Historical log of times I played tennis:

Mild	Cool	Mild	Hot	Mild	Mild	Mild	Cool	Mild	Cool	Cool	Hot	Hot	Hot	Temp
Rain	Rain	Rain	Overcast	Overcast	Sunny	Rain	Sunny	Sunny	Overcast	Rain	Overcast	Sunny	Sunny	Outlook
High	Normal	High	Normal	High	Normal	Normal	Normal	High	Normal	Normal	High	High	High	Humidity
False	True	True	False	True	True	False	False	False	True	False	False	True	False	Windy
Yes	No	No	Yes	Yes	Yes	Yes	Yes	No	Yes	Yes	Yes	No	No	Played

```
def will_play(temp, outlook, humidity,\
    windy):

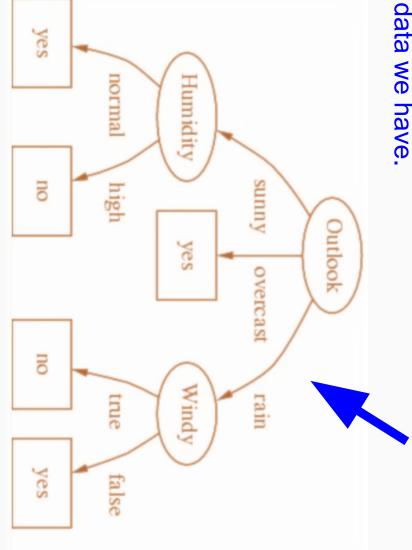
if outlook == 'sunny':
    if humidity == 'normal':
        return True
    else: # humidity == 'high'
        return False

else: # outlook == 'overcast':
    return True:
    return False
else: # windy == True:
    return True
```

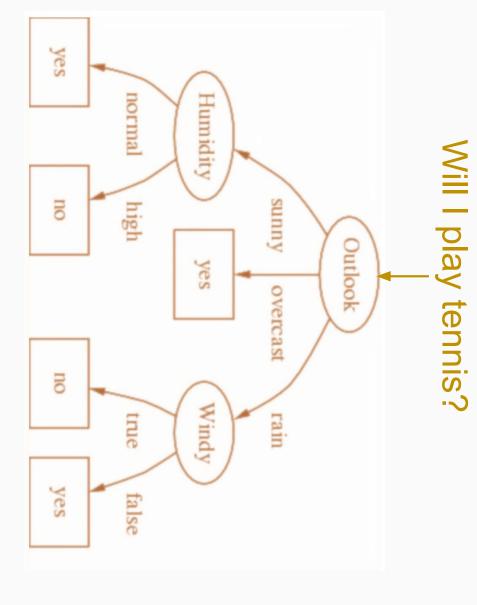
DON'T WRITE CODE LIKE THIS!!!! AHHH!!! #%#%#%@#%!#\$^^*%&(%^&*\$%^&#\$%

```
def will_play(temp, outlook,
                                                                                                                                                                                                                                                                                                                                                           j.
                                                                                                           else:
                                                                                                                                                                                          elif outlook == 'overcast':
                                                                                                                                                                                                                                                                                                                                                          outlook == 'sunny':
                                                                                                                                                                                                                                                                          else: # humidity == 'high'
                          else: \# windy ==
                                                                                if windy == True:
                                                                                                                                                                return True
                                                                                                                                                                                                                                                                                                                               if humidity == 'normal':
                                                                                                           # outlook == 'rain'
                                                                                                                                                                                                                                                                                                    return True
                                                     return False
                                                                                                                                                                                                                                                return False
return True
                                                                                                                                                                                                                                                                                                                                                                                                              windy):
                          False:
                                                                                                                                                                                                                                                                                                                                                                                                                                          humi
                                                                                                                                                                                                                                                                                                                                                                                                                                         ity,
```

Instead, let's write an algorithm to build a **Decision Tree** for us, based on the training data we have.



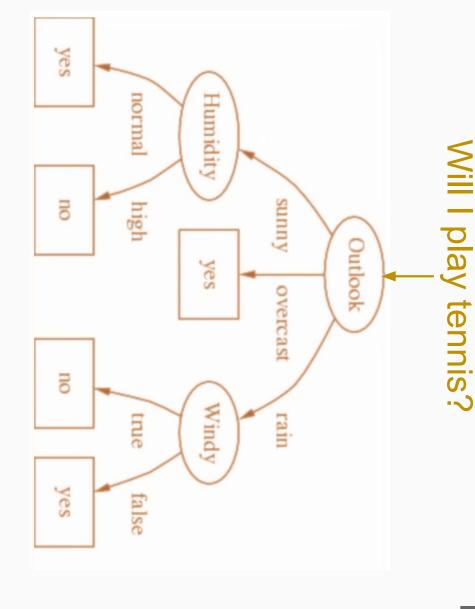
Benefits of a decision tree:



