pr(>F)
## 1    1142
## 2    1092 50 243.39 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

linearHypothesis(mod.2ii.4, year.coefficients, test = "F")

## Linear hypothesis test
##

```

```

## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0
## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lrob ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state) + factor(year)
##
##   Res.Df Df       F    Pr(>F)
## 1     1114
## 2     1092 22 12.392 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# 5
mod.2ii.5 <- lm_robust(lrob ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), clusters = state, se_type = "stata", data = guns)
# summary(mod.2ii.5)
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2ii.5, year.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0

```

```

## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lrob ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##      pw1064 + pm1029 + factor(state) + factor(year)
##
##      Res.Df Df      F    Pr(>F)
## 1      1114
## 2      1092 22 24.73 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

### 2iii: Dependent variable ln(mur)

```

# 1
mod.2iii.1 <- lm_robust(lmur ~ shall, data = guns, se_type = "stata")
# summary(mod.2iii.1)

# 2
mod.2iii.2 <- lm_robust(lmur ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029, data = guns, se_type = "stata")
# summary(mod.2iii.2)

# 3
mod.2iii.3 <- lm_robust(lmur ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state),
  se_type = "stata", data = guns)
# summary(mod.2iii.3) F-statistic:
coef.names <- names(mod.2iii.3$coefficients)
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
linearHypothesis(mod.2iii.3, state.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0

```

```

## factor(state)Florida = 0
## factor(state)Georgia = 0
## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state>Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0
## factor(state>Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lmur ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##      pw1064 + pm1029 + factor(state)
##
##      Res.Df Df      F    Pr(>F)
## 1      1164
## 2      1114 50 88.219 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

# 4
mod.2iii.4 <- lm_robust(lmur ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), se_type = "stata", data = guns)
# summary(mod.2iii.4) F-statistic:
coef.names <- mod.2iii.4$coefficients %>% names
state.coefficients <- coef.names[startsWith(coef.names, "factor(state)")]
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2iii.4, state.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(state)Alaska = 0
## factor(state)Arizona = 0
## factor(state)Arkansas = 0
## factor(state)California = 0
## factor(state)Colorado = 0
## factor(state)Connecticut = 0
## factor(state)Delaware = 0
## factor(state)District of Columbia = 0
## factor(state)Florida = 0
## factor(state)Georgia = 0
## factor(state)Hawaii = 0
## factor(state)Idaho = 0
## factor(state)Illinois = 0
## factor(state)Indiana = 0
## factor(state>Iowa = 0
## factor(state)Kansas = 0
## factor(state)Kentucky = 0
## factor(state)Louisiana = 0
## factor(state>Maine = 0
## factor(state)Maryland = 0
## factor(state)Massachusetts = 0
## factor(state)Michigan = 0
## factor(state)Minnesota = 0
## factor(state)Mississippi = 0
## factor(state)Missouri = 0
## factor(state)Montana = 0
## factor(state)Nebraska = 0
## factor(state)Nevada = 0
## factor(state)New Hampshire = 0
## factor(state)New Jersey = 0
## factor(state)New Mexico = 0
## factor(state)New York = 0
## factor(state)North Carolina = 0
## factor(state)North Dakota = 0
## factor(state)Ohio = 0
## factor(state)Oklahoma = 0
## factor(state)Oregon = 0
## factor(state)Pennsylvania = 0
## factor(state)Rhode Island = 0
## factor(state)South Carolina = 0
## factor(state)South Dakota = 0

```

```

## factor(state)Tennessee = 0
## factor(state)Texas = 0
## factor(state)Utah = 0
## factor(state)Vermont = 0
## factor(state)Virginia = 0
## factor(state)Washington = 0
## factor(state)West Virginia = 0
## factor(state)Wisconsin = 0
## factor(state)Wyoming = 0
##
## Model 1: restricted model
## Model 2: lmur ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##      pw1064 + pm1029 + factor(state) + factor(year)
##
##      Res.Df Df      F    Pr(>F)
## 1      1142
## 2      1092 50 106.69 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

linearHypothesis(mod.2iii.4, year.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0
## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lmur ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##      pw1064 + pm1029 + factor(state) + factor(year)
##
##      Res.Df Df      F    Pr(>F)
## 1      1114
## 2      1092 22  9.7281 < 2.2e-16 ***

