Problem. Last Halloween, I ate 84 Starburst candies. However, not all grad students have an unquenchable need for Starburst. I don't know how many Starburst grad students ate on average, but I'm interested in finding out the variance in Starburst consumption last Halloween because I want to know just how out of hand my Starburst habit was.

I tracked down the Starburst consumption for n=31 grad students. The average was $\bar{x}=22$ and the variance was $s^2=14$. Someone told me that the true variance in Starburst consumption is actually $\sigma_0^2=8$. I think they're full of crap and I want to demonstrate how wrong they are with 95% confidence. Can I?

Solution. The test being performed is

$$H_0: \sigma^2 = 8,$$

$$H_1: \sigma^2 \neq 8.$$

The test statistic is

$$\chi^2 = \frac{(n-1)s^2}{\sigma_0^2} = \frac{(30)14}{8} = 52.5.$$

The two critical value can be found on the χ^2 table, row 30, the columns with 0.975 and 0.025. The lower critical value is $\chi^2_{30,0.975} = 16.799$, and the upper critical value is $\chi^2_{30,0.025} = 46.979$. Since the test statistic is beyond the interval [19.799, 46.997], which means it is in the rejection region, we reject the null hypothesis. Thus, I can tell that person how full of crap they are at 5% significance¹: "If your guess was true, then there's a less than 5% chance that I'd have actually calculated $s^2 = 14$. So you're probably wrong."

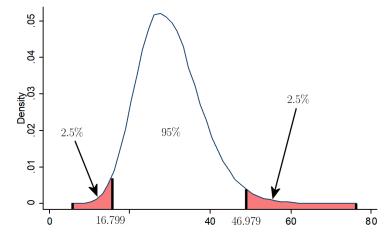


FIGURE 1: If the null is true, then there's a less than 5% chance of seeing a χ^2 statistic in the red regions. Since we found $\chi^2 = 52.5$, we reject the null.

[&]quot;Full of crap at 5% significance" is not standard statistical jargon.