

Contents

3	LOFAR LBA 3C 295 and Boötes	1
3.1	Introduction	2
3.2	Observations & data reduction	3
3.2.1	Data reduction	4
3.2.2	Imaging and cleaning	9
3.3	Results	9
3.3.1	Source detection	15
3.3.2	Astrometric uncertainties	15
3.3.3	Flux density uncertainties	18
3.3.4	Completeness and reliability	20
3.4	Analysis	22
3.4.1	Source counts	22
3.4.2	Spectral indices	26
3.4.3	Ultra-steep spectrum sources	29
3.5	Conclusions	32
3.A	Extended sources at 62 MHz	34
3.B	SED & photo-z fitting results	39
3.C	Source counts at 62 MHz for the Boötes field and 3C 295 fields	43
	Bibliography	45

CHAPTER
3

LOFAR Low-band antenna observations of the 3C 295 and Boötes fields: source counts and Ultra-Steep Spectrum sources

We present LOFAR Low Band observations of the Boötes and 3C 295 fields. Our images made at 34, 46, and 62 MHz reach noise levels of 12, 8, and 5 mJy beam⁻¹, making them the deepest images ever obtained in this frequency range. In total, we detect between 300 and 400 sources in each of these images, covering an area of 17 to 52 deg². From the observations we derive Euclidean-normalized differential source counts. The 62 MHz source counts agree with previous GMRT 153 MHz and VLA 74 MHz differential source counts, scaling with a spectral index of -0.7 . We find that a spectral index scaling of -0.5 is required to match up the LOFAR 34 MHz source counts. This result is also in agreement with source counts from the 38 MHz 8C survey, indicating that the average spectral index of radio sources flattens towards lower frequencies. We also find evidence for spectral flattening using the individual flux measurements of sources between 34 and 1400 MHz and by calculating the spectral index averaged over the source population. To select ultra-steep spectrum ($\alpha < -1.1$) radio sources, that could be associated with massive high redshift radio galaxies, we compute spectral indices between 62 MHz, 153 MHz and 1.4 GHz for sources in the Boötes field. We cross-correlate these radio sources with optical and infrared catalogues and fit the spectral energy distribution to obtain photometric redshifts. We find that most of these ultra-steep spectrum sources are located in the $0.7 \lesssim z \lesssim 2.5$ range.

van Weeren, R. J., Williams, W. L., Tasse, C., et al.
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3.1 Introduction

3.1 Introduction

Low-frequency surveys of the sky are an important tool to address various open questions in astrophysics ranging from the evolution of galaxies, active galactic nuclei (AGN), galaxy clusters, to pulsars. The half power beam width (HPBW) of radio telescopes scales with wavelength, making low-frequency radio observations ($\lesssim 300$ MHz) an efficient way to carry out large-area surveys. In addition, these observations take advantage of the steep synchrotron spectra ($F_\nu \propto \nu^\alpha$, with α the spectral index) of many extragalactic radio sources, with the flux densities increasing towards lower frequencies.

Low-frequency observations are particularly important to locate distant high-redshift radio galaxies (HzRG). Empirically it has been found that the radio spectral index correlates with the redshift of host galaxies, with the steepest spectra corresponding to the highest redshifts. Therefore massive high-redshift galaxies can be found by selecting radio sources with ultra-steep radio spectra (USS), especially in combination with an optical or near-IR magnitude cut (e.g., De Breuck et al. 2000; Miley & De Breuck 2008; Ker et al. 2012). However, USS sources are rare so large surveys are needed to find them. The fraction of USS sources with $\alpha_{\sim 350}^{1400} < -1.3$ is about 0.5% (De Breuck et al. 2000). Deep observations at $\lesssim 150$ MHz have the potential to detect sources with $\alpha \lesssim -2$, because these sources become too faint to be detected in sensitive high-frequency observations.

Radio sources in the last stages of the AGN evolution (both short and long-lived) are also most efficiently selected at low-frequencies. These relic or dying radio sources have steep and curved radio spectra due to synchrotron and inverse Compton losses as the central energy supply has been switched off (e.g., Parma et al. 2007; Kunert-Bajraszewska et al. 2010; Murgia et al. 2011).

Recently, most deep low-frequency surveys have been carried out with the GMRT at around 150 MHz (e.g., Ishwara-Chandra & Marathe 2007; Sirothia et al. 2009; Ishwara-Chandra et al. 2010; Intema et al. 2011; Williams et al. 2013). These surveys reach a rms noise level of the order of a mJy per beam. Below 100 MHz, there are no radio surveys that reach a similar depth. Cohen et al. (2004) carried out a 165 deg^2 74 MHz survey with a central noise of 24 mJy beam^{-1} at a resolution of $25''$. Tasse et al. (2006) surveyed the XMM-LSS field at 74 MHz with a resolution of $30''$, covering an area of 132 deg^2 . The median rms noise over the field was 32 mJy beam^{-1} . Larger, but shallower surveys below 100 MHz, are the 74 MHz VLSS (Cohen et al. 2007; Lane et al. 2014) and 38 MHz (Hales et al. 1995; Rees 1990) surveys.

The LOw Frequency ARray (LOFAR) is a new generation radio telescope operating at 10–240 MHz (van Haarlem et al. 2013). With its multi-beaming capabilities, high-spatial resolution, and large fractional bandwidth, it is an ideal instrument to carry out large surveys. Here we report on the first LOFAR Low Band Antenna commissioning observations of the Boötes and the 3C 295 fields (which includes the Groth Strip). Both the Boötes field and the Groth Strip have been extensively studied at higher radio frequencies and other parts of the electromagnetic spectrum. For the Boötes field, observations have been carried out at 153 MHz (Intema et al. 2011; Williams et al. 2013), 325 MHz (Croft et al. 2008), 1.4 GHz (de Vries et al. 2002; Higdon et al. 2005), and 3.1 GHz (Croft et al. 2013). The Groth strip has been observed at 1.4 GHz (Ivison et al. 2007).

The outline of this paper is as follows. The observations and data reduction are described in Sect. 3.2. The results and analysis are presented in Sects. 3.3 and 3.4. This is followed by the conclusions in Sect. 3.5. All coordinates and images use the J2000 coordinate system.

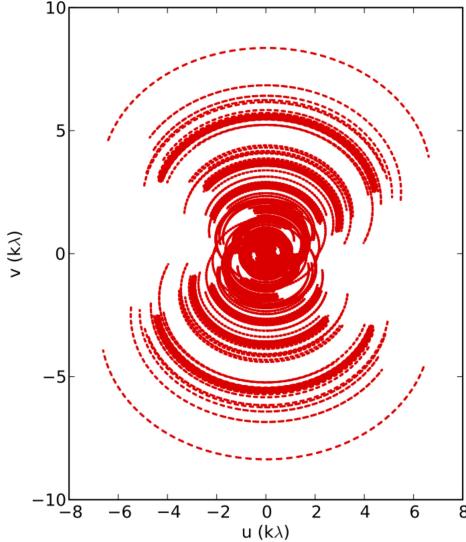


Figure 3.1: UV-coverage of the 3C 295 observations. The relatively large fractional bandwidth fills the uv-plane radially (not shown in the figure).

3.2 Observations & data reduction

The Boötes and 3C 295 fields were simultaneously observed on April 12, 2012 as part of a multi-beam observation with the LOFAR Low Band Antenna (LBA) stations. The idea behind the multi-beam setup is that we use the 3C 295 observations as a calibrator field to transfer the gain amplitudes to the (target) Boötes field. The total integration time on both fields was 10.25 hr. An overview of the observations is given in Table 3.1. Complete frequency coverage was obtained between 54 and 70 MHz for both fields, while non-contiguous frequency coverage was obtained between 30 and 54 MHz for the 3C 295 only. All four correlation products were recorded. By default, the frequency band was divided into subbands, each 195.3125 kHz wide. Each subband was further divided in 64 channels and the integration time was 1 s.

Nine Dutch remote stations were used, and 22 core stations, giving baselines that range between 90 m and 80 km. The resulting uv-coverage is displayed in Fig. 3.1. The LBA_OUTER configuration was used. In the LBA_OUTER configuration 48 LBA antennas are used, located mostly in the outer part of the stations (which have diameters of about 81 m). This increases the sidelobe levels for the station beams, but reduces the field of view (FoV) with respect to other station antenna configurations available. The HPBW is about 3.6° , 4.8° , and 7.2° at 60, 45, and 30 MHz, respectively. It should be noted though that the station beams are complex-valued, time and direction dependent, and differ from station to station.

3.2 Observations & data reduction

Table 3.1: LBA Observations

Observations ID	L56691
Pointing center 3C 295	14 ^h 11 ^m 20.9 ^s , +52°13'55"
Pointing center Boötes	14 ^h 32 ^m 03.0 ^s , +34°16'33"
Integration time	1 s
Observation date	12 April, 2012
Total on-source time	10.25 hr
Correlations	XX, XY, YX, YY
Frequency setup	54–70 MHz ^a full coverage 40–54 MHz ^b 25 subbands* 30–40 MHz ^c 21 subbands*
Bandwidth	16 MHz ^a , 4.9 MHz ^b , 4.1 MHz ^c
Bandwidth per subband	195.3125 kHz
Channels per subband	64

^a 54–70 MHz Boötes and 3C 295 fields

^b 40–54 MHz 3C 295 field

^c 30–44 MHz 3C 295 field

* subbands are more or less evenly distributed within this frequency range, the total bandwidth is reported in Table 3.2

3.2.1 Data reduction

Our data reduction broadly consists of the following steps: (1) flagging, (2) bright off-axis source removal, (3) averaging, (4) solving for the 3C 295 complex gains (in a circular basis to deal with differential Faraday Rotation), (5) transfer of the amplitude solutions from 3C 295 to the Boötes field, and (6) phase-only calibration of the Boötes field against a GMRT model, and (7) imaging of the 3C 295 field and Boötes fields. All calibration steps are performed with the BlackBoard Selfcal (BBS) software system (Pandey et al. 2009). Below these steps are explained in more detail.

Flagging, bright off-axis source removal, and averaging

The first step in the reduction consisted of the automatic flagging of radio frequency interference (RFI) using the AOFlagger (Offringa et al. 2010, 2012). The first and last three channels of each subband were also flagged. Typically about 2% of the data was flagged as RFI in the 50 to 70 MHz range. Between 30 and 40 MHz this percentage increases by a factor of $\sim 2\text{--}3$ (see Offringa et al. 2013, for an overview of the LOFAR RFI environment). About a dozen subbands were lost due to failures of the data storage system.

A next step consisted of the removal of the bright “A-team” radio sources Cas A and Cyg A. These sources have integrated flux densities of 18 and 17 kJy at 74 MHz, respectively. Although they are located outside the main FoV, they are sufficiently bright to prevent proper calibration and imaging of sources in the central part of the FoV if detected in the secondary lobes of the

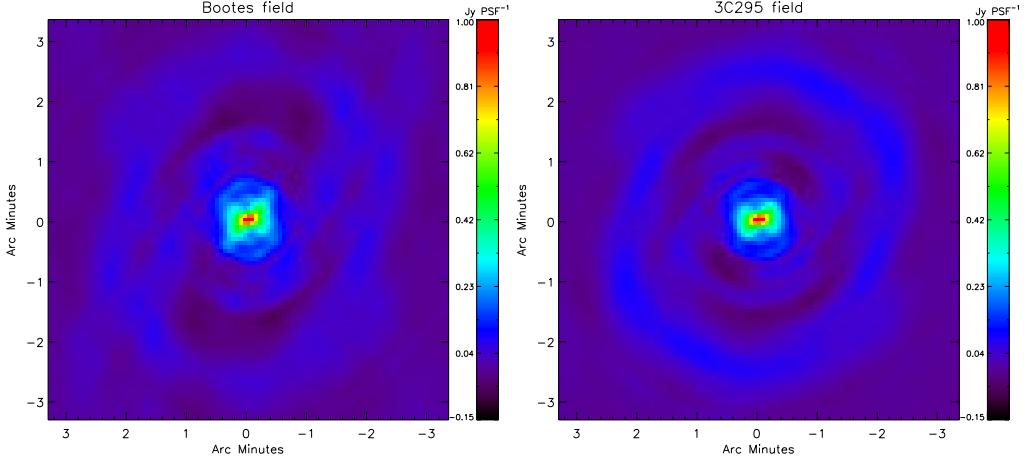


Figure 3.2: Point Spread Functions for the Boötes (*left*) and 3C 295 (*right*) images covering the 54–70 MHz frequency range.

beam. The amplitudes of these off-axis sources are strongly modulated as they move in and out of the station beam sidelobes. These sources were removed with the “demixing” method described by van der Tol et al. (2007) and which is part of the standard LOFAR pre-processing pipeline (Heald et al. 2010). For the models of Cas A and Cyg A we took the clean component models at 74 MHz from Very Large Array (VLA) A-array¹ observations (Kassim et al. 2007) with a resolution of 25''. After flagging and subtracting out Cas A and Cyg A, we averaged the data in time to 5 s and one channel per subband. The time resolution is set by the requirement to avoid decorrelation due to rapid ionospheric phase variations. At large radial distances from the field center there is some bandwidth smearing. At the HPBW, the source width increases by a factor of ~ 1.2 at 62 MHz and a factor of ~ 1.9 at 34 MHz, due to this effect.

3C 295 field

The primary calibrator 3C 295 has a sufficiently high flux density that it dominates the total flux in the main FoV. 3C 295 consists of two main source components (e.g., Perley & Taylor 1991) and has an angular size of only $\sim 5''$. Given that our longest baseline is ~ 80 km (corresponding to a resolution of about 10''), we used a simple two clean component model for the source. The integrated flux density of the source is given by the model of Scaife & Heald (2012).

Before calibrating, we converted the linear XX, XY, YX, YY correlations (V_{XY}) to circular RR, RL, LR, LL correlations V_{RL} using the transformation described by Hamaker & Bregman (1996)

$$V_{RL} = C_A V_{XY} C_A^*, \quad (3.1)$$

¹<http://lwa.nrl.navy.mil/tutorial/>

3.2 Observations & data reduction

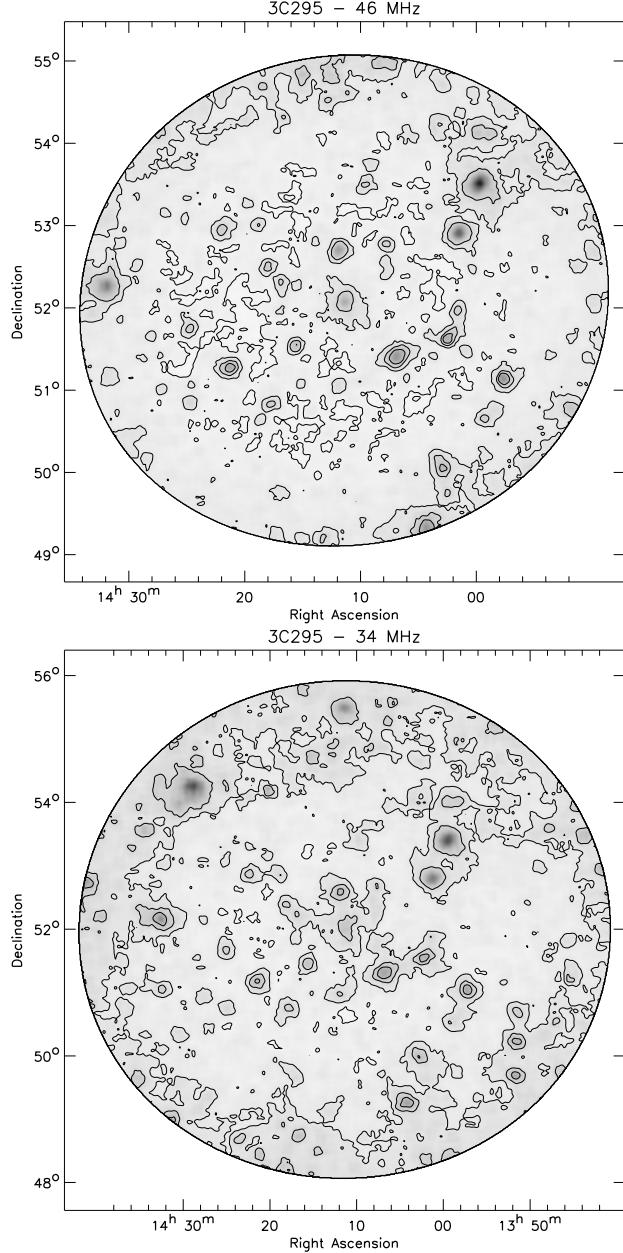


Figure 3.3: Figures showing the local rms noise in the images. A box size of 80×80 pixels was used in computing the local rms noise. The pixel sizes are listed in Table 3.2. The gray scales display the range from $0.5\sigma_{\text{rms}}$ to $10\sigma_{\text{rms}}$, with the σ_{rms} values taken from Table 3.2. Contour levels are drawn at $(\sqrt{2})^n \times \sigma_{\text{rms}}$, with n ranging from -1 to 3. The local noise variations are correlated with the position of strong sources.

