

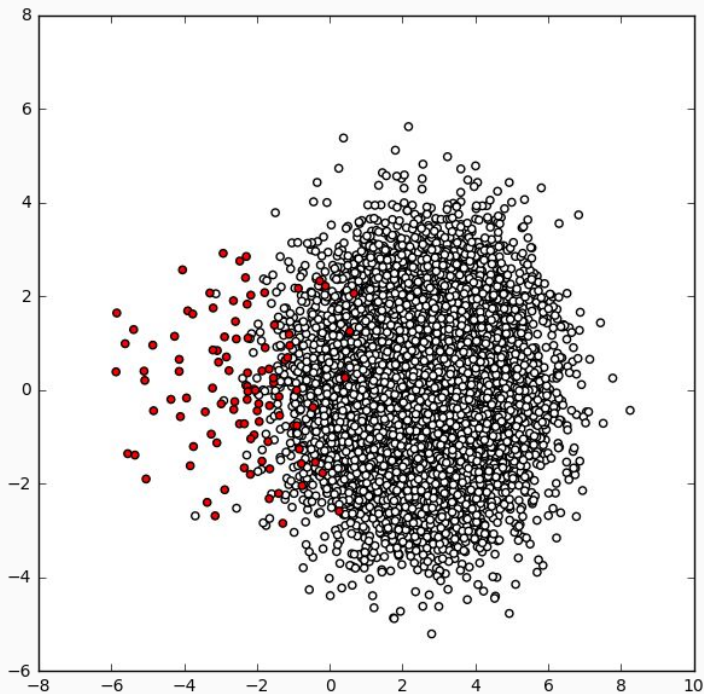


Profit Curves & Imbalanced Classes

Galvanize
Moses Marsh

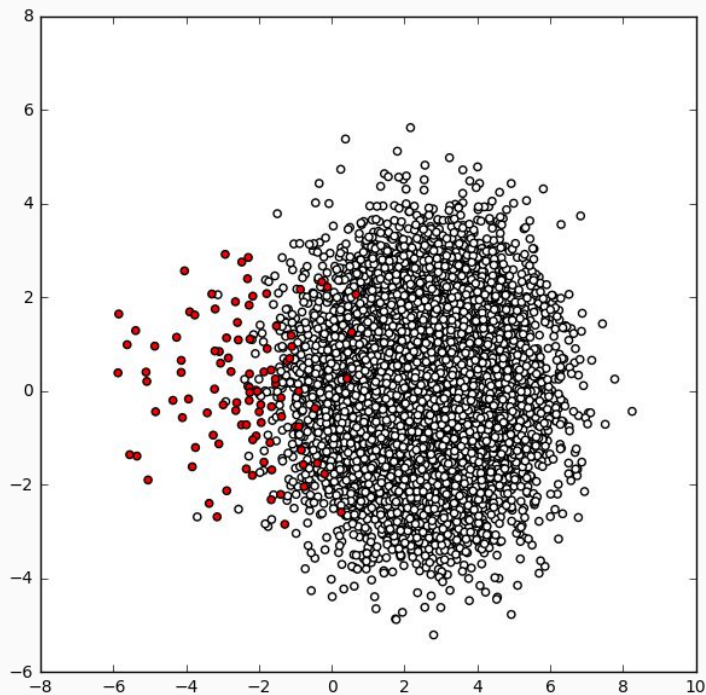
OBJECTIVES: answer the following

- How do we incorporate **business costs** into model evaluation?
- What is a **cost-benefit** matrix?
- How is a **profit curve** constructed?
- What are some issues with **imbalanced classes**?
- How can the class balance be changed?



Example : 100 pos, 10000 neg

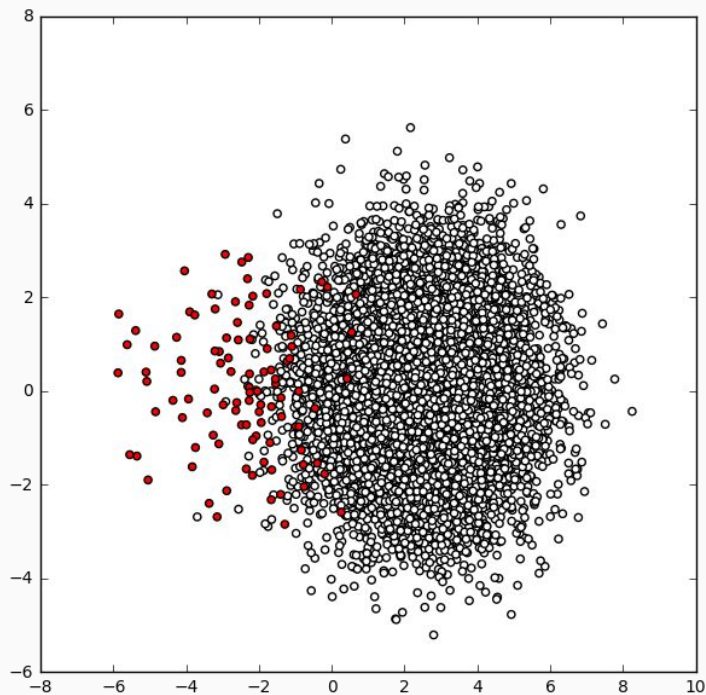
- Classification datasets can be “imbalanced”.
 - i.e. many observations of one class, few of another
- Accuracy-driven models will over-predict the majority class.
- Costs of a false positive is often different from cost of a false negative.
 - e.g. missing fraud can be more costly than screening legitimate activity



Example : 100 pos, 10000 neg

What's a possible problem during LEARNING
(fitting the model) ?

