# **Decision Trees**

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galvanize

- Decision Trees
- Entropy
- Information Gain
- Recursion
- How to build a tree



# Decision Tree Objectives

- Describe pros/cons of decision tree algorithm
- Describe common measures for making splits in a decision tree
- Explain the concept of recursion and relate it to decision trees
- Identify pruning techniques for decision trees

**Exercise: Implement decision tree algorithm in Python** 

### Historical log of times I played tennis:



Temp	Outlook	Humidity	Windy	Played
Hot	Sunny	High	False	No
Hot	Sunny	High	True	No
Hot	Overcast	High	False	Yes
Cool	Rain	Normal	False	Yes
Cool	Overcast	Normal	True	Yes
Mild	Sunny	High	False	No
Cool	Sunny	Normal	False	Yes
Mild	Rain	Normal	False	Yes
Mild	Sunny	Normal	True	Yes
Mild	Overcast	High	True	Yes
Hot	Overcast	Normal	False	Yes
Mild	Rain	High	True	No
Cool	Rain	Normal	True	No
Mild	Rain	High	False	Yes

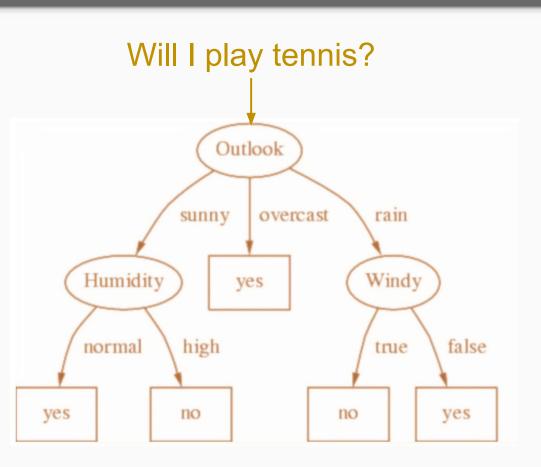
```
def will play(temp, outlook, humidity,\
              windy):
    if outlook == 'sunny':
        if humidity == 'normal':
            return True
        else: # humidity == 'high'
            return False
    elif outlook == 'overcast':
        return True
    else: # outlook == 'rain'
        if windy == True:
            return False
        else: # windy == False:
            return True
```



```
def will_play(temp, outlook, humi_ity,\
              windy):
    if outlook == 'sunny':
        if humidity == 'normal':
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    elif outlook == 'overcast':
        return True
    else: # outlook == 'rain'
        if windy == True:
            return False
        else: # windy == False:
            return True
```

Instead, let's write an algorithm to build a **Decision Tree** for us, based on the training data we have. Outlook sunny overcast rain Windy Humidity yes normal high false true ves no no ves

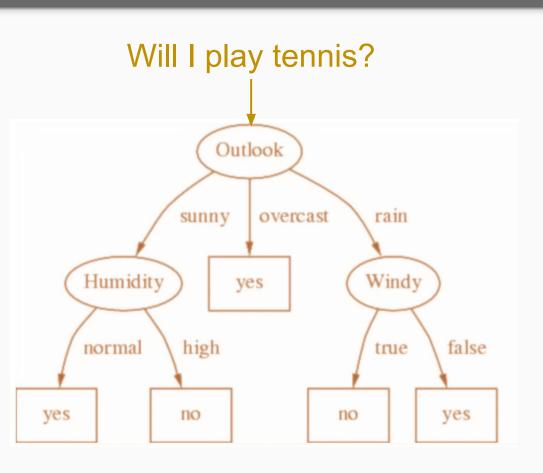




### Benefits:

- non-parametric, non-linear
- can be used for classification and for regression
- real and/or categorical features
- easy to interpret
- computationally cheap prediction
- handles missing values and outliers
- can handle irrelevant features



