$$V_A - V_B = \int_A^\infty ec{E} \cdot \overrightarrow{dr} - \int_B^\infty ec{E} \cdot \overrightarrow{dr} = \int_A^B ec{E} \cdot \overrightarrow{dr} = \int_A^B ec{E} \cdot \overrightarrow{d\ell} \quad ext{(Electric force is conservative force)}$$

Change in potential energy:

$$q(V_A - V_B) = K_B - K_A$$

### **Potential Gradient**

$$ec{E}=rac{Q}{4\pi\epsilon_0 r^2}\hat{r}, \quad V=rac{Q}{4\pi\epsilon_0 r}$$

$$rac{dV}{dr}\hat{r} = -rac{Q}{4\pi\epsilon_0 r^2}\hat{r} \quad \Rightarrow \quad ec{E} = -rac{dV}{dr}\hat{r}$$

$$|E_x| = \left|rac{\Delta V}{\Delta x}
ight|_{yz}, \quad |E_y| = \left|rac{\Delta V}{\Delta y}
ight|_{xz}, \quad |E_z| = \left|rac{\Delta V}{\Delta z}
ight|_{xy}$$

$$\Rightarrow ec{E} = -(rac{\partial V}{\partial x}\hat{x} + rac{\partial V}{\partial y}\hat{y} + rac{\partial V}{\partial z}\hat{z}) = -grad\ V$$

#### Coulomb's Law

Force acting between two charge.

$$ec{F}_{1,2} = k rac{q_1 q_2}{r^2} \hat{r}_{1,2}, \quad k = rac{1}{4 \pi \epsilon_0} pprox 9 imes 10^9 mF^{-1}$$

 $ec{F}_{1,2}$  is force by charge 1 on charge 2

 $\hat{r}_{1,2}$  is unit vector from charge 1 to 2

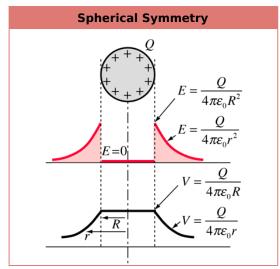
#### **Electric Field Intensity**

$$ec{E}=rac{kQ}{r^2}\hat{r}, \quad k=rac{1}{4\pi\epsilon_0}pprox 9 imes 10^9 mF^{-1}$$

#### **Electric Flux**

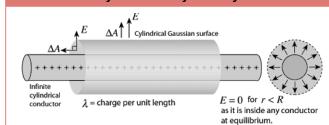
First of the four equations of Maxwell

$$\phi = \oint_S ec{E} \cdot \overrightarrow{dA} = rac{\sum Q_{enc}}{\epsilon_0}$$



# **Cyllindrical Symmetry**

**Electric Field** 



# $\sigma$ = sheet charge density in Coulombs per square meter $\sigma A$ = charge inside $\Delta A \downarrow \downarrow E$

Gaussian surface

Flat Sheet

#### **Equipotential Surfaces**

A surface with same electric potential at every point

The surface of a conductor is equipotential regardless of its shape

At equipotential surfaces, electric field lines are perpendicular to the

A charge put on the surface at rest will accelerate perpendicular to the

**Electric potential** 

**Electrostatics** 

Charge

#### **Electric Potential**

Work done to bring unit charge from infinity to distance R from charge

$$V = \int_{R}^{\infty} rac{ec{F}_{el}}{q} \cdot ec{dr} = rac{Q}{4\pi\epsilon_0 R}$$

$$W_{ext} = qV \Rightarrow W_{el} = -qV$$

#### **Electrostatic Potential Energy**

$$W_{ext} = \int_{\infty}^{R} ec{F}_{ext} \cdot \overrightarrow{dr} = \int_{R}^{\infty} ec{F}_{el} \cdot \overrightarrow{dr} = rac{q_1 q_2}{4\pi\epsilon_0} \int_{R}^{\infty} rac{dr}{R^2} = rac{q_1 q_2}{4\pi\epsilon_0 R}$$

#### **Types of charges**

Positive: Cellulose acetate rubbed with cotton

Negative: polythene rubbed with dry woolen material

#### **Electroscope**

Device to indicate charge

#### **Electrostatic Induction**

A conductor is charged by bringing a charge body near it without contact.

#### **Methods of Charging**

Friction

Contact

Induction

**Charge Distribution on a Conductor** 

## Charge Density = $\frac{Q}{A}$

Charge Density  $\propto$  curvature

Flat surfaces have low charge densities.

Sharp edges have high charge densities.

#### **Applications**

**Electrostatic Spray Painting** 

**Dust Extraction** 

Van de Graaff Generator

#### **Consevation of Charge**

In a closed system,  $\sum Q=$  constant