What's a possible problem during EVALUATION
(scoring the model) ?



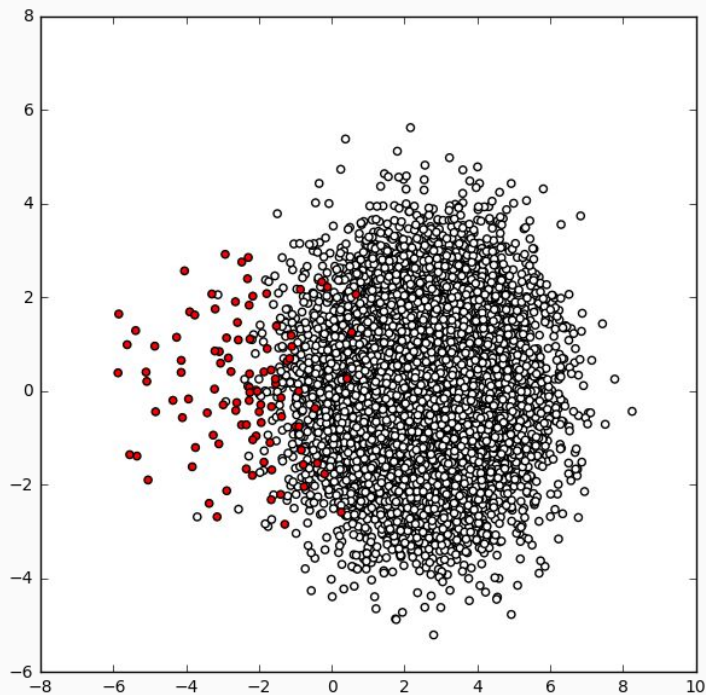
Example : 100 pos, 10000 neg

What's a possible problem during LEARNING
(fitting the model) ?

The model will overpredict the majority class

What's a possible problem during EVALUATION
(scoring the model) ?

**False positives and false negatives may have
different business costs**



Example : 100 pos, 10000 neg

What's a possible problem during LEARNING
(fitting the model) ?

**Solution: cost-sensitive learning,
oversampling/undersampling**

What's a possible problem during EVALUATION
(scoring the model) ?

Solution: cost-benefit matrix

Solutions

Cost-sensitive learning & evaluation:

- cost-benefit matrices & “profit curves”
- modified objective functions

Sampling:

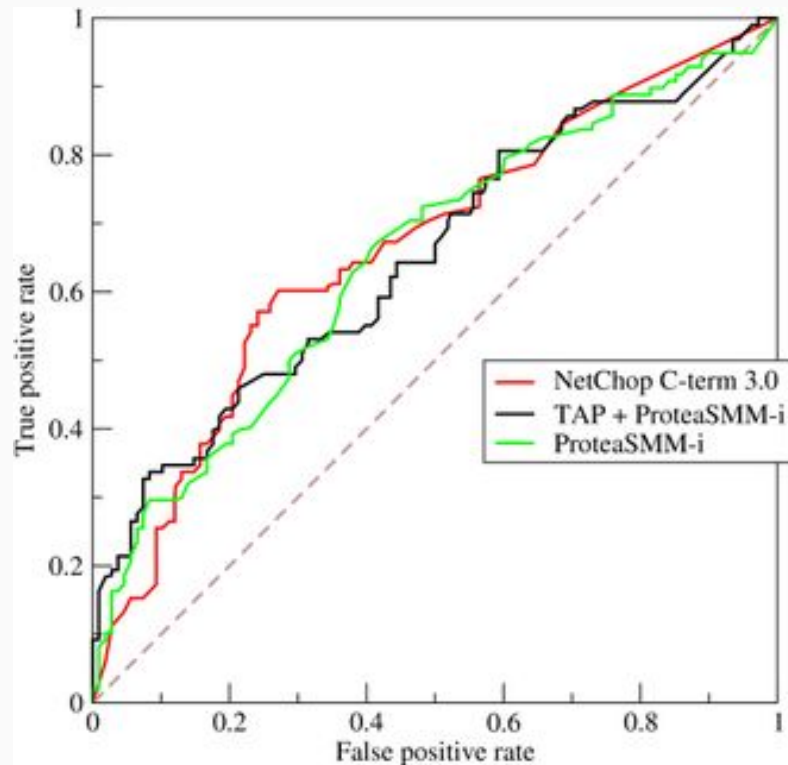
- Oversampling
- Undersampling
- SMOTE - Synthetic Minority Oversampling TEchnique

Recall the ROC Curve:

- ROC shows $FPR = (1 - TNR)$ vs TPR (aka Recall)
- doesn't give preference to one over the other

Q: How to handle unequal error costs?