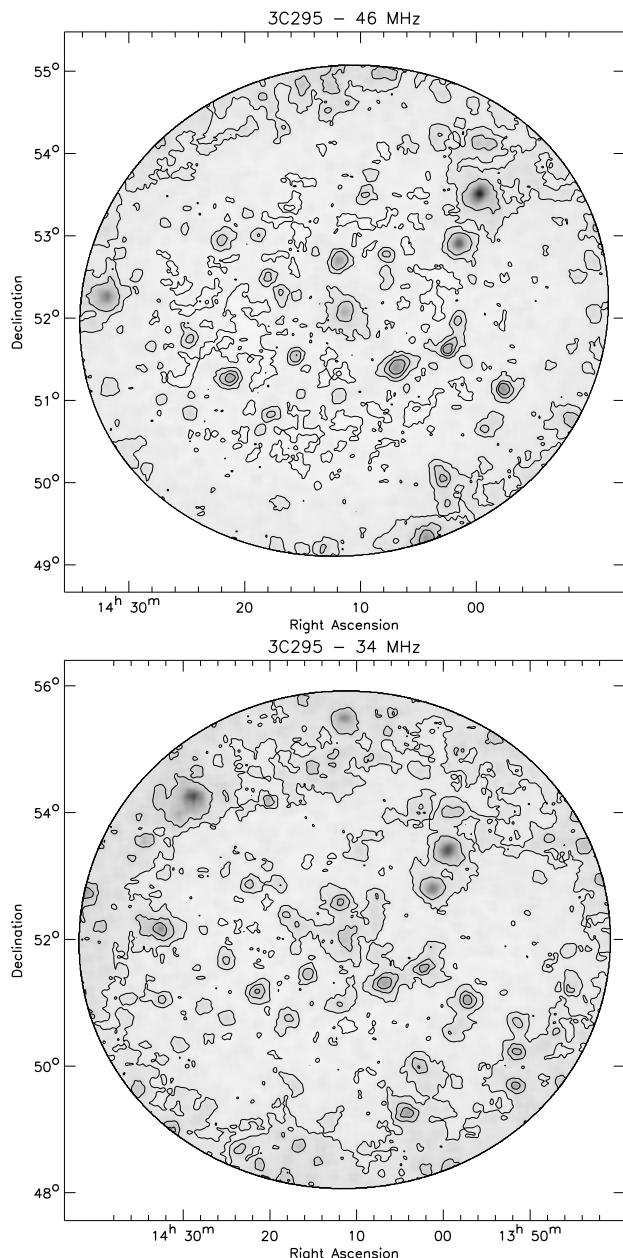


Figure 3.3: Continued.

3.2 Observations & data reduction

with

$$C_A = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ 1 & -i \end{pmatrix}. \quad (3.2)$$

This transformation was done via a Python script. The effects of the station beams¹ were taken out as well in the direction of 3C 295 with BBS. This is needed because the LBA stations do not record “true” linear correlation products due to the fixed orientation of the dipole antennas on the ground.

The (only) reason for converting to circular correlations is that differential Faraday Rotation, which is important in the LBA frequency range, only affects the RR and LL phases, while in linear correlations, flux from XX and YY leaks into the cross-hand XY and YX correlations. Therefore by converting to circular correlations the calibration is simplified, since we only have to solve for the RR and LL phases to remove the effects of differential Faraday Rotation (e.g., Smirnov 2011). The conversion from linear to circular correlations depends on the accuracy of the beam models. It is also possible to solve for differential Faraday Rotation in a more direct way using the observed linear correlations but this requires solving for an extra free parameter.

After converting to circular correlations we obtained amplitude and phase solutions for the RR and LL correlations for each subband using the 3C 295 model (with BBS). We used a solution interval of 5 s. This takes care of the frequency dependence of ionospheric phase variations, differential Faraday Rotation, clock errors, and the overall LBA bandpass (with a single complex gain correction for each time interval per subband). Good quality solutions were obtained over the entire time and frequency range, except for time periods affected by RFI. We then subtracted 3C 295 from the data using these gain solutions. This avoids many clean cycles and clean dynamic range limitations such as described in Cotton & Uson (2008). After the 3C 295 gain calibration we converted back the calibrated visibilities from circular to linear correlations because of limitations in the imaging software.

Boötes field

We transferred the amplitude solutions from the corresponding frequencies of the 3C 295 observation to the Boötes field dataset. The Boötes field does not contain any bright dominating sources. This means that there is not enough signal available per subband for a phase-only calibration on a timescale of 5 sec. To increase the signal to noise, all subbands were combined into a new measurement set consisting of 81 channels covering the entire 54–70 MHz range, with each channel corresponding to one individual subband. We then performed a phase-only calibration for groups of 27 channels each to obtain sufficient signal to noise to calibrate the distant remote stations against the GMRT 153 MHz model.

For the Boötes field, the calibration model is derived from a deep GMRT 153 MHz image (Williams et al. 2013) using the PyBDSM source detection software².

¹The station beam model is derived using the dipole beam model based on the interpolation of electromagnetic simulations of the LBA dipole beam response, and the dipole locations within a station (Hamaker & Bregman 1996).

²<http://dl.dropboxusercontent.com/u/1948170/html/index.html>

3.2.2 Imaging and cleaning

Imaging and cleaning was carried out with `awimager` (Tasse et al. 2013), which incorporates the complex valued, time varying and frequency dependent individual station beams using A-Projection (Bhatnagar et al. 2008). For LOFAR, all 4×4 Mueller terms have to be taken into account in the A-Projection. For `awimager` a hybrid AW-projection algorithm was developed to apply the time, frequency, baseline, and direction dependent effects in full-polarization in an efficient way. Also, a new parallel gridding technique is used, which differs from the `casapy`¹ griddler.

For the imaging, we combined all available 54–70 MHz subbands for the Boötes and 3C 295 fields to improve the uv-coverage with multi-frequency synthesis (MFS). We did not correct for the spectral index of individual sources (Rau & Cornwell 2011) because such an algorithm is not yet implemented for `awimager`. For the 3C 295 field, we made two additional images from the subbands in the ranges 30–40 MHz and 40–54 MHz. We employed various robust weighting schemes (Briggs 1995) to find that a robust parameter of about 0.0 typically gave the lowest rms noise level. All final images have sizes of 8192² pixels and were made with a robust value of 0.0 and all baselines were included. The Point Spread Functions for the 54–70 MHz images are shown in Fig. 3.2. An overview of the image properties is given in Table 3.2.

We used clean masks during the final imaging step to minimize clean bias effects (e.g., Condon et al. 1998; White et al. 1997). The mask was derived from a previous imaging run without any mask. The clean mask was generated with PyBDSM, detecting islands of emission with a $3\sigma_{\text{rms}}$ island threshold, a pixel threshold of $5\sigma_{\text{rms}}$, and a locally varying rms box with a size of 80×80 pixels to take into account artifacts around strong sources. The 80-pixels approximately correspond to the spatial scale over which the local rms noise changes in the presence of strong sources. Maps of the local rms noise are shown in Fig. 3.3.

3.3 Results

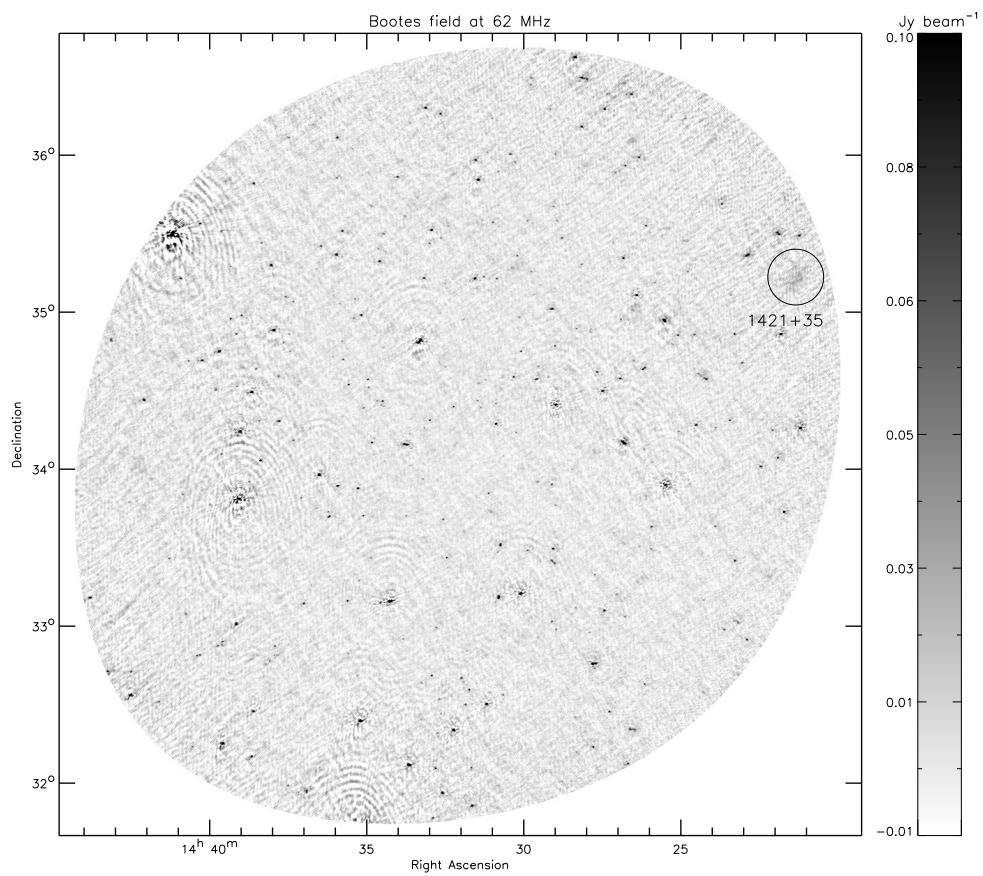
An overview of the resulting images, resolution, FoV, and noise levels obtained is given Table 3.2. The primary beam corrected images are displayed in Figs. 3.4 to 3.7. The artifacts visible around the brighter sources in the fields are due to imperfect calibration and errors in the station beam model. These artifacts also give rise to the increased noise around bright sources (Fig. 3.3). The “spoke”-like patterns are likely caused by direction dependent ionospheric phase errors. The spokes are not visible at the position of 3C 295 because the ionospheric phase variations in this direction were properly taken into account (phase calibration was performed in the 3C 295 direction).

The “smudge” visible in the 3C 295 field (labeled with a circle in Figs. 3.6 and 3.7) at $14^{\text{h}}03^{\text{m}} +54^{\circ}21'$ is the galaxy NGC 5457 (M101). In the Boötes field, faint diffuse emission is found at $14^{\text{h}}21.5^{\text{m}} +35^{\circ}12'$, labeled with a circle in Fig. 3.4. This source (1421+35) was previously also noted by Delain & Rudnick (2006) and Williams et al. (2013). A more detailed study of the source was performed by de Gasperin et al. (2014). They conclude that the extended radio emission is the remnant of a past AGN activity cycle of NGC 5590 at $z = 0.0107$.

¹<http://casa.nrao.edu>

3.3 Results

Figure 3.4: Primary beam corrected Boötes field 62 MHz image. The image is blanked beyond a primary beam attenuation factor of 0.4. The position of the diffuse source 1421+35 is indicated.



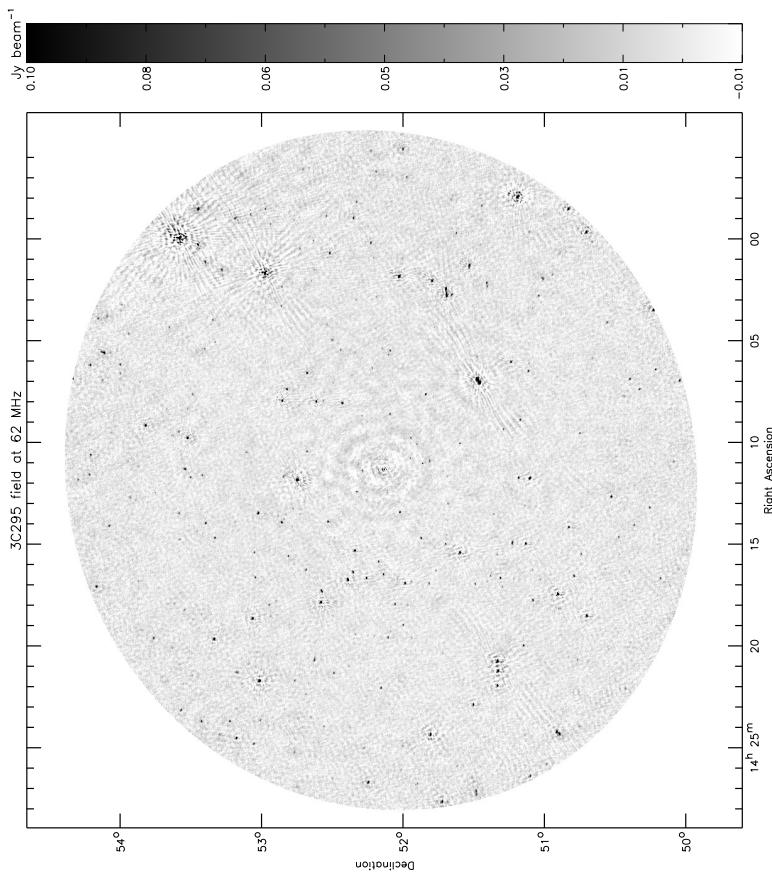
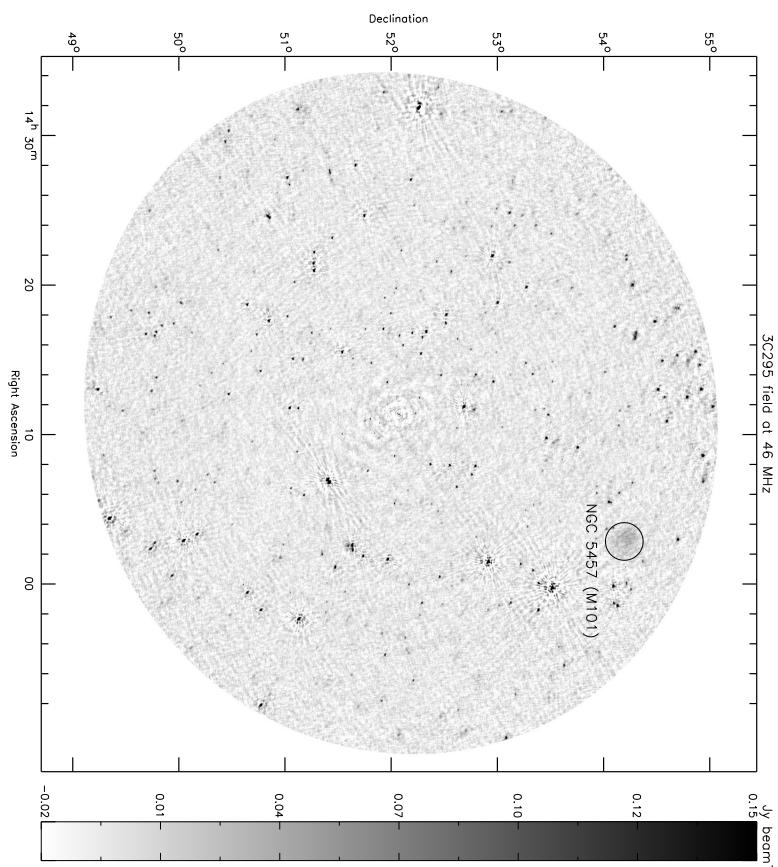


Figure 3.5: Primary beam corrected 3C295 field 62 MHz image. The image is blanked beyond a primary beam attenuation factor of 0.4.

