# ECN 102, Spring 2020

Week 7 Section Multiple Choice Questions

The OLS estimator

- (a) minimizes  $\sum_{i=1}^{n} (y_i \hat{y}_i)^2$
- **(b)** minimizes  $\sum_{i=1}^{n} (y_i \bar{y})^2$
- (c) minimizes  $\sum_{i=1}^{n} (\hat{y}_i \bar{y}_i)^2$
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**Answer: a.** OLS minimizes the sum of squared residuals (RSS). Remember, the residuals measure how far off the regression line is from the actual data, and we want a line that is as close a possible to the data. Minimizing how far off something is is equivalent to maximizing how close something is.

For linear regression, the conditional mean of y given  $x = x^*$  equals

(a) 
$$b_1 + b_2 x^*$$

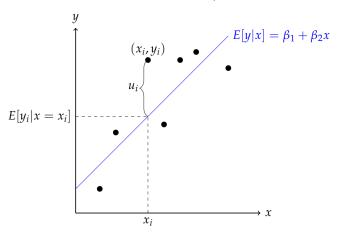
**(b)** 
$$b_1 + b_2 x^* + e$$

(c) 
$$\beta_1 + \beta_2 x^*$$

(d) 
$$\beta_1 + \beta_2 x^* + u$$

(e) none of the above

**Answer: c.** A line of best fit for the population tells us what we expect y to be for any value of x, expressed  $E[y|x] = \beta_1 + \beta_2 x$ . (The sample equivalent is called the **fitted value**, expressed  $\hat{y} = b_1 + b_2 x$ .)



The standard error of the regression is a measure of

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- (b) the standard deviation of the intercept coefficient
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**Answer: d.** The standard error of the regression is sometimes called the **standard error of the residual** or the **root mean square error (RMSE)**. That is because it's given by

$$s_{\mathrm{e}} \equiv \sqrt{rac{\mathsf{RSS}}{n-2}} = \sqrt{rac{1}{n-2} \sum_{i=1}^n (y_i - \hat{y}_i)^2},$$

which hopefully you recognize is really just a standard deviation formula.

We regress y on x and find that  $b_2 = 10$  with standard error 2. Given only this information,

- (a) the regressor x is highly statistically significant and highly economically significant
- (b) the regressor x is highly statistically significant
- (c) the regressor x is highly economically significant
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Economically significant: slope coefficient is non-zero enough that it has practical importance. Suppose this regression says that an extra year of schooling is associated with an extra 10 cents of annual income. Economically insignificant, even though it's statistically significant.

The standard error of the slope coefficient

- (a) increases with increases in the sample size
- (b) decreases with increases in the variability of the regressors
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Second, denominator is essentially standard deviation of the regressor. When there's more variation in the regressor, the denominator gets bigger, and therefore  $se(b_2)$  gets smaller.

The Stata command regress y x, vce(robust)

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**Answer:** d. We use option vce(robust) when we suspect heteroskedasticity (i.e. most of the time in practice). This gives a different standard error, and therefore a different t-statistic (which is a function of the standard error), and therefore a different p-value (which is a function of the t-statistic).

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Answer: a. The correlation coefficient is defined to be

$$r_{xy}=\frac{s_{xy}}{s_x s_v}.$$

Standard deviations cannot be negative, so if we divide by both positive numbers, then the sign of the entire fraction is still positive.

Regression of y on x yields slope coefficient 0.50 and correlation coefficient 0.40. It follows that regression of x on y using the same data yields

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**Answer: b.** The slope of the reverse regression is *not* the reciprocal of the slope we get from regression y on x. To see this, note

regress y x 
$$\implies$$
 slope coefficient:  $\frac{s_{xy}}{s_x^2}$   
regress x y  $\implies$  slope coefficient:  $\frac{s_{yx}}{s_x^2}$ 

We know  $s_{xy} = s_{yx}$  (and  $r_{xy} = r_{yx}$ ), but there's no reason to believe variance of x and variance of y are the same, ergo different slope coefficients in generality.

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- (b) assumptions 1-4 hold and the error term is normally distributed
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**Answer: b.** Recapping the implications of the assumptions:

- OLS1-2: estimates are unbiased
- OLS1-4: estimates are consistent and BLUE
- OLS1-5: OLS estimates are BUE and  $(b_2 \beta_2)/\sec(b_2)$  is drawn from exact T(n-2) distribution

Suppose  $b_2=-5$  and  $R^2=0.25$ . Then the correlation coefficient is

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- **(b)**  $r_{xy} = 0.0625$
- (c) not enough information
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**Answer: d.** Recall that  $R^2 = r_{xy}^2$ . Therefore

$$r_{xy}^2 = 0.25$$
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Okay, there's a plus and a minus square root. Because the slope coefficient is negative, it must be the case that  $r_{xy} = -0.5$ .