

# Review:

Confusion matrix:

		<u>true</u>	
		P	N
<u>predicted</u>	P	T.P.	F.P.
	N	F.N.	T.N.

$$T = TP + FP + FN + TN$$

$$\text{accuracy} = \frac{TP + TN}{T}$$

$$\text{precision} = \frac{TP}{TP + FP}$$

$$\text{recall} = \frac{TP}{TP + FN}$$

← aka "TPR" or  
"sensitivity" or  
"hit rate"

$$\text{FPR} = \frac{FP}{FP + TN}$$

$$\text{specificity} = \frac{TN}{FP + TN}$$

← FRR = 1 - specificity  
←

## Profit Curves:

I have 5 models, each with a different accuracy (a):

$$\left[ \begin{array}{ccc} a = 0.977 & a = 0.02 & a = 0.98 \\ & a = 0.88 & a = 0.748 \end{array} \right]$$

Which is the best model?

(correct answer is "not enough info")

Okay fine, I'll give you the precision (p) and recall (r):

$$\left[ \begin{array}{ccc} p = 0.44 & p = 0.02 & p = 0.0 \\ r = 0.6 & r = 1.0 & r = 0.0 \\ & p = 0.115 & p = 0.0672 \\ & r = 0.75 & r = 0.9 \end{array} \right]$$

Which is the best model?

(correct answer is "not enough info")

What else do you want to know?

(correct answer is "description of prediction problem" and/or "a confusion matrix")

Okay fine.

Domain: Fraud detection ('Fr' vs. 'Not')

Confusion matrices:

		true	
		Fr	Not
pred	Fr	12	15
	Not	8	965

		true	
		Fr	Not
pred	Fr	20	980
	Not	0	0

		true	
		Fr	Not
pred	Fr	0	0
	Not	20	980

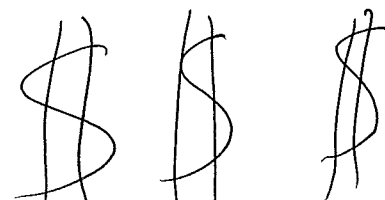
		true	
		Fr	Not
pred	Fr	15	115
	Not	5	865

		true	
		Fr	Not
pred	Fr	18	250
	Not	2	730

Now... which model is better?  
(crickets... maybe model X?)

New question: which of these results would the business owner be interested in?  
(accuracy? precision? recall?  $F_1$ ?  
confusion matrices?)

Answer: None of them. He wants:

  
money money money

Let's create costs & benefits of each outcome.  
 We'll put these in the shape of a confusion matrix to match what we already have.

Cost-benefit Matrix:

benefit T.P.	cost. F.P.
cost F.N.	benefit T.N.

For our bank, we look at history + ~~personnel~~ personnel costs:

Cost-benefit Matrix:

-5	-5
-1000	0

Let's now calculate the "expected profit" of each of our original 5 models:

$$\text{profit} = -8.135 \quad \text{profit} = -5.0 \quad \text{profit} = -20.0$$

$$\text{profit} = -5.650 \quad \boxed{\text{profit} = -3.340} \leftarrow \text{winner!}$$

## Other examples:

- Sending mail (direct mail marketing)
- predicting cancer
- betting ~~at the casino~~ on football (the booky keeps the 'juice', so getting 750% isn't enough)
- predicting spam - how much would a user prefer to see a spam email vs miss a legit one?