A: Assign a cost/profit to each type of error/success




| | Pred: Y | Pred: N |
|--------------|------------|------------|
| Actual: y | TP | FN |
| Actual: n | FP | TN |

Confusion Matrix

$P = TP + FN$ = count of actual y

$N = FP + TN$ = count of actual n

VALUES ARE COUNTS



| | Pred: Y | Pred: N |
|--------------|------------|------------|
| Actual: y | TP | FN |
| Actual: n | FP | TN |

| | Pred: Y | Pred: N |
|--------------|------------|------------|
| Actual: y | $p(Y,y)$ | $p(N,y)$ |
| Actual: n | $p(Y,n)$ | $p(N,n)$ |

Confusion Matrix

$P = TP + FN = \text{count of actual } y$

$N = FP + TN = \text{count of actual } n$

VALUES ARE COUNTS

Probability Matrix


$p(Y,y) = TP / (P + N)$

$p(Y,n) = FP / (P + N)$

$p(N,y) = FN / (P + N)$

$p(N,n) = TN / (P + N)$

VALUES ARE
PROBABILITIES



| | Pred: Y | Pred: N |
|-----------|---------|---------|
| Actual: y | TP | FN |
| Actual: n | FP | TN |

Confusion Matrix

$P = TP + FN$ = count of actual y
 $N = FP + TN$ = count of actual n

VALUES ARE COUNTS

| | Pred: Y | Pred: N |
|-----------|----------|----------|
| Actual: y | $p(Y,y)$ | $p(N,y)$ |
| Actual: n | $p(Y,n)$ | $p(N,n)$ |

Probability Matrix

$p(Y,y) = TP / (P + N)$
 $p(Y,n) = FP / (P + N)$
 $p(N,y) = FN / (P + N)$
 $p(N,n) = TN / (P + N)$

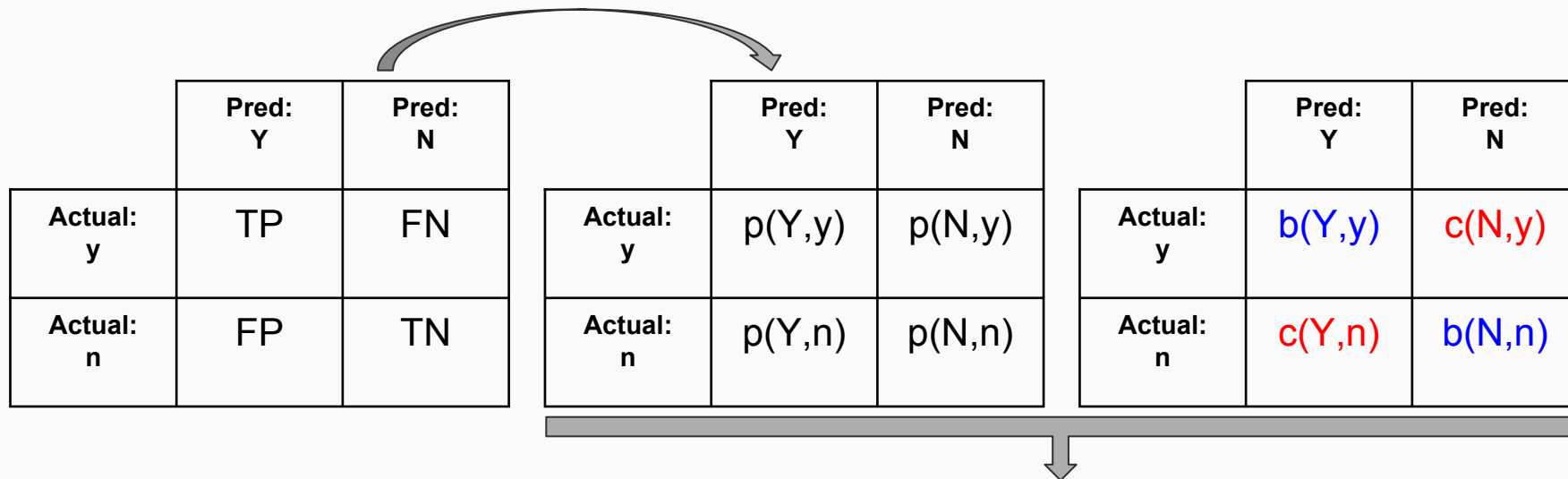
VALUES ARE
PROBABILITIES

| | Pred: Y | Pred: N |
|-----------|----------|----------|
| Actual: y | $b(Y,y)$ | $c(N,y)$ |
| Actual: n | $c(Y,n)$ | $b(N,n)$ |