3.3 Results

Figure 3.6: Primary beam corrected 3C 295 field 46 MHz image. The image is blanked beyond a primary beam attenuation factor of 0.4. The position of NGC 5457 (M101) is indicated.



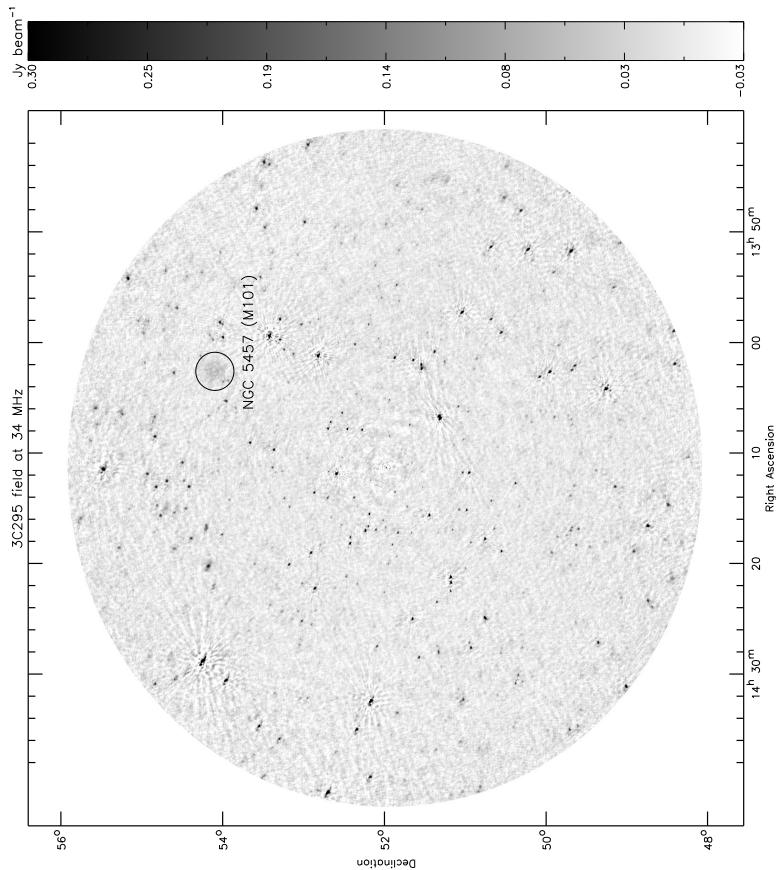


Figure 3.7: Primary beam corrected 3C295 field 34 MHz image. The image is blanked beyond a primary beam attenuation factor of 0.4. The position of NGC 5457 is indicated.

3.3 Results

Table 3.2: LOFAR LBA image characteristics

field	frequency MHz	field of view ^a deg ²	bandwidth MHz	rms noise (σ_{rms}) mJy beam ⁻¹	synthesized beam arcsec	pixel size arcsec
Boötes	62	19.4	16	4.8	31 × 19	4.0
3C295	62	17.0	16	5.3	29 × 18	4.0
3C295	46	30.5	4.9	8.2	40 × 24	6.0
3C295	34	52.3	4.1	12	56 × 30	8.0

^a with a primary beam correction factor < 0.4

3.3.1 Source detection

We used the PyBDSM software for source detection. PyBDSM works by identifying islands of contiguous pixels above a certain detection threshold and fitting each island with Gaussians. For detecting islands, we took a threshold of $3\sigma_{\text{rms}}$ and a pixel threshold of $5\sigma_{\text{rms}}$, meaning that at least one pixel in each island needs to be above $5\sigma_{\text{rms}}$. We used a locally varying rms noise with a sliding box size of 80×80 pixels to take into account the rms noise increase around the bright sources. We manually inspected the output source catalogues to remove about a dozen false detections. These false detections were associated to side-lobes near bright sources. No sources beyond a primary beam attenuation factor of 0.4 were included.

Because the sources are distorted and smeared, and this distortion varies across FoV due to the ionosphere, the fitted major and minor axes for the Gaussian components cannot be simply used to determine whether a source is resolved or not. To first order, the derived integrated flux densities for the sources should not be affected by the smearing. We carried out a visual inspection for actual resolved sources, images of these sources are given in Appendix 3.A. In Fig. 3.8 we plot histograms of the fitted major and minor axes for the sources in the 3C 295 and Boötes fields. The decrease of the effective resolution towards lower frequencies can be seen by the broadening of the distribution of fitted major and minor axes. The final source list at 62 MHz contains 329 sources for both the Boötes and 3C 295 fields. At 46 and 34 MHz, the lists contain 367 and 392 sources for the 3C 295 field, respectively. Our LBA images reach a similar depth as the 325 MHz WENSS survey (scaling with a spectral index of -0.7). Because of the ionospheric distortions, we do not classify resolved or unresolved sources. The uncertainties for the measured flux densities and positions are discussed in Sects. 3.3.2 and 3.3.3. An example of the source catalogues is shown in Table 3.3. For each source we list the source name, the flux weighted coordinates and uncertainties, and the integrated flux densities and uncertainties.

3.3.2 Astrometric uncertainties

Ionospheric phase distortions and residual calibration errors can have an effect on the source positions. To assess the accuracy of the LBA source positions we compared them to the source positions from the 325 MHz WENSS survey (Rengelink et al. 1997). The positional accuracy of the WENSS survey is reported to be $5 - 10''$ for the faintest sources and increases to $1.5''$ for the brighter sources.

For all our sources detected in the LOFAR images, we searched for the closest counterpart in the WENSS survey. The difference between the LOFAR positions and WENSS positions are displayed in Fig. 3.9. The positional offsets ($\Delta\alpha, \Delta\delta$) are a combination of imperfect calibration, noise dependent offsets from position determination using Gaussian fitting by PyBDSM, and offsets due to differences in source structure between 325 and 34–62 MHz, related to spectral index variations across the sources and/or differences in resolution between the WENSS and LOFAR images.

The median source position offsets between LOFAR and WENSS are smaller than 1/10th of the beam size for all frequencies, and therefore we do not correct our lists for systematic position offsets. To reduce the effect of the noise dependent term in the position offsets, we re-calculated the offsets taking only sources that are detected with a signal to noise ratio larger than 20 in the LOFAR images. Using only these bright sources, we find a scatter of $(\sigma_\alpha, \sigma_\delta = 1.8'', 1.9'')_{\text{Boötes}, 62\text{MHz}}, (\sigma_\alpha, \sigma_\delta = 2.1'', 3.1'')_{\text{3C 295}, 62\text{MHz}}, (\sigma_\alpha, \sigma_\delta = 3.7'', 5.6'')_{\text{3C 295}, 46\text{MHz}}$,

3.3 Results

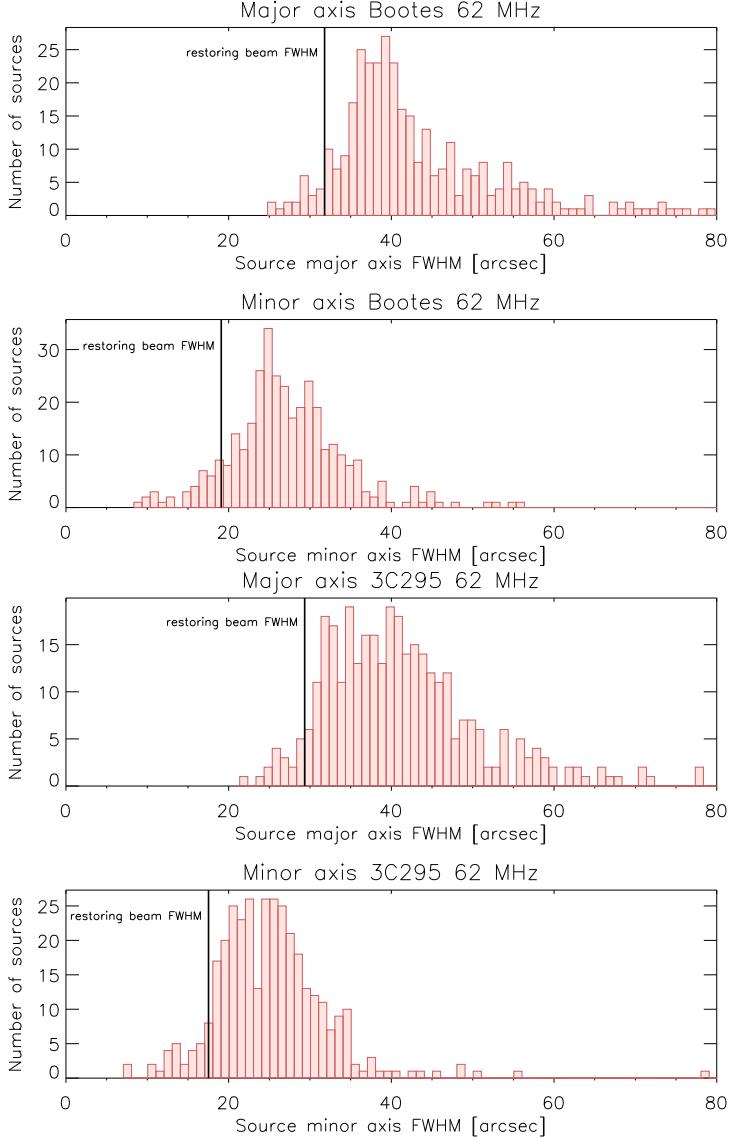
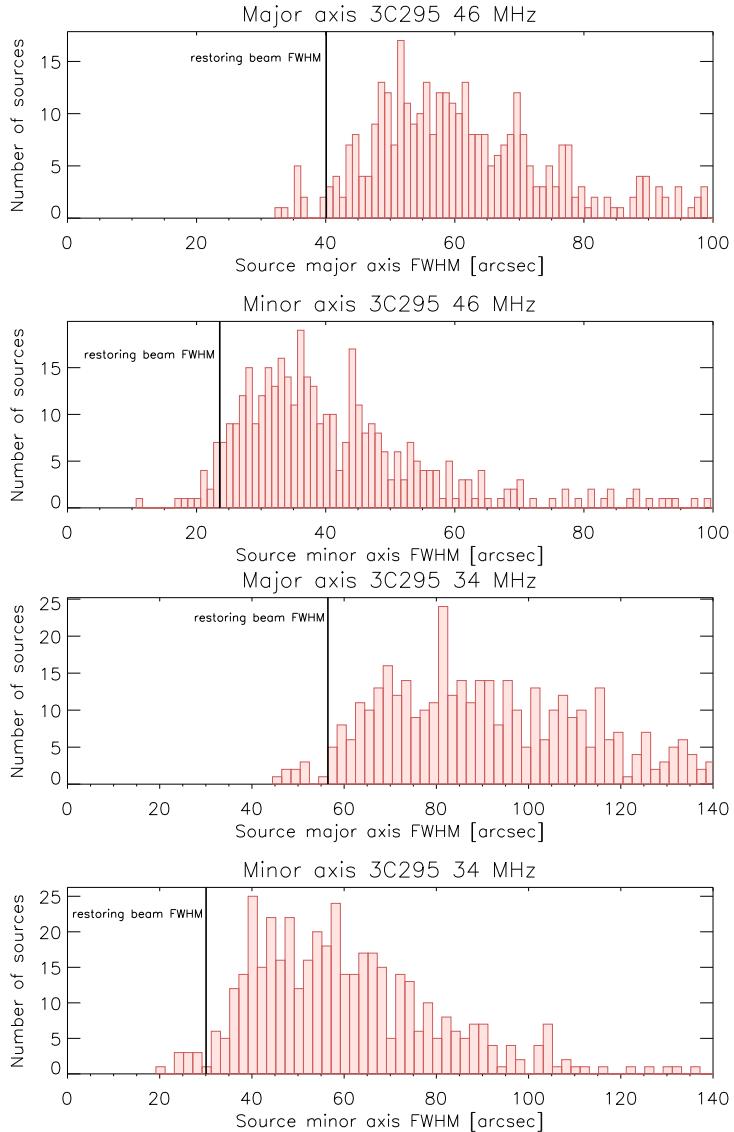


Figure 3.8: Distribution of fitted major and minor axes (full width half maximum) for the Boötes and 3C295 fields. These values are not deconvolved by the beam. Solid black line indicates the fitted restoring beam based on the uv coordinates. Uncorrected ionospheric phase variations causes “smearing” of sources and decreases the effective resolution. This effect increases towards lower frequencies.

**Figure 3.8: Continued.**

3.3 Results

Table 3.3: Sample of the LOFAR 62 MHz Boötes field source catalogue

Source ID	RA [deg]	σ_{RA} [""]	DEC [deg]	σ_{DEC} [""]	$S \pm \sigma_S$ [mJy]
J143859.5+345312	219.74800	2.2	34.88676	2.1	237 ± 40
J143856.4+343310	219.73524	3.2	34.55297	2.5	145 ± 29
J143849.0+335015	219.70420	1.8	33.83753	1.9	6469 ± 1008
J143849.3+341553	219.70580	1.8	34.26481	1.9	2816 ± 439
J143850.4+350020	219.71027	2.0	35.00571	2.0	298 ± 49
J143831.3+335652	219.63057	4.4	33.94792	3.2	174 ± 36
J143828.9+343107	219.62059	1.8	34.51874	1.9	2035 ± 317
J143819.1+321149	219.57987	2.1	32.19706	2.1	566 ± 91
J143831.6+355053	219.63205	2.1	35.84832	2.1	516 ± 81
J143817.1+322905	219.57145	1.8	32.48483	2.0	1251 ± 196
J143821.6+344000	219.59040	2.6	34.66683	2.2	194 ± 34
J143814.2+342010	219.55944	2.8	34.33632	2.2	148 ± 27
J143810.9+340500	219.54543	1.8	34.08339	1.9	797 ± 125
J143814.8+352807	219.56189	2.6	35.46880	2.3	186 ± 32
J143750.2+345451	219.45921	1.8	34.91425	2.1	2106 ± 328

and $(\sigma_\alpha, \sigma_\delta = 6.5'', 10.2'')_{\text{3C 295, 34MHz}}$ between LOFAR and WENSS. We added these values in quadrature to the position uncertainties determined from the Gaussian fitting. The strong increase in the scatter towards the lower frequencies suggests that this is the result of residual ionospheric phase errors. The Boötes field has the smallest spread in position offsets.

3.3.3 Flux density uncertainties

For our absolute flux calibration (bootstrapping) we took the scale from Scaife & Heald (2012) for 3C 295. Scaife & Heald report an uncertainty in the 3C 295 flux-scale of about 8% at 34 MHz, 6% at 46 MHz, and 4% at 62 MHz.