Benefits:

- non-parametric, non-linear
- can be used for classification and for regression
- real and/or categorical features
- easy to interpret
- computationally cheap prediction
- handles missing values and outliers
- can handle irrelevant features

Drawbacks of Decision Trees

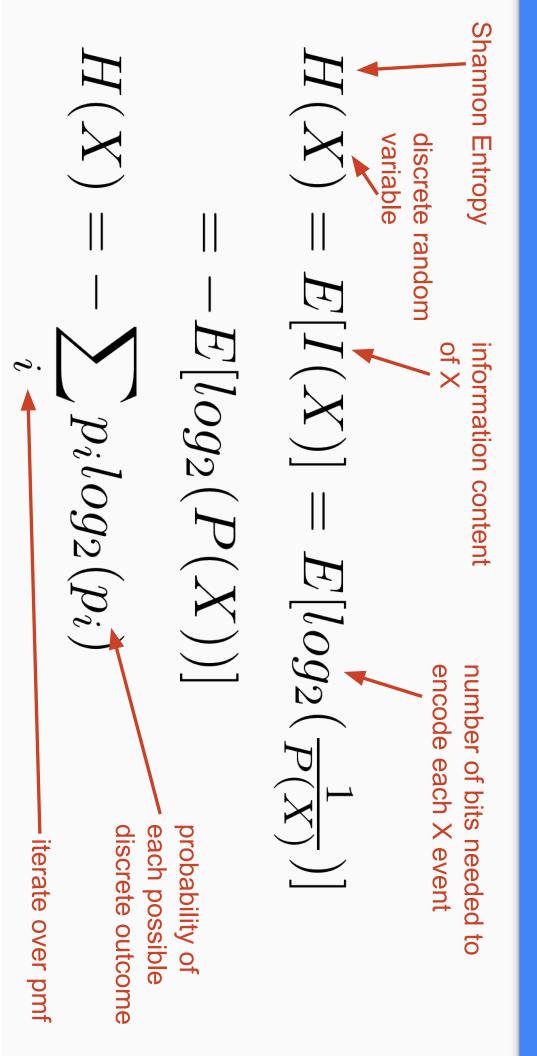


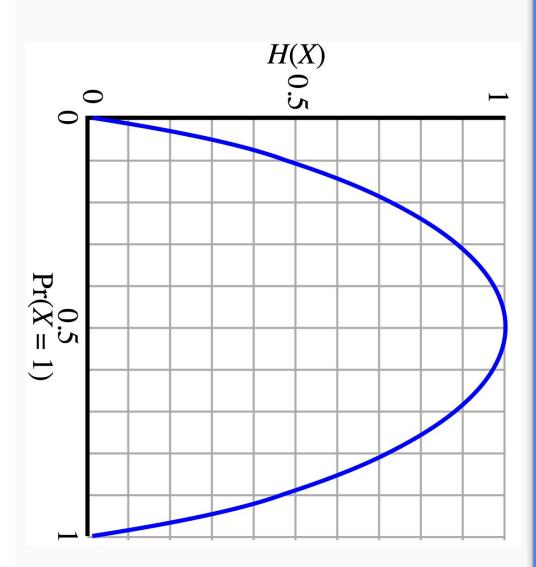
Drawbacks:

- expensive to train
- greedy algorithm (local maxima)
- easily overfits
- right-angle decision boundaries only

But how can we build one of these from training data?

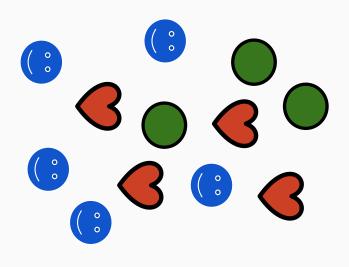
Entropy (a measure of information in an event stream)





Shannon Entropy Diversity Index (aka, the Shannon Index)

We can measure the diversity of a set using Shannon Entropy (H) if we interpret the frequency of elements in the set as probabilities