Cost-Benefit Matrix

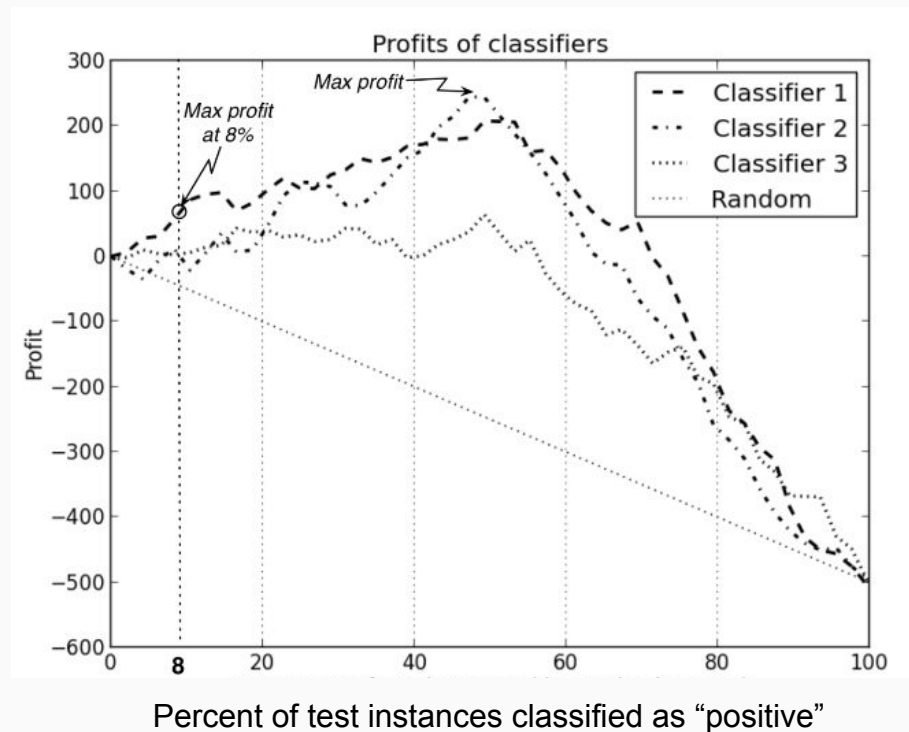
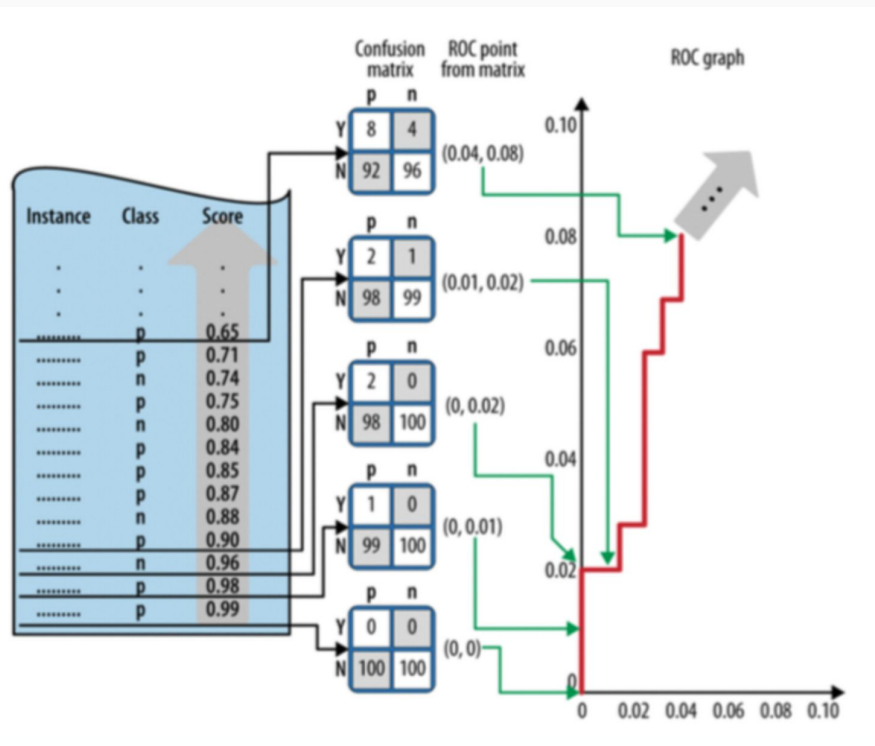
VALUES ARE \$\$\$!