We performed a check on the accuracy of the beam model and bootstrapping of the flux-scale. We did this by checking for flux density variations within the FoV, and by looking for an overall scaling factor (which applies to all sources within a field). For this, we compared the measured LBA flux densities to predicted flux densities from external surveys. These predicted fluxes are based on the NVSS (Condon et al. 1998), WENSS (Rengelink et al. 1997), GMRT 153 MHz (Williams et al. 2013, in the case of the Boötes field only), and VLSS Redux (VLSSr, Lane et al. 2014) surveys. We fitted second order polynomials to these flux measurements in $\log(S) - \log(\nu)$ space. We use these polynomial fits to predict the flux densities at the relevant LBA frequencies. To obtain reliable predictions, we only included LOFAR sources that were detected in all external surveys.

For the Boötes field, we find a scatter of 15% between the measured and predicted 62 MHz fluxes and a mean flux ratio of 0.8 (measured flux divided by predicted flux), see Fig. 3.10. If we use the polynomial fits from NVSS, WENSS, and GMRT 153 MHz to predict the VLSSr fluxes we find a scatter of 5%. Therefore, some of the scatter can be attributed to the intrinsic

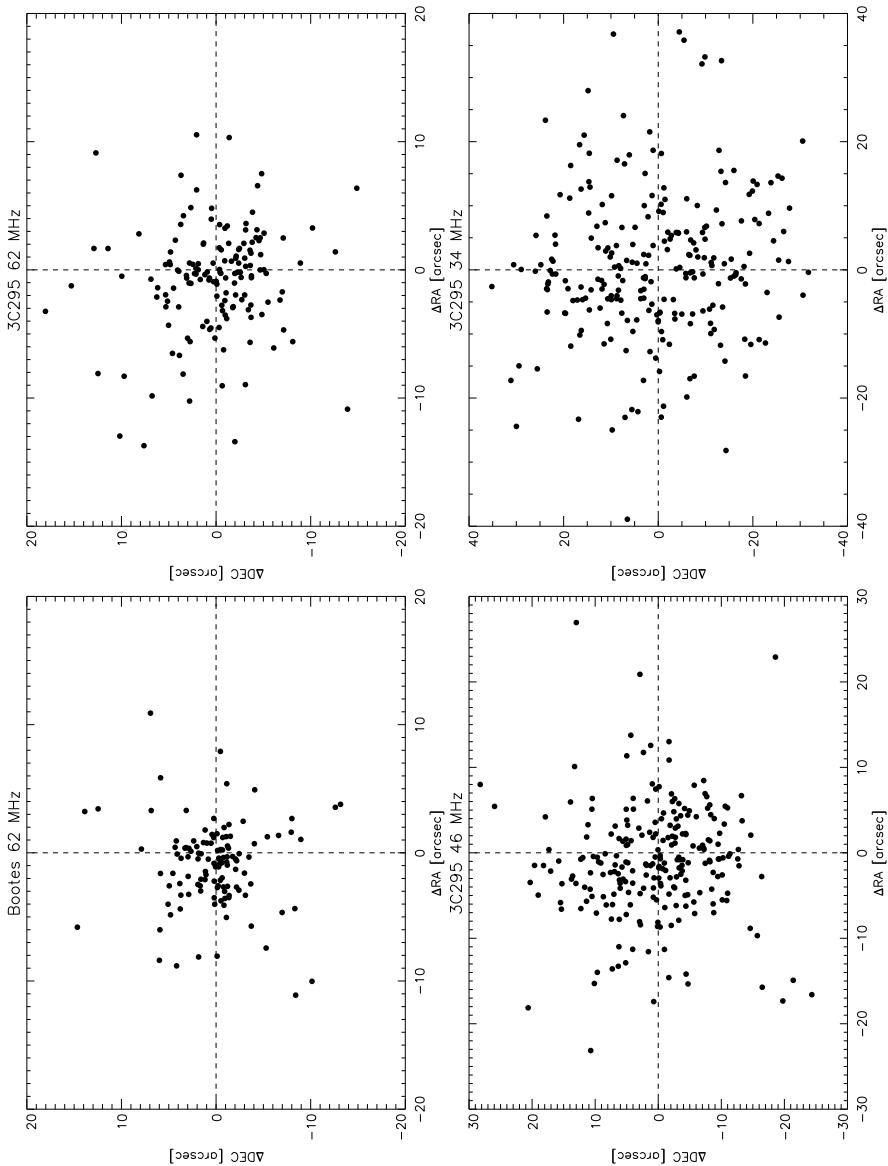


Figure 3.9: The position offsets between the LOFAR LBA and the 325 MHz WENSS sources.

3.3 Results

uncertainties in the predicted LOFAR LBA fluxes due to measurement errors. For the 3C 295 field, we find a scatter of 18%, 29%, 48%, at 62, 46 and 34 MHz, respectively. No clear trends with radial distance from the field center are found. The increase in the scatter for the 3C 295 field at 62 MHz, compared to the Boötes field, is not unexpected since we do not have high-quality GMRT 153 MHz flux density measurements available which help to predict the LBA fluxes. In addition, the predicted 46 and 34 MHz flux densities are considerably more uncertain as we extrapolate from higher frequency data. We therefore argue that the Boötes field 62 MHz fluxes are best suited to determine the flux-scale accuracy across the FoV.

The average measured to predicted flux ratios for the 3C 295 field are 1.0, 1.0, and 1.05, at 62, 46 and 34 MHz, respectively. The mean flux density ratios for the 3C 295 field are consistent with the uncertainty in the adopted flux-scale for 3C 295 itself, reported by Scaife & Heald (2012). The mean flux ratio of 0.8 for the Boötes field likely resulted from the amplitude transfer from 3C 295 to the Boötes field. This transfer relies on the accuracy of the global beam model. At the time of our observations there were issues with the remote station processing (RSP) boards which could have affected the beam shapes and sensitivities of some stations, resulting in errors when transferring the flux-scale from one pointing to another. The RSP boards were fixed about half a year after our observations.

From the above results, we conclude that the relative uncertainties in the flux-scale within a single FoV due to uncertainties in the beam model, are likely less than 15%. We note that this 15% refers to the averaged beam model of all stations over the entire period of the observations. This result is similar to the $\sim 10\%$ we found for LBA observations of Abell 2256 (van Weeren et al. 2012). The transfer of the flux-scale from one field to the other (i.e., from calibrator to target) seems to be more uncertain, in our case we find a mean ratio of 0.8 (Fig. 3.10). To bring the Boötes field flux densities to the same scale as the 3C 295 field, we multiplied them by a factor of 1.25.

The integrated flux density errors (σ_S , Eq. 3.3) are thus a combination of the uncertainties from 3C 295 flux-scale, the uncertainties from the Gaussian fitting (σ_{gauss}), and a conservative 15% uncertainty to account for the beam model used during the imaging process:

$$\sigma_S^2 = \begin{cases} (0.04S)^2 + \sigma_{gauss}^2 + (0.15S)^2 & 62 \text{ MHz} \\ (0.06S)^2 + \sigma_{gauss}^2 + (0.15S)^2 & 46 \text{ MHz} \\ (0.08S)^2 + \sigma_{gauss}^2 + (0.15S)^2 & 34 \text{ MHz} \end{cases} \quad (3.3)$$

In addition, averaging over a wide frequency range leads to an additional flux density error that depends on spectral index of the source. In this work we neglect this error as it is smaller than 1% for a source with $\alpha = -1$.

3.3.4 Completeness and reliability

To quantify the completeness and reliability of the source lists, we performed a Monte-Carlo (MC) simulation in which we generated 25 random fields corresponding to each LOFAR image. Each field contains ~ 1200 randomly positioned point sources with peak flux densities between 2.5 mJy and 6.3 Jy (the catalogue range) for the Boötes 62 MHz field, 2.3 mJy and 6.6 Jy for the 3C 295 62 MHz field, 3.9 mJy and 8.3 Jy for the 3C 295 46 MHz field, and 8.9 mJy and 8.0 Jy for the 3C 295 34 MHz field. The source flux densities are drawn randomly from the source count distribution, $dN/dS \propto S^{-1.6}$ (Williams et al. 2013). We neglect the deviation of the true source

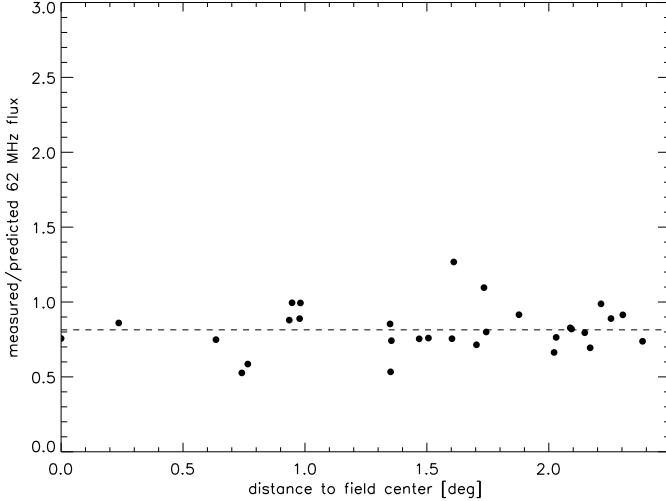


Figure 3.10: Measured flux densities over the predicted flux densities as function of radial distance to the Boötes field center. Dashed line shows the robust mean of the plotted data points.

counts from a power law slope at high flux densities because there are very few sources at these flux densities. The effect of the beam is naturally taken into account by inserting sources in the noise-inhomogeneous maps. We also deal with non-Gaussian noise (calibration errors) in this way. Our MC simulation also accounts for the strong ionospheric and bandwidth smearing in the real LOFAR images by scaling the size of the point sources with radial distance from the centre of the field. The radial scaling factor is determined by the median value within radial distance bins of the ratio of the measured fitted major-axes to the beam major axis in each field. For comparison we also ran the MC simulation without any smearing. Simulated sources were inserted into the residual images resulting after source detection with PyBDSM. Source detection was performed for each randomly simulated field in the same manner as described in Sect. 3.3.1. Only $\sim 300 - 400$ sources in each field satisfy the detection criterion of peak flux density $> 5\sigma$.

We have estimated the catalogue completeness by plotting the fraction of detected sources in our MC simulation as a function of integrated flux density (left panel of Fig. 3.11), i.e., the fraction of input sources that have a catalogued flux density using the same detection parameters. The completeness at a given flux density is determined by integrating the detected fraction upwards from a given flux density limit and is plotted as a function of integrated flux density in the right panel of Fig. 3.11. Due to the variation in the rms noise across the image, the detection fraction has first been multiplied by the fraction of the total area in which the source can be detected. We thus estimate that the catalogue is 95 per cent complete above a peak flux density of 37 mJy (Boötes 62 MHz) and 88 mJy, 51 mJy, and 30 mJy (3C 295 34, 46 and 62 MHz respectively).

The reliability of the catalogue indicates how many sources above a given flux density are real. In the left panel of Figs. 3.12 and 3.12, the false detection rate FDR , i.e., the fraction of catalogued sources that do not have an input source, is plotted as a function of the integrated flux density. Integrating up from a given limit and multiplying by the normalized source flux

3.4 Analysis

distribution, we can determine an estimate of the overall *FDR* or reliability, $R = 1 - FDR$, of the catalogue. The reliability is plotted as a function of integrated flux density limit in the right panel of Figs. 3.12 and Fig. 3.12. We thus estimate that the source list is 95 per cent reliable above a peak flux density of 42 mJy (Boötes 62 MHz) and 108 mJy, 53 mJy, and 32 mJy (3C 295 34, 46 and 62 MHz respectively). These estimates include source smearing.

3.4 Analysis

3.4.1 Source counts

We use the source lists to compute the Euclidean-normalized source counts at 62, 46 and 34 MHz. For this, we have to take into account the large variations of the rms noise across the images (e.g., Windhorst et al. 1985). We choose the flux density bin sizes such that we have approximately 30–60 sources per bin, except for the first and last bins. We corrected these source counts using the Monte-Carlo simulations described in Sect. 3.3.4 with the detected fraction of sources as a function of flux density. The propagated errors in the source counts are based on the Poissonian uncertainties and the uncertainties in the derived detection fraction, see Table 3.4. The resulting Euclidean-normalized source counts are shown in Figs. 3.13 and 3.14.

Only a few source count studies exist below 100 MHz. Cohen et al. (2003, 2004) and Tasse et al. (2006) published source counts at 74 MHz with the VLA. We compare our source counts with those from Cohen et al. (2004) and Tasse et al. (2006) because they go to fainter flux densities than those from Cohen et al. (2003). For that comparison, we rescale the Cohen et al. (2004) and Tasse et al. (2006) flux densities to the newly adopted VLSSr flux-scale (Lane et al. 2014). The VLSSr counts are included as well (Lane et al. 2014). We also compare with 153 MHz source counts from the GMRT for the Boötes field (Williams et al. 2013) because it overlaps to a large extent with our Boötes field data.

The combined source counts at 62 MHz from the Boötes and 3C 295 fields show very good agreement with the results at 74 MHz, which are scaled using $\alpha = -0.7$. The 62 MHz counts reach significantly fainter (about a factor of 6), flux density levels than the 74 MHz counts. The 62 MHz counts fall slightly below the GMRT 153 MHz counts, if we scale these with a spectral index of -0.7 . The simulated 151 MHz SKAD S³-SEX counts (Wilman et al. 2008) closely follow the GMRT 153 MHz counts.

The 34 MHz source counts fall significantly below the extrapolated source counts from 153 and 74 MHz if we scale with $\alpha = -0.7$. This is also the case for the simulated 151 MHz SKAD S³-SEX counts. The 46 MHz differential source counts show a similar situation, although the difference is most pronounced below 0.5 Jy. Scaling with $\alpha = -0.5$ gives a better agreement with the 34 and 46 MHz source counts, an indication that the average spectral index of the sources flattens towards lower frequencies, a result that has been reported before (e.g., Lacy et al. 1992). However, part of the difference could also be caused by field to field variations (Heywood et al. 2013). To check this, we compared the separate source counts for the two fields at 62 MHz, instead of the combined counts that are shown in Fig. 3.13. We find that the 3C 295 field source counts are generally about 20–30% lower than for the Boötes field (see Fig. 3.C.1) so this could explain some of the difference.