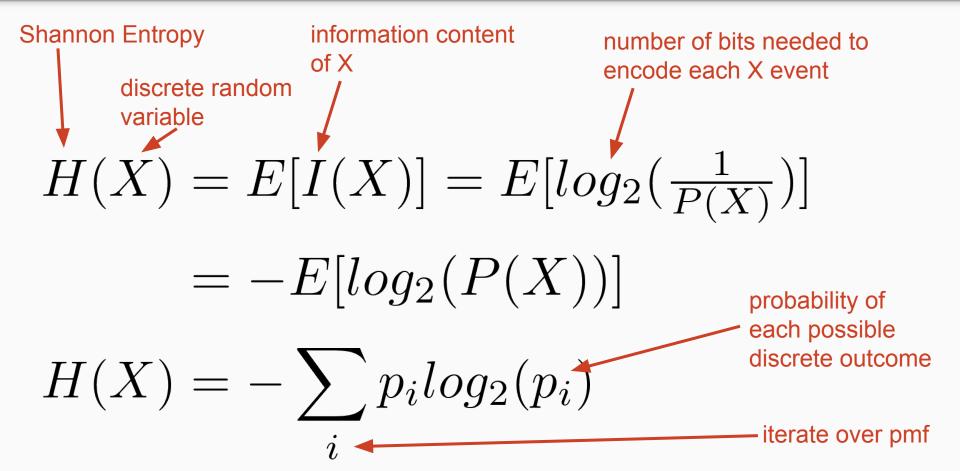


### Drawbacks:

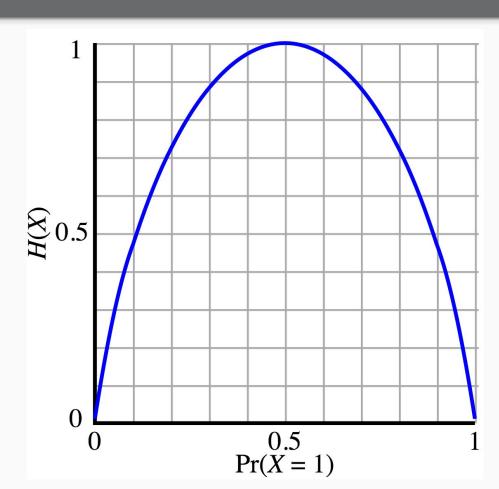
- expensive to train
- greedy algorithm (local maxima)
- easily overfits
- right-angle decision boundaries only

But how can we build one of these from training data?



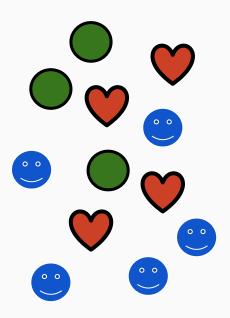








We can measure the diversity of a set using Shannon Entropy (H) if we interpret the frequency of elements in the set as probabilities.



