# Problem 1 (Ch. 12)

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**Productivity**: the amount of goods and services a worker can produce per hour.

(a) Complete the table below.

	<b>Physical Capital</b>	<b>Labor Force</b>	Physical Capital per Worker	<b>Labor Hours</b>	Output	<b>Labor Productivity</b>
Year	(Looms)	(Workers)	(Looms)	(Hours)	(Garments)	(Garments per hour of labor)
2026	40	20		1,000	6,000	
2027	120	40		1,400	12,600	

- **(b)** A(n) [increase or decrease] in physical capital per worker is associated with a(n) [increase or decrease] in labor productivity from.
- (c) Which of the following policies would lead to greater productivity in the weaving industry?
  - Sharply increasing the interest rate on student loans to people pursuing advanced degrees in weaving
  - Encouraging saving by allowing workers to set aside a portion of their earnings in tax-free retirement accounts
  - Imposing restrictions on foreign ownership of domestic capital
  - Imposing a tax on looms

### Problem 1 Answers

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**2026** 40 capital with 20 workers means each worker has 2 capital to work with. It takes 1000 labor hours to create 6000 garments, so that's 6000/1000 = 6 garments per hour of labor.

**2027** 120 capital with 40 workers means each worker has 3 capital to work with. It takes 1400 labor hours to create 12600 garments, so that's 12600/1400 = 9 garments per hour of labor.

Physic	al Capital pe	r Worker	Labor Productivity		
(Looms)			(Garments per hour of labor)		
	2	✓		6	✓
	3	✓		9	✓

There is an *increase* in physical capital per worker and an *increase* in labor productivity.

Productivity is determined by

- Human capital per worker (e.g. health and education)
- Natural resources per worker
- Physical capital per worker
- Technological knowledge

Encouraging saving will expand the pool of savings available for investment in physical capital.

# Problem 2 (Ch. 13)

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GDP in this closed-economy country is \$900 million. Find consumption. (Recall: GDP = C + I + G + XM. A closed economy means XM = 0.)

	Value		
National Income Account	(Millions of dollars)		
Government Purchases $(G)$	250		
Taxes minus Transfer Payments $(T)$	325		
Consumption $(C)$			
Investment $(I)$	275		

- **Private saving** is defined as Y T C.
- Public saving is defined as T G.
- National saving, denoted S, is defined as S = Y C G. Notice that national saving is private saving plus public saving:

$$(Y - T - C) + (T - G) = Y - C - G = S.$$

Find each type of saving. Is the government running a budget surplus or deficit?

### Problem 2 Answers

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### Consumption

Because Y = C + I + G in a closed economy, it follows that C = Y - I - G. Therefore,

$$C = 900 - 275 - 250 = 375.$$

**Private Saving** Y - T - C = 900 - 325 - 375 = 200

**Public Saving** T - G = 325 - 250 = 75

**National Saving** Y - C - G = 900 - 375 - 250 = 275

Notice that in a closed economy, we can also write I = Y - C - G. Therefore, in a closed economy, it is always the case that S = I. (This is an accounting identity.)

Public saving is positive, so the government is running a budget surplus.

OMG YOU WON TEH LOTTERY!!!!!11 Yeah, um, you can receive the money either

- as a lump sum you receive \$2,850 today, or
- you get \$1,000 today, \$1,000 a year from today, and \$1,000 two years from today.
- (a) The interest rate is 5% per year. Assuming you want the option that gives you the most purchasing power, would you rather take the lump sum or the payments over time?
- **(b)** What about if the interest rate is 8% per year?

#### At 5% Interest Rate

- The present value of \$1,000 received one year from now is \$1000/1.05 = \$952.38.
- Present value of \$1,000 received two years from now is  $$1000/(1.05^2) = $907.03$ .
- Therefore the three payments discounted at an interest rate of 5% is

$$$1000 + $952.38 + $907.03 = $2859.41.$$

• This is more than the lump sum of \$2850, so better off taking the three payments.

#### At 8% Interest Rate

- The present value of \$1,000 received one year from now is 1000/1.08 = 925.93.
- Present value of \$1,000 received two years from now is  $1000/(1.08^2) = 857.34$ .
- Therefore the three payments discounted at an interest rate of 8% is

$$$1000 + $925.93 + $857.34 = $2783.26.$$

• This is less than the lump sum of \$2850, so better off taking the lump sum.

# Future Value, Present Value, and Discounting

#### Future Value

- Suppose you have the choice of receiving \$100 today or \$105 tomorrow. Which would give you more purchasing power? It depends on the interest rate.
- Suppose the interest rate is 2%. Then you could accept \$100 today, invest it for a year at 2%, and have \$102 one year from now—this is the **future value** of the \$100. But you would have been better off just accepting the second option of \$105 one year from now.
- Suppose the interest rate is 10%. Then you could accept \$100 today, invest it for a year at 10%, and have \$110 one year from now—again, this is the future value. This is more than the \$105 you'd have received if you'd chosen the second option.

#### Present Value

Instead of figuring out what \$100 is worth one year from now, we can figure out what amount of money today is equivalent to \$100 one year from now—this is called **discounting**. Solve

$$\$x \times (1+r) = \$100 \implies \$x = \frac{\$100}{1+r},$$

where r is the interest rate. This gives the **present value** of \$100 one year from now. We can apply the same logic to any number of years. For instance, \$100 ten years from now is today worth

$$\$x \times (1+r)^{10} = \$100 \implies \$x = \frac{\$100}{(1+r)^{10}}$$