Spectral flattening is expected for some sources because of absorption effects and low-frequency spectral indices are flatter than high-frequency ones due to spectral ageing operating at higher

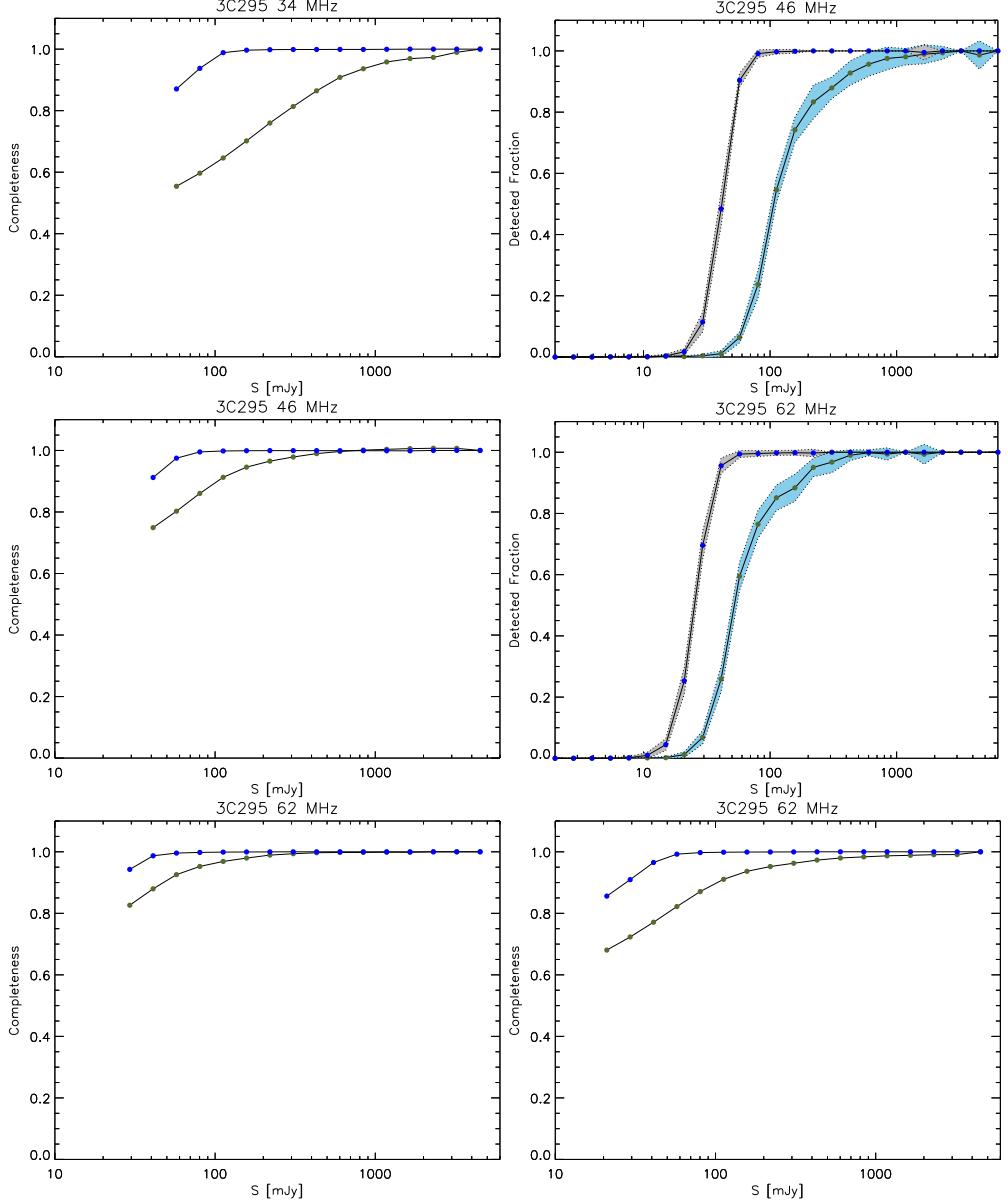


Figure 3.11: Detection fraction and completeness. From *top to bottom*: 3C295 34, 46 and 62 MHz and Boötes 62 MHz. *Left*: Fraction of sources detected as a function of integrated flux density calculated from 25 Monte-Carlo simulations. The solid line shows the mean of all 25 randomly generated fields and the shaded areas show the 1σ uncertainty. The blue shaded areas and olive points include source smearing in the MC simulations (see the main text of Sect. 3.3.4). The grey shaded areas and blue points do not include source smearing. *Right*: Estimated completeness of the catalogue as a function of integrated flux density limit accounting for the varying sensitivity across the field of view. The olive points include source smearing, the blue points do not.

3.4 Analysis

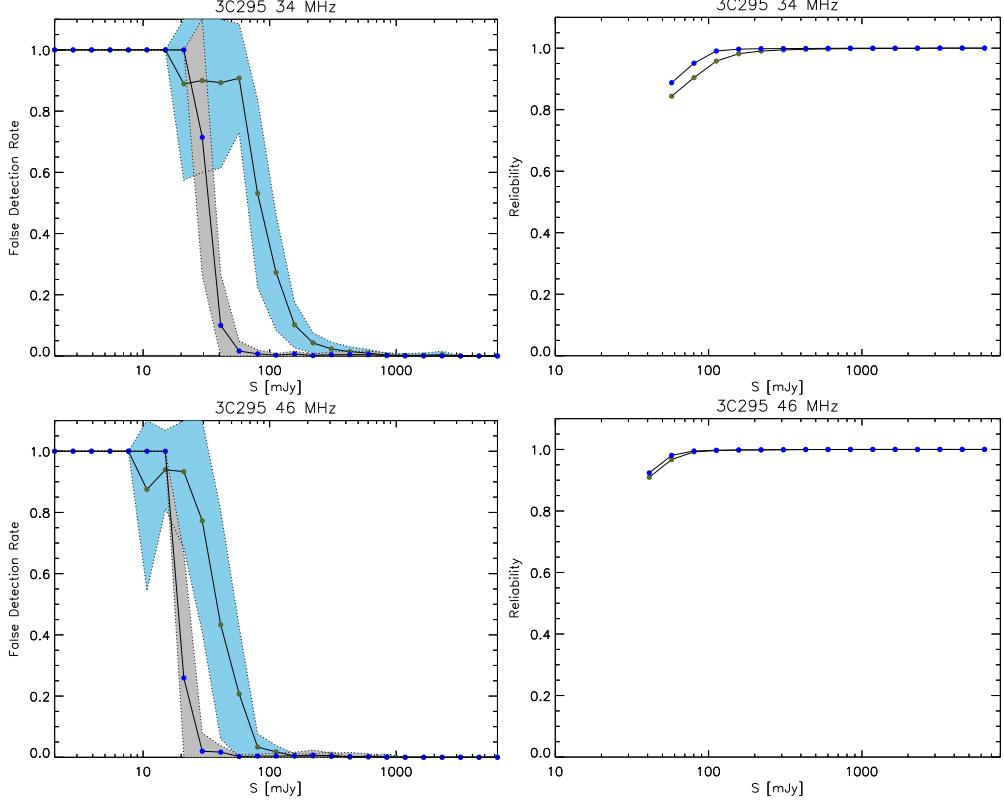


Figure 3.12: False detection rate and reliability. From *top to bottom*: 3C 295 34 and 46 MHz. *Left*: False detection rate as a function of peak flux density to local signal-to-noise ratio calculated from 25 Monte-Carlo simulations. The solid line shows the mean of all 25 randomly generated fields and the shaded areas show the 1σ uncertainty. The blue shaded areas and olive points include source smearing in the MC simulations (see main the text of Sect. 3.3.4). The grey shaded areas and blue points do not include source smearing. *Right*: Estimated reliability of the catalogue as a function of integrated flux density limit accounting for the varying sensitivity across the field of view. The olive points include source smearing, the blue points do not.

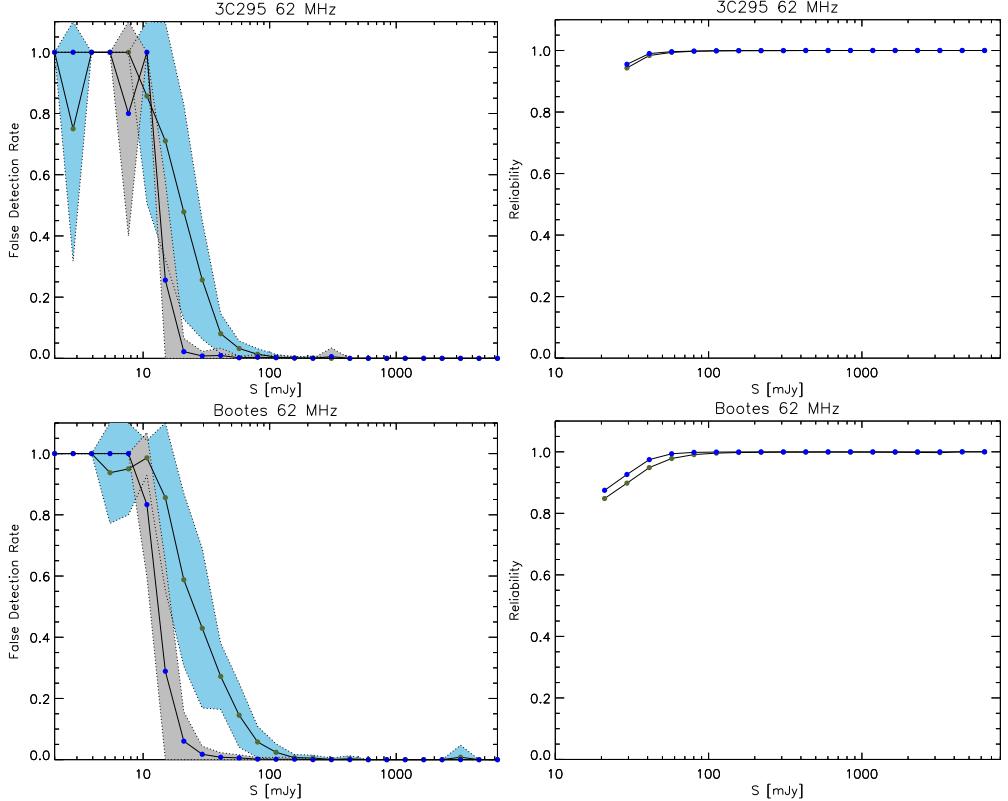


Figure 3.12: False detection rate and reliability. From top to bottom: 3C295 62 MHz and Boötes 62 MHz. Left: False detection rate as a function of peak flux density to local signal-to-noise ratio calculated from 25 Monte-Carlo simulations. The solid line shows the mean of all 25 randomly generated fields and the shaded areas show the 1σ uncertainty. The blue shaded areas and olive points include source smearing in the MC simulations (see main the text of Sect. 3.3.4). The grey shaded areas and blue points do not include source smearing. Right: Estimated reliability of the catalogue as a function of integrated flux density limit accounting for the varying sensitivity across the field of view. The olive points include source smearing, the blue points do not.

3.4 Analysis

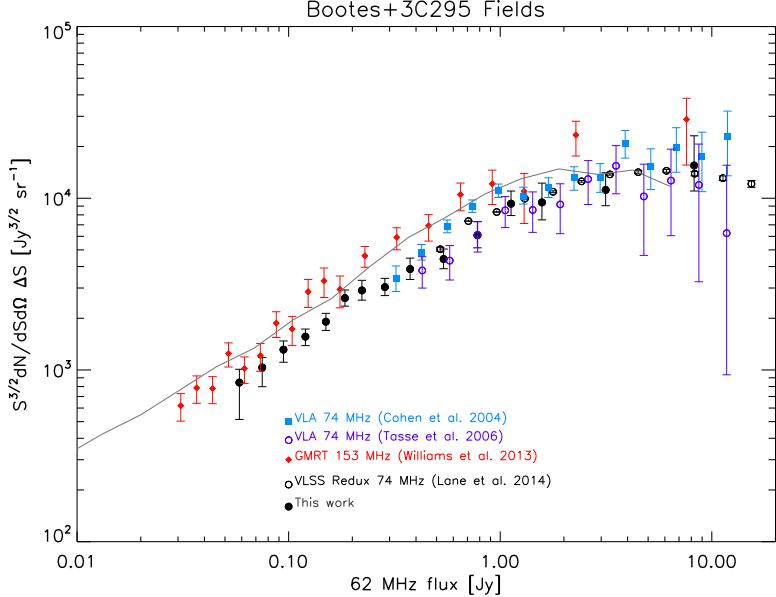


Figure 3.13: Euclidean-normalized differential source counts at 62 MHz combining the Boötes and 3C 295 fields. The LOFAR points are indicated by the black symbols. Red diamonds are Boötes field source counts at 153 MHz, scaled to 62 MHz using $\alpha = -0.7$. Black open circles, blue squares and purple open circles are 74 MHz differential source counts from Tasse et al. (2006); Cohen et al. (2004); Lane et al. (2014) and the solid grey line displays the counts from the 151 MHz SKADS S^3 -SEX simulation (Wilman et al. 2008). These are all scaled to 62 MHz assuming $\alpha = -0.7$.

frequencies. We note though that our flux reference 3C 295 also incorporates a strong spectral turnover below ~ 60 MHz and hence we have to be careful to conclude whether the flattening is intrinsic, or is caused by our uncertain calibrator flux-scale. Fortunately, the 8C 38 MHz counts allow for a more direct comparison at flux densities above ~ 1 Jy (Rees 1990; Hales et al. 1995). We find good agreement between our 34 MHz source counts and those from the 8C survey. In addition, the 8C counts match up with the extrapolated counts from the VLSSr (at 74 MHz) and the GMRT (at 153 MHz) using a spectral index scaling of $\alpha = -0.5$. The 8C source counts at 38 MHz are not consistent with the VLSSr and GMRT counts if we scale with a spectral index of $\alpha = -0.7$. This indeed shows that on average the spectral indices of sources flatten. It is important to note that the VLSSr and 8C counts are not affected by field to field variations given the large sky area they cover.

3.4.2 Spectral indices

In the above section we found evidence for spectral flattening of sources towards lower frequencies. In this subsection we investigate the spectral properties of the detected LBA sources.

For the Boötes field sources we search for counterparts in the NVSS and GMRT 153 MHz catalogs using a matching radius of $20''$. If more than one counterpart to a 62 MHz source is

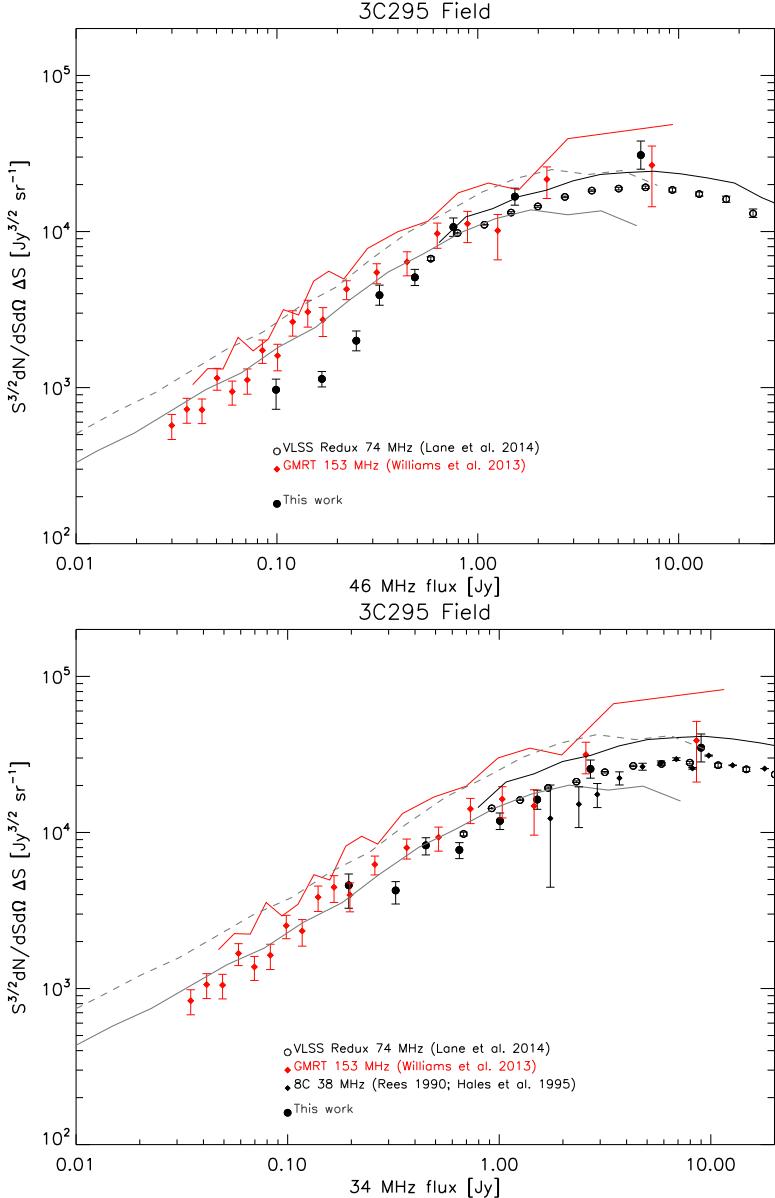


Figure 3.14: Euclidean-normalized differential source counts at 46 (*left*) and 34 MHz (*right*) for the 3C295 field. The LOFAR points are indicated by the black circles. The red diamonds are Boötes field source counts at 153 MHz and the black open circles show the VLSSr counts at 74 MHz (Lane et al. 2014), both scaled with $\alpha = -0.5$. Red and black solid lines show the same source counts but scaled with $\alpha = -0.7$. The solid and dashed grey lines displays the counts from the 151 MHz SKADS S^3 -SEX simulation (Wilman et al. 2008) scaled with $\alpha = -0.5$ and $\alpha = -0.7$, respectively. For the 34 MHz panel we have also plotted the 8C source counts at 38 MHz with black diamonds. The 8C source counts are complete to a flux level of about 5 Jy. Below a flux density of 5 Jy we have corrected the source counts using the information provided in fig. 7 from Rees (1990).