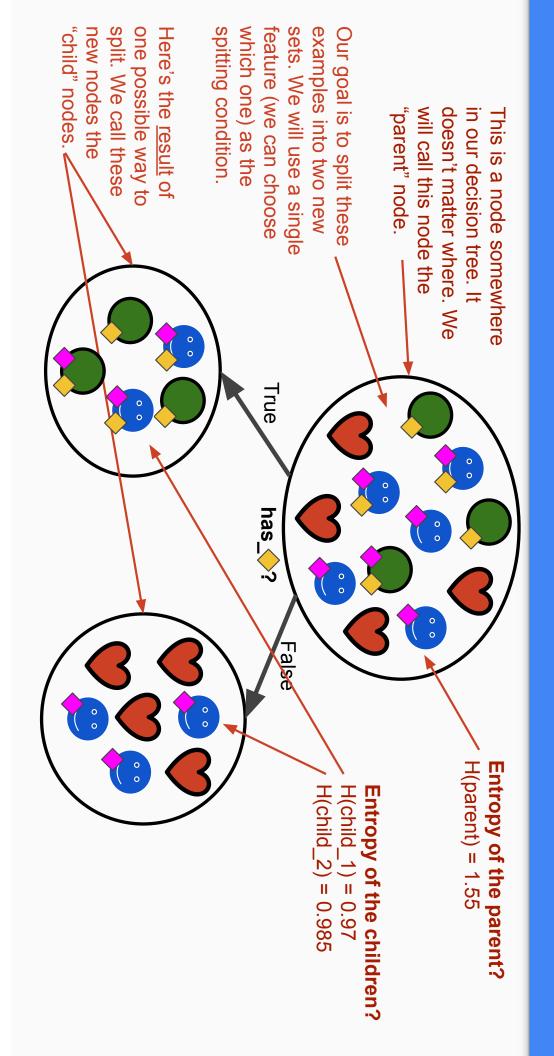
Estimate:

$$P(\bigcirc) = 3/12 = 0.25$$

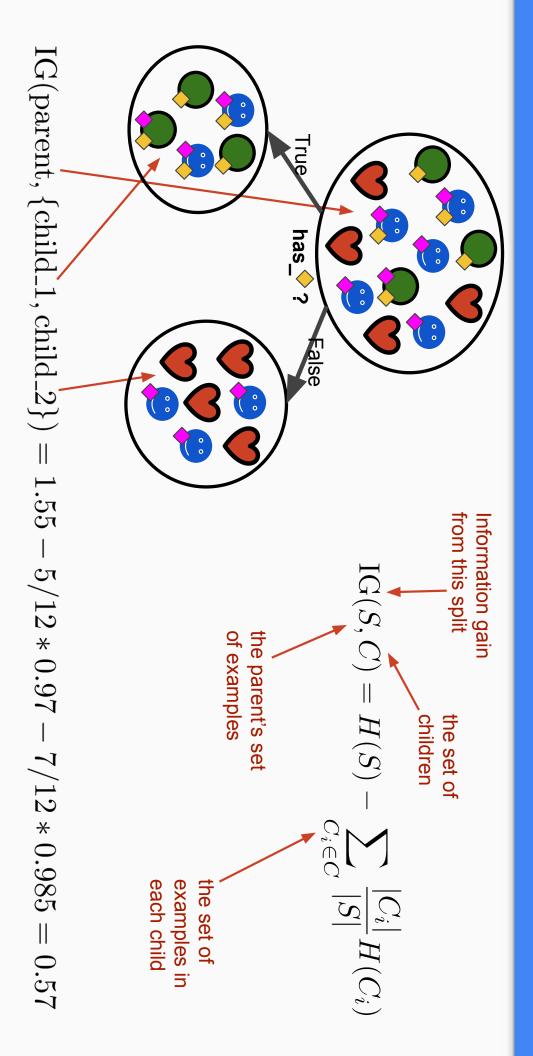
 $P(\bigcirc) = 4/12 = 0.33$
 $P(\bigcirc) = 5/12 = 0.42$

H = 1.55

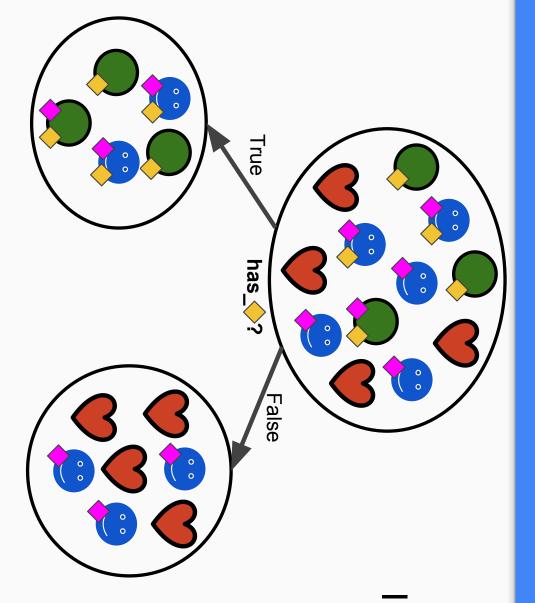
One level in a decision tree:



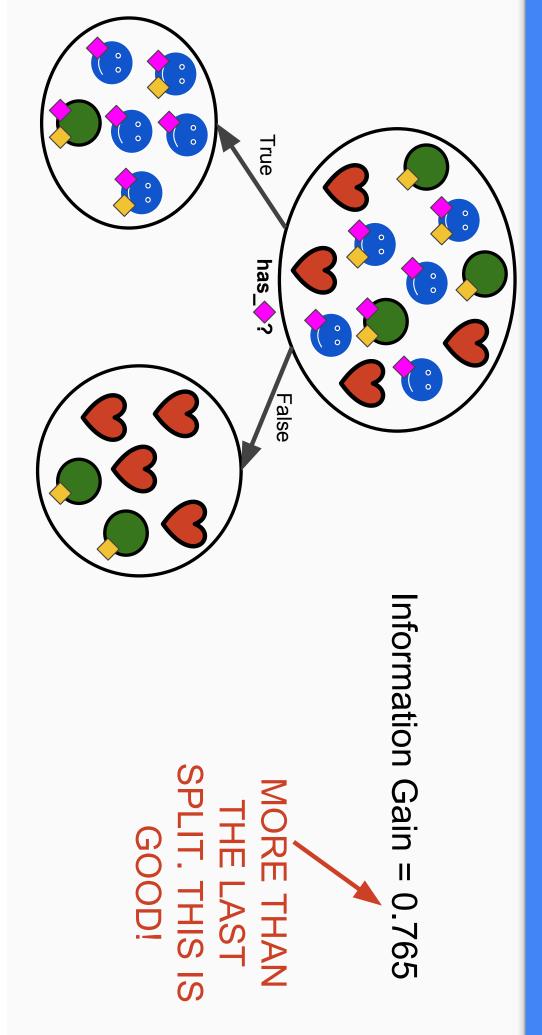
Information Gain (using Shannon Entropy Diversity Index)



Information Gain



Information Gain = 0.57



Splitting Algorithm:

Possible Splits:

Consider all binary splits based on a single feature:

- if the feature is categorical, split on <u>value</u> or <u>not value</u>.
- if the feature is numeric, split at a threshold: <u>>threshold</u> or <=threshold

Splitting Algorithm:

- 1. Calculate the information gain for all possible splits.
- 2. Commit to the split that has the highest information gain.

Recursion

What is this function?

$$f(x) = \prod_{i=1}^{n} i$$

Is this an equivalent function?

$$f(x) = \begin{cases} 1, & \text{if } x \leq 1\\ xf(x-1), & \text{otherwise} \end{cases}$$

```
if x \leq 1
```

i Ė

_name__ == '__main__':

import doctest

doctest.testmod()

```
def
                                                                                                                                                                                  f(x):
                                                                                                   120
                    else:
                                                           if x <= 1:
                                                                                                                      >>> f(5)
                                                                                                                                          This function returns x!.
                                       return 1
return x * f(x-1)
```

How to build a decision tree (pseudocode):

function BuildTree:

If every item in the dataset is in the same class

or there is no feature left to split the data:

return a leaf node with the class label

Else:

find the best feature and value to split the data

split the dataset

create a node

for each split

call BuildTree and add the result S D മ child of the

node

return node

The Gini Index

drawn from the set is classified according to the distribution of classes in the set A measure of impurity: the probability of a misclassification if a random sample

Scikit-learn doesn't use Shannon Entropy Diversity by default. It uses the

Gini Index:

$$Gini(S) = 1 - \sum_{i \in S} p_i^2$$

Information gain using the Gini Index:

$$IG(S, C) = Gini(S) - \sum_{C_i \in C} \frac{|C_i|}{|S|} Gini(C_i)$$

Regression Trees

Targets are real values... so...

now we can't use Information Gain or Gini Index for splitting! What do we do?

Use variance! Cool, now we can train.

How do we predict?

Either predict the mean value of the leaf, or do linear regression within the leaf!

Pruning

Overfitting is likely if you build your tree all the way until every leaf is pure.

Prepruning ideas (prune while you build the tree):

- leaf size: stop splitting when #examples gets small enough
- depth: stop splitting at a certain depth
- **purity:** stop splitting if enough of the examples are the same class
- gain threshold: stop splitting when the information gain becomes too small

Postpruning ideas (prune after you've finished building the tree):

- merge leaves if doing so decreases test-set error
- (see pair.md for details)

Algorithm Names:

name. Here are a few you'll often see The details of training a decision tree vary... each specific algorithm has a

- ID3: category features only, information gain, multi-way splits, ...
- okay, pruning, ... C4.5: continuous and categorical features, information gain, missing data
- splits only, ... **CART:** continuous and categorical features and targets, gini index, binary
- ...