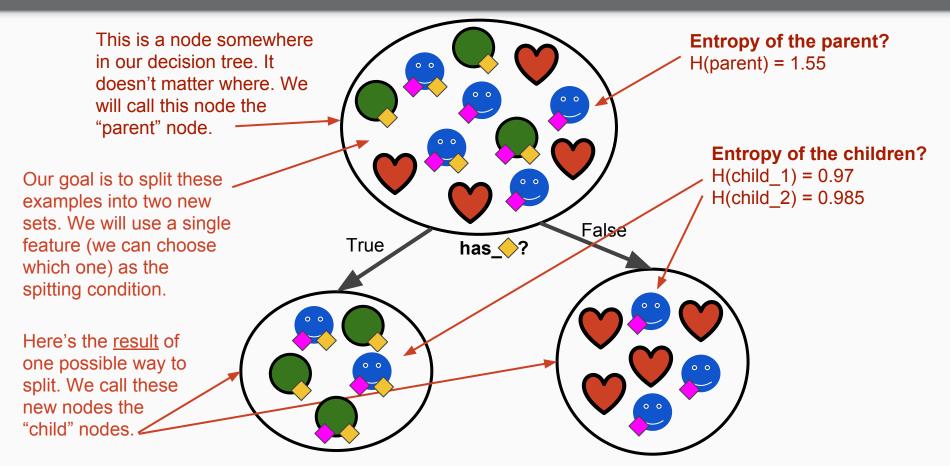
### **Estimate:**

$$P(\bigcirc) = 3/12 \approx 0.25$$
  
 $P(\bigcirc) = 4/12 \approx 0.33$   
 $P(\bigcirc) = 5/12 \approx 0.42$ 

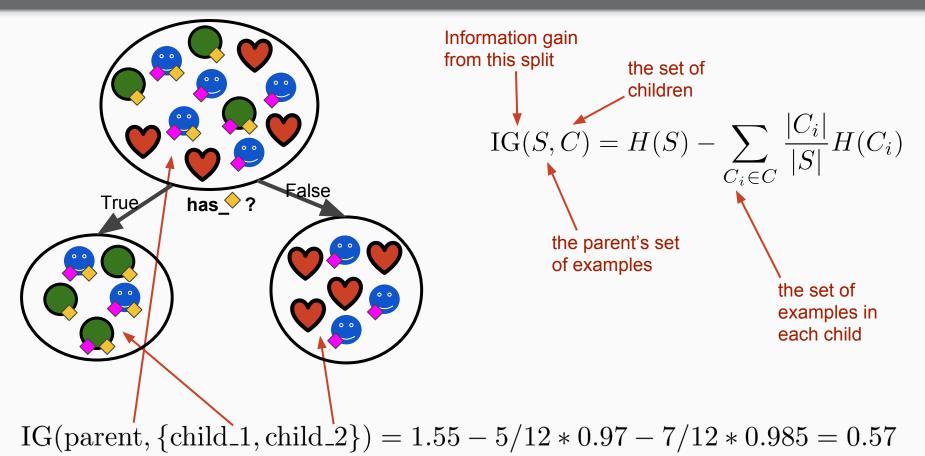
 $H \approx 1.55$ 

#### One level in a decision tree:

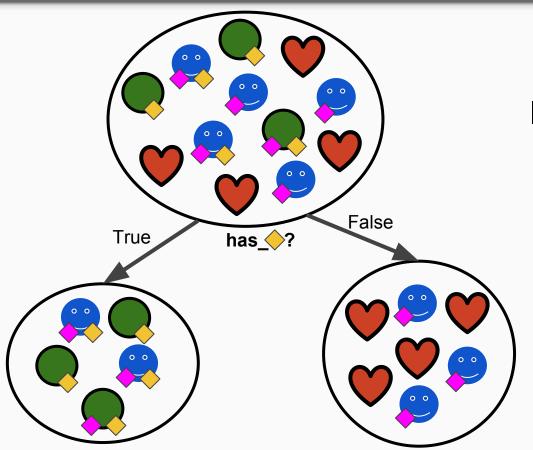




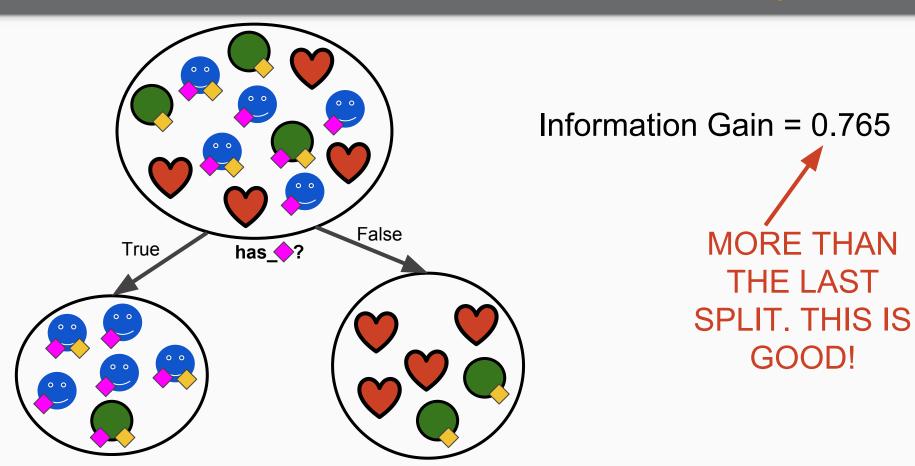








Information Gain = 0.57





# Splitting Algorithm:

### **Possible Splits:**

Consider all binary splits based on a single feature:

- if the feature is categorical, split on <u>value</u> or <u>not value</u>.
- if the feature is numeric, split at a threshold: <u>>threshold</u> or <=threshold</li>

### **Splitting Algorithm:**

- 1. Calculate the information gain for all possible splits.
- 2. Commit to the split that has the highest information gain.

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### Recursion

#### What is this function?

$$f(x) = \prod_{i=1}^{x} i$$

Is this an equivalent function?

$$f(x) = \begin{cases} 1, & \text{if } x \le 1\\ xf(x-1), & \text{otherwise} \end{cases}$$

```
def f(x):
    1 1 1
    This function returns x!.
    >>> f(5)
    120
    . . .
    if x <= 1:
        return 1
    else:
        return x * f(x-1)
  name == ' main ':
    import doctest
    doctest.testmod()
```

### How to build a decision tree (pseudocode):



```
function BuildTree:
    If every item in the dataset is in the same class
    or there is no feature left to split the data:
        return a leaf node with the class label
    Else:
        find the best feature and value to split the data
        split the dataset
        create a node
        for each split
            call BuildTree and add the result as a child of the node
        return node
```

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### The Gini Index

A measure of impurity: the probability of a misclassification if a random sample drawn from the set is classified according to the distribution of classes in the set

Scikit-learn <u>doesn't</u> use *Shannon Entropy Diversity* by default. It uses the *Gini Index*:

$$Gini(S) = 1 - \sum_{i \in S} p_i^2$$

Information gain using the *Gini Index*:

$$IG(S, C) = Gini(S) - \sum_{C_i \in C} \frac{|C_i|}{|S|} Gini(C_i)$$



# Regression Trees

Targets are real values... so... now we can't use Information Gain or Gini Index for splitting! What do we do?

Use variance! Cool, now we can train.

### How do we predict?

Either predict the mean value of the leaf, or do linear regression within the leaf!



Overfitting is likely if you build your tree all the way until every leaf is pure.

Prepruning ideas (prune while you build the tree):

- leaf size: stop splitting when #examples gets small enough
- depth: stop splitting at a certain depth
- purity: stop splitting if enough of the examples are the same class
- gain threshold: stop splitting when the information gain becomes too small

Postpruning ideas (prune after you've finished building the tree):

- merge leaves if doing so decreases test-set error
- (see pair.md for details)



# Algorithm Names:

The details of training a decision tree vary... each specific algorithm has a name. Here are a few you'll often see:

- **ID3:** category features only, information gain, multi-way splits, ...
- C4.5: continuous and categorical features, information gain, missing data okay, pruning, ...
- CART: continuous and categorical features and targets, gini index, binary splits only, ...
- ...



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