3.4 Analysis

Table 3.4: Source Counts

flux bin Jy	raw counts	corrected counts	normalized counts $\text{Jy}^{3/2} \text{ sr}^{-1}$
62 MHz Boötes and 3C295			
0.051–0.066 32	181	844^{+164}_{-329}	
0.066–0.084 47	143	$1,032^{+150}_{-234}$	
0.084–0.105 51	119	$1,312^{+162}_{-204}$	
0.105–0.135 62	111	$1,562^{+167}_{-175}$	
0.135–0.165 52	78	$1,909^{+226}_{-210}$	
0.165–0.204 65	83	$2,621^{+300}_{-267}$	
0.204–0.240 45	53	$2,904^{+422}_{-354}$	
0.240–0.330 65	75	$3,037^{+376}_{-327}$	
0.330–0.420 44	49	$3,869^{+612}_{-505}$	
0.420–0.660 55	59	$4,424^{+634}_{-538}$	
0.660–0.900 31	32	$6,087^{+1,206}_{-945}$	
0.900–1.35 36	37	$9,295^{+1,716}_{-1,367}$	
1.35–1.80 16	16	$9,456^{+2,792}_{-1,975}$	
1.80–4.50 20	20	$11,175^{+2,899}_{-2,132}$	
4.5–12.0 7	7	$15,509^{+7,595}_{-4,491}$	
46 MHz 3C 295			
0.072–0.126 27	155	969^{+165}_{-242}	
0.126–0.208 46	76	$1,136^{+132}_{-127}$	
0.208–0.288 39	48	$1,998^{+308}_{-278}$	
0.288–0.360 38	44	$3,913^{+622}_{-542}$	
0.360–0.612 65	72	$5,087^{+637}_{-577}$	
0.612–0.900 55	54	$10,686^{+1,535}_{-1,367}$	
0.900–2.16 66	68	$16,747^{+2,218}_{-1,994}$	
2.16–10.8 23	23	$30,898^{+7,133}_{-5,812}$	
34 MHz 3C 295			
0.136–0.252 40	505	$4,615^{+843}_{-1323}$	
0.252–0.396 50	163	$4,257^{+591}_{-773}$	
0.396–0.504 51	105	$8,270^{+984}_{-1090}$	
0.504–0.792 63	105	$7,726^{+883}_{-927}$	
0.792–1.22 61	80	$11,864^{+1,467}_{-1,422}$	
1.22–1.80 46	53	$16,252^{+2,409}_{-2,178}$	
1.80–3.60 55	61	$25,548^{+3,574}_{-3,262}$	
3.60–14.4 23	25	$34,940^{+7,840}_{-6,624}$	

found we add up the flux of all counterparts within the $20''$ radius. In Fig. 3.15 we plot α_{62}^{1400} against the 62 MHz flux density. From this we find an average spectral index of -0.79 . This average drops to -0.74 for α_{62}^{153} and increases to -0.81 for α_{153}^{1400} . The average spectral index between 1400 and 153 MHz we find is within the range of previously reported values: -0.87 , (Williams et al. 2013), -0.79 (Intema et al. 2011), -0.78 (Ishwara-Chandra et al. 2010), -0.82 (Sirothia et al. 2009), and -0.85 (Ishwara-Chandra & Marathe 2007).

We compute the same values for the 3C 295 field, but starting with the 34 MHz source catalog. We find an average spectral index of -0.81 between 1400 and 34 MHz for the sources. This decreases to -0.85 between 1400 and 62 MHz and increases to -0.64 between 62 and 34 MHz, indicating that the average spectral index flattens towards lower frequencies. The value of -0.64 is somewhat steeper than the -0.5 suggested by the source count scalings.

For the brighter, $S_{34} \gtrsim 1$ Jy, 34 MHz sources we also fitted the radio spectra with a second order polynomial ($\log_{10}(S) = a_0 + a_1 \log_{10}(\nu) + a_2 (\log_{10}(\nu))^2$), including the flux densities from the VLSSr, WENSS and NVSS surveys. In total we compute spectra for 27 sources, basically all 34 MHz sources that have a counterpart in the VLSSr survey (the VLSSr survey has a rms noise level of ~ 0.1 Jy beam $^{-1}$). From the polynomial fits we derive the spectral curvature between 500 and 50 MHz, i.e., the difference in the slope (spectral index) between 50 and 500 MHz. The resulting histogram is displayed in Fig. 3.15 (right panel). The histogram shows an excess of sources with curved spectra. We find that 14 sources have curved spectra ($a_2 < -\sigma_{a_2}$, where σ_{a_2} is the uncertainty in a_2), while 13 other sources have fits that are consistent with straight (power-law) spectra. None of these sources had an inverted spectrum, with $a_2 > \sigma_{a_2}$. The average spectral curvature of 0.3 is consistent with the increase of the average spectral index from $\alpha_{153}^{1400} = -0.85$ to $\alpha_{34}^{62} = -0.64$ which we found earlier. This average was based on 133 sources so it shows that the spectral flattening is not only confined to the 27 brighter ($S_{34} \gtrsim 1$ Jy) 34 MHz sources.

3.4.3 Ultra-steep spectrum sources

A large number of deep surveys at multiple wavelengths are available that cover the Boötes field, in particular at radio wavelengths. We therefore carried out a search for sources which have ultra-steep radio spectra to select candidate HzRGs. USS sources that are detected at low frequencies could be missed by the higher frequency WENSS and/or NVSS survey due to their steep spectra. We therefore selected all sources detected at 62 and 153 MHz (from Williams et al. 2013), but that are missed in either the WENSS or NVSS survey. In total we find 5 of these sources, see Table 3.5. In addition, we selected sources from the 62 MHz source list that satisfied the criteria $\alpha_{62}^{153} < -1.1$ and $\alpha_{153}^{1400} < -1.1$, since a large part of our field overlaps with the deep 1.4 GHz WSRT survey of the Boötes field from de Vries et al. (2002) which can be used to compute the spectral indices. Three additional sources were found in this way (Table 3.5).

Croft et al. (2008) also searched for HzRGs in the Boötes field. They selected candidate HzRGs with $S_{1400} > 1$ mJy in a matched 325 MHz/1.4 GHz sample. The five sources with the steepest radio spectra and without optical counterparts were followed up with deep K-band imaging. None of the sources listed in Table 3.5 are reported by Croft et al. (2008), as all but one of the sources from Croft et al. have $\alpha_{325}^{1400} > -1.0$. The source with the steepest spectral index from Croft et al. (J142631+341557) is not detected in our LOFAR 62 MHz image. The source is detected at 153 MHz with an integrated flux of 20 ± 5 mJy, giving $\alpha_{153}^{1400} = -1.3$.

3.4 Analysis

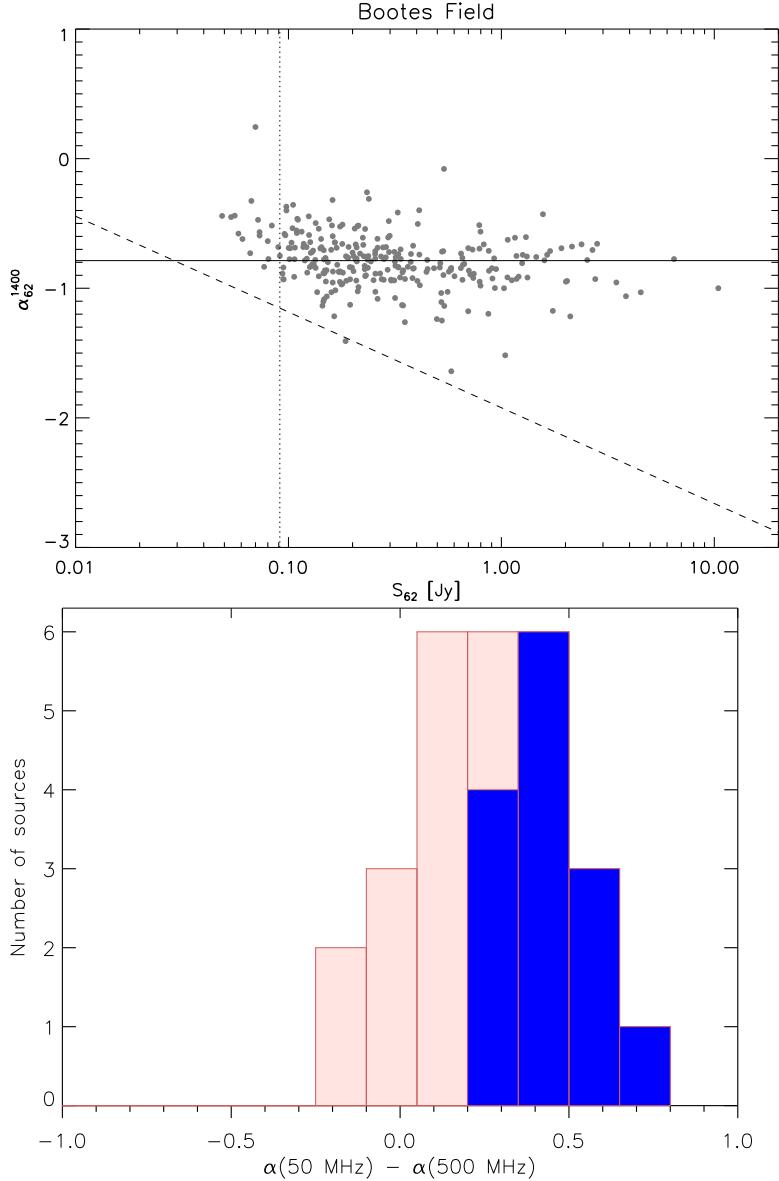


Figure 3.15: Top: Spectral index between 62 and 1400 MHz of sources in the Boötes field plotted against the integrated flux density. The solid line represents the average spectral index of the sources. The vertical dotted line is drawn at $10\sigma_{\text{rms},\text{avg}}$ and the dashed line indicates the completeness limit due to the NVSS sensitivity. Bottom: Histogram of spectral curvature between 500 and 50 MHz for bright 34 MHz sources. The spectral curvature was computed by fitting second order polynomials to the flux density measurements. The blue colors represent sources that cannot be properly fitted with power-law spectra and have $|a_2| > \sigma_{a_2}$, see Sect. 3.4.2.

Table 3.5: USS sources

source	RA, DEC ^a [J2000]	S_{62} [mJy]	S_{153} [mJy]	S_{1400}^{b} [mJy]	α_{62}^{153}	α_{153}^{1400}
J143117.9+351549 ^{*c}	14 ^h 31 ^m 18 ^s .1 +35°15'50"	252 ± 41	53 ± 11	1.74 ± 0.08	-1.72 ± 0.29	-1.54 ± 0.10
J143127.4+343506 ^{*d}	14 ^h 31 ^m 27 ^s .3 +34°35'07"	140 ± 23	40 ± 8	3.00 ± 0.12	-1.39 ± 0.31	-1.17 ± 0.09
J143236.1+333251 [*]	14 ^h 32 ^m 36 ^s .3 +33°32'54"	65 ± 14	23 ± 5	2.00 ± 0.09	-1.15 ± 0.34	-1.10 ± 0.10
J143345.9+353856 [*]	14 ^h 33 ^m 46 ^s .0 +35°38'55"	153 ± 26	57 ± 12	2.86 ± 0.14 ^c	-1.09 ± 0.30	-1.35 ± 0.10
J143501.0+342531 [*]	14 ^h 35 ^m 01 ^s .0 +34°25'31"	173 ± 28	55 ± 11	2.18 ± 0.09	-1.27 ± 0.28	-1.46 ± 0.09
J143426.1+342809 ^{ce}	14 ^h 34 ^m 25 ^s .6 +34°28'19"	341 ± 54	115 ± 24	10.1 ± 0.5	-1.20 ± 0.29	-1.10 ± 0.10
J143506.8+350058	14 ^h 35 ^m 06 ^s .9 +35°00'59"	581 ± 91	141 ± 29	4.02 ± 0.16	-1.57 ± 0.29	-1.61 ± 0.09
J143520.5+345949	14 ^h 35 ^m 20 ^s .5 +34°59'50"	185 ± 31	57 ± 12	1.55 ± 0.07	-1.30 ± 0.30	-1.63 ± 0.10

* source not detected in the NVSS and/or WENSS survey

^a 1.4 GHz position from de Vries et al. (2002)^b 1.4 GHz flux density from de Vries et al. (2002)^c Source detected in the HerMES survey (Roseboom et al. 2010; Oliver et al. 2012; Smith et al. 2012)^d Position and flux density from the 1.4 GHz FIRST survey (White et al. 1997)^e Position from the 1.4 GHz FIRST survey and flux density from the NVSS survey

3.5 Conclusions

For the USS sources we identify candidate counterparts in the NOAO Deep Wide-Field Survey (NDWFS) I-band images. For the optical identification we use the likelihood ratio technique (Sutherland & Saunders 1992; Tasse et al. 2008). In this way we obtain a probability $P(i)$ that candidate i is the true optical counterpart to a given radio source. For the radio position we take the GMRT 153 MHz position, or when available the 1.4 GHz FIRST position. We then obtain flux measurements for all candidate counterparts (with $P(i) > 5\%$) from the NOAO Deep Wide Field Survey (NDWFS, B_W , R , I , K ; Jannuzi & Dey 1999), the Flamingos Extragalactic Survey (FLAMEX, J , K_s ; Elston et al. 2006), the zBoötes survey (z' ; Cool 2007), the Spitzer Deep Wide Field Survey (SDWFS, [3.6], [4.5], [5.8], [8.0]; Ashby et al. 2009), GALEX GR5 (NUV, FUV; Morrissey et al. 2007) and the MIPS AGN and Galaxy Evolution Survey (MAGES [24]; Jannuzi et al. 2010) to obtain photometric redshifts (z_{phot}). For the spectral energy distribution (SED) and z_{phot} -fitting we require measurements in at least 5 bands. The fitting is performed using both the LRT code from Assef et al. (2008) and EAZY¹ (Brammer et al. 2008) for comparison. A much more extensive description of the radio counterpart identification and SED fitting will be given in Williams et al. (in prep). The results of the fitting are summarized in Table 3.6. Figures showing the SEDs for each source and I band, IRAC 4.5 micron, IRAC 8.0 micron and MIPS 24 micron postage stamps, with GMRT (and FIRST where there is a source) contours, are shown in Appendix 3.B.

We find that the photometric redshifts of the sources are mostly in the $0.7 \lesssim z_{\text{phot}} \lesssim 2.5$ range. Given the correlation between optical brightness and redshift, counterparts without photo-z's are likely located at a higher redshift. For J143127.4+343506 and J143345.9+353856 the differences between the EAZY and LRT codes are substantial. We note that the LRT code is supposed to do a better job of fitting AGN and LRT also takes into account the upper limits. Larger USS samples are needed to detect more distant objects as they are more rare. However, steep-spectrum selection also misses a significant fraction of HzRGs (e.g., Jarvis et al. 2009) and not all USS sources are associated with HzRGs (e.g., Jarvis et al. 2001; Cruz et al. 2007; van Weeren et al. 2009). Therefore a combination of deep radio and optical/NIR survey data will be a more powerful way of identifying HzRGs by searching for optically/NIR faint counterparts to the radio sources (e.g., Brookes et al. 2006; Ker et al. 2012).