Computing the Expected Profit



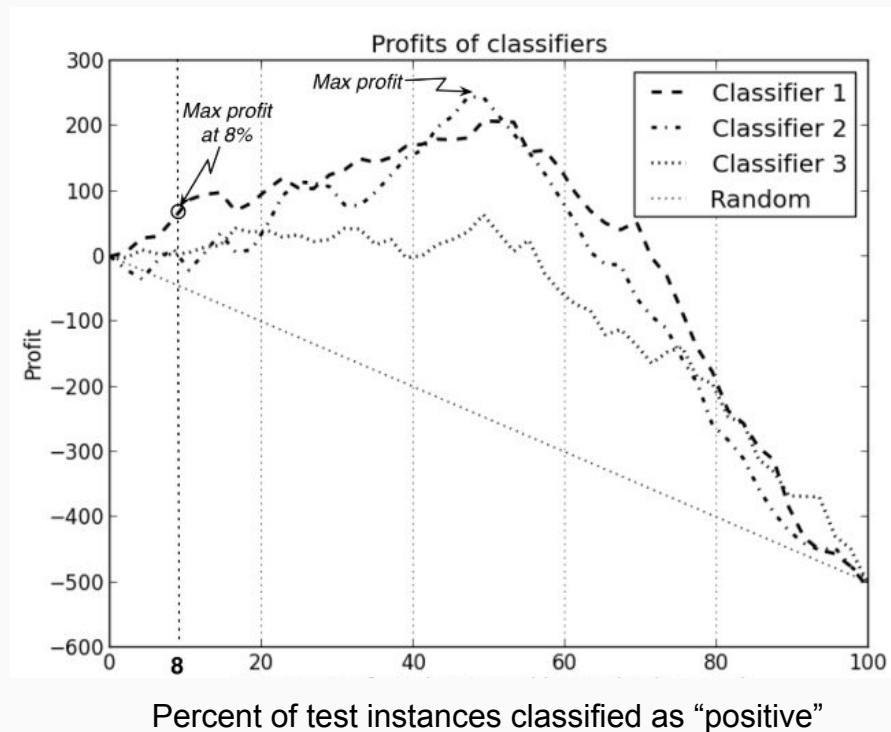
$$\begin{aligned} E[Profit] &= p(Y, y).b(Y, y) + p(Y, n).c(Y, n) \\ &\quad + p(N, y).c(N, y) + p(N, n).b(N, n) \\ &= p(Y | y).p(y).b(Y, p) + p(Y | n).p(n).c(Y, n) \\ &\quad + p(N | y).p(y).c(N, y) + p(N | n).p(n).b(N, n) \\ &= p(y).[p(Y | y).b(Y, p) + p(N | y).c(N, y)] \\ &\quad + p(n)[p(Y | n).c(Y, n) + p(N | n).b(N, n)] \end{aligned}$$

From Thresholding to Profit Curves



Profit Curve:

- Same idea as ROC curve but with expected profit
- For each threshold, compute the expected profit

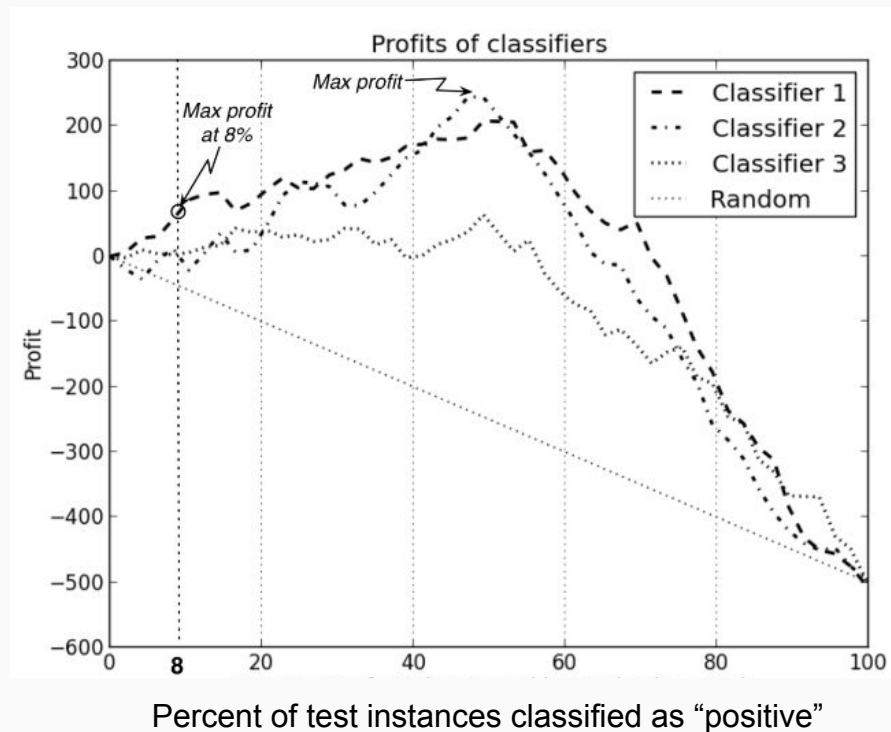


Profit Curve:

- Same idea as ROC curve but with expected profit
- For each threshold, compute the expected profit

Cost-sensitive evaluation:

- Select threshold with highest expected profit.



QUESTION: how would you pick your favorite matrix ?

| A | Pred: pos | Pred: neg |
|----------------|--------------|--------------|
| Actual: pos | 12 | 8 |
| Actual: neg | 15 | 965 |

| B | Pred: pos | Pred: neg |
|----------------|--------------|--------------|
| Actual: pos | 0 | 20 |
| Actual: neg | 0 | 980 |

| C | Pred: pos | Pred: neg |
|----------------|--------------|--------------|
| Actual: pos | 15 | 5 |
| Actual: neg | 115 | 865 |

| D | Pred: pos | Pred: neg |
|----------------|--------------|--------------|
| Actual: pos | 18 | 2 |
| Actual: neg | 250 | 730 |

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| D | Pred: pos | Pred: neg |
|-------------|-----------|-----------|
| | | |
| Actual: pos | 18 | 2 |
| Actual: neg | 250 | 730 |

DEFINE A BUSINESS PROBLEM

QUESTION: how would you pick your favorite matrix ?