```

```

## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# 5
mod.2iii.5 <- lm_robust(lmur ~ shall + incarc_rate + density +
  avginc + pop + pb1064 + pw1064 + pm1029 + factor(state) +
  factor(year), clusters = state, se_type = "stata", data = guns)
# summary(mod.2iii.5)
year.coefficients <- coef.names[startsWith(coef.names, "factor(year)")]
linearHypothesis(mod.2iii.5, year.coefficients, test = "F")

## Linear hypothesis test
##
## Hypothesis:
## factor(year)78 = 0
## factor(year)79 = 0
## factor(year)80 = 0
## factor(year)81 = 0
## factor(year)82 = 0
## factor(year)83 = 0
## factor(year)84 = 0
## factor(year)85 = 0
## factor(year)86 = 0
## factor(year)87 = 0
## factor(year)88 = 0
## factor(year)89 = 0
## factor(year)90 = 0
## factor(year)91 = 0
## factor(year)92 = 0
## factor(year)93 = 0
## factor(year)94 = 0
## factor(year)95 = 0
## factor(year)96 = 0
## factor(year)97 = 0
## factor(year)98 = 0
## factor(year)99 = 0
##
## Model 1: restricted model
## Model 2: lmur ~ shall + incarc_rate + density + avginc + pop + pb1064 +
##          pw1064 + pm1029 + factor(state) + factor(year)
##
##   Res.Df Df       F    Pr(>F)
## 1     1114
## 2     1092 22 18.751 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

### Question 3

**3a: What measures of firm performance would you include in an equation? What are some of the timing issues?**

Potential measures of firm performance include: stock prices, percentage change in stock prices (i.e., returns), firm's value (i.e., market capitalization), ROA, ROE, Net Income, and so on. Some of the timing issues can



be that the previous day market performance and firm's performance can influence the performance of the firm today. So, we may need to include lagged values of these performance measures.

### 3b: What other factors might you control for in the equation?

Firm's performance could be influenced by other factors in addition to overall market performance. Some of these factors that you need to control for can include i) firm specific factors such as size of the firm, management quality, leverage, corporate social responsibility, etc. and ii) other macroeconomic factors like inflation, GDP, interest rates, and so on.

### 3c: Write an equation that allows you to estimate the effects of the overall stock market performance on the percentage change in firm's stock price. How would you estimate this equation? Why would you choose this method?

An unobserved effects model is:

$$\log\left(\frac{P_{i,t}}{P_{i,t-1}}\right) = \beta_0 + \alpha_i + \lambda_t + \beta_1 \log\left(\frac{SP_{i,t}}{SP_{i,t-1}}\right) + \beta_2 \log(SIZE_{i,t}) + \dots + u_{i,t}$$

The outcome variable is the percentage change in stock prices or rate of return for firm  $i$  at time  $t$  and the ratio in the RHS is for the broad market.  $\beta_1$  is the percentage change in firm performance given a one percentage-point increase in the market index. It is likely that  $\alpha_i$  and  $\lambda_t$  are correlated with firm size, and other control factors. So fixed effects (i.e., time and firm) estimation is appropriate.

### 3d: Implement your strategy discussed above using data from Yahoo Finance for any ten US companies of your choice as well as the stock price for the S&P500

I don't think it's worth our time to go through this exercise since I'm doing multiple problem sets. Just a reminder here that the answer entails creating lagged and differenced variables, which we learned how to do in the context of time series (see: R guide to PS8 practice questions and R solutions to PS8 when I post them on Friday).