3.5 Conclusions

We have presented the results of LOFAR LBA observations of the Boötes and 3C 295 fields. In our 62 MHz Boötes field image, with a central noise level of $4.8 \text{ mJy beam}^{-1}$, we detect a total of 329 sources over a 19.4 deg^2 area. Our images of the 3C 295 field cover an area from 17 to 52.3 deg^2 from 62 to 34 MHz, respectively. We reach central noise levels of 5.3, 8.2 and 12 mJy beam^{-1} at 62, 46 and 34 MHz for the 3C 295 field. In total we detect 329, 367, 392 sources at 62, 46 and 34 MHz.

From our source lists, we derive the deepest differential source counts at 62, 46 and 34 MHz to date. At 62 MHz the source counts are in good agreement with 74 MHz counts from VLA observations and scaling with a spectral index of -0.7 . At 34 MHz the measured source counts fall significantly below extrapolated source counts from 74 and 153 MHz, using a spectral index scaling of -0.7 . Instead, we find that a spectral index scaling of -0.5 provides a better match to

¹EAZY does not use the 24 micron band for the fitting

Table 3.6: USS Sources SED fit results

source	gmrt id	P_{match}	N_{bands}	z_a	z_m	z_{eazy}	$\chi^2/\text{n.d.f.}$	z	z_{lrt}^t	$\chi^2/\text{n.d.f.}$
J143520.5+345949	428	99.6	11	0.746	0.743^{+0.056}	1.793	0.70	9.37		
J143506.8+350058	440	86.7	8	1.988	2.016 ^{+0.285}	1.054	2.46	1.32		
J143506.8+350058	440	13.0	2	-	-	-	-	-		
J143501.0+342531	445	99.4	11	1.400	1.380 ^{+0.171}	0.749	1.34	1.91		
J143426.1+342809	485	55.3	4	-	-	-	-	-		
J143426.1+342809	485	41.6	3	-	-	-	-	-		
J143345.9+353856	517	99.8	6	1.871	1.935 ^{+0.125}	1.534	2.45	1.93		
J143236.1+333251	591	99.1	11	0.967	1.033 ^{+0.096}	1.677	1.06	20.59		
J143127.4+343506	667	76.6	8	1.815	1.851 ^{+0.208}	1.549	0.32	0.28		
J143127.4+343506	667	23.2	1	-	-	-	-	-		
J143117.9+351549	679	92.4	7	1.548	2.253 ^{+0.750}	0.107	1.56	0.09		

The radio source name and GMRT radio source ID are given in Cols. 1 and 2; Col. 3 gives the probability that a given source is the true optical counterpart to the radio source. The highest probability match is marked in boldface; The number of bands available for SED fitting (N_{bands}) is given in Col. 4; Cols. 5 and 6 give the redshift obtained via EAZY, with z_a the redshift at the minimum χ^2 , and z_m the redshift marginalized over the $p(z)$ distribution, with the 68% confidence intervals; The reduced χ^2 of the fit is listed in Col. 7; The fitted redshift from the LRT code and corresponding reduced χ^2 are given in Cols. 8 and 9.

^a No SED/ z_{phot} fitting could be performed since there are less than 5 flux measurements were available.

3.A Extended sources at 62 MHz

the observed 34 MHz source counts. Our 34 MHz source counts are also consistent with those obtained from the 38 MHz 8C survey. In addition, evidence for spectral flattening is found from the increase of the average radio spectral index from high to low frequencies. From polynomial fits to the individual flux densities of bright ($\gtrsim 1$ Jy) 34 MHz sources, we conclude that about half of these sources have curved spectra. The curved spectra of these sources could be caused by absorption effects, as well as by spectral ageing.

We also selected sources with steep radio spectra ($\alpha < -1.1$) in the Boötes field to find candidate high- z radio galaxies. We identified optical counterparts to these sources and fitted the SEDs to obtain photometric redshifts. We conclude that most of these USS sources seem to be located in the $0.7 \lesssim z \lesssim 2.5$ range.

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Appendix

3.A Extended sources at 62 MHz

Figures 3.A.1 and 3.A.2 show the 62 MHz LOFAR images of extended sources in the Boötes and 3C 295 fields.

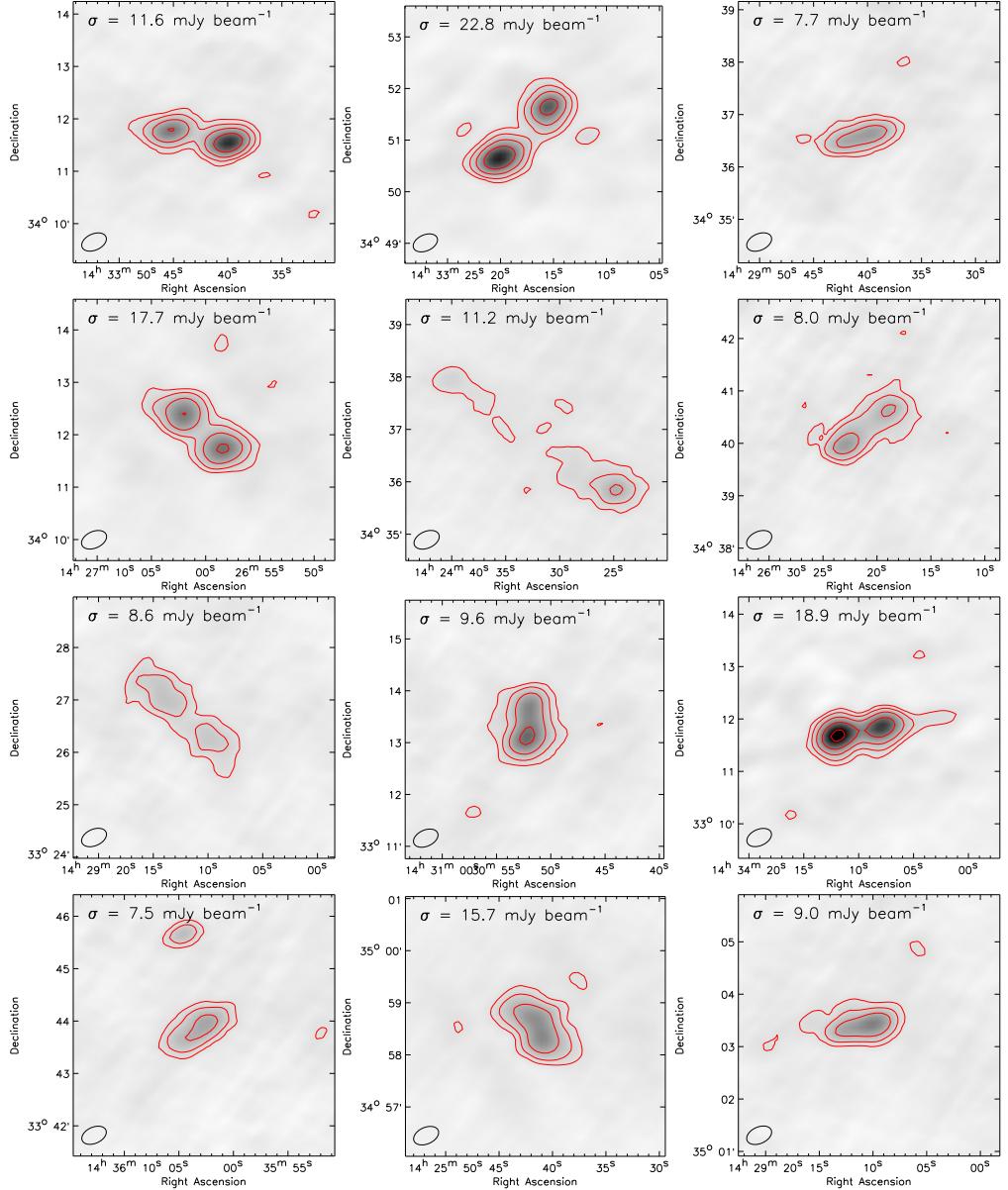


Figure 3.A.1: Images of resolved sources in the Boötes field at 62 MHz. Contour levels are drawn at $[1, 2, 4, 8, \dots] \times 3\sigma_{\text{local rms}}$, with $\sigma_{\text{local rms}}$ reported in each image. The beam size is shown in the bottom left corner of the images.

3.A Extended sources at 62 MHz

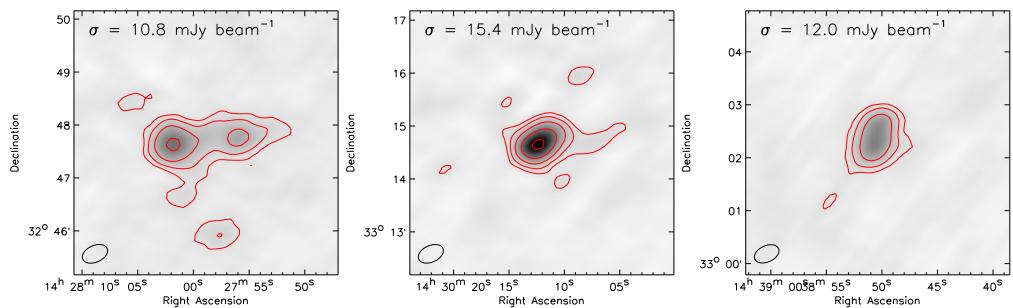


Figure 3.A.1: Continued.

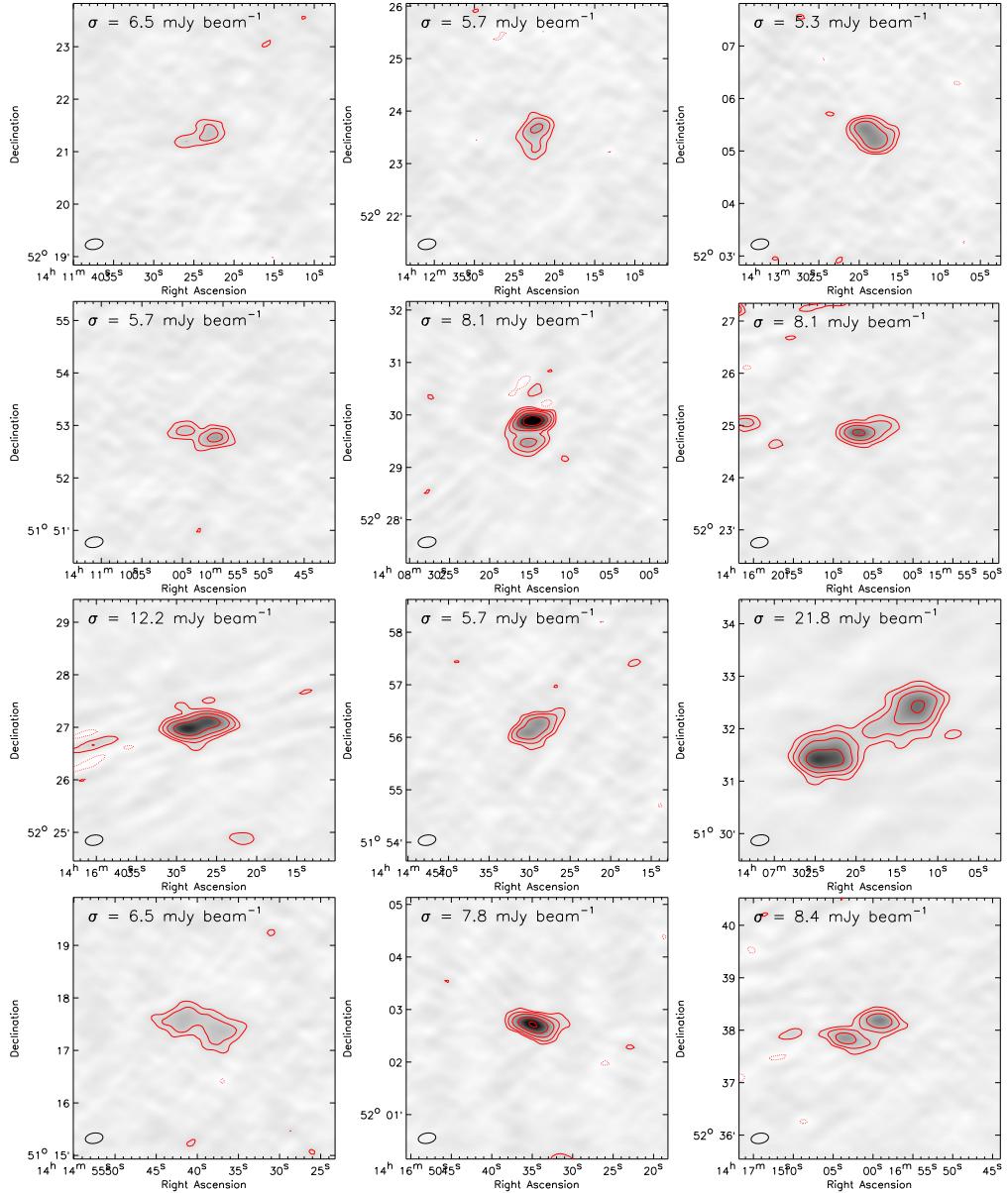


Figure 3.A.2: Images of resolved sources in the 3C 295 field at 62 MHz. Contour levels are drawn at $[1, 2, 4, 8, \dots] \times 3\sigma_{\text{local rms}}$, with $\sigma_{\text{local rms}}$ reported in each image. The beam size is shown in the bottom left corner of the images.

3.A Extended sources at 62 MHz

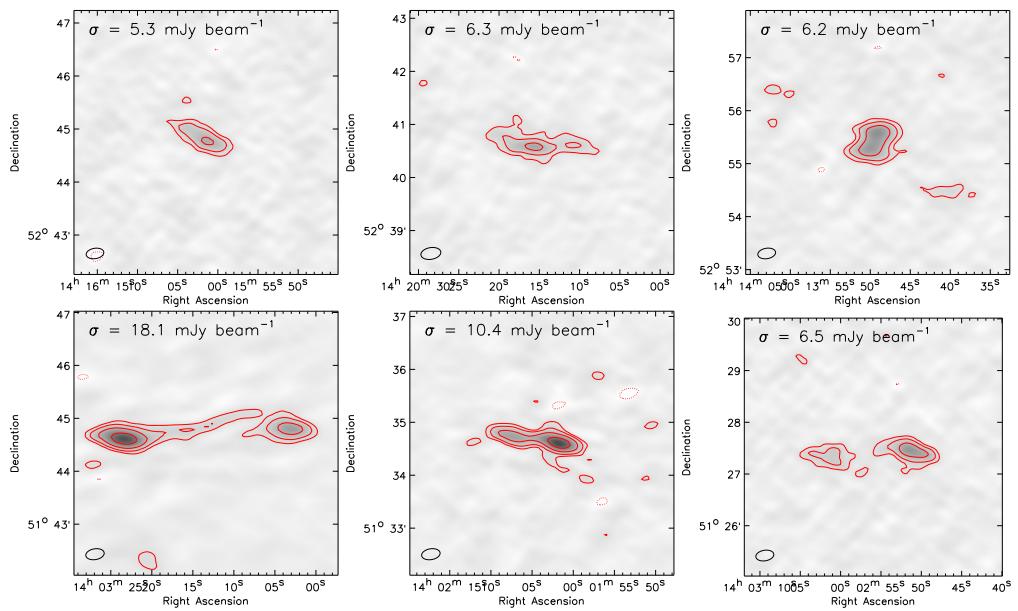


Figure 3.A.2: Continued.