FORMALIZE COSTS AND BENEFITS
DEFINE A BUSINESS PROBLEM

| A | Pred: pos | Pred: neg |
|---|-------------|-------------|
| | Actual: pos | Actual: neg |
| | 12 | 8 |
| | | |

| B | Pred: pos | Pred: neg |
|---|-------------|-------------|
| | Actual: pos | Actual: neg |
| | 0 | 980 |
| | | |

| C | Pred: pos | Pred: neg |
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| | Actual: pos | Actual: neg |
| | 15 | 5 |
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| | Pred: pos | Pred: neg |
|--|-------------|-------------|
| | Actual: pos | Actual: neg |
| | 18 | 2 |
| | 250 | 730 |

Cost-Benefit Matrix (example 1)

Prompt: You are building a model to predict if credit card charges are fraudulent.

- If we predict a fraudulent charge, we'll call the customer to confirm.
- If you miss a fraudulent charge, it on average costs \$100
- Calling someone to confirm if their charge was real costs on average \$4

Question: What is an appropriate cost benefit matrix?

| A | Predicted: fraud | Predicted: not fraud | |
|---|----------------------|-------------------------|------|
| | Actual: fraud | 96 | -100 |
| | Actual: not fraud | -4 | 0 |

| <i>B</i> | Predicted: fraud | Predicted: not fraud |
|----------------------|---------------------|-------------------------|
| Actual: fraud | -4 | -100 |
| Actual: not fraud | -4 | 0 |

| C | Predicted: fraud | Predicted: not fraud | |
|---|----------------------|-------------------------|---|
| | Actual: fraud | 96 | 0 |
| | Actual: not fraud | -4 | 0 |

Cost-Benefit Matrix (example 2)

You are building a model to **predict if customers will churn** from your online clothing store.

You'll use your model **to send a promotional email** to users you think are going to churn.

You'd like to use a cost benefit matrix so you can build **profit curves to determine the optimal model**.

- Customers on average spend **\$200/month**.
Your profit is **10%** of this revenue.
- A promotional email costs on average **\$2/customer** and prevents **50%** of users from churning for **6 months**.
- When the promotional email is sent to users who were not going to churn, it annoys **5%** of them and causes them to churn **2 months** earlier than they otherwise would have.

| | Predicted: churn | Predicted: not churn |
|----------------------|---------------------|-------------------------|
| Actual: churn | ? | ? |
| Actual: Not churn | ? | ? |

- Models with explicit objective function can be modified to incorporate classification cost.
 - e.g. **logistic regression**

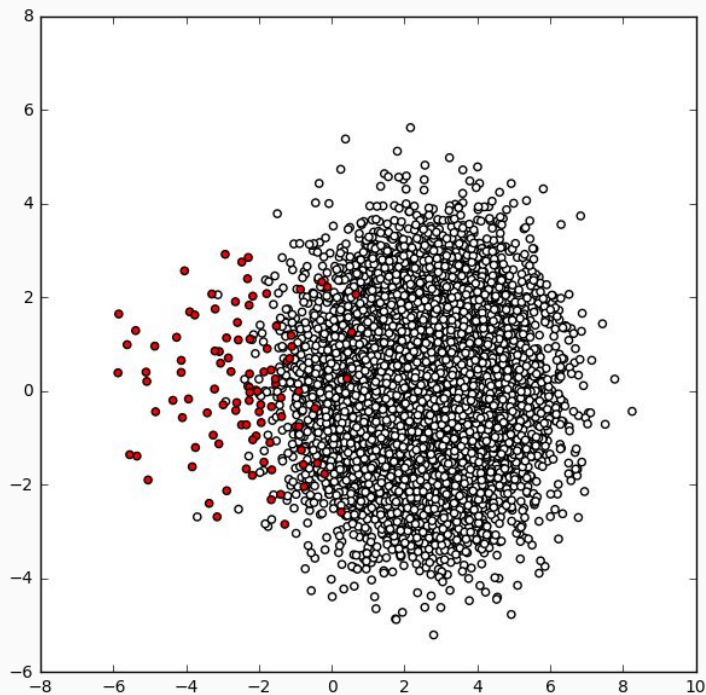
- Logistic regression's usual objective function:

$$\ln p(\vec{y}|X; \theta) = \sum_{i=1}^n (y_i \ln h_{\theta}(x_i) + (1 - y_i) \ln(1 - h_{\theta}(x_i)))$$

- New objective function, representing expected cost:

$$J^c(\theta) = \frac{1}{N} \sum_{i=1}^N \left(y_i(h_{\theta}(X_i)C_{TP_i} + (1 - h_{\theta}(X_i))C_{FN_i}) \right. \\ \left. + (1 - y_i)(h_{\theta}(X_i)C_{FP_i} + (1 - h_{\theta}(X_i))C_{TN_i}) \right).$$

- This will affect optimization.
 - e.g. cost-sensitive logistic regression is not convex!
- Not all models have a cost-sensitive implementation.