3.B SED & photo-z fitting results

Figure 3.B.1 shows the SEDs for each counterpart to a USS source and I band, IRAC 4.5 micron, IRAC 8.0 micron and MIPS 24 micron postage stamps, with GMRT (and FIRST where there is a source) contours overlaid.

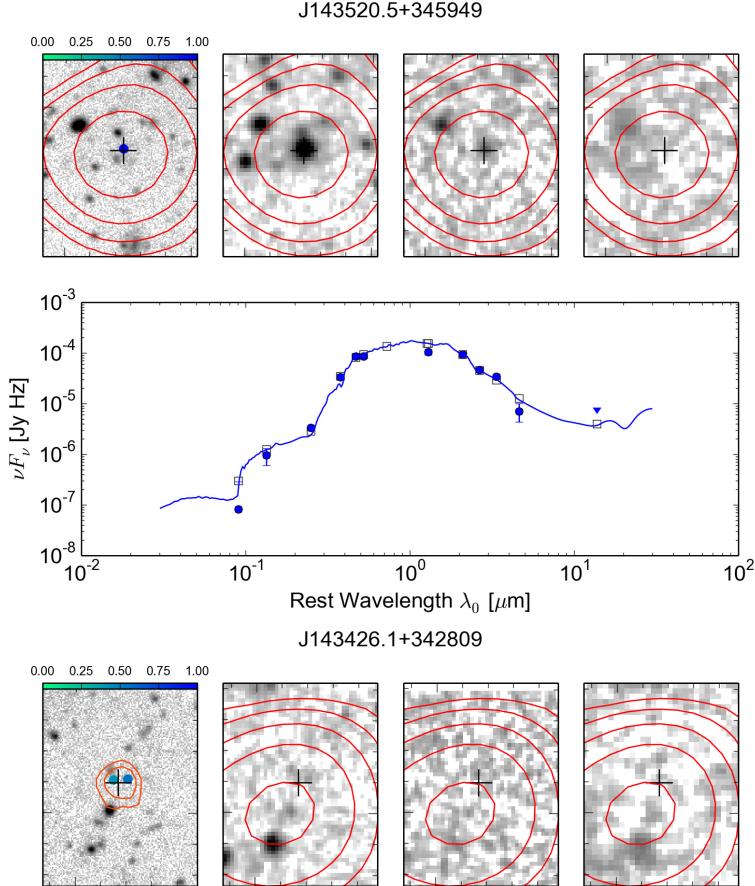


Figure 3.B.1: Top panels: postage stamps showing NDWFS I-band, IRAC 4.5 micron, IRAC 8.0 micron and MIPS 24 micron images. GMRT 153 MHz (red) and FIRST 1.4 GHz (orange, when available) contours are overlaid. Radio contour levels are drawn at $[1, 2, 4, \dots] \times 3\sigma_{\text{rms}}$. A black cross indicates the GMRT radio position and the color scale at the top of the I-band image shows the probability that the I-band source, marked with a colored point, is the true optical counterpart. Bottom panels: Spectral energy distribution and best fitted LRT model for the optical counterpart(s). The flux measurements were taken from Jannuzzi & Dey (1999); Elston et al. (2006); Cool (2007); Ashby et al. (2009); Morrissey et al. (2007); Jannuzzi et al. (2010).

3.B SED & photo-z fitting results

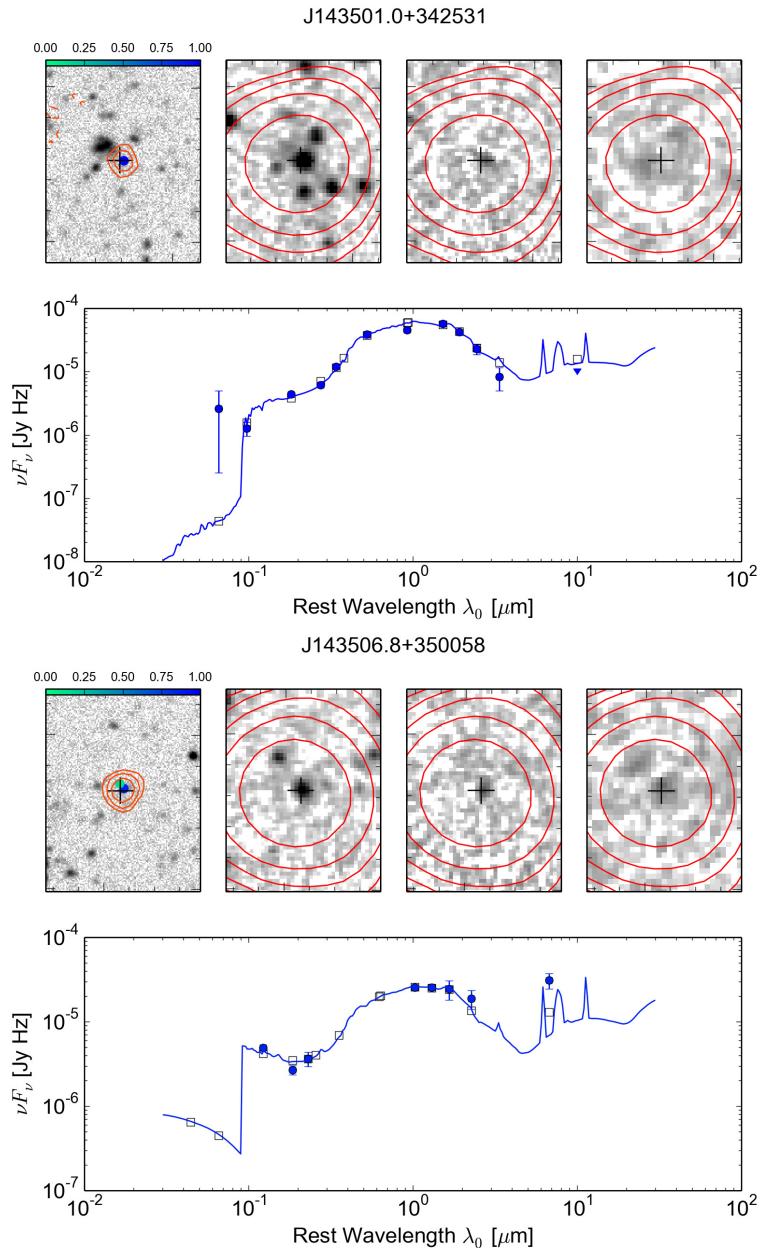
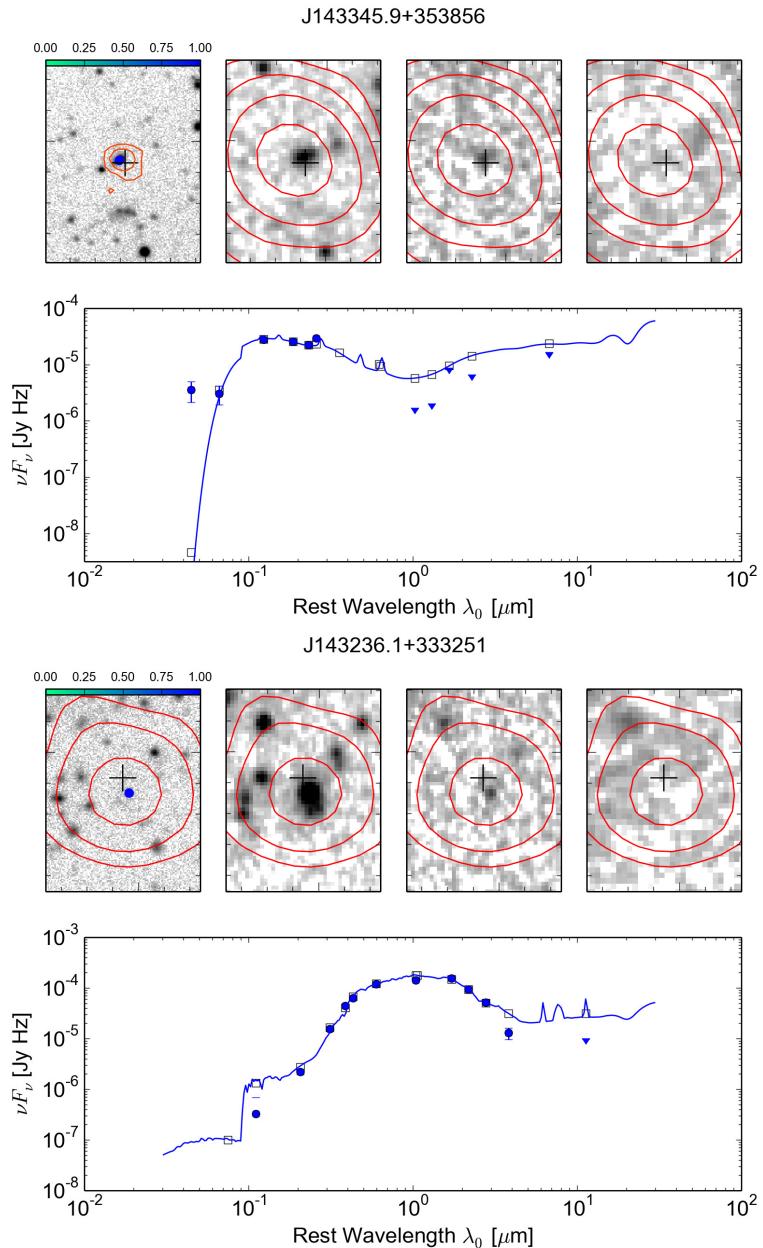


Figure 3.B.1: Continued.

**Figure 3.B.1:** Continued.

3.B SED & photo-z fitting results

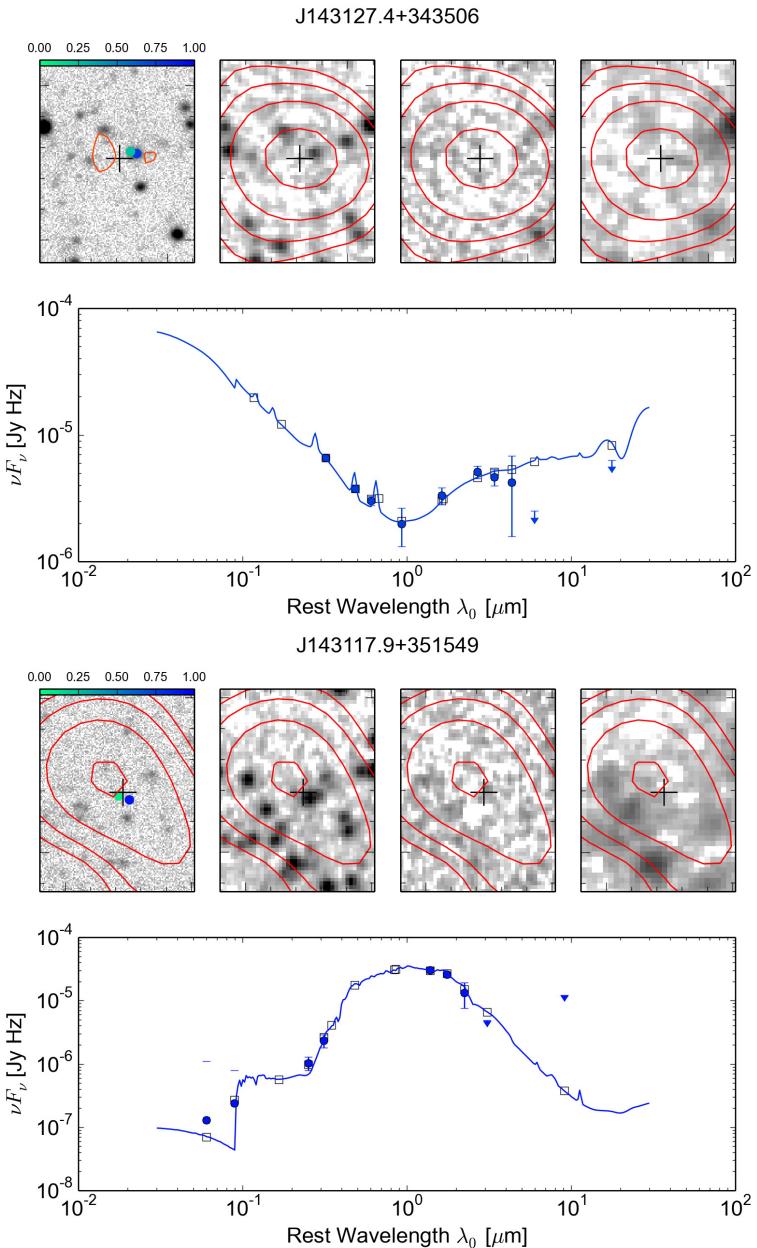


Figure 3.B.1: Continued.

3.C Source counts at 62 MHz for the Boötes field and 3C 295 fields

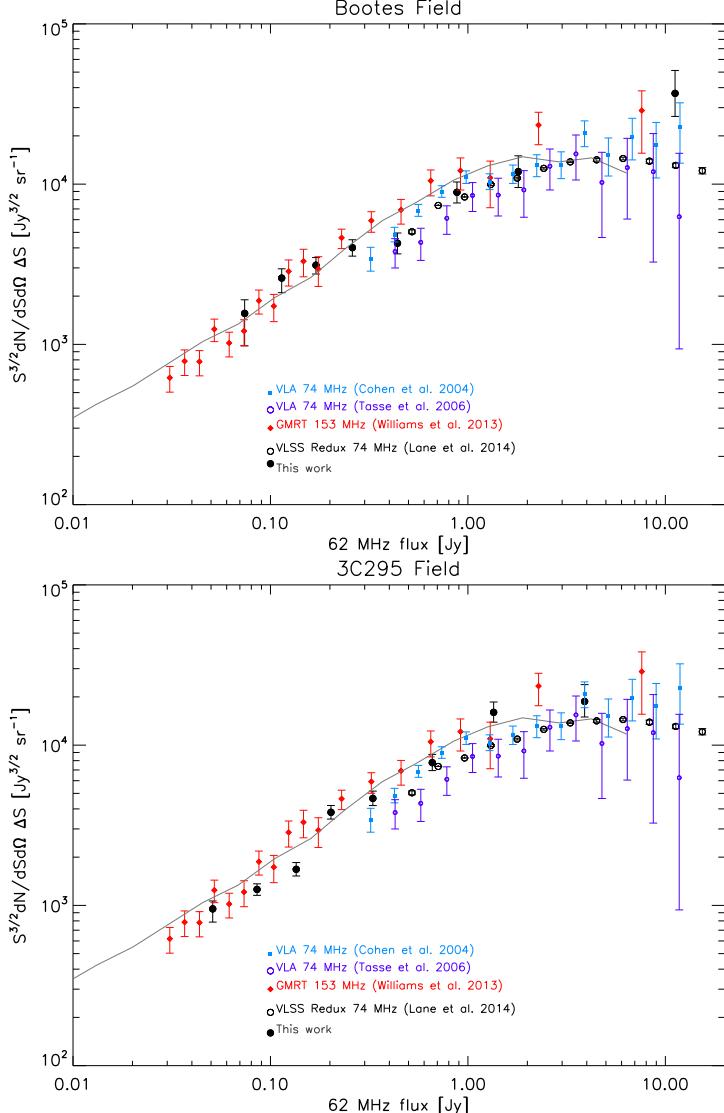


Figure 3.C.1: Euclidean-normalized differential source counts at 62 MHz for the Boötes and 3C 295 fields. The LOFAR points are indicated by the black symbols. Red diamonds are Boötes field source counts at 153 MHz, scaled to 62 MHz using $\alpha = -0.7$. Black open circles, blue squares and purple open circles are 74 MHz differential source counts from Tasse et al. (2006); Cohen et al. (2004); Lane et al. (2014) and the solid grey line displays the counts from the 151 MHz SKADS S³-SEX simulation (Wilman et al. 2008). These are all scaled to 62 MHz assuming $\alpha = -0.7$.

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