Example : 100 pos, 10000 neg

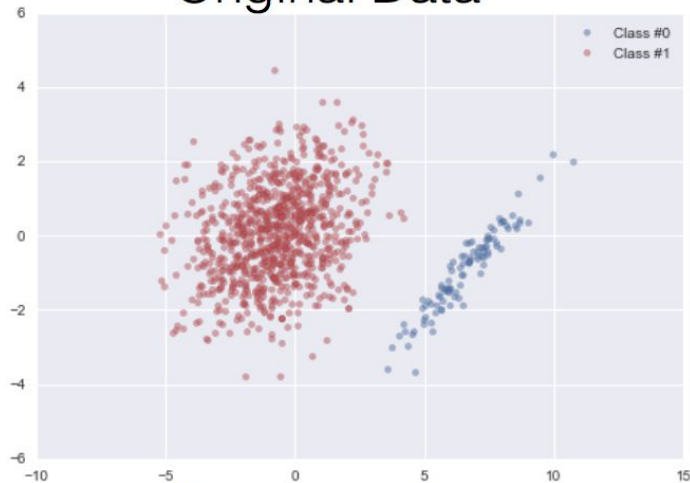
What's a possible problem during LEARNING
(fitting the model) ?

**Solution: cost-sensitive learning,
oversampling/undersampling**

What's a possible problem during EVALUATION
(scoring the model) ?

Solution: cost-benefit matrix

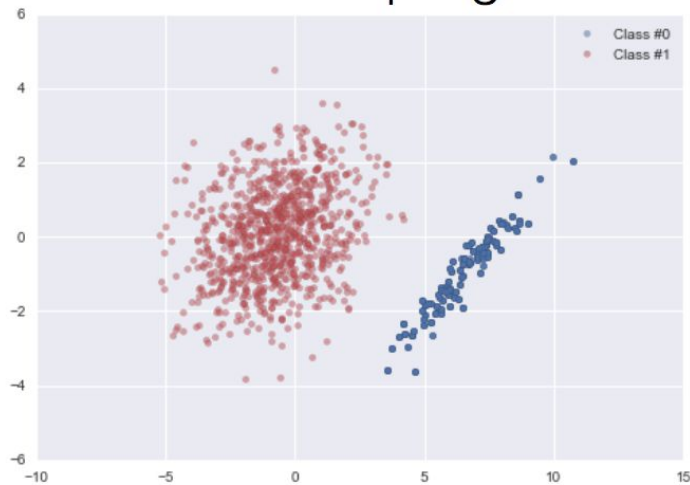
Original Data



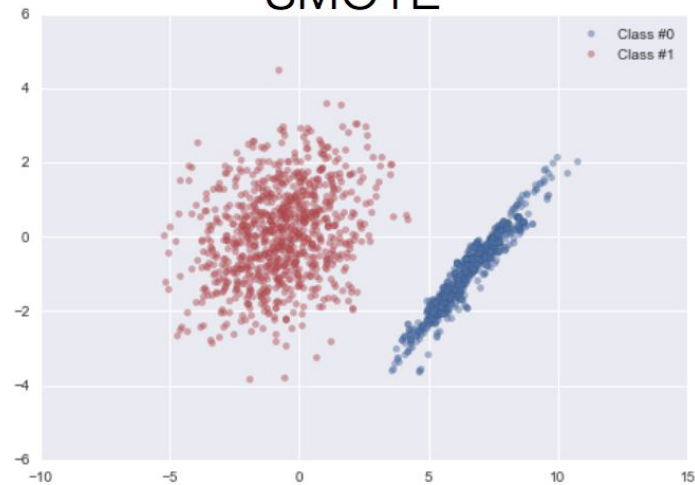
Undersampling



Oversampling



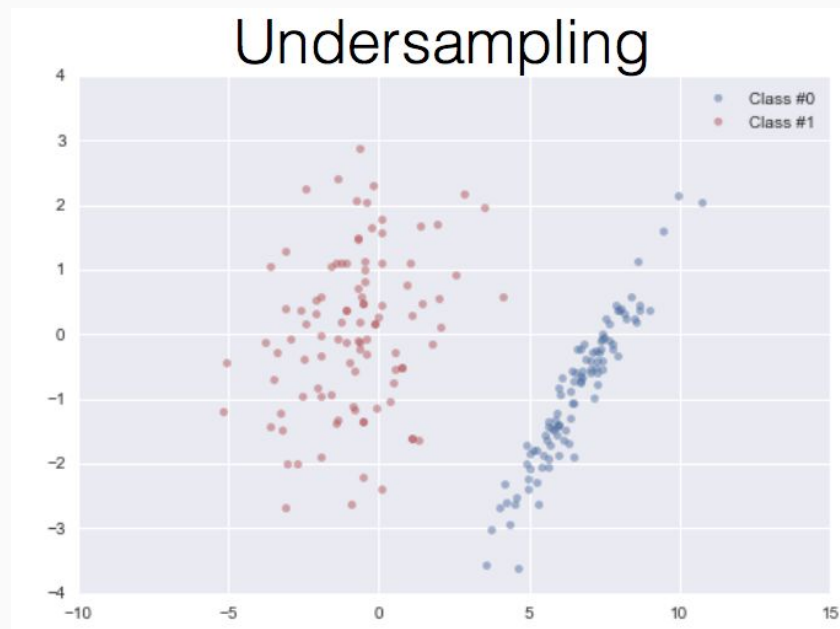
SMOTE



Undersampling randomly discards majority class observations to balance training sample.

PRO: Reduces runtime on very large datasets.

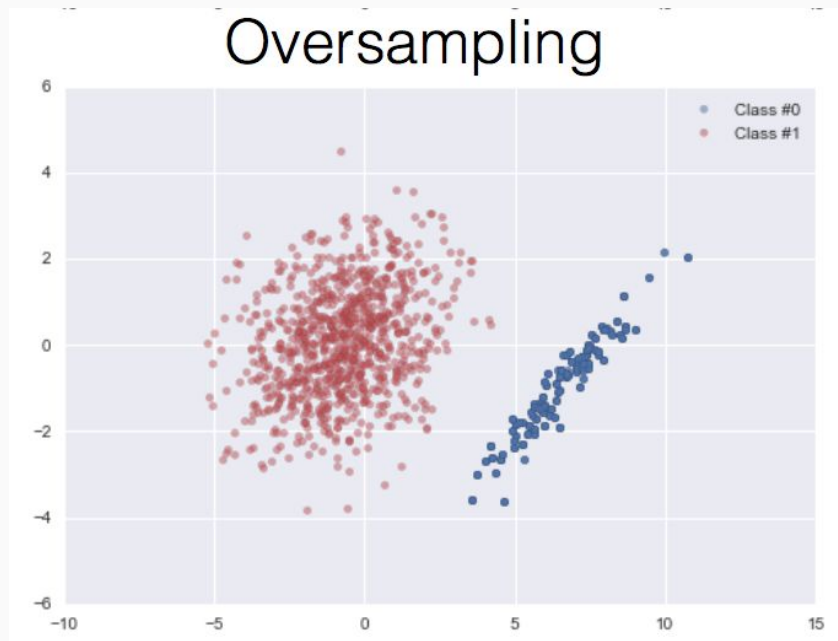
CON: Discards potentially important observations.



Oversampling replicates observations from minority class to balance training sample.

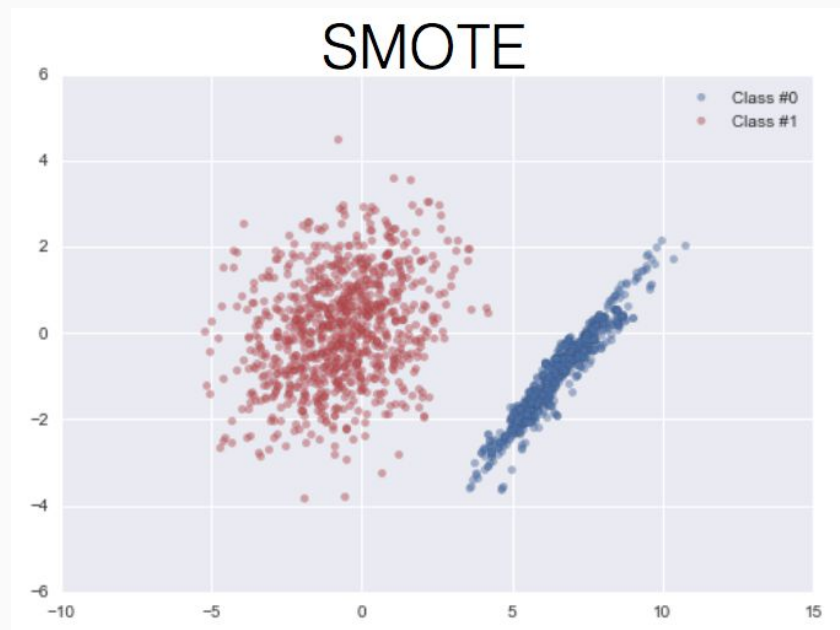
PRO: Doesn't discard information.

CON: Likely to overfit.



Generates new observations from minority class.

For each minority class observation and for each feature, randomly generate between it and one of its k-nearest neighbors.



SMOTE pseudocode

```
synthetic_observations = []  
while len(synthetic_observations) + len(minority_observations) < target:  
    obs = random.choice(minority_observations):  
    neighbor = random.choice(kNN(obs, k)) # randomly selected neighbor  
    new_observation = {}  
    for feature in obs:  
        weight = random() # random float between 0 and 1  
        new_feature_value = weight*obs[feature] \  
                               + (1-weight)*neighbor[feature]  
        new_observation[feature] = new_feature_value  
    synthetic_observations.append(new_observation)
```

Sampling Techniques

What's the right amount of over-/under-sampling?

- The degree & kind of resampling is another set of hyperparameters to tune
- Mix it up! You may get the best results by both oversampling and undersampling
- Evaluation: ***profit*** if you have a cost-benefit matrix, otherwise ***ROC-AUC*** score, ***F1***, etc.

Cost Sensitivity vs Sampling

- Neither is strictly superior.
- Oversampling tends to work better than undersampling on small datasets.
- Some algorithms don't have an obvious cost-sensitive adaptation, requiring sampling.

See also "Cost-Sensitive Learning vs. Sampling: Which is Best for Handling Unbalanced Classes with Unequal Error Costs?" <http://storm.cis.fordham.edu/gweiss/papers/dmin07-weiss.pdf>